Course: ENSF694 – Summer 2025

Lab #: Lab 2

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Part I

Exercise A

```
* my_lab2exe_A.cpp
* ENSF 694 Lab 2 Exercise A
* Created by Mahmood Moussavi
* Completed by: John Zhou
*/
int my_strlen(const char *s);
/* Duplicates my_strlen from <cstring>, except return type is int.
* REQUIRES
* s points to the beginning of a string.
* PROMISES
* Returns the number of chars in the string, not including the
* terminating null.
*/
void my_strncat(char *dest, const char *source, int n);
/* Duplicates my_strncat from <cstring>, except return type is void.
* REQUIRES
   dest points to the beginning of a string
   source points to the beginning of a string
    n integer that define the length of the string added to the destination
* PROMISES
* Appends at most n characters from source to the end of dest
*/
```

```
#include <iostream>
#include <cstring>
using namespace std;
int main(void)
  char str1[7] = "banana";
  const char str2[] = "-tacit";
  const char *str3 = "-toe";
  /* point 1 */
  char str5[] = "ticket";
  char my_string[100] = "";
  int bytes;
  int length;
  /* using my_strlen libarary function */
  length = (int)my_strlen(my_string);
  cout << "\nLine 1: my_string length is " << length;</pre>
  /* using sizeof operator */
  bytes = sizeof(my_string);
  cout << "\nLine 2: my_string size is " << bytes << " bytes.";</pre>
  /* using strcpy libarary function */
  strcpy(my_string, str1);
  cout << "\nLine 3: my_string contains: " << my_string;</pre>
  length = (int)my_strlen(my_string);
```

```
cout << "\nLine 4: my_string length is " << length << ".";</pre>
my\_string[0] = '\0';
cout << "\nLine 5: my_string contains:\"" << my_string << "\"";</pre>
length = (int)my_strlen(my_string);
cout << "\nLine 6: my_string length is " << length << ".";</pre>
bytes = sizeof(my_string);
cout << "\nLine 7: my_string size is still " << bytes << " bytes.";</pre>
/* my_strncat append the first 3 characters of str5 to the end of my_string */
my_strncat(my_string, str5, 3);
cout << "\nLine 8: my_string contains:\"" << my_string << "\"";
length = (int)my_strlen(my_string);
cout << "\nLine 9: my_string length is " << length << ".";</pre>
my_strncat(my_string, str2, 4);
cout << "\nLine 10: my_string contains:\"" << my_string << "\"";
/* my_strncat append ONLY up ot '\0' character from str3 -- not 6 characters */
my_strncat(my_string, str3, 6);
cout << "\nLine 11: my_string contains:\"" << my_string << "\"";</pre>
length = (int)my_strlen(my_string);
cout << "\nLine 12; my_string has " << length << " characters.";</pre>
cout << "\n\nUsing strcmp - C library function: ";</pre>
```

```
cout << "\n\"ABCD\" is less than \"ABCDE\" ... strcmp returns: " << strcmp("ABCD", "ABCDE");
  cout << "\n\"ABCD\" is less than \"ABND\" ... strcmp returns: " << strcmp("ABCD", "ABND");</pre>
  cout << "\n\"ABCD\" is equal than \"ABCD\" ... strcmp returns: " << strcmp("ABCD", "ABCD");</pre>
  cout << "\n\"ABCD\" is less than \"ABCd\" ... strcmp returns: " << strcmp("ABCD", "ABCd");</pre>
  cout << "\n\"Orange\" is greater than \"Apple\" ... strcmp returns: " << strcmp("Orange", "Apple") <<
endl;
  return 0;
}
int my_strlen(const char *s){
  int count=0;
  while (*s){
    count++;
    s++;
  }
  return count;
}
void my_strncat(char *dest, const char *source, int n) {
  while (*dest != '\0') {
    dest++;
  }
```

```
int i = 0;
while (i < n && *source != '\0') {
    *dest = *source;
    dest++;
    source++;
    i++;
}
*dest = '\0';
}</pre>
```

