

# EE 443 Capstone Presentation

Jonathan Wong

Dataset	Baseline	?	?	?	?	?
Full						
0.1						
0.02						
0.005						
Average Improvement:						

Welcome!

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Jonathan Wong

Dataset	Baseline	?	?	?	?	?
Full						
0.1						
0.02						
0.005						
Average Improvement:						

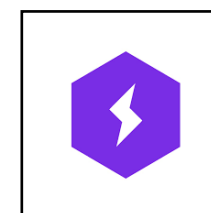
## Experiment #1: Establishing a Baseline

### Motivation:

Establish point of reference for evaluating performance of future experiments.

### Procedures:

Architecture Sweep, Hyperparameter Sweep.



# Establishing a Baseline: Code

## Dataset

```
class BaseDataset(Dataset):
    def __init__(self, datastore, input, image_size=224, da=False):
        if isinstance(input, str):
            with open(input) as f:
                json_data = json.load(f)
                self.data = json_data['annotations']
        elif isinstance(input, list):
            self.data = input

        self.datastore = datastore
        self.image_size = image_size
        self.da = da
        self.transform = A.Compose(
            [
                A.ShiftScaleRotate(shift_limit=0.05, scale_limit=0.15, rotate_limit=15, p=0.5),
                A.RGBShift(r_shift_limit=15, g_shift_limit=15, b_shift_limit=15, p=0.5),
                A.RandomBrightnessContrast(p=0.5)
            ]
        )

    def __len__(self):
        return len(self.data)
```

...

Loads Json, Data Augmentation, Normalization

## DataLoader

```
def get_dataloaders(dataset, batch_size=16, num_workers=2):
    # Calculate Split
    val_split = 0.2 # Hardcoded 20%
    dataset_size = len(dataset)
    indices = list(range(dataset_size))
    split = int(np.floor(val_split * dataset_size))

    # Shuffle Data
    np.random.shuffle(indices)

    # Split Base Dataset into Training and Validation Datasets
    train_indices, val_indices = indices[split:], indices[:split]
    train_sampler = SubsetRandomSampler(train_indices)
    val_sampler = SubsetRandomSampler(val_indices)

    # Dataloaders
    train_dataloader = DataLoader(dataset, batch_size, num_workers=num_workers, sampler=train_sampler)
    val_dataloader = DataLoader(dataset, batch_size, num_workers=num_workers, sampler=val_sampler)

    return train_dataloader, val_dataloader

def get_test_dataloader(datastore, test_json):
    testset = BaseDataset(datastore, test_json)
    test_dataloader = DataLoader(testset, batch_size=32, num_workers=2)
    return test_dataloader
```

...

Sets Batch Size

# Establishing a Baseline: Code

## Model

```
class BaseNet(LightningModule):
    def __init__(self, model_type='efficientnet_b0', lr=4e-4, weighted_loss=None, hist=None, beta=None):
        super().__init__()
        self.save_hyperparameters()

        # Create backbone
        backbone = timm.create_model(model_type, pretrained=True)
        layers = list(backbone.children())[:-1]
        [fc] = list(backbone.children())[-1:]
        self.feature_extractor = nn.Sequential(*layers)
        self.classifier = nn.Linear(fc.in_features, 50)

        # Weighted Loss
        self.weighted_loss = WeightedLoss(weighted_loss, hist, beta)

        # Metrics
        self.train_acc = torchmetrics.Accuracy()
        self.valid_acc = torchmetrics.Accuracy()
        self.test_acc = torchmetrics.Accuracy()
        self.preds = []
        self.labels = []
```



...

Architecture, Metrics, Loss Function

## Training Script

```
class Baseline(ExperimentInterface):
    def run_experiment(self, args: dict) -> None:
        # 1) Init Data Components
        train_json = str(Path(args['datastore']) / 'train.json')
        test_json = str(Path(args['datastore']) / 'test.json')
        dataset = BaseDataset(args['datastore'], train_json, image_size=args['image_size'], da=args['augment_data'])

        train_dataloader, val_dataloader = get_dataloaders(dataset, batch_size=args['batch_size'], num_workers=args['num_workers'])
        test_dataloader = get_test_dataloader(args['datastore'], test_json)

        # 2) Init Model
        if args['weighted_loss'] is not None:
            hist = get_histogram(process_json(train_json))
            model = BaseNet(model_type=args['model'], lr=args['lr'], weighted_loss=args['weighted_loss'], hist=hist, beta=args['beta'])
        else:
            model = BaseNet(model_type=args['model'], lr=args['lr'])

        # 3) Init Trainer
        trainer = Trainer(gpus=args['gpus'], max_epochs=args['epochs'],
                        checkpoint_callback=True,
                        logger=TensorBoardLogger(save_dir='lightning_logs'))

        # 4) Run Training
        trainer.fit(model, train_dataloader, val_dataloader)
        trainer.save_checkpoint("training_end.ckpt")

        # 5) Run Inference
        result = trainer.test(model, test_dataloader)
        print(result)
```

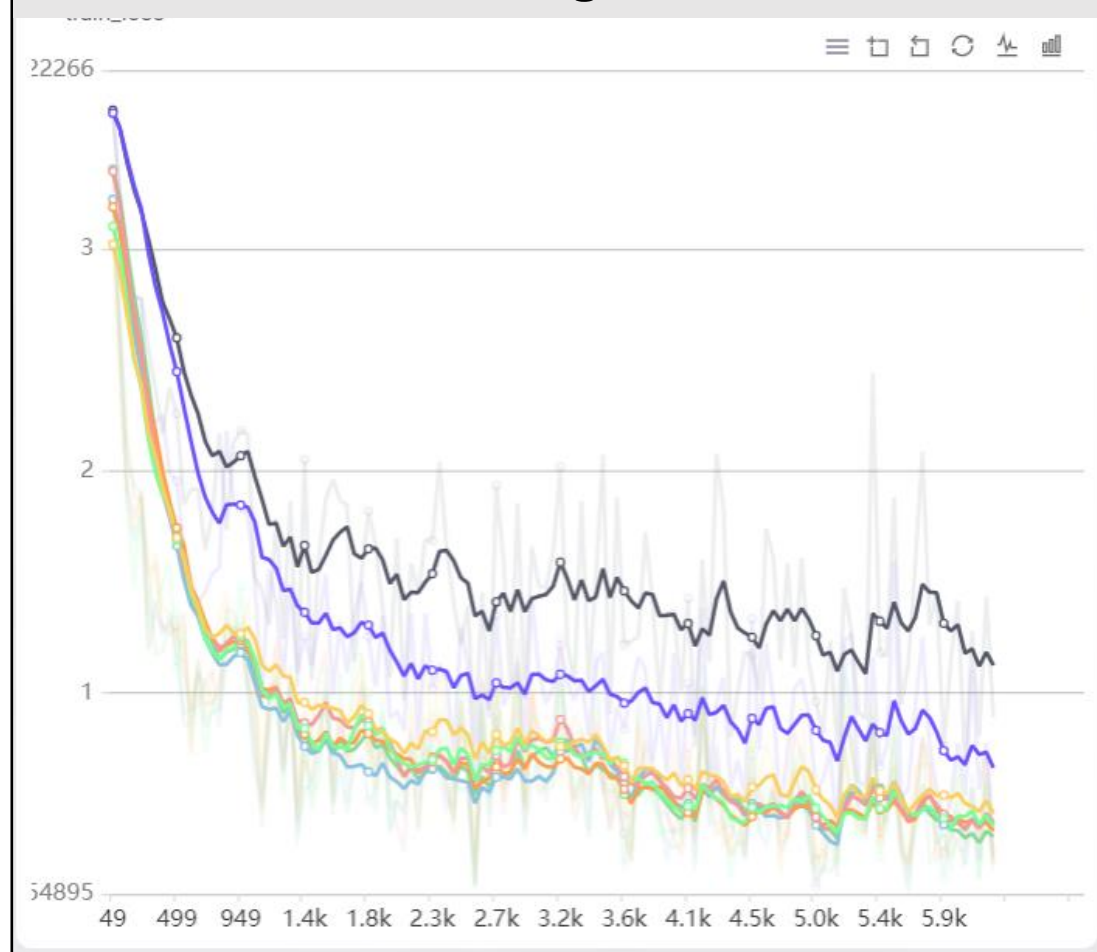


...

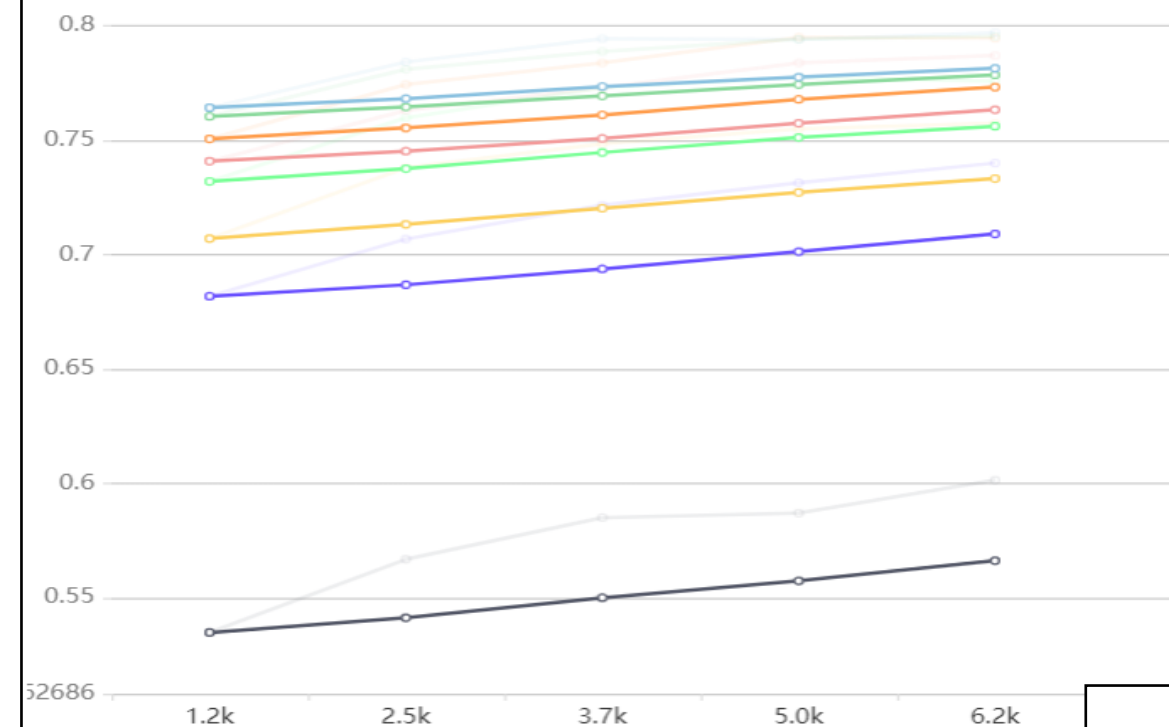
Dataset, DataLoader, Trainer

# Establishing a Baseline: Architecture Sweep

## Training Loss



## Validation Accuracy



GRID-AI

```
train.py \  
--datastore grid:cifar50:2 \  
--model "['resnet34d', 'resnet50', 'resnet50d', \  
'densenet121', 'efficientnet_b0', 'efficientnet_b1_pruned']"
```

# Establishing a Baseline: Architecture Sweep

## Results

Model Name	Test Accuracy	# Parameters
efficientnet_b2	0.804	10 M
resnet50d	0.793	22 M
efficientnet_b1	0.7892	8 M
efficientnet_b0	0.788	5 M
densenet121	0.770	20 M
resnet50	0.758	22 M
resnet34d	0.730	20 M



Selected **efficientnet0** architecture as baseline.

