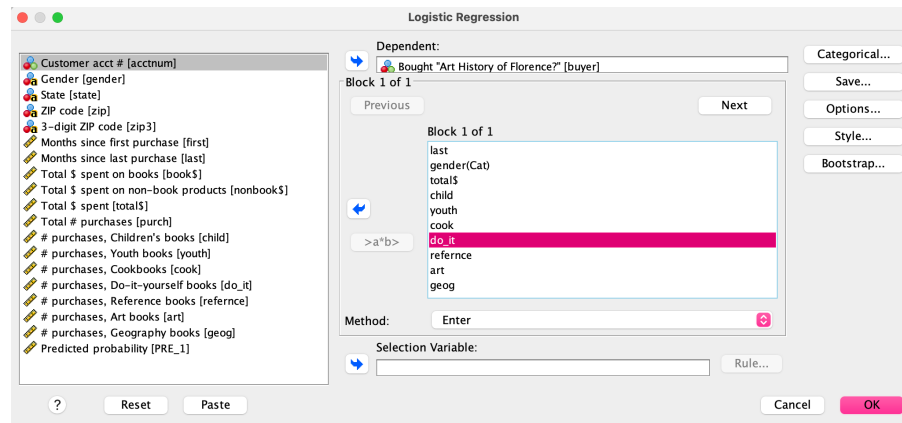


Part I: Logistic Regression

1. Estimate a logistic regression model using BUYER as the dependent variable and the following as predictor variables: (Use 'Analyze/Regression/Binary Logistic' in SPSS. Save the predicted probabilities by clicking on the 'Save' button and then on 'Probabilities' under 'Predicted Values').



2. Summarize and interpret the results (so that a marketing manager can understand them). Which variables are significant? Which seem to be 'important'? Interpret the coefficients for each of the predictors.

| Variables in the Equation | | | | | | | |
|---------------------------|-----------------------------------|--------|------|----------|----|-------|--------|
| | | B | S.E. | Wald | df | Sig. | Exp(B) |
| Step 1 ^a | Months since last purchase | -.095 | .003 | 1150.401 | 1 | <.001 | .910 |
| | Gender(1) | .761 | .036 | 452.515 | 1 | <.001 | 2.140 |
| | Total \$ spent | .001 | .000 | 31.701 | 1 | <.001 | 1.001 |
| | # purchases, Children's books | -.186 | .017 | 116.097 | 1 | <.001 | .830 |
| | # purchases, Youth books | -.113 | .026 | 18.724 | 1 | <.001 | .893 |
| | # purchases, Cookbooks | -.270 | .017 | 249.075 | 1 | <.001 | .763 |
| | # purchases, Do-it-yourself books | -.539 | .027 | 399.777 | 1 | <.001 | .583 |
| | # purchases, Reference books | .235 | .027 | 78.087 | 1 | <.001 | 1.265 |
| | # purchases, Art books | 1.156 | .022 | 2723.273 | 1 | .000 | 3.176 |
| | # purchases, Geography books | .574 | .019 | 950.087 | 1 | <.001 | 1.776 |
| | Constant | -2.361 | .049 | 2293.523 | 1 | .000 | .094 |

a. Variable(s) entered on step 1: Months since last purchase, Gender, Total \$ spent, # purchases, Children's books, # purchases, Youth books, # purchases, Cookbooks, # purchases, Do-it-yourself books, # purchases, Reference books, # purchases, Art books, # purchases, Geography books.

As the results showed, P-values of all variables are less than 0.05, indicating all variables are significant for the dependent variable.

(Based on all other predictors are the same)

Along with length of **time since last purchase** increasing 1 unite, the odds of purchasing the book decreases a factor of 0.91.

For every increase in **total dollars spent**, the odds of making a purchase increase by 10.01%.

For **Gender (1)**, it increases the odds of purchasing by a factor of 2.14.

For every increase in the total number of **children's books** purchased, it decrease the odds of purchasing by a factor of 0.83.