Execution result

```
$ g++ -Wall lab2exe_A.cpp -o lab2A
 john2@John-Desktop /cygdrive/c/Users/john2/Desktop/uofc/c++/ENSF-604-assignment-repo/assignment2
$ ./lab2A.exe
 Line 1: my_string length is 0
 Line 2: my_string size is 100 bytes.
 Line 3: my_string contains: banana
 Line 4: my_string length is 6.
 Line 5: my_string contains:""
 Line 6: my_string length is 0.
 Line 7: my_string size is still 100 bytes.
 Line 8: my_string contains:"tic"
 Line 9: my_string length is 3.
 Line 10: my_string contains:"tic-tac"
 Line 11: my_string contains:"tic-tac-toe"
 Line 12; my_string has 11 characters.
 Using strcmp - C library function:
 "ABCD" is less than "ABCDE" ... strcmp returns: -1
 "ABCD" is less than "ABND" ... strcmp returns: -1
 "ABCD" is equal than "ABCD" ... strcmp returns: 0
 "ABCD" is less than "ABCd" ... strcmp returns: -1
 "Orange" is greater than "Apple" ... strcmp returns: 1
```

Exercise B

```
/*
* my_lab1exe_B.cpp
* ENSF 694 Lab 2 Exercise B
* Created by Mahmood Moussavi
* Completed by: John Zhou
*/
#include <iostream>
#include <assert.h>
using namespace std;
int sum_of_array(const int *a, int n);
// REQUIRES
// n > 0, and elements a[0] ... a[n-1] exist.
// PROMISES:
// Return value is a[0] + a[1] + ... + a[n-1].
int main()
  int a[] = \{100\};
  int b[] = \{100, 200, 300, 400\};
  int c[] = \{-100, -200, -200, -300\};
  int d[] = {10, 20, 30, 40, 50, 60, 70};
  int sum = sum_of_array(a, 1);
  cout << "sum of integers in array a is: " << sum << endl;</pre>
```

```
sum = sum_of_array(b, 4);
  cout << "sum of integers in array b is: " << sum << endl;</pre>
  sum = sum_of_array(c, 4);
  cout << "sum of integers in array c is: " << sum << endl;</pre>
  sum = sum_of_array(d, 7);
  cout << "sum of integers in array d is: " << sum << endl;</pre>
  return 0;
}
int sum_of_array(const int *a, int n)
{
  // int sum = 0;
  // for(int i=0; i < n; i++)
  // sum += a[i];
  // return sum;
  if (n == 0)
  {
    return 0;
  }
  return (a[0] + sum_of_array(a + 1, n - 1));
}
```

Execution result

```
john2@John-Desktop /cygdrive/c/Users/john2/Desktop/uofc/c++/ENSF-604-assignment-repo/assignment2

$ ./lab2B.exe
sum of integers in array a is: 100
sum of integers in array b is: 1000
sum of integers in array c is: -800
sum of integers in array d is: 280

john2@John-Desktop /cygdrive/c/Users/john2/Desktop/uofc/c++/ENSF-604-assignment-repo/assignment2
```

Exercise C

```
/*
* lab1exe_C.cpp
* ENSF 694 Lab 1, exercise C
* Created by Mahmood Moussavi
* Completed by: John Zhou
*/
#include <iostream>
using namespace std;
void time_convert(int ms_time, int *minutes_ptr, double *seconds_ptr);
/*
* Converts time in milliseconds to time in minutes and seconds.
* For example, converts 123400 ms to 2 minutes and 3.4 seconds.
* REQUIRES:
* ms_time >= 0.
* minutes_ptr and seconds_ptr point to variables.
* PROMISES:
* 0 <= *seconds_ptr & *seconds_ptr < 60.0
* *minutes_ptr minutes + *seconds_ptr seconds is equivalent to
* ms_time ms.
*/
int main(void)
int millisec;
```

```
int minutes;
 double seconds;
 cout << "Enter a time interval as an integer number of milliseconds: ";</pre>
// printf("Enter a time interval as an integer number of milliseconds: ");
 cin >> millisec;
 if (!cin) {
  cout << "Unable to convert your input to an int.\n";</pre>
  exit(1);
 }
 cout << "Doing conversion for input of " << millisec <<" milliseconds ... \n";</pre>
 /* MAKE A CALL TO time_convert HERE. */
 time_convert(millisec,&minutes,&seconds);
 cout << "That is equivalent to " << minutes << " minute(s) and " << seconds << " second(s).\n";
 return 0;
}
/* PUT YOUR FUNCTION DEFINITION FOR time_convert HERE. */
void time_convert(int ms_time, int *minutes_ptr, double *seconds_ptr){
 *minutes_ptr=ms_time/60000;
 *seconds_ptr=ms_time%60000/1000.0;
}
```

