

Programming with `ispc`

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Agenda

SIMD on CPU

Auto-vectorisation

Programming in ISPC

ISPC Performance

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Auto-vectorisation

Programming in ISPC

ISPC Performance

What is SIMD?

- **Single Instruction Multiple Data.**
- Fixed-size *vector registers* that contain multiple values.
- *Vector instructions* that operate on vector registers.
 - ▶ A form of explicit ILP where instruction is the same.
 - ▶ If vector register contains four floats, then single SIMD instruction can replace four scalar instructions.
- Usually an extension to the scalar instruction set.

Scalar Operation

$$\begin{array}{l} A_1 \times B_1 = C_1 \\ A_2 \times B_2 = C_2 \\ A_3 \times B_3 = C_3 \\ A_4 \times B_4 = C_4 \end{array}$$

SIMD Operation

$$\begin{array}{|c|} \hline A_1 \\ \hline A_2 \\ \hline A_3 \\ \hline A_4 \\ \hline \end{array} \times \begin{array}{|c|} \hline B_1 \\ \hline B_2 \\ \hline B_3 \\ \hline B_4 \\ \hline \end{array} = \begin{array}{|c|} \hline C_1 \\ \hline C_2 \\ \hline C_3 \\ \hline C_4 \\ \hline \end{array}$$

Scalar Operation

$$A_1 \times B_1 = C_1$$

$$A_2 \times B_2 = C_2$$

$$A_3 \times B_3 = C_3$$

$$A_4 \times B_4 = C_4$$

SIMD Operation

$$\begin{matrix} A_1 \\ A_2 \\ A_3 \\ A_4 \end{matrix} \times \begin{matrix} B_1 \\ B_2 \\ B_3 \\ B_4 \end{matrix} = \begin{matrix} C_1 \\ C_2 \\ C_3 \\ C_4 \end{matrix}$$

2

x86 example

The registers `xmm0`–`xmm15` are 128 bits each, and operated on with instructions like `ADDSS`, `SUBSS`, `MULSS`.

- Instead of `add eax ebx` use e.g. `addss xmm0 xmm1`.
- Follows all the normal assembly rules.

²<https://medium.com/wasmer/webassembly-and-simd-13badb9bf1a8>

When is SIMD useful?

- In our ontology, SIMD is *first-order flat data parallelism* on vectors of static size.
- When program is not bottlenecked by IO or memory traffic.
 - Although bulk memory reads can sometimes be vectorised.

SIMD is cheap

- It's already part of the CPU and uses the same memory.
- Using an SIMD instruction has zero latency.
- Compare to GPUs, which have huge overhead.
- **SIMD is not multithreading**
 - Both techniques can be used simultaneously.
 - Will only focus on SIMD for this lecture.
- Speedup limited to SIMD vector size (in practice usually 4 or 8).
 - Often much less.

Applying vectorisation

- In principle, we can use SIMD instructions whenever independent operations with same operator occur:

```
float x = a + b;  
float y = b + c;  
float z = d + e;  
float v = e + f;
```

- Compilers *do* try to do this...
- ... but vectorisation mostly shines when doing bulk data parallel operations:

```
for (int i = 0; i < n; i++) {  
    xs[i] *= 2;  
}
```

Simple vectorisation

```
for (int i = 0; i < n; i++) {  
    xs[i] *= 2;  
}
```

Parallel?

Simple vectorisation

```
for (int i = 0; i < n; i++) {  
    xs[i] *= 2;  
}
```

Parallel?

Conceptually vectorise by *strip mining* the loop into chunks corresponding to the vector size (e.g. 4):

```
for (int j = 0; j < n; j += 4) {  
    for (int i = j; i < j+4; i++) {  
        xs[i] *= 2;  
    }  
}
```

- Innermost loop can be replaced with vector instructions.
- Separate loop for any remaining < 4 iterations.

```
for (int j = 0; j < n; j += 4)
    for (int i = j; i < j+4; i++)
        xs[i] *= 2;
```



```
# eax: j
# ebx: i*4
# ecx: n
# rdi: xs
```

```
loop:
```

```
    movdqu    xmm0, xmmword ptr [rdi + ebx]
    paddb     xmm0, xmm0
    movdqu    xmmword ptr [rdi + ebx], xmm0
    add       eax, 4
    add       ebx, 16
    cmp       eax, ecx
    jl        .loop
```

Vectoring functions

Suppose we extract the loop body into a function.

```
for (int i = 0; i < n; i++)  
    f(x[i], ...)
```

Then the vectorisation problem can be seen as transforming f into a function operating on a *vector* of arguments.

