```
MODULE StateAWSet -
EXTENDS AWSet
CONSTANTS Read(_)
VARIABLES
     aset,
                      aset[r]: the set of active elements maintained by r \in Replica
     tset,
                     tset[r]: the set of tombstone elements maintained by r \in Replica
      variables for network:
                     incoming[r]: incoming channel at replica r \in Replica
     incoming,
    lmsg,
                     lmsg[r]: the last message delivered at r \in Replica to the upper-layer protocol
      variables for SEC:
                       uset[r]: the set of updates seen by replica r \in Replica
     uset,
     uincoming
                      uincoming[r]: incoming channel for broadcasting/delivering updates at r \in Replica
nVars \stackrel{\triangle}{=} \langle incoming, lmsg \rangle
secVars \triangleq \langle uset, uincoming \rangle
vars \stackrel{\triangle}{=} \langle aset, tset, seq, nVars, secVars \rangle
Msg \triangleq [aid : Aid, A : SUBSET Element, T : SUBSET Element]
Network \stackrel{\triangle}{=} Instance BasicNetwork with incoming \leftarrow incoming, lmsg \leftarrow lmsg
ReadStateAWSet(r) \stackrel{\Delta}{=} \{ele.d : ele \in aset[r]\} read the state of r \in Replica
SEC \stackrel{\Delta}{=} INSTANCE \ StateSEC \ WITH \ uset \leftarrow uset, \ uincoming \leftarrow uincoming
TypeOK \stackrel{\triangle}{=}
     \land aset \in [Replica \rightarrow SUBSET \ Element]
     \land tset \in [Replica \rightarrow SUBSET \ Element]
     \wedge IntTypeOK
     \land Network!SMTypeOK
     \land SEC! SECTypeOK
Init \stackrel{\triangle}{=}
     \land aset = [r \in Replica \mapsto \{\}]
     \land tset = [r \in Replica \mapsto \{\}]
     \land IntInit
     \land Network \,! \, BNInit
     \land SEC! StateSECInit
```

```
Add(d, r) \triangleq
                   r \in Replica adds d \in Data
       \land \ aset' = [\overline{aset} \ \text{EXCEPT} \ ![r] = @ \cup \{[aid \mapsto [r \mapsto r, \ seq \mapsto seq[r]], \ d \mapsto d]\}]
       \wedge IntDo(r)
       \land SEC!StateSECDo(r)
       \land UNCHANGED \langle tset, nVars \rangle
Remove(d, r) \stackrel{\Delta}{=} r \in Replica \text{ removes } d \in Data
     \wedge LET E \triangleq \{ele \in aset[r] : ele.d = d\} E may be empty
        IN \wedge aset' = [aset \ EXCEPT \ ![r] = @ \setminus E]
               \wedge tset' = [tset \ EXCEPT \ ![r] = @ \cup E]
     \wedge IntDo(r)
     \land SEC!StateSECDo(r)
     \land UNCHANGED \langle nVars \rangle
Do(r) \triangleq
                We ignore ReadStateAWSet(r) since it does not modify states.
       \exists a \in Data : Add(a, r) \lor Remove(a, r)
Send(r) \triangleq
                   r \in Replica sends a message
       \land Network!BNBroadcast(r, [aid \mapsto [r \mapsto r, seq \mapsto seq[r]],
                                                A \mapsto aset[r], T \mapsto tset[r]
       \wedge IntSend(r)
       \land SEC! StateSECSend(r)
       \land UNCHANGED \langle aset, tset \rangle
Deliver(r) \stackrel{\triangle}{=} r \in Replica \text{ delivers a message } (lmsg'[r])
     \wedge IntDeliver(r)
     \land Network!BNDeliver(r)
     \land SEC!StateSECDeliver(r, lmsg'[r].aid)
     \land tset' = [tset \ EXCEPT \ ![r] = @ \cup lmsg'[r].T]
     \land \quad aset' = [aset \ EXCEPT \ ![r] = (@ \cup lmsg'[r].A) \setminus tset'[r]]
     ∧ UNCHANGED ⟨⟩
Next \triangleq \exists r \in Replica : Do(r) \lor Send(r) \lor Deliver(r)
Spec \stackrel{\triangle}{=} Init \wedge \Box [Next]_{vars}
\* Modification History
\* Last modified Wed Jun 26 15:12:53 CST 2019 by xhdn
\* Created Fri May 24 14:13:38 CST 2019 by xhdn
```