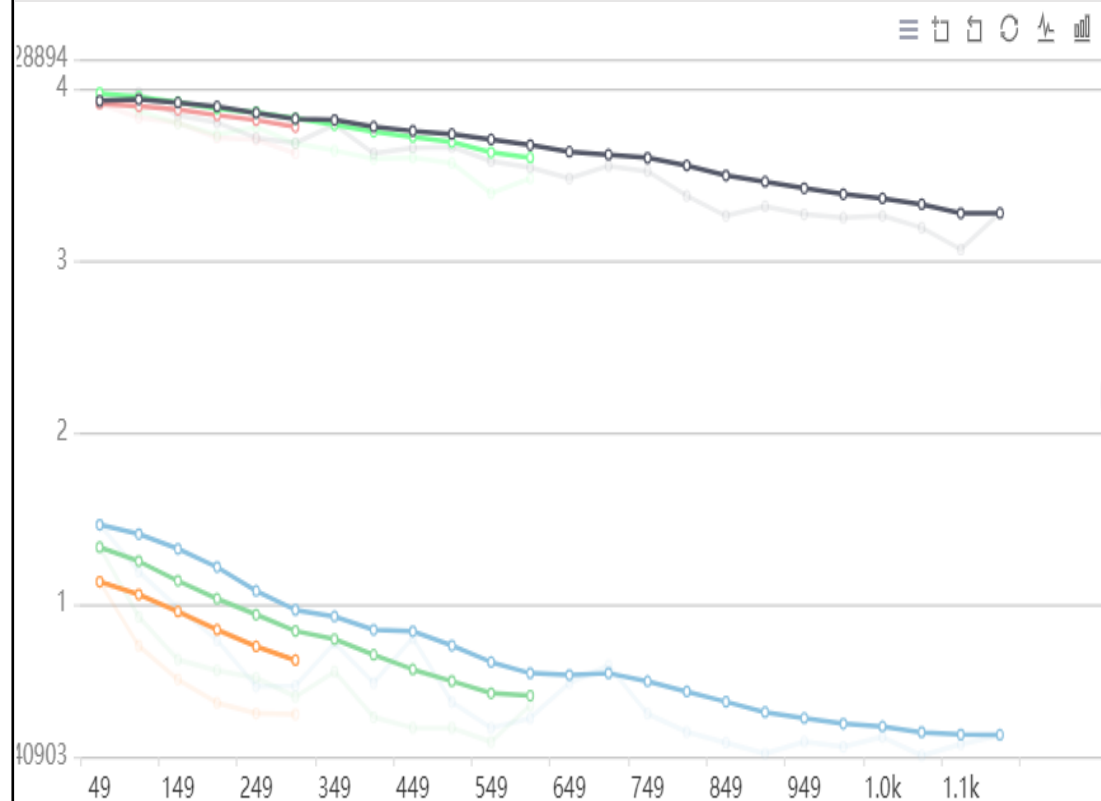
Least parameters for highest accuracy for quick training times.

## Analysis:

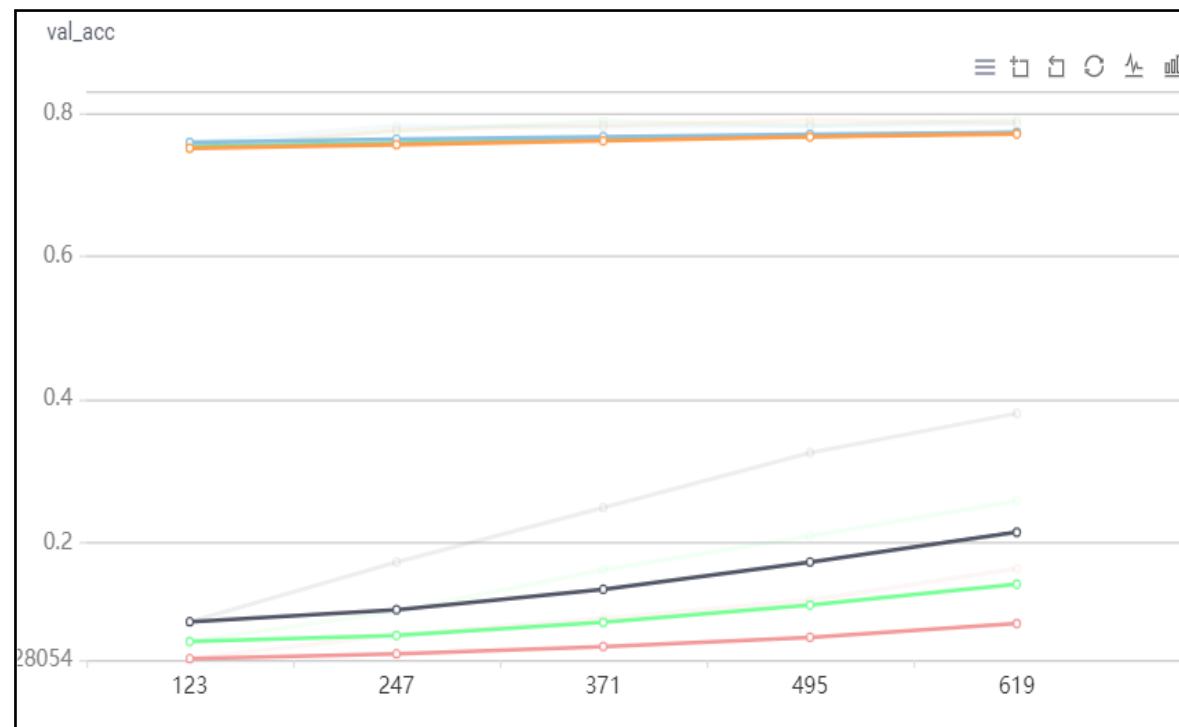
- Models with more hyperparameters tend to overfit
- EfficientNet family is most accurate for the least parameters, hence its name!

# Establishing a Baseline: Hyperparameter Sweep

## Training Loss



## Validation Accuracy



```
train.py \  
--datastore grid:cifar50-imbalance-01:2 \  
--model efficientnet_b0 \  
--batch_size "[16, 32, 64, 128]" \  
--lr "[1e-5, 4e-4, 8e-3, 2e-3]"
```

GRID-AI

# Establishing a Baseline: Hyperparameter Sweep

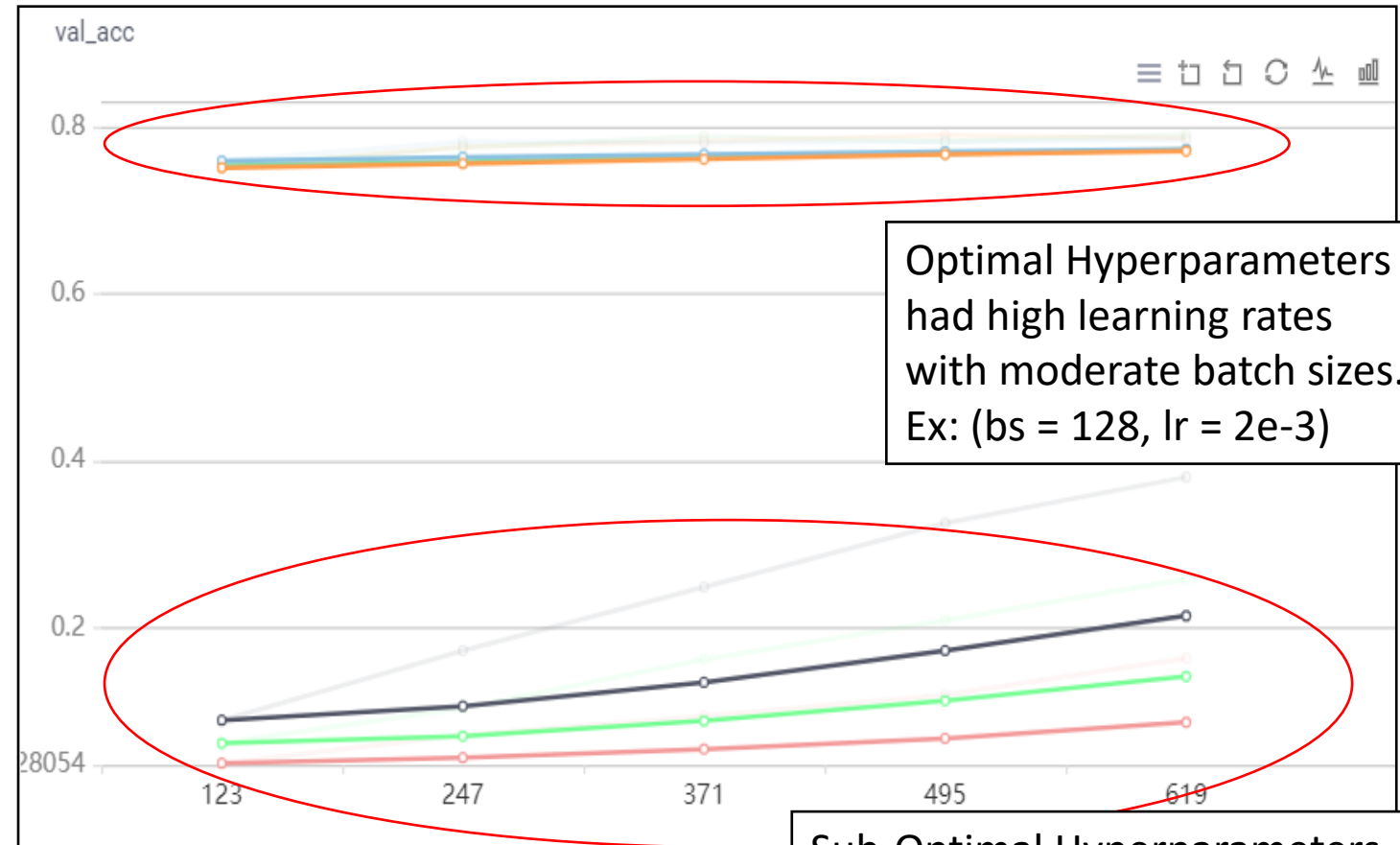
## Results

Repeat sweep for each dataset...

Dataset	Test Accuracy
Full	0.792
0.1	0.7296
0.02	0.6304
0.005	0.5446

## Analysis:

- Provided the most optimal hyperparameters, accuracy of model decreases by approximately 10% on with each imbalanced dataset.



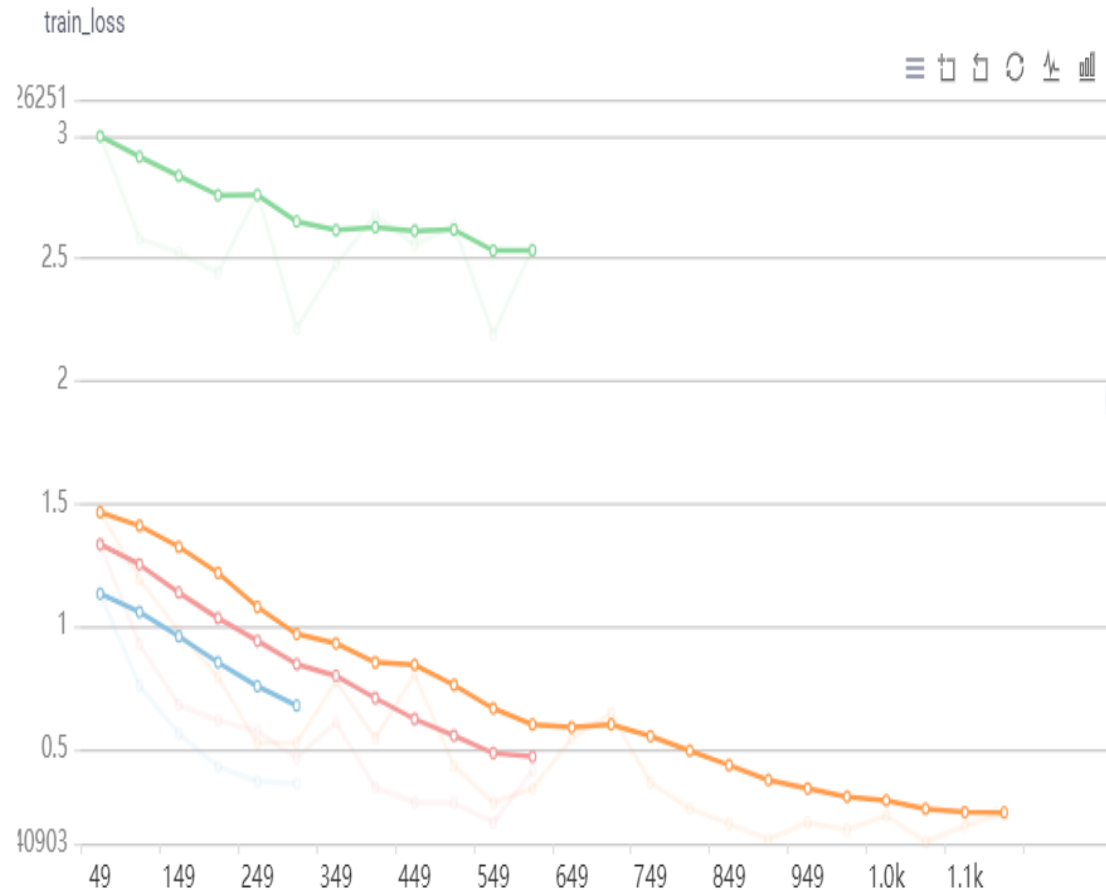
Optimal Hyperparameters had high learning rates with moderate batch sizes.  
Ex: (bs = 128, lr = 2e-3)

Sub-Optimal Hyperparameters had extremely low learning rates and large batch sizes.  
Ex: (bs = 512, lr = 1e-5)