Execution result

```
john2@John-Desktop /cygdrive/c/Users/john2/Desktop/uofc/c++/ENSF-604-assignment-repo
$ g++ -Wall lablexe_C.cpp -o exercise_C

john2@John-Desktop /cygdrive/c/Users/john2/Desktop/uofc/c++/ENSF-604-assignment-repo
$ ./exercise_C.exe
Enter a time interval as an integer number of milliseconds: 3213
Doing conversion for input of 3213 milliseconds ...
That is equivalent to 0 minute(s) and 3.213 second(s).

john2@John-Desktop /cygdrive/c/Users/john2/Desktop/uofc/c++/ENSF-604-assignment-repo
$ ./exercise_C.exe
Enter a time interval as an integer number of milliseconds: 232323
Doing conversion for input of 232323 milliseconds ...
That is equivalent to 3 minute(s) and 52.323 second(s).

john2@John-Desktop /cygdrive/c/Users/john2/Desktop/uofc/c++/ENSF-604-assignment-repo
$ []
```

Exercise D

```
/*
* fibonacci.cpp
* ENSF 694 Lab 2 Exercise D
* Created by Mahmood Moussavi
* Completed by: John Zhou
*/
#include <stdio.h>
#include <time.h>
#include <stdlib.h>
#include <iostream>
#include <iomanip>
#include <chrono>
using namespace std;
#define N 2
void myPlot(int *x, double *y1, double *y2, int size)
{
  FILE *gnuplotPipe = popen("gnuplot -persist", "w");
  if (gnuplotPipe == NULL)
    printf("Error: Could not open pipe to Gnuplot.\n");
    return;
  }
  fprintf(gnuplotPipe, "set title 'Fibonacci Complexity Comparison'\n");
  fprintf(gnuplotPipe, "set xlabel 'N (Input Size)'\n");
```

```
fprintf(gnuplotPipe, "set ylabel 'Execution Time (Seconds)'\n");
  fprintf(gnuplotPipe, "set key outside\n");
  fprintf(gnuplotPipe, "set grid\n");
  fprintf(gnuplotPipe, "set terminal x11\n");
  fprintf(gnuplotPipe, "set yrange [0:0.3]\n");
  fprintf(gnuplotPipe, "set xtics rotate by -45\n");
  fprintf(gnuplotPipe, "plot '-' using 1:2 with points pt 7 ps 1.5 lc rgb 'blue' title 'Iterative Method', '-'
using 1:2 with points pt 7 ps 1.5 lc rgb 'red' title 'Matrix Exponentiation Method'\n");
  for (int i = 0; i < size; i++)
  {
    fprintf(gnuplotPipe, "%d %f\n", x[i], y1[i]);
  }
  fprintf(gnuplotPipe, "e\n");
  for (int i = 0; i < size; i++)
  {
    fprintf(gnuplotPipe, "%d %f\n", x[i], y2[i]);
  }
  fprintf(gnuplotPipe, "e\n");
  fclose(gnuplotPipe);
}
void myPlot_for_recursive_method(int *x, double *y1, int size)
```

```
{
  FILE *gnuplotPipe = popen("gnuplot -persist", "w");
  if (gnuplotPipe == NULL)
  {
    printf("Error: Could not open pipe to Gnuplot.\n");
    return;
  }
  fprintf(gnuplotPipe, "set title 'Fibonacci Recursive Method'\n");
  fprintf(gnuplotPipe, "set xlabel 'N (Input Size)'\n");
  fprintf(gnuplotPipe, "set ylabel 'Execution Time (Seconds)'\n");
  fprintf(gnuplotPipe, "set key outside\n");
  fprintf(gnuplotPipe, "set grid\n");
  fprintf(gnuplotPipe, "set terminal x11\n");
  fprintf(gnuplotPipe, "set yrange [0:0.00001]\n");
  fprintf(gnuplotPipe, "set xtics rotate by -45\n");
  // Only one dataset plotted
  fprintf(gnuplotPipe, "plot '-' using 1:2 with points pt 7 ps 1.5 lc rgb 'red' title 'Recursive Method'\n");
  for (int i = 0; i < size; i++)
  {
    fprintf(gnuplotPipe, "%d %f\n", x[i], y1[i]);
  }
  fprintf(gnuplotPipe, "e\n");
  fclose(gnuplotPipe);
}
```

```
// Function to multiply two matrices of size N x N
void multiplyMatrices(int A[N][N], int B[N][N], int result[N][N])
{
  for (int i = 0; i < N; i++)
  {
    for (int j = 0; j < N; j++)
    {
       result[i][j] = 0;
    }
  }
  for (int i = 0; i < N; i++)
  {
    for (int j = 0; j < N; j++)
       for (int k = 0; k < N; k++)
       {
         result[i][j] += A[i][k] * B[k][j];
       }
    }
  }
}
// Recursive funciont
void powerMatrix(int base[N][N], int exp, int result[N][N])
{
  if (exp == 0)
  {
```

```
result[0][0] = 1;
    result[0][1] = 0;
    result[1][0] = 0;
    result[1][1] = 1;
    return;
  }
  int temp[N][N];
  powerMatrix(base, exp / 2, temp);
  multiplyMatrices(temp, temp, result);
  if (exp % 2 == 1)
  {
    multiplyMatrices(result, base, temp);
    for (int i = 0; i < N; i++)
    {
      for (int j = 0; j < N; j++)
      {
         result[i][j] = temp[i][j];
      }
    }
  }
// Function to calculate the nth Fibonacci number using recursive matrix exponentiation
int fibonacciRecursive(int n)
```