For every increase in the total number of **youth books** purchased, it decreases the odds of purchasing by a factor of 0.893.

For every increase in the total number of **cookbooks** purchased, it decreases the odds of purchasing by a factor of 0.763.

For every increase in the total number of **do-it-yourself books** purchased, it decreases the odds of purchasing by a factor of 0.583.

For every increase in the total number of **reference books** purchased, it increases the odds of purchasing by a factor of 1.265.





The odds of buying a copy of The Art History of Florence change by a factor of 3.176 with **art books** purchased.

For every increase in the total number of **geography books** purchased, it increases the odds of purchasing by a factor of 1.776.

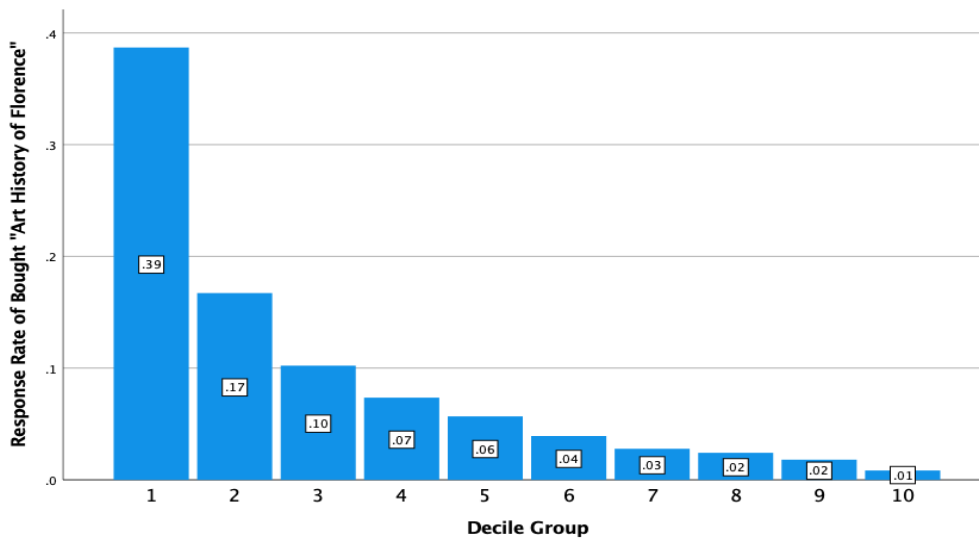
Gender and the variable related whether the customer purchased the art books are seems more important. They can lead to a 2 to 3 times probability for customers purchasing the 'The Art History of Florence'.

Part II: Decile Analysis of Logistic Regression Results

1. Assign each customer to a decile based on his or her predicted probability of purchase.

|  PRE_1 |  NPRED_1 |  PRE_1 |  NPRED_1 |
|---|---|---|---|
| .02003 | 8 | .02700 | 8 |
| .01661 | 9 | .25937 | 1 |
| .01583 | 9 | .01990 | 9 |
| .07688 | 4 | .00334 | 10 |
| .02012 | 8 | .01198 | 9 |
| .04695 | 6 | .08997 | 3 |
| .01109 | 10 | .12084 | 3 |
| .08707 | 3 | .01865 | 9 |
| .39124 | 1 | .04524 | 6 |
| .03298 | 7 | .03929 | 6 |
| .05267 | 5 | .00987 | 10 |
| .03636 | 7 | .01513 | 9 |
| .02025 | 8 | .02385 | 8 |
| .11323 | 3 | .44132 | 1 |
| .00681 | 10 | .12550 | 3 |
| .06426 | 4 | .05370 | 5 |
| .05766 | 5 | .10948 | 3 |
| .13945 | 2 | .08150 | 4 |
| | | .04192 | 6 |

2. Create a bar chart plotting response rate by decile.



3. Generate a report showing number of customers, the number of buyers of “The Art History of Florence’ and the response rate to the offer by decile.