Vectorising functions with straight-line code is easy

Suppose to want to vectorise this single function to operate on a vector of values:

```
int f(int x, int y) {  
    return (x + y) / 2;  
}
```

Scalar version handles one x/y pair at a time.

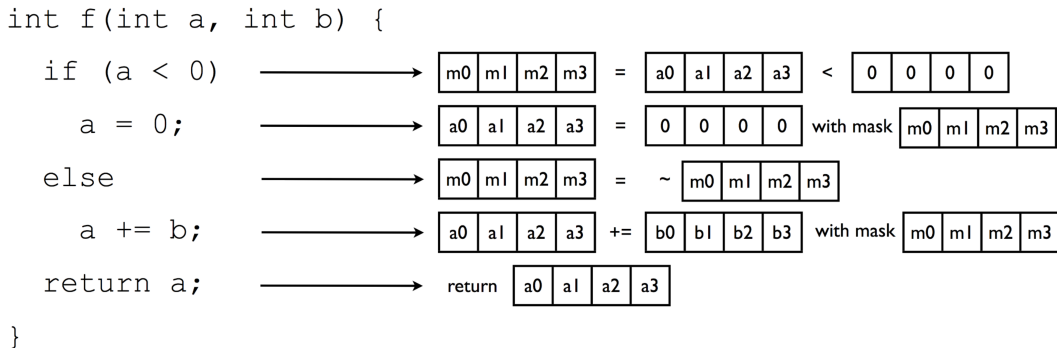
```
add edi, esi  
shr esi, 31
```

Vector version handles four x/y pairs at a time.

```
paddq    xmm1, xmm0  
psrad    xmm1, 1
```

What about control flow?

Vectorising scalar function with control flow³



- **Masking**, similar to NumPy.
- Control flow turned into data flow (arithmetic).
- Doing this by hand gets very tiresome and is error-prone.
- Vector capabilities differ a lot between architectures.

³Example from ispc paper.

SIMD extensions added to x86 over time

1997 **MMX**: New 64-bit registers (MM0–MM7), 57 new integer instructions.

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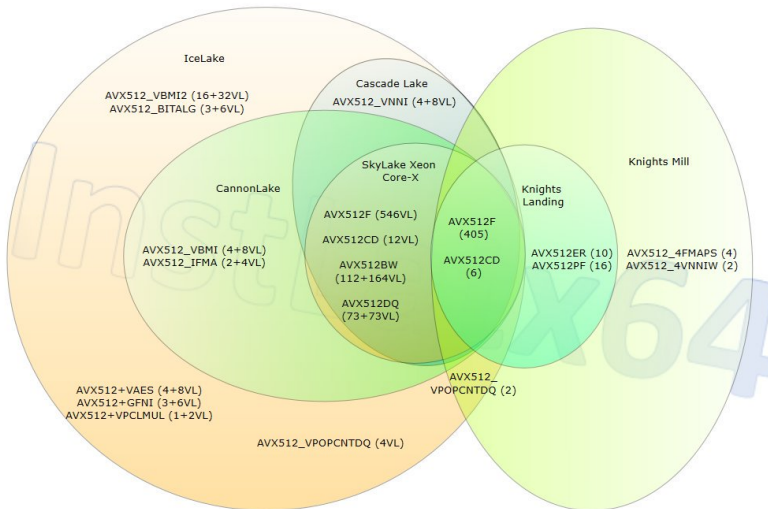
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- 2016 **AVX-512**: 512-bit registers (ZMM0–ZMM31), and a zoo of layers, not expected to be in all processors.
- 2023 **AVX10**: 512 bit registers no longer guaranteed, some new instructions.

The 17+1 levels of AVX512 in Intel processors
2018-03-02
according to the 32th Intel ISA-ER
v1.2



SIMD on CPU

Auto-vectorisation

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ISPC Performance

Auto-vectorisation

Write ordinary C code and hope that a sufficiently smart compiler can figure out what you mean and make use of whatever instruction set is supported on your computer.

Good: you don't have to learn anything new!