}

{

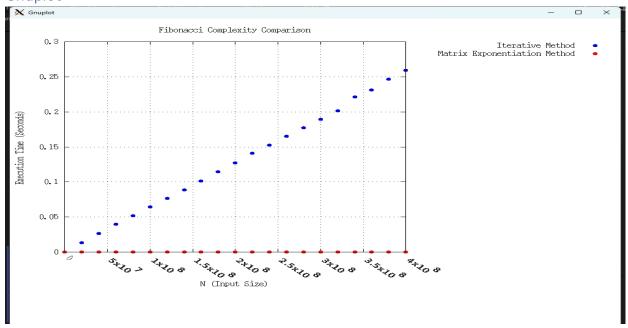
```
if (n == 0)
    return 0;
  }
  if (n == 1)
  {
    return 1;
  }
  int base[N][N] = \{\{1, 1\}, \{1, 0\}\};
  int result[N][N];
  powerMatrix(base, n - 1, result);
  return result[0][0];
}
// Function to calculate the nth Fibonacci number iteratively
int fibonaccilterative(int n)
{
  int prev = 0;
  int cur = 1;
  if (n == 0)
  {
    return 0;
  }
  if (n == 1)
    return 1;
  }
```

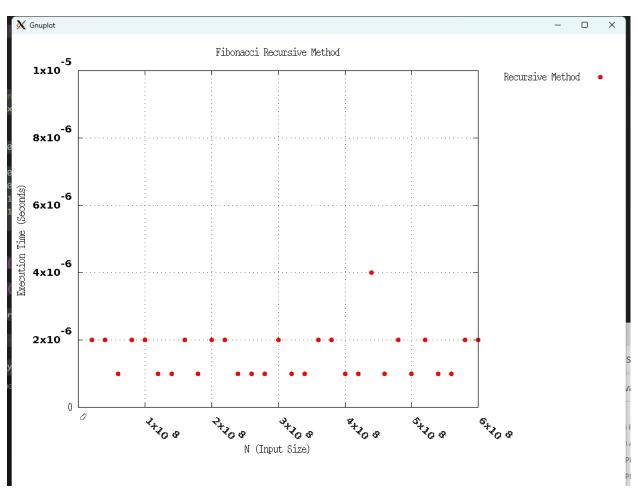
```
for (int i = 2; i < n; i++)
  {
    int temp = prev + cur;
    prev = cur;
    cur = temp;
  }
  return cur;
}
// Function to measure the time taken by a function to calculate the nth Fibonacci number
// This function is using a pointer to a funciton called fibonacciFunc
double measureTime(int (*fibonacciFunc)(int), int n)
{
  using namespace std::chrono;
  auto start = high_resolution_clock::now();
  fibonacciFunc(n);
  auto end = high_resolution_clock::now();
  duration<double> time_taken = end - start;
  return time_taken.count(); // returns time in seconds
}
int main(void)
{
  const int maxN = 400000000; // Adjust maxN based on the range you want to test
```

```
double recursive_result[50];
double iterative_result[50];
int N_value[50];
cout << "Recursive Matrix Exponentiation Method\n";</pre>
cout << setw(12) << "N" << setw(12) << "Time\n";
for (int n = 20000000, i = 0; n <= \max N; n += 20000000, i++)
{
  double time = measureTime(fibonacciRecursive, n);
  recursive_result[i] = time;
  cout << setw(12) << n << setw(12) << recursive_result[i] << endl;</pre>
}
cout << "\nIterative Method\n";</pre>
cout << setw(12) << "N" << setw(12) << "Time\n";
for (int n = 20000000, i = 0; n <= \max N; n += 20000000, i++)
{
  double time = measureTime(fibonaccilterative, n);
  iterative_result[i] = time;
  cout << setw(12) << n << setw(12) << iterative_result[i] << endl;</pre>
  N value[i] = n;
}
myPlot(N_value, iterative_result, recursive_result, 30);
myPlot_for_recursive_method(N_value, recursive_result, 30 );
return 0;
```