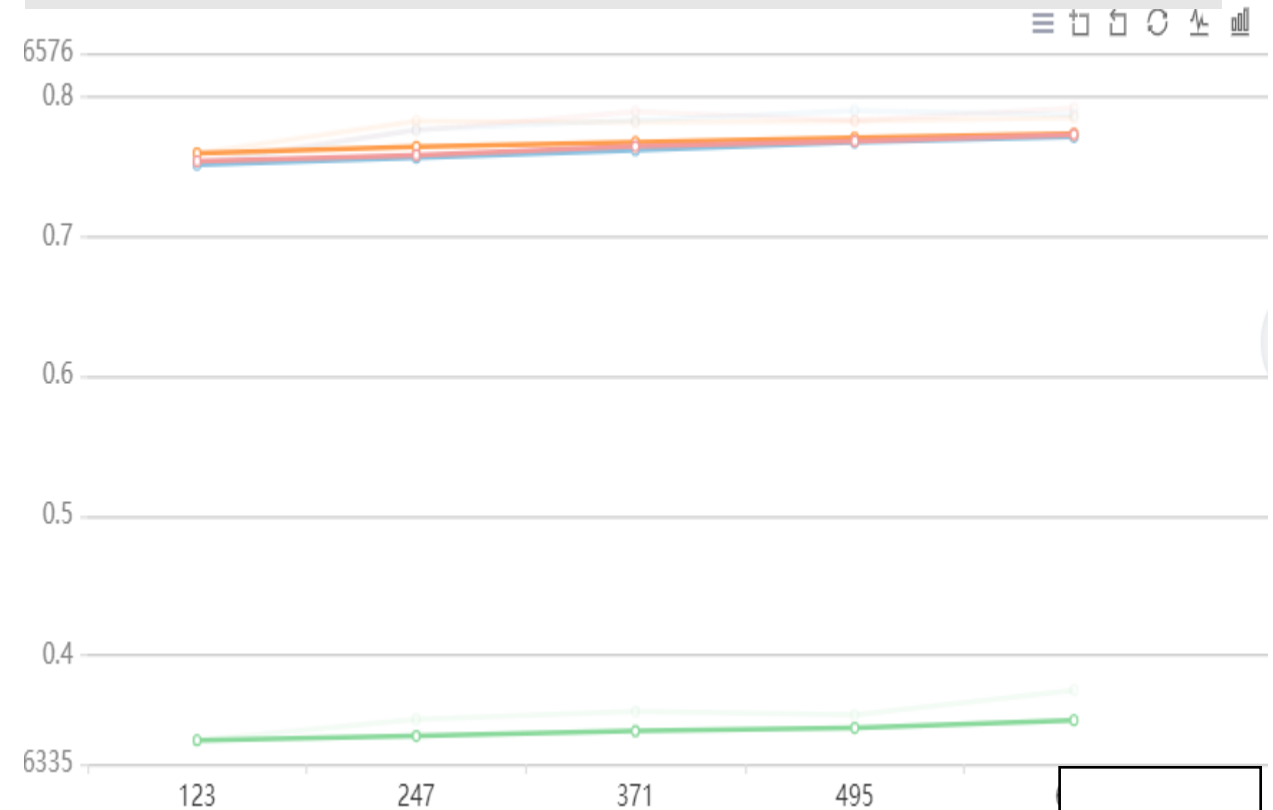


# Establishing a Baseline: How about Data Augmentation?

## Training Loss



## Validation Accuracy



```
train.py \  
--datastore grid:cifar50-imbalance-01:2 \  
--augment_data True \  
--batch_size 64 \  
--lr 2e-3
```

**GRID-<sup>AI</sup>**

Performs Very Poorly!

# Model Summary

Dataset	Baseline	?	?	?	?	?
Full	0.792					
0.1	0.7296					
0.02	0.6304					
0.005	0.5446					
Average Improvement:						

Experiment 1 Complete!

# Model Summary

Dataset	Baseline	Artificial Balancing	?	?	?	?
Full	0.792					
0.1	0.7296					
0.02	0.6304					
0.005	0.5446					
Average Improvement:						

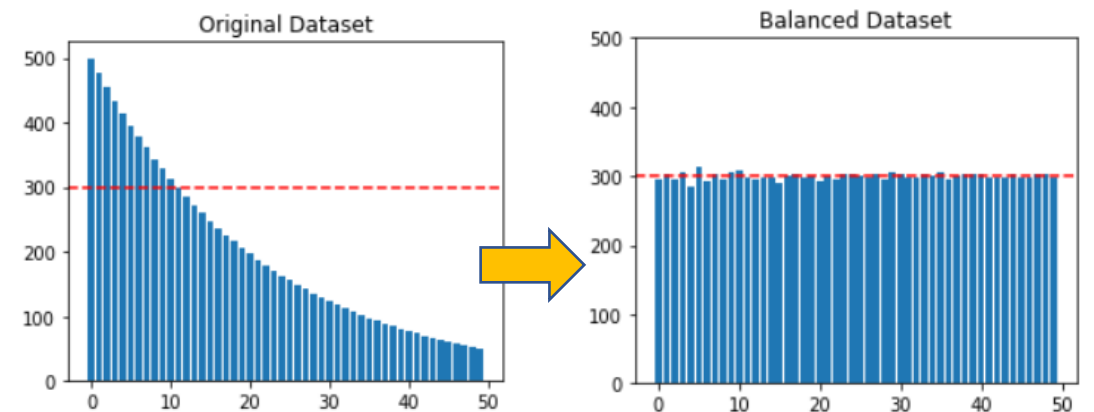
## Experiment #2: Artificial Balancing

### Motivation:

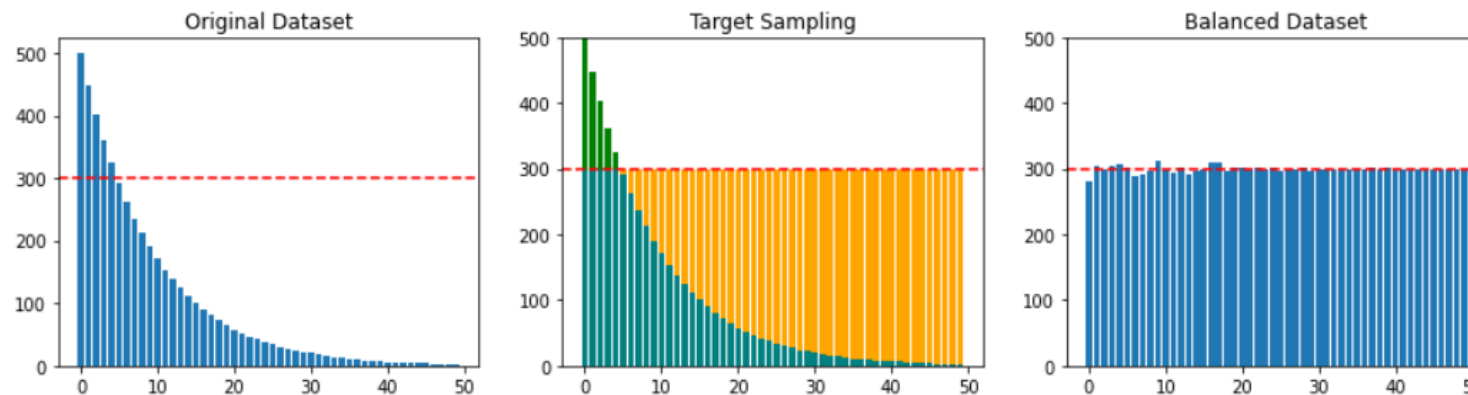
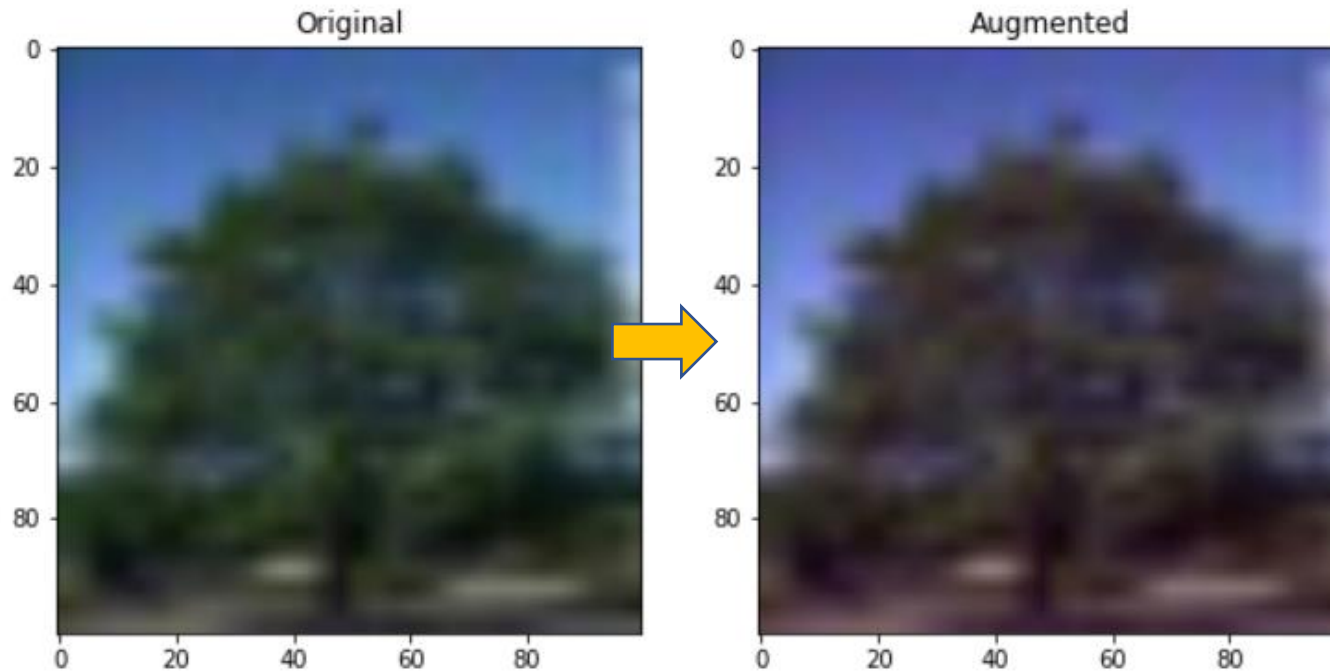
Shape the training dataset match the uniform test distribution.

### Procedures:

Downsampling and Upsampling with Data Augmentation.



# Artificial Balancing: Implementation



Algorithm:

- 1) Calculate Histogram
- 2) Calculate Sampling Rate:  
Threshold Value / Count

Ex: Threshold Value = 300

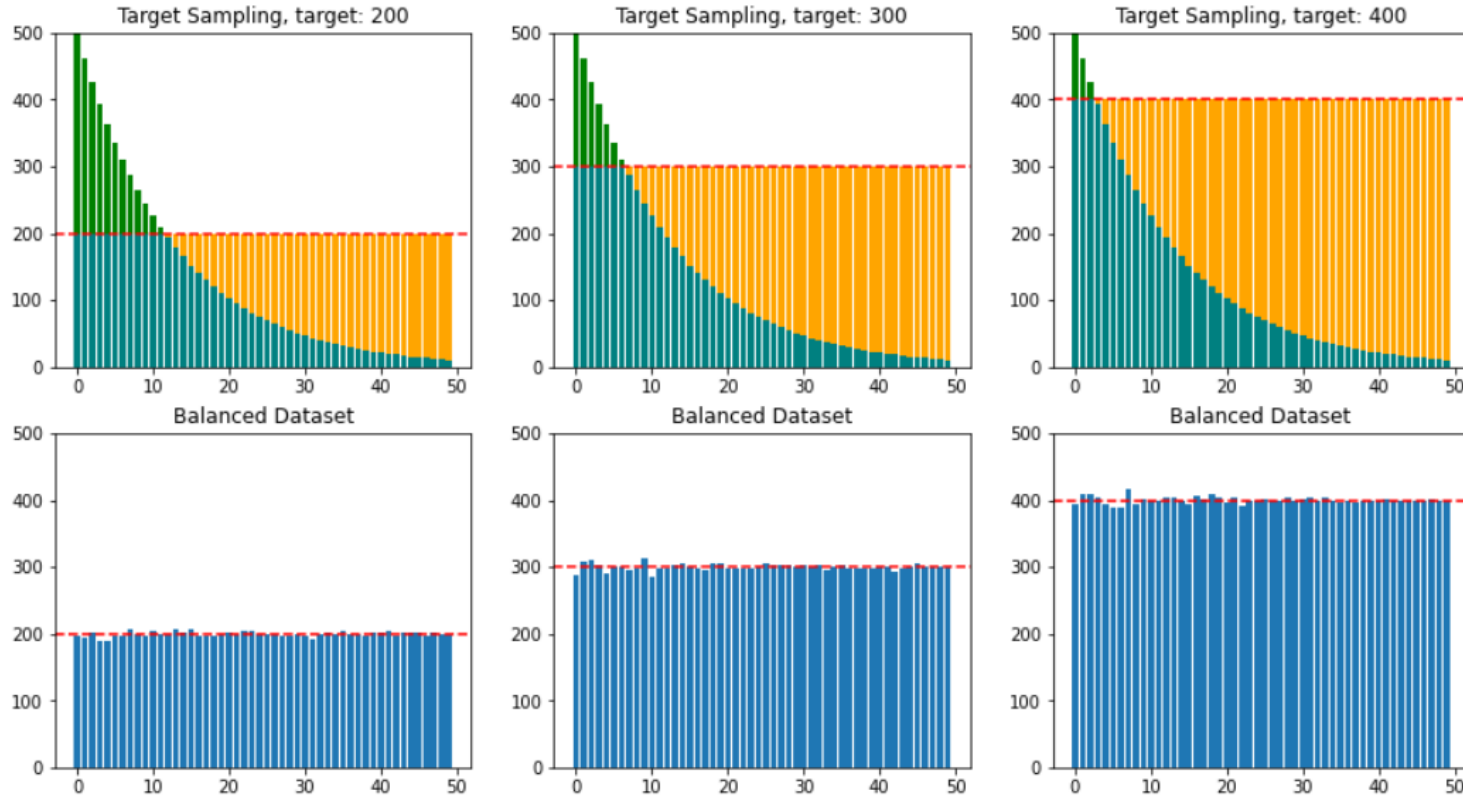
(Class = 0, Count = 500)  $\Rightarrow 300/500 \Rightarrow 0.6$

(Class = 20, Count = 100)  $\Rightarrow 300/100 \Rightarrow 3$

For decimal values, we generate a random number and perform down/up sampling if the number lies with the  $[0-0.x]$  range.