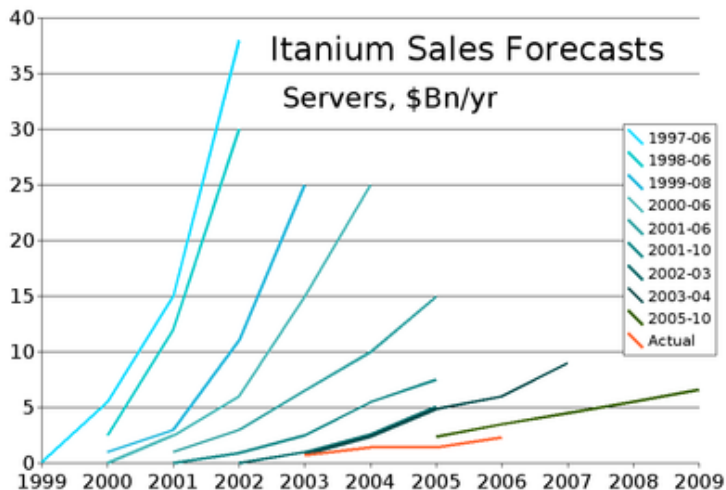
Auto-vectorisation

Write ordinary C code and hope that a sufficiently smart compiler can figure out what you mean and make use of whatever instruction set is supported on your computer.

Good: you don't have to learn anything new!

Bad: does it work?

What happened last time we depended on Sufficiently Smart Compilers?



Auto-vectorisation, example A

```
void A(int n, int *xs) {  
    for (int i = 0;  
        i < n;  
        i++) {  
        xs[i] *= 2;  
    }  
}
```

```
$ gcc -O3 A.c -S
```

Auto-vectorisation, example A

```
void A(int n, int *xs) {  
    for (int i = 0;  
        i < n;  
        i++) {  
        xs[i] *= 2;  
    }  
}
```

```
$ gcc -O3 A.c -S
```

```
.L4:  
    movdqu    xmm0, XMMWORD PTR [rax]  
    add       rax, 16  
    psllq     xmm0, 1  
    movups    XMMWORD PTR [rax-16], xmm0  
    cmp       rax, rcx  
    jne       .L4
```

Auto-vectorisation, example A

```
void A(int n, int *xs) {  
    for (int i = 0;  
        i < n;  
        i++) {  
        xs[i] *= 2;  
    }  
}
```

```
$ gcc -O3 A.c -S
```

Vectorised!

```
.L4:  
    movdqu    xmm0, XMMWORD PTR [rax]  
    add       rax, 16  
    psllq     xmm0, 1  
    movups    XMMWORD PTR [rax-16], xmm0  
    cmp       rax, rcx  
    jne       .L4
```

Auto-vectorisation, example B

```
int B(int n, int *xs) {  
    int res = 0;  
    for (int i = 0;  
         i < n;  
         i++) {  
        res += xs[i];  
    }  
    return res;  
}
```


Auto-vectorisation, example B

```
int B(int n, int *xs) {  
    int res = 0;  
    for (int i = 0;  
         i < n;  
         i++) {  
        res += xs[i];  
    }  
    return res;  
}
```

```
.L4:  
    movdqu    xmm2, XMMWORD PTR [rax]  
    add       rax, 16  
    paddb     xmm0, xmm2  
    cmp       rdx, rax  
    jne       .L4  
    movdqa    xmm1, xmm0  
    mov       edx, ecx  
    psrldq    xmm1, 8  
    and       edx, -4  
    paddb     xmm0, xmm1  
    movdqa    xmm1, xmm0  
    psrldq    xmm1, 4  
    paddb     xmm0, xmm1  
    mov       eax, xmm0  
    test      cl, 3  
    je        .L11
```

Auto-vectorisation, example B

```
int B(int n, int *xs) {  
    int res = 0;  
    for (int i = 0;  
         i < n;  
         i++) {  
        res += xs[i];  
    }  
    return res;  
}
```

Tricky, but **vectorised**!

```
.L4:  
    movdqu    xmm2, XMMWORD PTR [rax]  
    add       rax, 16  
    paddb     xmm0, xmm2  
    cmp       rdx, rax  
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    psrldq    xmm1, 4  
    paddb     xmm0, xmm1  
    mov       eax, xmm0  
    test      cl, 3  
    je       .L11
```

Auto-vectorisation, example C

```
void C(int n,  
      int *ys,  
      int *xs) {  
    int acc = 0;  
    for (int i = 0;  
        i < n;  
        i++) {  
        acc += xs[i];  
        ys[i] = acc;  
    }  
}
```