| Case Summaries | | | | | |
|-----------------------------------|-------|------|------|----------------|--------------|
| Bought "Art History of Florence?" | | | | | |
| Percentile Group of PRE_1 | N | Sum | Mean | % of Total Sum | % of Total N |
| 1 | 5000 | 1935 | .39 | 42.8% | 10.0% |
| 2 | 5000 | 836 | .17 | 18.5% | 10.0% |
| 3 | 5000 | 511 | .10 | 11.3% | 10.0% |
| 4 | 5000 | 368 | .07 | 8.1% | 10.0% |
| 5 | 5000 | 284 | .06 | 6.3% | 10.0% |
| 6 | 5000 | 196 | .04 | 4.3% | 10.0% |
| 7 | 5001 | 139 | .03 | 3.1% | 10.0% |
| 8 | 4999 | 121 | .02 | 2.7% | 10.0% |
| 9 | 5000 | 90 | .02 | 2.0% | 10.0% |
| 10 | 5000 | 42 | .01 | 0.9% | 10.0% |
| Total | 50000 | 4522 | .09 | 100.0% | 100.0% |

Values in N column are the number of customers.

Values in Sum is the number of buyers of ‘The Art History of Florence’.

The customers response rate is the value in Mean.

4. Generate a report showing the mean values of the following variables by probability of purchase decile:

Total \$ spent

Months since last purchase, and

Number of books purchased for each of the seven categories (i.e., children, youth, cookbooks, do-it-yourself, reference, art and geography).

Case Summaries

Mean

| Percentile Group of PRE_1 | Total \$ spent | Months since last purchase | # purchases, Children's books | # purchases, Youth books | # purchases, Cookbooks | # purchases, Do-it-yourself books | # purchases, Reference books | # purchases, Art books | # purchases, Geography books |
|---------------------------|----------------|----------------------------|-------------------------------|--------------------------|------------------------|-----------------------------------|------------------------------|------------------------|------------------------------|
| 1 | 257.3526 | 7.19 | 1.06 | .51 | 1.07 | .47 | .56 | 1.50 | 1.33 |
| 2 | 224.8692 | 7.96 | .84 | .39 | .85 | .39 | .40 | .75 | .89 |
| 3 | 214.2284 | 8.62 | .79 | .37 | .80 | .37 | .38 | .48 | .70 |
| 4 | 207.6430 | 8.78 | .75 | .36 | .80 | .34 | .31 | .30 | .54 |
| 5 | 199.1118 | 9.57 | .76 | .33 | .82 | .37 | .27 | .22 | .46 |
| 6 | 199.1302 | 10.94 | .75 | .36 | .86 | .39 | .26 | .16 | .39 |
| 7 | 191.3457 | 12.37 | .76 | .35 | .84 | .42 | .23 | .13 | .29 |
| 8 | 191.5499 | 14.42 | .81 | .36 | .91 | .45 | .21 | .11 | .25 |
| 9 | 193.6108 | 17.86 | .96 | .41 | 1.12 | .65 | .25 | .13 | .32 |
| 10 | 204.3416 | 25.87 | 1.07 | .46 | 1.31 | .77 | .25 | .07 | .29 |
| Total | 208.3183 | 12.36 | .85 | .39 | .94 | .46 | .31 | .39 | .55 |

5. Summarize and interpret the decile analysis results. Are the patterns in the decile analysis consistent with your conclusions from the logistic regression?