- 3) Iterate through dataset applying sampling rate.

# Artificial Balancing: Implementation



## Algorithm:

- 1) Calculate Histogram
- 2) Calculate Sampling Rate:  
Threshold Value / Count

Ex: Threshold Value = 300

(Class = 0, Count = 500)  $\Rightarrow 300/500 \Rightarrow 0.6$

(Class = 20, Count = 100)  $\Rightarrow 300/100 \Rightarrow 3$

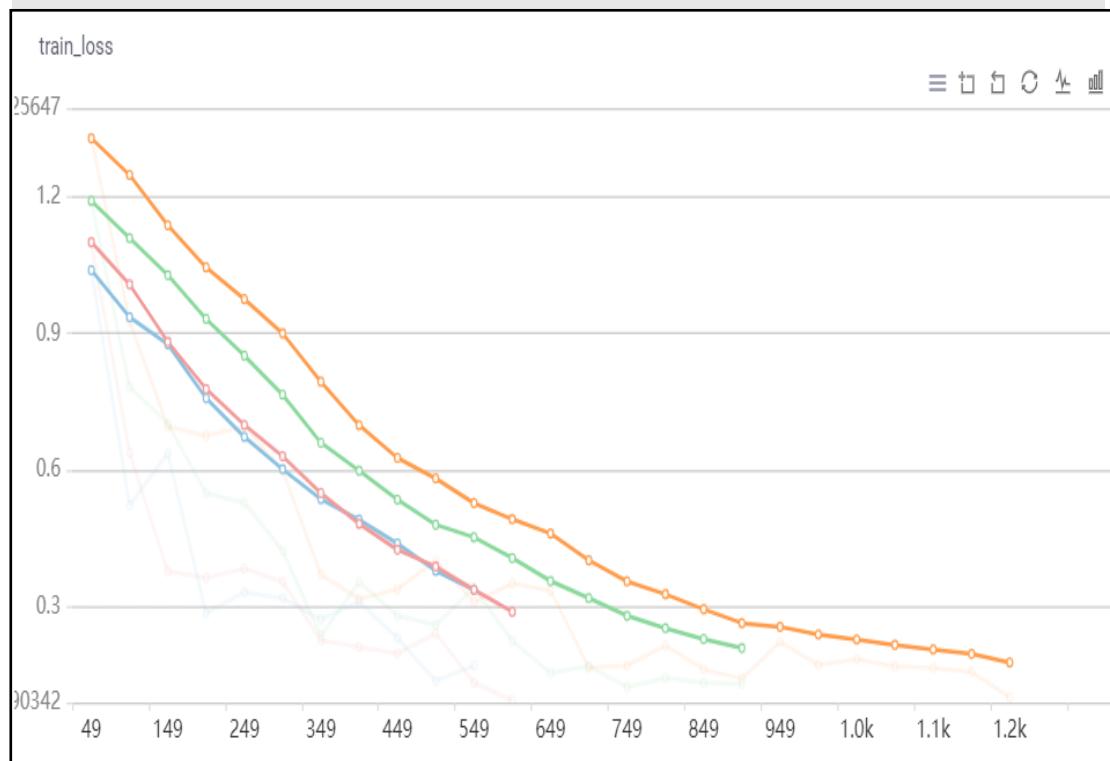
For decimal values, we generate a random number and perform down/up sampling if the number lies with the  $[0-0.x]$  range.

- 3) Iterate through dataset applying sampling rate.

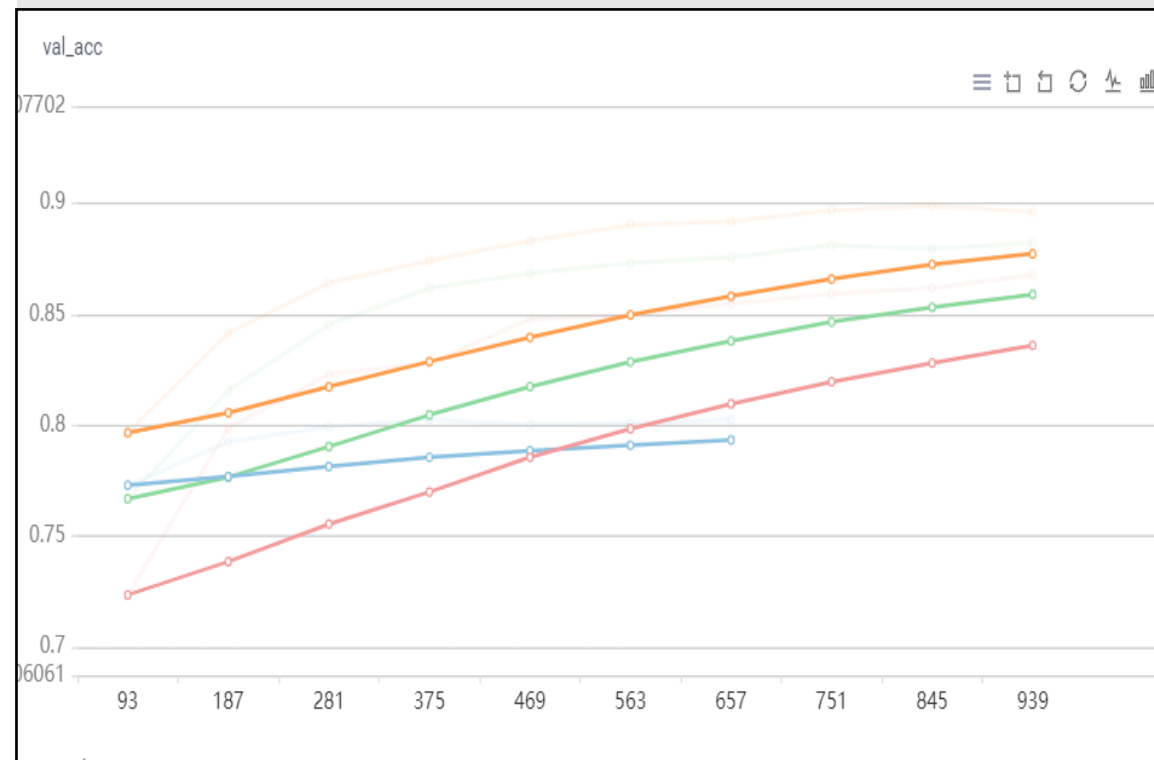
Threshold Value is also configurable and factored into hyperparameter sweep. In general, a low threshold produced higher performance, in which benefits of upsampling balanced benefits of downsampling.

# Artificial Balancing: Training

## Training Loss



## Validation Accuracy



```
train.py \  
--datastore grid:cifar50-balanced-0005:4 \  
--batch_size 128 \  
--lr 2e-3 \  
--epochs 10
```

**GRID-AI**

Performs Better!

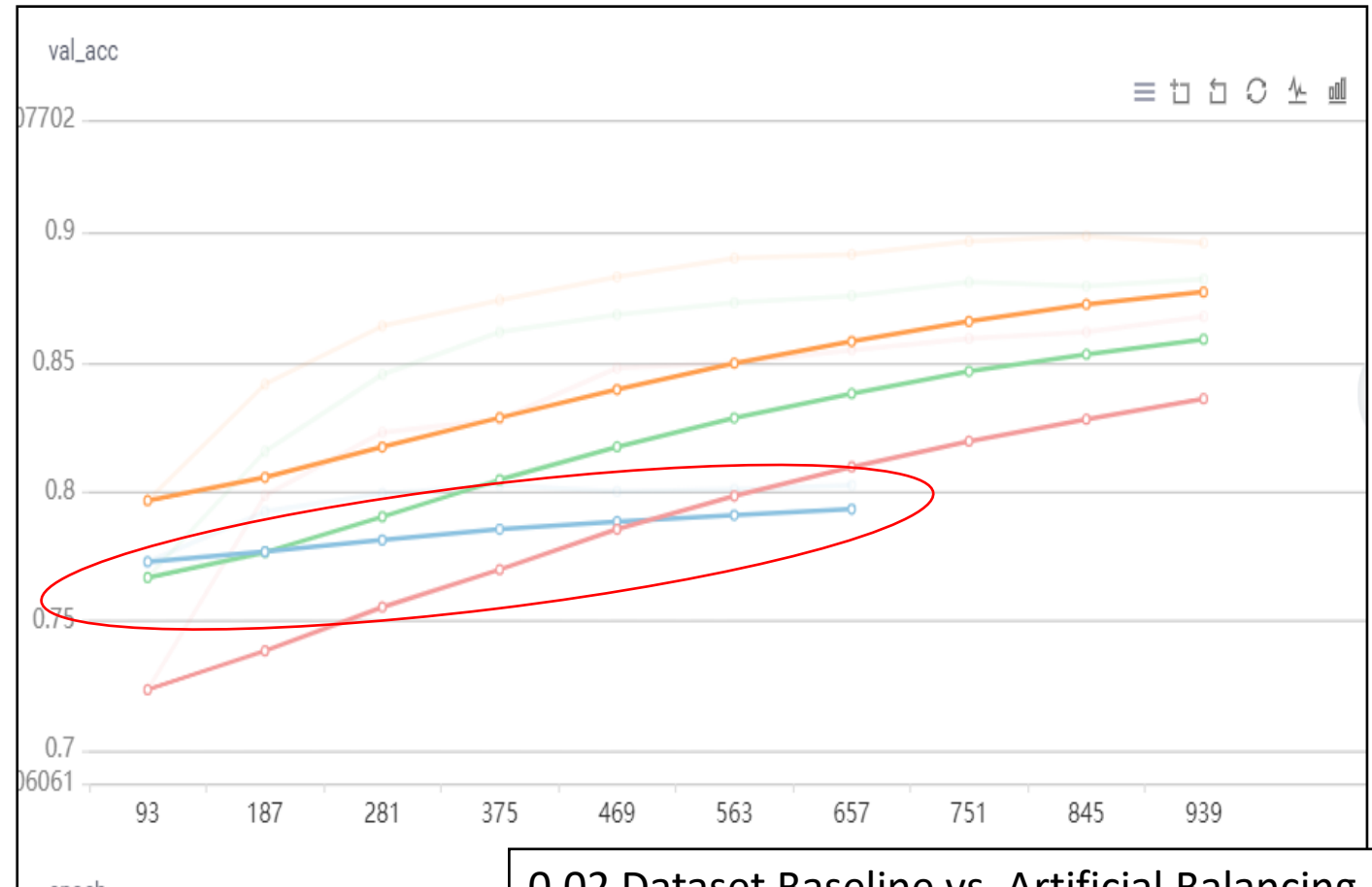
# Artificial Balancing: Training

## Results

Repeat Balancing for each dataset...

Dataset	Test Accuracy
Full	N/A
0.1	0.733
0.02	0.6788
0.005	0.5688

Average Improvement:	0.024
----------------------	-------



0.02 Dataset Baseline vs. Artificial Balancing at thresholds of [200, 300, 400].

All exceed previous accuracy!

# Model Summary

Dataset	Baseline	Artificial Balancing	?	?	?	?
Full	0.792					
0.1	0.7296	0.733				
0.02	0.6304	0.6788				
0.005	0.5446	0.5688				
Average Improvement:		0.024				

Experiment 2 Complete!

Artificial Balancing is labor-intensive and not a scalable solution. Can we do better?



# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	?	?	?
Full	0.792					
0.1	0.7296	0.733				
0.02	0.6304	0.6788				
0.005	0.5446	0.5688				
Average Improvement:		0.024				

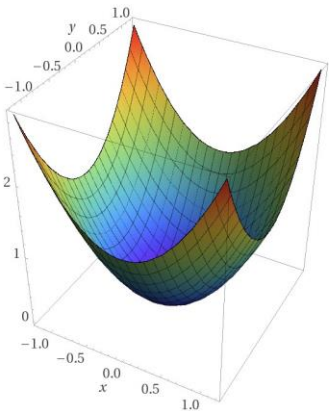
## Experiment #3: Weighted Loss

### Motivation:

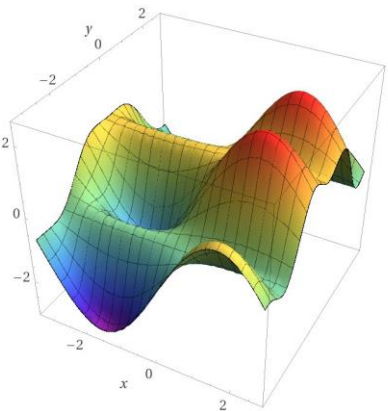
Emulate uniform training distribution without artificially balancing dataset.