Auto-vectorisation, example C

```
void C(int n,  
       int *ys,  
       int *xs) {  
    int acc = 0;  
    for (int i = 0;  
         i < n;  
         i++) {  
        acc += xs[i];  
        ys[i] = acc;  
    }  
}
```

```
.L3:  
    add    ecx, DWORD PTR [rdx+rax]  
    mov    DWORD PTR [rsi+rax], ecx  
    add    rax, 4  
    cmp    rdi, rax  
    jne    .L3
```

Auto-vectorisation, example C

```
void C(int n,  
        int *ys,  
        int *xs) {  
    int acc = 0;  
    for (int i = 0;  
         i < n;  
         i++) {  
        acc += xs[i];  
        ys[i] = acc;  
    }  
}
```

Not vectorised.

```
.L3:  
    add    ecx, DWORD PTR [rdx+rax]  
    mov    DWORD PTR [rsi+rax], ecx  
    add    rax, 4  
    cmp    rdi, rax  
    jne    .L3
```

Vectorising powi()

```
float powi(float a, int b) {  
    float r = 1;  
    while (b-->0) r *= a;  
    return r;  
}
```

Vectorising powi()

```
float powi(float a, int b) {  
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}
```

Two ways of vectorising

1. Make a single call `powi(a,b)` faster by trying to do multiple iterations of the `while` loop in parallel (probably infeasible).

Vectorising powi()

```
float powi(float a, int b) {  
    float r = 1;  
    while (b-- > 0) r *= a;  
    return r;  
}
```

Two ways of vectorising

1. Make a single call `powi(a,b)` faster by trying to do multiple iterations of the `while` loop in parallel (probably infeasible).
2. Make multiple *instances* of `powi(a,b)` faster:

```
for (int i = 0; i < n; i++) {  
    cs[i] = powi(as[i], bs[i]);  
}
```

- (1) much harder, (2) often what we want.
- **How would a compiler know?**

Vectorising powi() with option (2)

```
float powi(float a, int b) {  
    float r = 1;  
    while (b-->0) r *= a; // AVX2 assembly for this loop below  
    return r;  
}
```

Vectorising powi() with option (2)

```
float powi(float a, int b) {  
    float r = 1;  
    while (b-->0) r *= a; // AVX2 assembly for this loop below  
    return r;  
}
```

```
.LBB1_3:  
    vpaddd    ymm8, ymm1, ymm5          # Decrement b.  
    vblendvps ymm1, ymm1, ymm8, ymm7    # Only active lanes.  
    vmulps    ymm7, ymm3, ymm0          # r * a.  
    vblendvps ymm3, ymm3, ymm7, ymm6    # Only active lanes.  
    vpcmpeqd  ymm8, ymm1, ymm4          # Compare b with zero.  
    vmovaps   ymm7, ymm6                # Compute which lanes  
    vpandn    ymm6, ymm8, ymm6          # still active.  
    vpand     ymm8, ymm6, ymm2          # AND with current.  
    vmovmskps eax, ymm8                # Any lanes active?  
    test      eax, eax                  # ...  
    jne       .LBB1_3                  # Redo if so.
```

A C compiler will not do this.

Motivation for `ispc`

- Around 2010, Matt Pharr from Intel's graphics group had too much time and too much trouble with extant auto-vectorisers.

- **Motivating problem: graphics**

- ▶ Often embarrassingly parallel:

```
for (int j = 0; j < height; j++) {  
    for (int i = 0; i < width; i++) {  
        // compute pixel i,j  
    }  
}
```

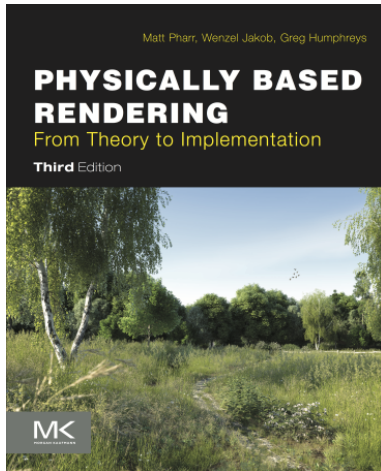
- ▶ Often lots of control flow in the loop body.
 - ▶ If we could have one vector lane compute one pixel, then we could compute 4/8/16 pixels simultaneously.
 - ▶ Even today, auto-vectorisers choke on anything non-trivial (ask Cosmin about stencils).