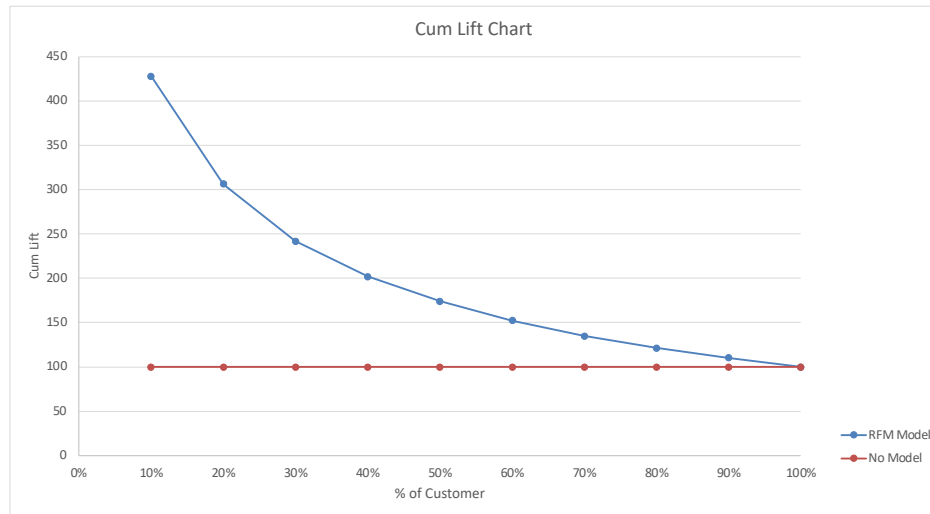
The deciles from 1 to 10 are descending by the probability of purchase. In the first group, with the highest probability, customers spent most on books, about total \$257, but have the longest interval since last purchase. As to the associations between different book categories and the purchase probability, Reference, Art and Geography books have a positive correlation with it. The rest of book categories, such as children's book, youth books and cookbooks purchased with a higher volume in the first group. With the decreased probability in next groups, the numbers of each category decrease and then increase, even to the largest sales. The patterns in the decile analysis are consistent with the conclusions from the logistic regression.

Part III: Lifts and Gains

1. Use the information from the report in 2c) above to create a chart showing the lift and cumulative lift for each decile. You may want to use Excel for these calculations.

| Percentile Groups | # of Customer | Cum of Customer | # of Response | Cum of Response | Response Rate | Cum of Total Response Rate | Lift | Cum Lift |
|-------------------|---------------|-----------------|---------------|-----------------|---------------|----------------------------|------|----------|
| 1 | 5000 | 5000 | 1935 | 1935 | 38.7% | 38.7% | 428 | 428 |
| 2 | 5000 | 10000 | 836 | 2771 | 16.7% | 27.7% | 185 | 306 |
| 3 | 5000 | 15000 | 511 | 3282 | 10.2% | 21.9% | 113 | 242 |
| 4 | 5000 | 20000 | 368 | 3650 | 7.4% | 18.3% | 81 | 202 |
| 5 | 5000 | 25000 | 284 | 3934 | 5.7% | 15.7% | 63 | 174 |
| 6 | 5000 | 30000 | 196 | 4130 | 3.9% | 13.8% | 43 | 152 |
| 7 | 5001 | 35001 | 139 | 4269 | 2.8% | 12.2% | 31 | 135 |
| 8 | 4999 | 40000 | 121 | 4390 | 2.4% | 11.0% | 27 | 121 |
| 9 | 5000 | 45000 | 90 | 4480 | 1.8% | 10.0% | 20 | 110 |
| 10 | 5000 | 50000 | 42 | 4522 | 0.8% | 9.0% | 9 | 100 |
| Total | 50000 | 50000 | 4522 | 4522 | 9.0% | | 100 | 0 |

2. Create a chart showing the cumulative lift by decile.



3. Use the information from the report in 2c) above to create a chart showing the gains and cumulative gains for each decile. You may want to use Excel for these calculations.