### Procedures:

Weighted Loss Equations



Computed by Wolfram|Alpha



Computed by Wolfram|Alpha

# Weighted Loss: Implementation

## Equations:

### Inverse Number of Samples (INS)

$$w_{n,c} = \frac{1}{\text{Number of Samples in Class } c}$$

### Inverse Square Number of Samples (ISNS)

$$w_{n,c} = \frac{1}{\sqrt[2]{\text{Number of Samples in Class } c}}$$

### Effective Number of Samples (ENS)

$$w_{n,c} = \frac{1}{E_{n_c}}$$

$$E_{n_c} = \frac{1 - \beta^{n_c}}{1 - \beta}$$

## Code:

```
# Weighted Loss Functions
class WeightedLoss:
    def __init__(self, weighted_loss, hist, beta=None):
        # Store arguments, Calculate Normalized Weights
        if weighted_loss == "ins":
            weights = torch.tensor([1.0 / sample_count for sample_count in hist.values()])
            self.weight_map = weights / torch.sum(weights)

        elif weighted_loss == "isns":
            weights = torch.sqrt(torch.tensor([1.0 / sample_count for sample_count in hist.values()]))
            self.weight_map = weights / torch.sum(weights)

        elif weighted_loss == "ens":
            sample_counts = torch.tensor(list(hist.values()))
            e_numerator = 1.0 - torch.pow(beta, sample_counts)
            e_denominator = 1.0 - beta
            weights = e_denominator / e_numerator
            self.weight_map = weights / torch.sum(weights)

        else: # Identity
            self.weight_map = torch.ones(50)

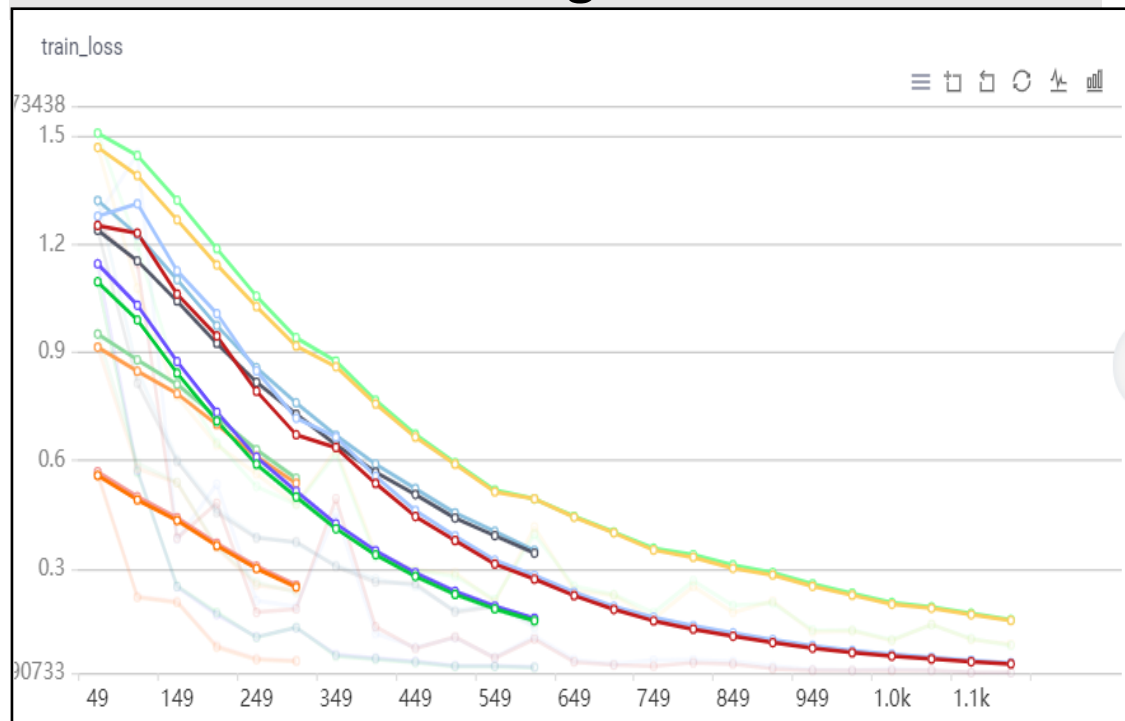
        # Store weights inside Cross Entropy Module
        self.loss = nn.CrossEntropyLoss(weight=self.weight_map.cuda())

    def __call__(self, logits, labels):
        return self.loss(logits, labels)
```

Simply Pass Weight Vectors  
to PyTorch Module

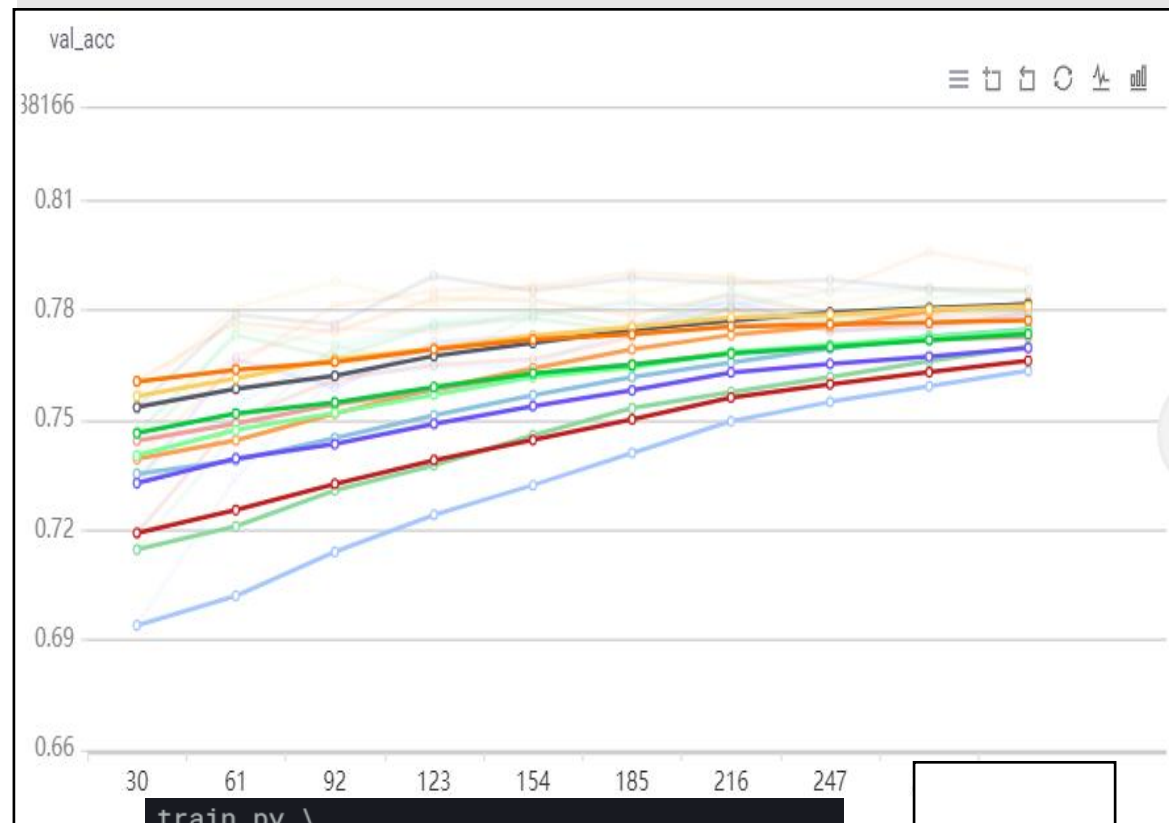
# Weighted Loss: Loss Function Sweep

## Training Loss



```
train.py \  
--datastore grid:cifar50-imbalance-01:2 \  
--batch_size "[64, 128, 256]" \  
--lr "[8e-3, 2e-3]" \  
--weighted_loss "['ins', 'isns']" \  
--epochs 10
```

## Validation Accuracy



```
train.py \  
--datastore grid:cifar50-imbalance-01:2 \  
--batch_size "[64, 128, 256]" \  
--lr "[8e-3, 2e-3]" \  
--epochs 10 \  
--weighted_loss ens \  
--beta "[0.99, 0.999]"
```

**GRID-AI**

Repeated for each dataset.

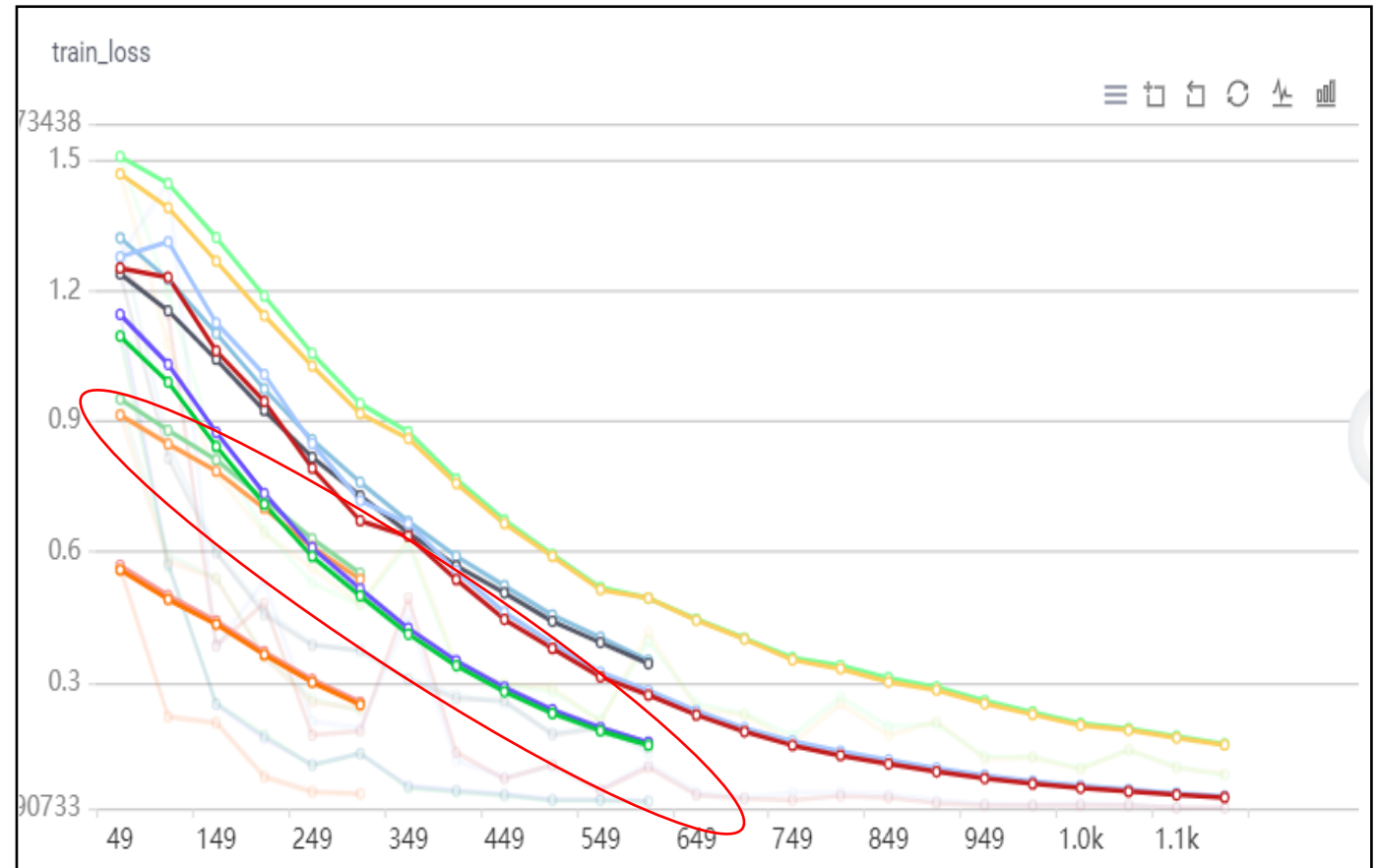
# Weighted Loss: Loss Function Sweep

## Results

Repeat Balancing for each dataset...

Dataset	Test Accuracy
Full	N/A
0.1	0.7458
0.02	0.6798
0.005	0.5352

Average Improvement:	0.019
----------------------	-------



0.01 Dataset trained on ins, isns, and ens loss functions. Comparable performance, no one weighted loss function is better in this case.

All exceed previous accuracy!

# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	?	?	?
Full	0.792					
0.1	0.7296	0.733	0.7458			
0.02	0.6304	0.6788	0.6798			
0.005	0.5446	0.5688	0.5352			
Average Improvement:		0.024	0.019			

Experiment 3 Complete!

Weighted Loss serves as good substitute to Artificial Balancing.

# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging	?	?
Full	0.792					
0.1	0.7296	0.733	0.7458			
0.02	0.6304	0.6788	0.6798			
0.005	0.5446	0.5688	0.5352			
Average Improvement:		0.024	0.019			

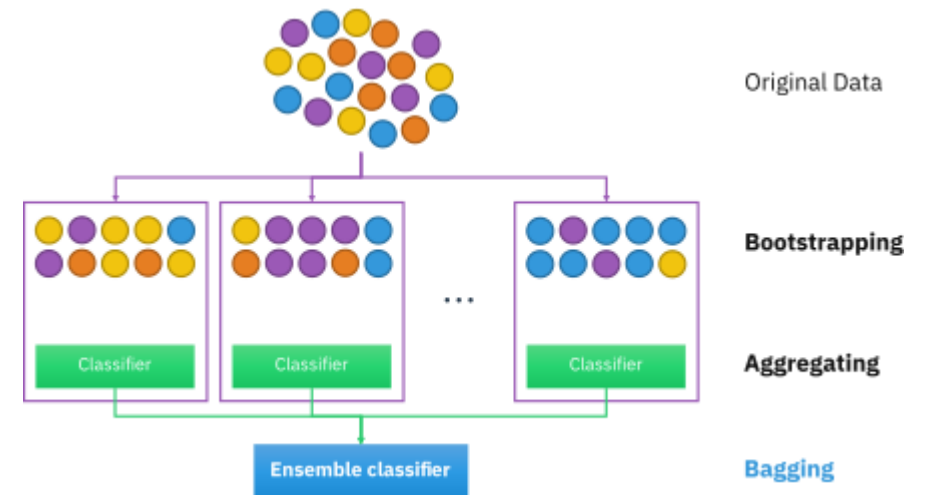
## Experiment #4: Ensemble Training, Bagging

### Motivation:

Combine multiple model copies to form more robust predictor.

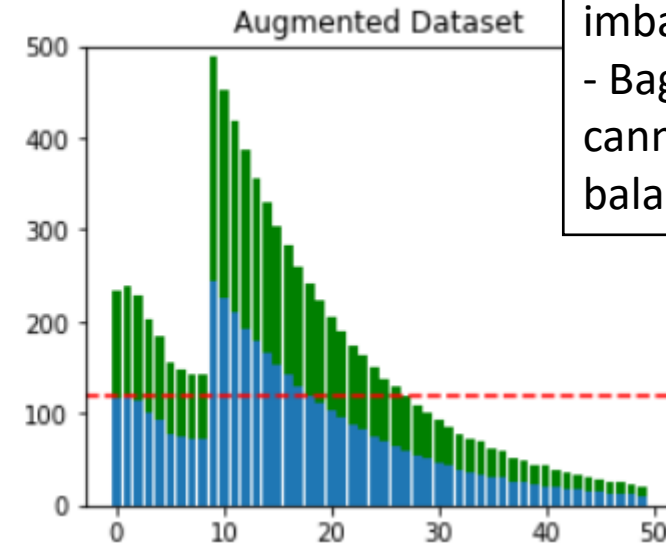
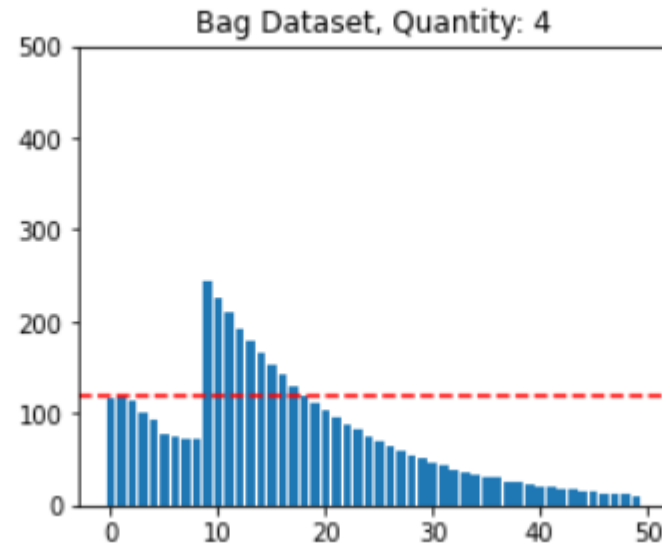
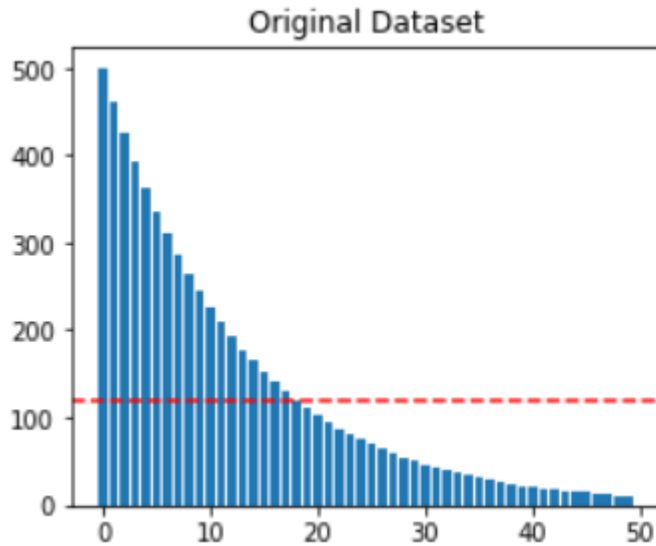
### Procedures:

Balanced Dataset Creation



# Bagging: Implementation

## Dataset Curation

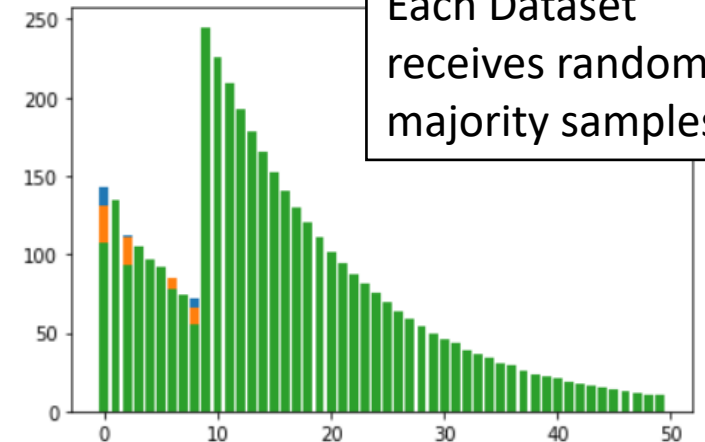


Comments:

- DA worsens class imbalance
- Bagged Datasets cannot be completely balanced.

Algorithm:

- 1) Compute Histogram on Training Dataset
- 2) Compute number of bags based on threshold value ( $\text{max} // \text{threshold}$ )
- 3) Split Dataset on Median
- 4) Copy samples in minority class to each bag
- 5) Deal out remaining samples from randomly shuffled majority class



Each Dataset receives random majority samples.

# Bagging: Implementation

## Code

```
def create_bags(args, imbalanced_json):  
    # 1) Load Data  
    entries = process_json(imbalanced_json)
```

```
    # 2) Calculate Number of Learners
```

```
    hist = get_histogram(entries)
```

```
    num_bags = max(hist.values()) // args['threshold']
```

```
    # 3) Create Datasets
```

```
    majority, minority = split_histogram(hist, entries, args['threshold'])
```

```
    random.shuffle(majority) # need shuffle the deck!
```

```
    bags = []
```

```
    for start in range(num_bags):
```

```
        current_bag = majority[start:num_bags] + minority
```

```
        bags.append(BaseDataset())
```

```
    return bags
```

1) Calculate Histogram

2) Compute Number of Bags

3) Split Histogram into Majority/Minority Classes

4) Shuffle and deal out decks



# Bagging: Implementation

## Code

```
class ModelEnsemble(LightningModule):
    def __init__(self, models):
        super().__init__()
        # Create Models
        self.models = models

        # For Metrics
        self.test_acc = torchmetrics.Accuracy()
        self.preds = []
        self.labels = []

    def forward(self, x):
        prediction = torch.zeros(50).cuda()
        weight = 1.0 / len(self.models)
        for model in self.models:
            model.eval()
            prediction = prediction + (weight * F.softmax(model(x), dim=1))
        return prediction
```

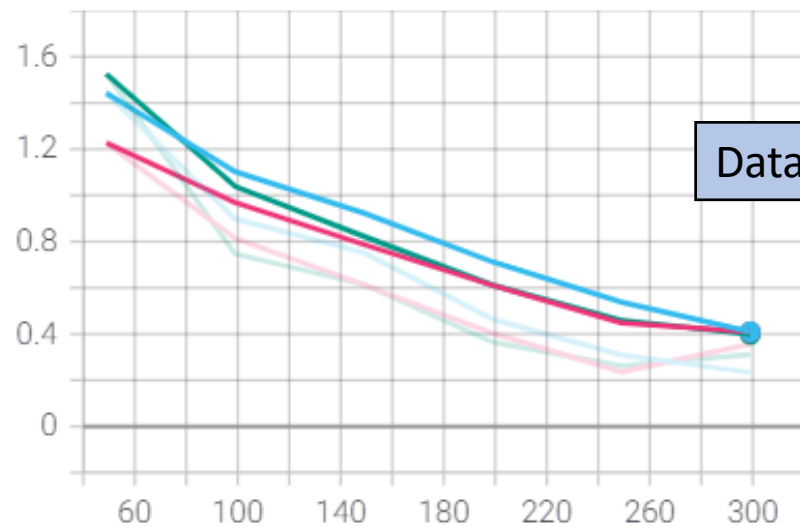
1) Accept List of Trained Models

2) Forward Pass performs simple average over softmax output

# Bagging: Training

## Training Loss

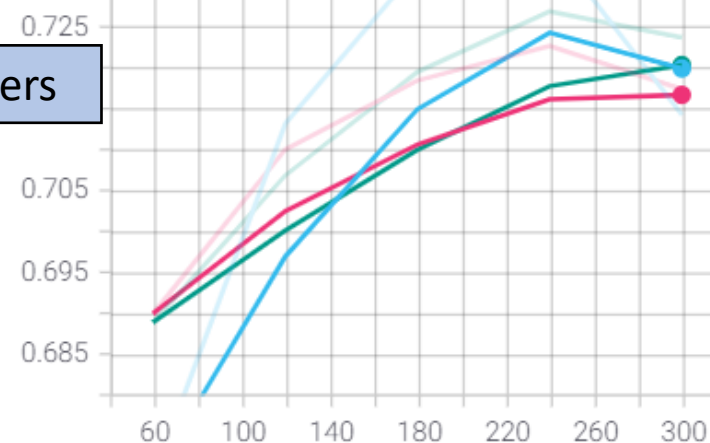
train\_loss



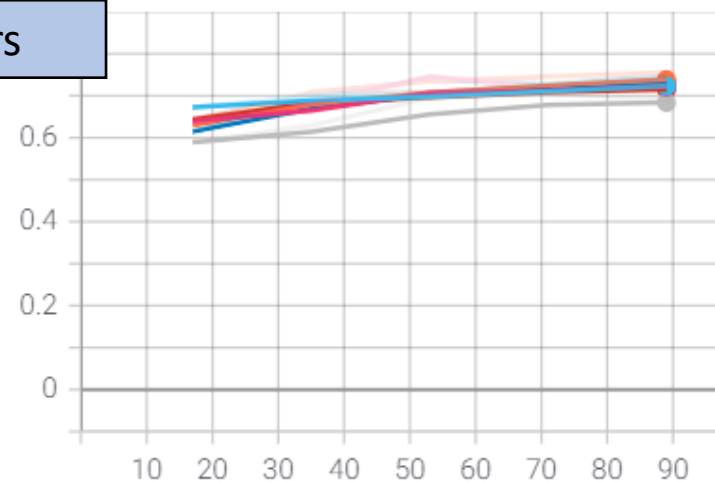
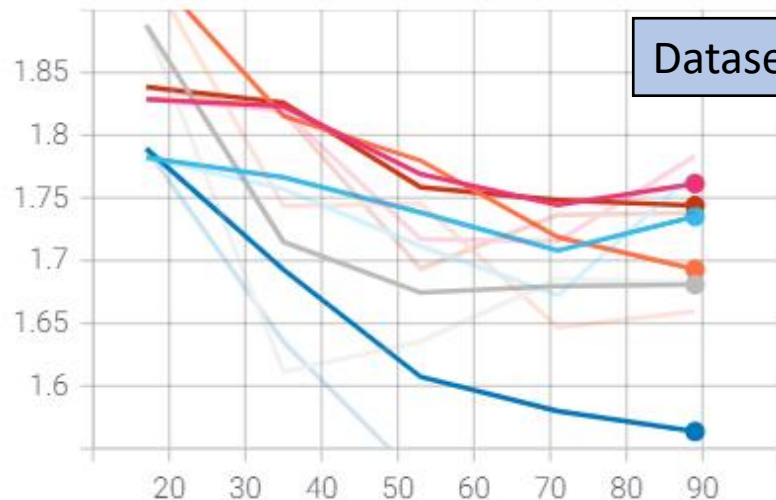
Dataset: 0.1 - 3 Learners