Quotes from Matt Pharr

1. *They'd inform the graphics folks that they'd improved their auto-vectorizer in response to our requests and that it did everything we had asked for.*
2. *We'd try it and find that though it was better, boy was it easy to write code that wasn't actually compiled to vector code—it'd fail unpredictably.*
3. *We'd give them failing cases, a few months would would pass and they'd inform us that the latest version solved the problem.*

They tried to patch things up at first but eventually they threw up their hands and came up with `#pragma simd`, which would disable the “is it safe to vectorize this” checks in the auto-vectorizer and vectorize the following loop no matter what. (Once a `#pragma` is proposed to solve a hard problem, you know things aren't in a good place.)

As an aside, Matt Pharr is likely the only programming language designer to win an Academy Award



Winner of a 2014 Scientific and Technical Academy Award

Auto-vectorisation is not a programming model

- A compiler can easily tell you *what* fails to vectorise.
- Not so clear *why*.
- You need to become an expert in the compiler and tickle your code in just the right way.
- **This is a horrible way to program.**

And then they release a new compiler with subtly different behaviour...

With a proper programming model, then the programmer learns the model (which is hopefully fairly clean), one or more compilers implement it, the generated code is predictable (no performance cliffs), and everyone's happy.

Single Program Multiple Data (SPMD)

- Essentially the model also used by CUDA.
- Multiple *instances* of program is running.
- Group of running instances is called a *gang*.

```
void inc(int xs[], int ys[], int result[]) {  
    result[programIndex] =  
        (xs[programIndex] + ys[programIndex]) / 2;  
}
```

- In principle, one instance per array element.
- On GPU, *many* instances are useful to allow latency hiding.
- On CPU, rarely more than twice the SIMD width.
 - In practice usually exactly the SIMD width.

SIMD on CPU

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Programming in ISPC

ISPC Performance

Intel SPMD Program Compiler

ispc is a compiler for a variant of the C programming language, with extensions for "single program, multiple data" (SPMD) programming.

ispc is

- a variant of C—much scalar C is also valid ispc.
- a *low-level parallel language*.
- *not guaranteed to be deterministic*.
- a compiler with only few *compiler optimisations*.

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ispc is

- a variant of C—much scalar C is also valid ispc.
- a *low-level parallel language*.
- *not guaranteed to be deterministic*.
- a compiler with only few *compiler optimisations*.

What makes it relevant for our course is that it is a good example of using *the right programming model*.

Disclaimer

I am not an `ispc` expert.

I am merely an enthusiast, and I think its design is a masterpiece of simplicity, worthy of study.

Most of what I know is from

1. *ispc: A SPMD Compiler for High-Performance CPU Programming* (paper)
2. *The story of `ispc`* (series of blog posts by Matt Pharr)⁴
3. The User's Guide⁵

⁴<https://pharr.org/matt/blog/2018/04/18/ispc-origins.html>

⁵<https://ispc.github.io/ispc.html>

ispc SPMD gang abstraction using SIMD instructions

SPMD implementation in ispc

- Call to `ispc` function spawns gang of program instances.
- All instances done when function returns.
- Gang size is SIMD width or a small multiple.
- Lockstep execution one "line" at a time.
- Each instance gets a copy of each non-uniform variable.

```
export void f(uniform int n, uniform float as[]) {  
    for (int i = programIndex;  
         i < n;  
         i += programCount) {  
        float a = as[i];  
        // All instances finish previous line  
        // before continuing  
        as[i] = a * 2;  
    }  
}
```

Abstraction versus implementation

- **Model is SPMD**

- ▶ Running a gang spawns `programCount` logical execution flows.
- ▶ Each has distinct value of `programIndex`.
- ▶ (PMPH students: sound familiar?).
- ▶ We program against this **abstraction**.

- **Implementation is SIMD**

- ▶ Variables mapped to slots in SIMD registers.
- ▶ SIMD instructions carry out work of gang.
- ▶ Control flow implemented by masking or arithmetic.

- **Abstraction is intentionally leaky**

- ▶ uniform values and cross-instance communication (later) let us mess up.
- ▶ `ispc` concerned with real-world performance, not purity.
- ▶ An expert programmer can often predict the SIMD instructions generated by compiler.