}

Gnuplot





execution output

```
john 2 @ John - Desktop / cygdrive/c/Users/john 2 / Desktop/uofc/c++/ENSF-604-assignment-repo/assignment 2 / Desktop/uofc/c++/ENSF-604-assignment 2 / Desktop/uofc/c+-/ENSF-604-assignment 2 / Desktop/uofc/c--/ENSF-604-assignment 2 / Desktop/uo
• $ ./fib.exe
Recursive Matrix Exponentiation Method
                   20000000
                   40000000
                                                              1.4e-06
                                                              1.8e-06
                   60000000
                  80000000
                                                              1.4e-06
                100000000
                                                              1.4e-06
                120000000
                                                              1.4e-06
                140000000
                                                              1.3e-06
               160000000
                                                              1.8e-06
                180000000
                                                              1.8e-06
                200000000
                                                              1.3e-06
                220000000
                                                              1.9e-06
               240000000
                260000000
                280000000
                                                              1.6e-06
                 300000000
                                                              1.7e-06
                                                              1.6e-06
                320000000
                340000000
                                                              1.5e-06
                                                             1.5e-06
1.5e-06
                360000000
                380000000
                400000000
                                                              1.6e-06
      Iterative Method
                                                                    Time
                   20000000
                                                      0.0131903
                   40000000
                                                      0.0266255
                   60000000
                                                      0.0395505
                  80000000
                                                      0.0518534
               100000000
                                                      0.0647543
               120000000
                                                        0.076752
                140000000
                                                      0.0889486
                160000000
                                                          0.10134
                180000000
                                                          0.114622
                                                          0.127063
                220000000
                                                           0.14113
                240000000
                                                          0.152367
                260000000
                                                          0.165288
                280000000
                                                          0.177258
                 300000000
                                                          0.189529
                 320000000
                                                          0.201896
                340000000
                                                           0.22159
                360000000
                                                          0.231099
                 380000000
                                                          0.246746
                                                          0.259617
```

Exercise E

```
* compare_sorts.cpp
* ENSF 694 Lab 2 Exercise E
* Created by Mahmood Moussavi
* Completed by: John Zhou
*/
#include "compare_sorts.h"
void to_lower(char *str)
  while (*str)
    *str = std::tolower(*str);
    ++str;
  }
}
void strip_punctuation(char *word)
{
  int i = 0, j = 0;
  while (word[i])
    if ((word[i] >= 'a' \&\& word[i] <= 'z') || (word[i] >= 'A' \&\& word[i] <= 'Z') || word[i] == '-' ||
(word[i] >= '0' \&\& word[i] <= '9'))
    {
      word[j] = word[i];
      j++;
    }
    i++;
  word[j] = '\0';
```