## Validation Accuracy

val\_acc



Dataset: 0.005 - 5 Learners



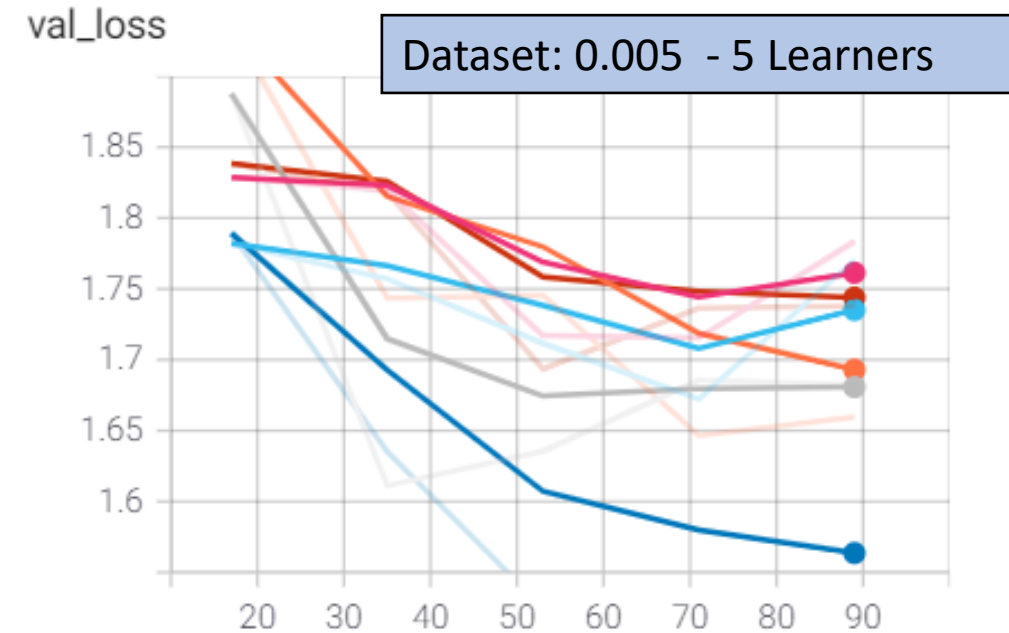
# Bagging: Training

## Results

Repeat Balancing for each dataset...

Dataset	Test Accuracy	Average Learner Accuracy
Full	N/A	N/A
0.1	0.7350	0.72
0.02	0.6760	0.65
0.005	0.5454	0.53

<b>Average Improvement:</b>	0.019
-----------------------------	-------



Each learner descends down objective function in different directions and ends up at different loss. Combined learners make for stronger predictor.

# Bagging: Training

## Results

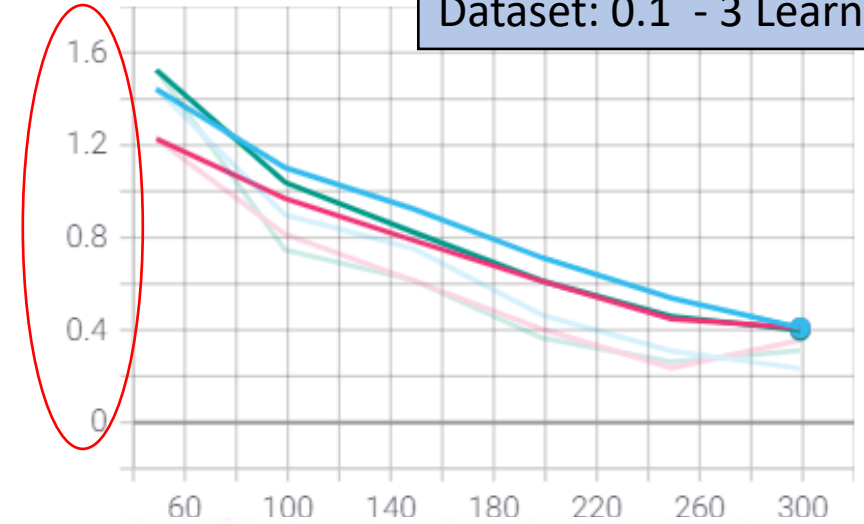
Repeat Balancing for each dataset...

Dataset	Test Accuracy	Average Learner Accuracy
Full	N/A	N/A
0.1	0.7350	0.72
0.02	0.6760	0.65
0.005	0.5454	0.53

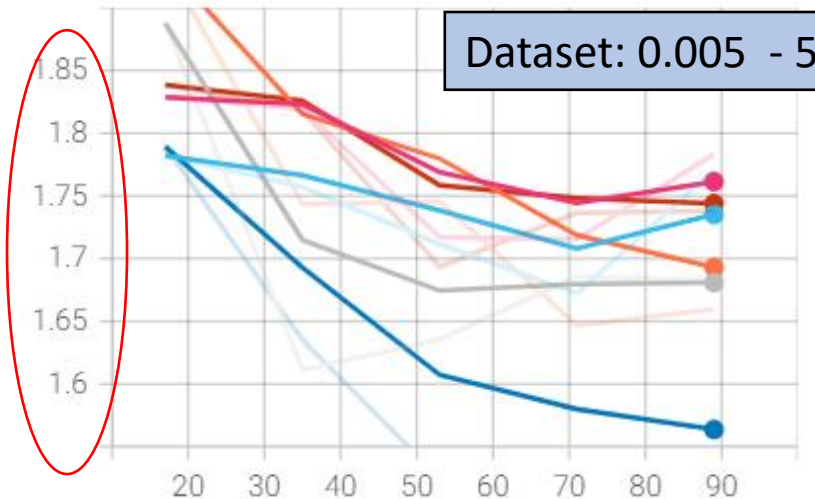
**Average Improvement:** 0.019

train\_loss

Dataset: 0.1 - 3 Learners



Dataset: 0.005 - 5 Learners



Potential to learn more with more data.

# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging / WL	?	?
Full	0.792					
0.1	0.7296	0.733	0.7458	0.7350		
0.02	0.6304	0.6788	0.6798	0.6760		
0.005	0.5446	0.5688	0.5352	0.5454		
Average Improvement:		0.024	0.019	0.015		

Experiment 4 Complete!

Ensemble Techniques show promise with more data. Let's give each model more data.

# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging / WL	Stacking	?
Full	0.792					
0.1	0.7296	0.733	0.7458	0.7350		
0.02	0.6304	0.6788	0.6798	0.6760		
0.005	0.5446	0.5688	0.5352	0.5454		
Average Improvement:		0.024	0.019	0.015		

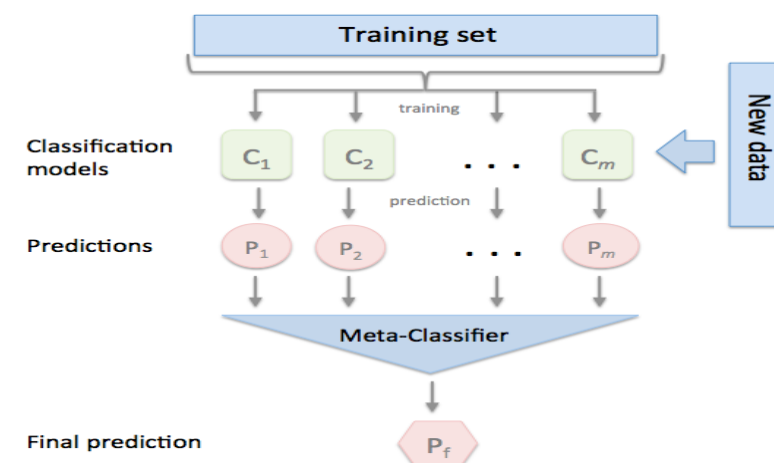
## Experiment #5: Ensemble Training, Stacking

### Motivation:

Apply ensemble techniques to entire dataset.  
Additionally, create more diverse ensemble of learners.

### Procedures:

Model Architecture Ensemble.



# Stacking: Implementation

## Code

```
hps_full = {'batch_size': 128, "lr": 2e-3, "epochs": 5,
            "weighted_loss": None, "output_dir": 'stacking-01'}

# 0) For reference
seed.seed_everything(1)

# 1) Init Ensemble Components
model_types = ['efficientnet_b0', 'efficientnet_b1', 'efficientnet_b2']
trainer = Trainer(gpus=1, max_epochs=hps_full['epochs'], logger=TensorBoardLogger(save_dir=hps_full['output_dir']))
dataset = BaseDataset(train_json)

# 2) Train Models
models = []
for i in range(3):
    train_dataloader, val_dataloader = get_dataloaders(dataset, batch_size=hps_full['batch_size'])
    test_dataloader = get_test_dataloader(test_json)
    hist = get_histogram(process_json(train_json))
    index = i % len(model_types)
    model = BaseNet(model_type=model_types[index], lr=hps_full['lr'], weighted_loss=hps_full['weighted_loss'], hist=hist)
    trainer = Trainer(gpus=1, max_epochs=hps_full['epochs'], logger=TensorBoardLogger(save_dir=hps_full['output_dir']))
    trainer.fit(model, train_dataloader, val_dataloader)
    models.append(model)
    trainer.test(model, test_dataloader)

# 3) Combine Models and Inference
test_dataloader = get_test_dataloader(test_json)
for model in models:
    if torch.cuda.is_available():
        model.cuda()
ensemble = ModelEnsemble(models)
trainer.test(ensemble, test_dataloader)
```

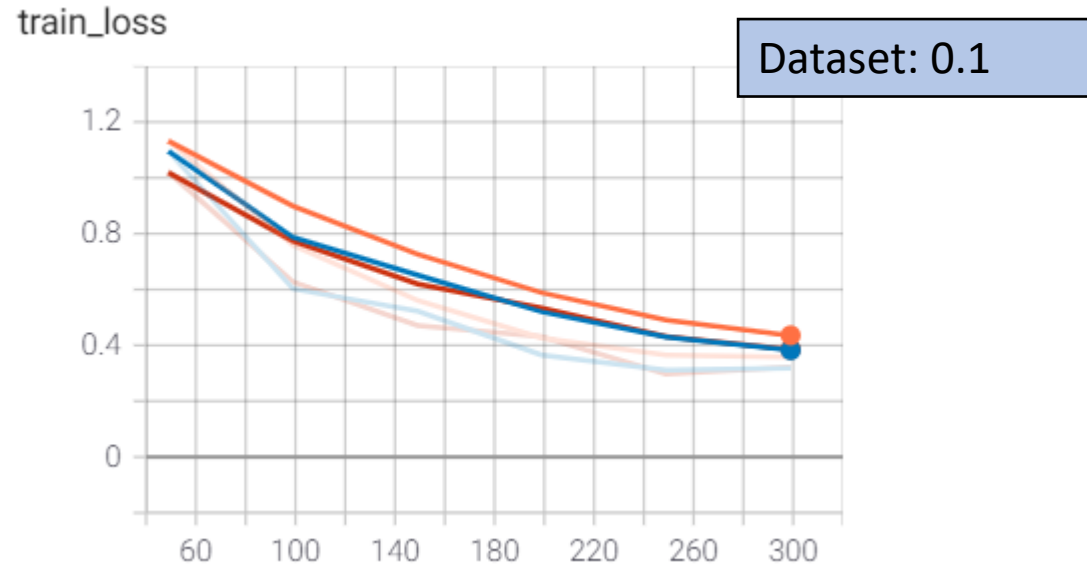
Same training procedure as bagging, except for two changes:

- 1) Each model trains on entire dataset
- 2) Each model is initialized under different model architecture.

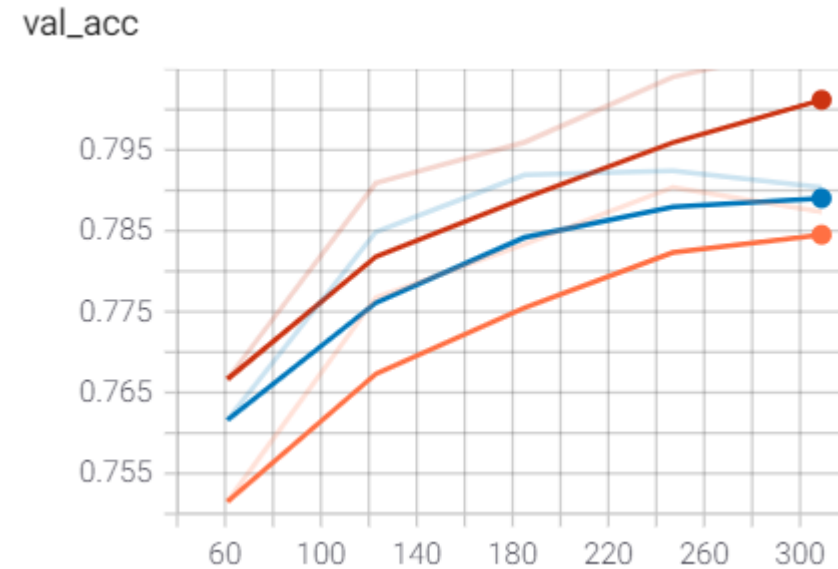
Three Model Architectures selected were EfficientNets 0-2.

# Stacking: Training

Training Loss



Validation Accuracy



Unlike Bagging, which had a variable number of learners for each balanced sub-dataset, all datasets using stacking had 3 learners corresponding to each model architecture.