In principle, `ispc` could also generate GPU code! **Good idea?**

Previous example in ispc

```
float powi(float a, int b) {  
    float r = 1;  
    while (b-->0) r *= a;  
    return r;  
}  
  
export void f(uniform int n,  
             uniform float as[],  
             uniform int bs[],  
             uniform float cs[]) {  
    for (int i = 0; i < n; i += programCount) {  
        cs[i] = powi(as[i], bs[i]);  
    }  
}
```

Previous example in `ispc` (better)

```
float powi(float a, int b) {  
    float r = 1;  
    while (b-->0) r *= a;  
    return r;  
}  
  
export void f(uniform int n,  
              uniform float as[],  
              uniform int bs[],  
              uniform float cs[]) {  
    foreach (i = 0 ... n) {  
        cs[i] = powi(as[i], bs[i]);  
    }  
}
```

To inspect generated assembly

```
$ ispc powi.isc --target=avx2 --emit-asm -o powi.s
```


To inspect generated assembly

```
$ ispc powi.isc --target=avx2 --emit-asm -o powi.s
```

To generate object file and header file

```
$ ispc powi.isc --target=avx2 -o powi.o -h powi.h
```

Then from some C program we can say

```
#include "powi.h"
```

```
...
```

```
float *as = malloc(1024*sizeof(float));
```

```
int *bs = malloc(1024*sizeof(int));
```

```
float *cs = malloc(1024*sizeof(float));
```

```
... initialize as, bs, cs ...
```

```
f(1024, as, bs, cs);
```

Mandelbrot in C

```
static inline int mandel(float c_re, float c_im, int count) {  
    float z_re = c_re, z_im = c_im;  
    int i;  
    for (i = 0; i < count; ++i) {  
        if (z_re * z_re + z_im * z_im > 4.)  
            break;  
        float new_re = z_re*z_re - z_im*z_im;  
        float new_im = 2.f * z_re * z_im;  
        z_re = c_re + new_re;  
        z_im = c_im + new_im;  
    }  
    return i;  
}
```

Also valid ispc!

Mandelbrot in C

```
void mandelbrot_c(float x0, float y0,
                  float x1, float y1,
                  int width, int height,
                  int maxIterations,
                  int output[]) {
    float dx = (x1 - x0) / width, dy = (y1 - y0) / height;
    for (int j = 0; j < height; j++) {
        for (int i = 0; i < width; i++) {
            float x = x0 + i * dx, y = y0 + j * dy;
            int index = j * width + i;
            output[index] = mandel(x, y, maxIterations);
        }
    }
}
```

Mandelbrot in ispc

```
export void mandelbrot_ispc
    (uniform float x0, uniform float y0,
     uniform float x1, uniform float y1,
     uniform int width, uniform int height,
     uniform int maxIterations,
     uniform int output[]) {
    float dx = (x1 - x0) / width, dy = (y1 - y0) / height;
    for (uniform int j = 0; j < height; j++) {
        foreach (i = 0 ... width) {
            float x = x0 + i * dx, y = y0 + j * dy;
            int index = j * width + i;
            output[index] = mandel(x, y, maxIterations);
        }
    }
}
```

Benefits of **uniform**

- A **uniform** variable has same value in all program instances:
 - + Can be stored in non-vector register.
 - + Takes less space in memory if spilled.
 - + CPU can co-issue with vector instructions.
 - + Dereferencing **uniform** pointer is load, not vector gather.
 - + **uniform** branching avoids masking.
- Unadorned types are **variant** by default:
 - ▶ Each program instance has its own copy.
 - ▶ **uniform** converts automatically to **variant**.

```
float foo[10];           // 10 floats per program instance  
uniform float bar[10]; // 10 floats total
```

uniform and control flow

```
float a = ...;
uniform int b = 0;
if (a == 0) {
    ++b;
    // b is 1
}
else {
    b = 10;
    // b is 10
}
```

- Whether b is 1 or 10 depends on whether any of the values of a in the executing gang were 0.
- Be careful!

SIMD on CPU

Auto-vectorisation

Programming in ISPC

ISPC Performance

Summation in ispc

```
export uniform int sum_ispc(uniform int input[],
                           uniform int n) {
    uniform int sum = 0;
    foreach (i = 0 ... n) {
        sum += reduce_add(input[i]);
    }

    return sum;
}
```

- `reduce_add()` takes varying value and returns uniform sum of that value across all of the active program instances.
- Is this correct?
- Is this optimal?

Summation in ispc – better

```
export uniform int sum_ispc(uniform int input[],  
                           uniform int n) {  
    int sum = 0;  
    foreach (i = 0 ... n ) {  
        sum += input[i];  
    }  
  
    return reduce_add(sum);  
}
```

Writing `reduce_add()` ourselves

```
uniform int own_reduce_add(int x) {  
    uniform int sums[programCount];  
    sums[programIndex] = x;  
    if (programIndex == 0) {  
        for (uniform int i = 1; i < programCount; i++) {  
            sums[0] += sums[i];  
        }  
    }  
    return sums[0];  
}
```

Builtin one is probably smarter.

