

HWL PL

if you buy call and put on same stock. you get

$$C - P = |S(T) - K| \quad \text{payoff} \quad (S(T) \text{ value of stock at } T)$$

You get same payoff

if you buy stock and borrow loan for K
i.e.

$$\text{payoff} = S(T) - K \quad (\text{value in portfolio})$$

If these portfolios were set

one is cheaper than the other

you may short the ~~cheap~~^{pricey} portfolio
and call the ~~pricey~~^{cheap} portfolio
pocketing the difference with no
liabilities at maturity.

this is risk free profit and not possible
under arbitrage-free assumption.

∴

$$C(t) - P(t) = S(t) - K \quad \forall t.$$