# Stacking: Training

## Results

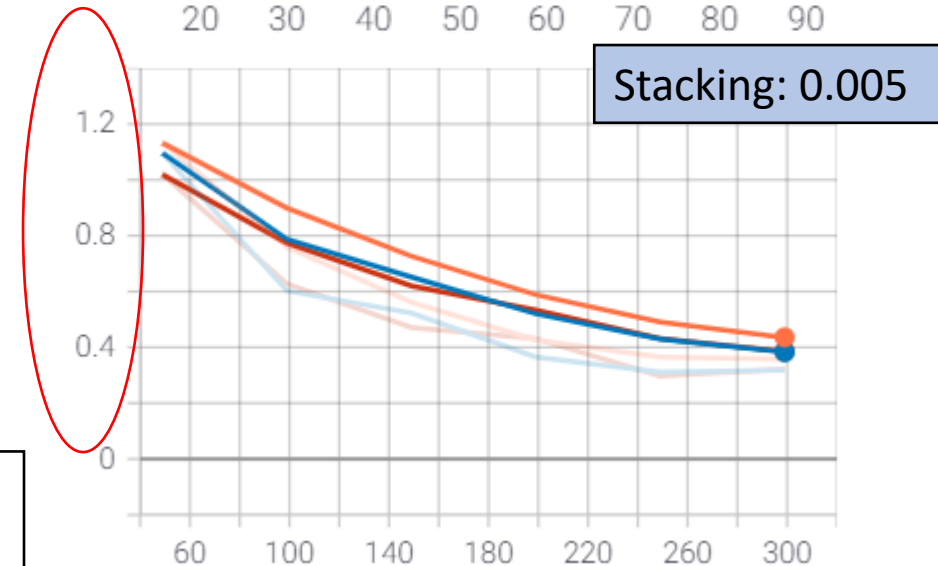
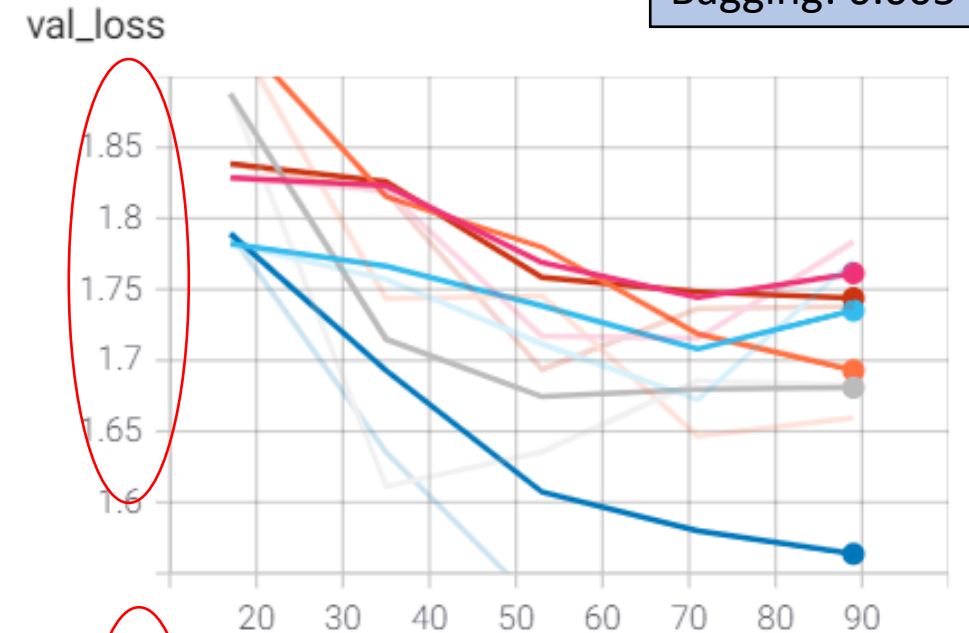
Repeat Balancing for each dataset...

Dataset	Test Accuracy	Average Learner Accuracy
Full	N/A	N/A
0.1	0.7720	0.7335
0.02	0.6614	0.6360
0.005	0.5626	0.5436

**Average  
Improvement:**

0.030

More data produces  
stronger learner base.



# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging / WL	Stacking	?
Full	0.792					
0.1	0.7296	0.733	0.7458	0.7350	0.7720	
0.02	0.6304	0.6788	0.6798	0.6760	0.6614	
0.005	0.5446	0.5688	0.5352	0.5454	0.5626	
Average Improvement:		0.024	0.019	0.015	0.030	

Experiment 5 Complete!

All that is left is to turn on individual model balancing.

# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging / WL	Stacking	?
Full	0.792					
0.1	0.7296	0.733	0.7458	0.7350	0.7720	
0.02	0.6304	0.6788	0.6798	0.6760	0.6614	
0.005	0.5446	0.5688	0.5352	0.5454	0.5626	
Average Improvement:		0.024	0.019	0.015	0.030	

## Experiment #6: Ensemble Training, Stacking with Weighted Loss

### Motivation:

Combine successes of weighted loss and stacking ensemble technique.

### Procedures:

Simply repeat last experiment turning on weighted loss!

# Stacking with Weighted Loss: Training

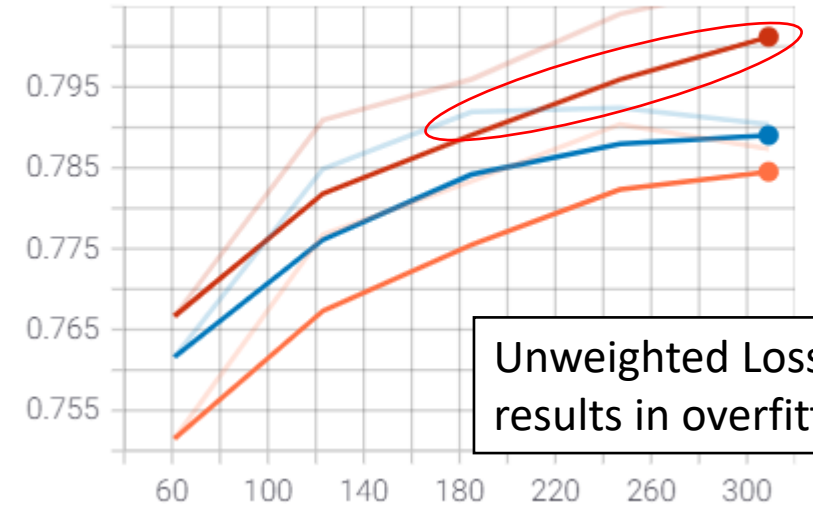
## Results

Repeat Balancing for each dataset...

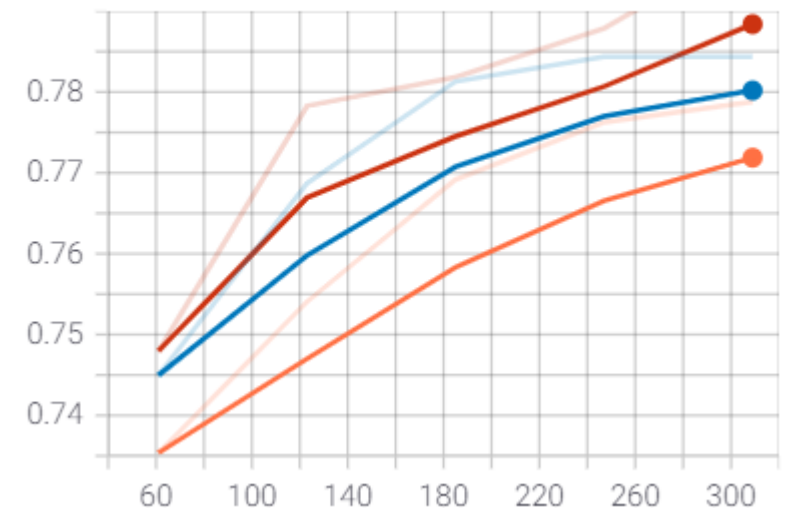
Dataset	Test Accuracy	Average Learner Accuracy
Full	N/A	N/A
0.1	0.7933	0.7482
0.02	0.7253	0.6935
0.005	0.6218	0.5997

**Average Improvement:** 0.079

val\_acc



val\_acc



# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging / WL	Stacking	Stacking / WL
Full	0.792					
0.1	0.7296	0.733	0.7458	0.7350	0.7720	0.7933
0.02	0.6304	0.6788	0.6798	0.6760	0.6614	0.7253
0.005	0.5446	0.5688	0.5352	0.5454	0.5626	0.6218
Average Improvement:		0.024	0.019	0.015	0.030	0.079

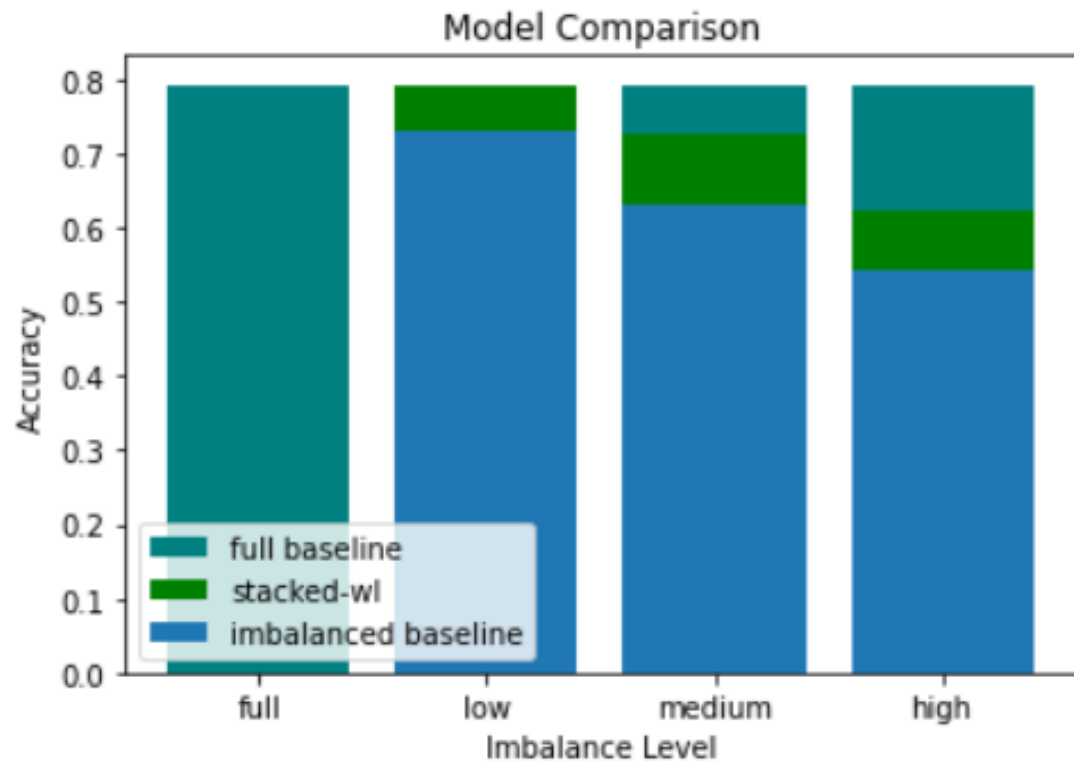
Experiment 6 Complete!

# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging / WL	Stacking	Stacking / WL
Full	0.792					
0.1	0.7296	0.733	0.7458	0.7350	0.7720	0.7933
0.02	0.6304	0.6788	0.6798	0.6760	0.6614	0.7253
0.005	0.5446	0.5688	0.5352	0.5454	0.5626	0.6218
Average Improvement:		0.024	0.019	0.015	0.030	0.079

## Best Results

Dataset	Baseline Accuracy	Maximum Accuracy	Improvement	Modeling Technique
0.1	0.7296	0.793	0.064	Stacking/WL
0.02	0.6304	0.725	0.095	Stacking/WL
0.005	0.5446	0.622	0.077	Stacking/WL



Model Name	Test Accuracy	# Parameters
efficientnet_b2	0.804	10 M
resnet50d	0.793	22 M
efficientnet_b1	0.7892	8 M
efficientnet_b0	0.788	5 M
densenet121	0.770	20 M
resnet50	0.758	22 M
resnet34d	0.730	20 M

Model Ensemble = 23 M  
ResNet50 = 22 M !

## Best Results

Dataset	Baseline Accuracy	Maximum Accuracy	Improvement	Modeling Technique
0.1	0.7296	0.793	0.064	Stacking/WL
0.02	0.6304	0.725	0.095	Stacking/WL
0.005	0.5446	0.622	0.077	Stacking/WL

# Model Summary

Dataset	Baseline	Artificial Balancing	Weighted Loss	Bagging / WL	Stacking	Stacking / WL
Full	0.792					
0.1	0.7296	0.733	0.7458	0.7350	0.7720	0.7933
0.02	0.6304	0.6788	0.6798	0.6760	0.6614	0.7253
0.005	0.5446	0.5688	0.5352	0.5454	0.5626	0.6218
Average Improvement:		0.024	0.019	0.015	0.030	0.079

Thank You!