Other functions for cross-instance communication

```
// Returns 'x' provided by program instance 'i'.  
uniform int32 extract(int32 x, uniform int i);
```

Other functions for cross-instance communication

```
// Returns 'x' provided by program instance 'i'.  
uniform int32 extract(int32 x, uniform int i);  
  
// Returns 'x' provided by program  
// instance 'offset' steps away.  
int32 rotate(int32 value, uniform int offset)
```

Other functions for cross-instance communication

```
// Returns 'x' provided by program instance 'i'.  
uniform int32 extract(int32 x, uniform int i);
```

```
// Returns 'x' provided by program  
// instance 'offset' steps away.  
int32 rotate(int32 value, uniform int offset)
```

```
// Exclusive scan of provided 'v's'.  
int32 exclusive_scan_add(int32 v)
```

1D stencil

```
static inline void relax_c(float *output,  
                           float* input,  
                           int n) {  
    for (int i = 0; i < n; i++) {  
        float l, c, r;  
        l=input[i == 0 ? n-1 : i-1];  
        c=input[i];  
        r=input[(i+1) % n];  
        output[i] = (l + c + r)/3;  
    }  
}
```

Runtime for n=1000000: 140 μ s

Try it with ispc

```
export void relax_ispc_naive(uniform float output[],  
                             uniform float input[],  
                             uniform int n) {  
    foreach (i = 0 ... n) {  
        float l, c, r;  
        l=input[i == 0 ? n-1 : i-1];  
        c=input[i];  
        r=input[(i+1) % n];  
        output[i] = (l + c + r)/3;  
    }  
}
```

Try it with ispc

```
export void relax_ispc_naive(uniform float output[],
                             uniform float input[],
                             uniform int n) {
    foreach (i = 0 ... n) {
        float l, c, r;
        l=input[i == 0 ? n-1 : i-1];
        c=input[i];
        r=input[(i+1) % n];
        output[i] = (l + c + r)/3;
    }
}
```

Runtime for $n=1000000$: $403\mu s$ – **what happened?**

ispc compiler output

```
relax.ispc:6:13: Performance Warning: Modulus  
      operator with varying types is very inefficient.  
      r=input[(i+1) % n];  
              ^^^^^^^
```

```
relax.ispc:4:7: Performance Warning: Gather required  
      to load value.  
      l=input[i == 0 ? n-1 : i-1];  
              ^^^^^^^^^^^^^^^^^
```

```
relax.ispc:6:7: Performance Warning: Gather required  
      to load value.  
      r=input[(i+1) % n];  
              ^^^^^^^
```

Forces **scalarisation**—but at least the compiler will tell us!

Better way of writing it

```
export void relax_ispc(uniform float output[],  
                      uniform float input[],  
                      uniform int n) {  
    if (programIndex == 0) {  
        output[0] =(input[n-1]+input[0]+input[1])/3;  
        output[n-1] = (input[n-2]+input[n-1]+input[0])/3;  
    }  
    foreach (i = 1 ... n-2) {  
        float l, c, r;  
        c=input[i];  
        l=input[i-1];  
        r=input[i+1];  
        output[i] = (l + c + r)/3;  
    }  
}
```

Runtime for $n=1000000$: $32\mu s$ – much better!

Better way of writing it

```
export void relax_ispc(uniform float output[],
                      uniform float input[],
                      uniform int n) {
    if (programIndex == 0) {
        output[0] =(input[n-1]+input[0]+input[1])/3;
        output[n-1] = (input[n-2]+input[n-1]+input[0])/3;
    }
    foreach (i = 1 ... n-2) {
        float l, c, r;
        c=input[i];
        l=input[i-1];
        r=input[i+1];
        output[i] = (l + c + r)/3;
    }
}
```

Runtime for $n=1000000$: $32\mu s$ – **much better!**

If we do the same thing to the C implementation... $38\mu s$.

Memory accesses

Uniform `vs[i]; // 'uniform' i`

```
movss  xmm0, dword ptr [rdi + 4*rax]
shufps xmm0, xmm0, 0
```

Regular `vs[programIndex];`

```
movups (%rdi), %xmm0
```

Irregular `vs[is[programIndex]];`

```
movss    xmm0, dword ptr [rdi + rsi]
insertps xmm0, dword ptr [rdi + rcx], 16
insertps xmm0, dword ptr [rdi + r8], 32
insertps xmm0, dword ptr [rdi + rax], 48
```

ispc can always fall back to scalar code.