| Percentile Groups | # of Customer | Cum of Customer | # of Response | Cum of Response | Response Rate | Cum of Total Response Rate | Lift | Cum Lift | Gain | Cum Gain |
|-------------------|---------------|-----------------|---------------|-----------------|---------------|----------------------------|------|----------|--------|----------|
| 1 | 5000 | 5000 | 1935 | 1935 | 38.7% | 38.7% | 428 | 428 | 42.8% | 42.8% |
| 2 | 5000 | 10000 | 836 | 2771 | 16.7% | 27.7% | 185 | 306 | 18.5% | 61.3% |
| 3 | 5000 | 15000 | 511 | 3282 | 10.2% | 21.9% | 113 | 242 | 11.3% | 72.6% |
| 4 | 5000 | 20000 | 368 | 3650 | 7.4% | 18.3% | 81 | 202 | 8.1% | 80.7% |
| 5 | 5000 | 25000 | 284 | 3934 | 5.7% | 15.7% | 63 | 174 | 6.3% | 87.0% |
| 6 | 5000 | 30000 | 196 | 4130 | 3.9% | 13.8% | 43 | 152 | 4.3% | 91.3% |
| 7 | 5001 | 35001 | 139 | 4269 | 2.8% | 12.2% | 31 | 135 | 3.1% | 94.4% |
| 8 | 4999 | 40000 | 121 | 4390 | 2.4% | 11.0% | 27 | 121 | 2.7% | 97.1% |
| 9 | 5000 | 45000 | 90 | 4480 | 1.8% | 10.0% | 20 | 110 | 2.0% | 99.1% |
| 10 | 5000 | 50000 | 42 | 4522 | 0.8% | 9.0% | 9 | 100 | 0.9% | 100.0% |
| Total | 50000 | 50000 | 4522 | 4522 | 9.0% | | 100 | 0 | 100.0% | 100.0% |

4. Create a chart showing the cumulative gains by decile along with a reference line corresponding to 'no model'.



Part IV: Profitability Analysis

Use the following cost information to assess the profitability of using logistic regression to

determine which customers should receive a specific offer:

Cost to mail offer to customer: \$.50

Selling price (shipping included): \$18.00




Wholesale price paid by BookBinders: \$9.00

Shipping costs: \$3.00

1. What is the breakeven response rate?

Break-even Response Rate = $\$.5 / (\$18 - \$9 - \$3) * 100\% = 8.3\%$

2. Create a new variable (call it TARGET) with a value of 1 if the customer's predicted probability is greater than or equal to the breakeven response rate and 0 otherwise.

|  PRE_1 |  NPRE_1 |  Target |
|---|--|--|
| .02003 | 8 | 0 |
| .01661 | 9 | 0 |
| .01583 | 9 | 0 |
| .07688 | 4 | 0 |
| .02012 | 8 | 0 |
| .04695 | 6 | 0 |
| .01109 | 10 | 0 |
| .08707 | 3 | 1 |
| .39124 | 1 | 1 |
| .03298 | 7 | 0 |
| .05267 | 5 | 0 |
| .03636 | 7 | 0 |
| .02025 | 8 | 0 |
| .11323 | 3 | 1 |
| .00681 | 10 | 0 |
| .06426 | 4 | 0 |
| .05766 | 5 | 0 |
| .13945 | 2 | 1 |

3. Generate a report summarizing the number of customers, the number of buyers of 'The Art History of Florence' and the response rate to the offer by the TARGET variable.

Case Summaries

| Bought "Art History of Florence?" | | | | | |
|---|-------|------|------|-------------------|--------------|
| Compare with Break-even response rate | N | Sum | Mean | % of Total Sum | % of Total N |
| smaller than BER | 34390 | 1195 | .03 | 26.4% | 68.8% |
| larger than BER | 15610 | 3327 | .21 | 73.6% | 31.2% |
| Total | 50000 | 4522 | .09 | 100.0% | 100.0% |

4. What would the gross profit (in dollars, and also as a percentage of gross sales) and the return on marketing expenditures have been if BookBinders had mailed the offer to buy "The Art History of Florence" only to customers with a predicted probability of buying that was greater than or equal to the breakeven rate?

Cost to mail offer to customer: \$.50

Selling price (shipping included): \$18.00

Wholesale price paid by BookBinders: \$9.00

Shipping costs: \$3.00

Gross Profit: $(\$18 - \$9 - \$3) * 3327 - \$5 * 15610 = \$19,962 - \$7,805 = \$12,157$

ROI = $\$12,157 / \$5 * 15610 * 100\% = 156\%$