The GPU perspective

- GPUs have the notion of *coalesced memory*.
- In the same clock cycle, neighbouring threads should access neighbouring memory locations.
- Allows a single memory bus transaction to service multiple threads.

ispc is similar, but not identical.

- + GPU coalesced memory is *dynamic*—as long as the indexes are OK at runtime, all is well.
- With ispc, the indexing must be *statically* regular.
- This is because (most) CPUs do not actually have real gather instructions.
- GPUs are *throughput-oriented*, CPUs often more about *latency*.

Implementing filtering in `ispc`

```
int filter(float *output, float *input, int n) {  
    int j = 0;  
    for (int i = 0; i < n; i++) {  
        float v = input[i];  
        if (v >= 0) {  
            output[j++] = v;  
        }  
    }  
    return j;  
}
```

- `n=100000`: $461\mu s$
- Looks sequential, but we know better
- How do we filter in parallel?

Filtering in Futhark

```
def filter (as: []f32): []f32 =  
  let keep = map (\a -> if a >= 0 then 1 else 0) as  
  let offsets1 = scan (+) 0 keep  
  let num_to_keep = reduce (+) 0 keep  
  in scatter (replicate num_to_keep 0)  
    (map2 (\i k ->  
          if k == 1  
          then i-1  
          else -1)  
      offsets1 keep)  
    as
```

- scan then scatter
- Is that a good fit for ispc?

Filtering in Futhark

```
def filter (as: []f32): []f32 =  
  let keep = map (\a -> if a >= 0 then 1 else 0) as  
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  in scatter (replicate num_to_keep 0)  
    (map2 (\i k ->  
           if k == 1  
           then i-1  
           else -1)  
      offsets1 keep)  
    as
```

- scan then scatter
- Is that a good fit for ispc?
- **No**, because we do not need to *maximise* parallelism
- n=100000: 51.30 μ s on gpu04-diku-apl

Sliding-window SIMD

Idea: slide a programCount-sized window sequentially over the input.

```
uniform int m = 0;  
foreach (i = 0 ... n) {  
    float j = input[i];  
    int keep = j >= 0;  
    int offset = exclusive_scan_add(keep);  
    output[m + offset] = j;  
    m += reduce_add(keep);  
}  
return m;
```

Correct?

Sliding-window SIMD

Idea: slide a programCount-sized window sequentially over the input.

```
uniform int m = 0;  
foreach (i = 0 ... n) {  
    float j = input[i];  
    int keep = j >= 0;  
    int offset = exclusive_scan_add(keep);  
    output[m + offset] = j;  
    m += reduce_add(keep);  
}  
return m;
```

Correct?

No, might write garbage.

```
uniform int m = 0;  
foreach (i = 0 ... n) {  
    float j = input[i];  
    int keep = j >= 0;  
    int offset = exclusive_scan_add(keep);  
    if (keep) {  
        output[m + offset] = j;  
    }  
    m += reduce_add(keep);  
}  
return m;
```

- n=100000: 407 μ s
- What is the likely culprit?

```
uniform int m = 0;
foreach (i = 0 ... n) {
    float j = input[i];
    int keep = j >= 0;
    int offset = exclusive_scan_add(keep);
    if (keep) {
        output[m + offset] = j;
    }
    m += reduce_add(keep);
}
return m;
```

- $n=100000$: $407\mu s$
- What is the likely culprit?
- That **predicated memory write!**
- Optimisation: turn control flow into data.

```
uniform int m = 0;  
foreach (i = 0 ... n) {  
    float j = input[i];  
    int keep = j >= 0;  
    int offset = exclusive_scan_add(keep);  
    if (!keep) {  
        offset = programCount-1;  
    }  
    output[m + offset] = j;  
    m += reduce_add(keep);  
}  
return m;
```

- $n=100000$: $137\mu s$
- **Why is this valid?**

Summary

- Almost all CPUs support some kind of SIMD instructions.
- Utilising them can result in nontrivial speedup.
- Manual vectorisation sucks.
- Auto-vectorisation sucks.
- The SPMD programming model seems promising.

For the weekly assignment

- Several tasks about implementing things in `ispc`.
- See how fast you can make them go compared to C.
- $100\times$ is when you write Futhark programs; don't expect that much.
- On Hendrix, use `module load ispc`, but you can also use your own computer.