bool is_unique(char words[MAX_UNIQUE_WORDS][MAX_WORD_SIZE], int num_words, const char *word)

```
{
  for (int i = 0; i < num_words; i++)
    if (std::strcmp(words[i], word) == 0)
    {
       return false;
    }
  }
  return true;
}
void quicksort(int *indices, char words[MAX_UNIQUE_WORDS][MAX_WORD_SIZE], int left, int
right)
{
  if (left >= right)
    return;
  int pivot = indices[right];
  int i = left;
  for (int j = left; j <= right - 1; j++)
    if (strcmp(words[indices[j]], words[pivot]) < 0)</pre>
    {
       std::swap(indices[i], indices[j]);
       i++;
    }
  }
  std::swap(indices[i], indices[right]);
  int pivotPoint = i;
  quicksort(indices, words, left, pivotPoint - 1);
  quicksort(indices, words, pivotPoint + 1, right);
}
void shellsort(int *indices, char words[MAX_UNIQUE_WORDS][MAX_WORD_SIZE], int size)
```

```
{
  for (int gap = size / 2; gap > 0; gap \neq 2)
  {
    for (int i = gap; i < size; i++)
       int temp = indices[i];
       int j = i;
       while (j >= gap && std::strcmp(words[indices[j - gap]], words[temp]) > 0)
         indices[j] = indices[j - gap];
         j -= gap;
       }
       indices[j] = temp;
    }
  }
}
void bubblesort(int *indices, char words[MAX_UNIQUE_WORDS][MAX_WORD_SIZE], int size)
{
  for (int i = 0; i < size - 1; i++)
    for (int j = 0; j < size - 1 - i; j++)
       if (std::strcmp(words[indices[j]], words[indices[j + 1]]) > 0)
       {
         std::swap(indices[j], indices[j + 1]);
       }
     }
  }
}
```

```
void read words(const char *input file, char
words[MAX_UNIQUE_WORDS][MAX_WORD_SIZE], int &num_words)
{
  std::ifstream infile(input file);
  if (!infile)
    std::cerr << "Error opening input file.\n";
    exit(1);
  }
  char word[MAX_WORD_SIZE + 1];
  num_words = 0;
  while (infile >> word)
  {
    strip_punctuation(word);
    to lower(word);
    if (word[0] != '\0' && num words < MAX UNIQUE WORDS && is unique(words,
num words, word))
    {
      std::strncpy(words[num_words++], word, MAX_WORD_SIZE);
    }
  }
  infile.close();
}
void write words(const char *output file, char
words[MAX UNIQUE WORDS][MAX WORD SIZE], int *indices, int num words)
{
  std::ofstream outfile(output_file);
  if (!outfile)
  {
    std::cerr << "Error opening output file.\n";
    exit(1);
```

```
}
  for (int i = 0; i < num_words; ++i)
  {
    outfile << words[indices[i]] << '\n';
  }
  outfile.close();
}
void sort_and_measure_quicksort(char words[MAX_UNIQUE_WORDS][MAX_WORD_SIZE], int
*indices, int num words, void (*sort func)(int *,
char[MAX UNIQUE WORDS][MAX WORD SIZE], int, int), const char *sort name)
{
  auto start = std::chrono::high_resolution_clock::now();
  sort func(indices, words, 0, num words - 1);
  auto end = std::chrono::high resolution clock::now();
  std::chrono::duration<double> time taken = end - start;
  std::cout << sort name << "completed in " << time taken.count() << "seconds.\n";
}
void sort and measure shell bubble(char words[MAX UNIQUE WORDS][MAX WORD SIZE],
int *indices, int num_words, void (*sort_func)(int *,
char[MAX_UNIQUE_WORDS][MAX_WORD_SIZE], int), const char *sort_name)
{
  auto start = std::chrono::high resolution clock::now();
  sort func(indices, words, num words);
  auto end = std::chrono::high_resolution_clock::now();
  std::chrono::duration<double> time taken = end - start;
  std::cout << sort name << " completed in " << time taken.count() << " seconds.\n";
}
int main()
{
```

```
const char *input file = "C:\Users\{\john2\OneDrive\Desktop\uofc\c\ENSF-604-}
assignment-repo\\assignment2\\input.txt";
  char words[MAX_UNIQUE_WORDS][MAX_WORD_SIZE];
  int num words;
  read words(input file, words, num words);
  int indices[num words];
  for (int i = 0; i < num words; ++i)
  {
    indices[i] = i;
  }
  sort and measure quicksort(words, indices, num words, quicksort, "Quick Sort");
  write words("C:\\Users\\john2\\OneDrive\\Desktop\\uofc\\c\\ENSF-604-assignment-
repo\\assignment2\\output quicksort.txt", words, indices, num words);
  sort and measure shell bubble(words, indices, num words, shellsort, "Shell Sort");
  write words("C:\\Users\\john2\\OneDrive\\Desktop\\uofc\\c\\ENSF-604-assignment-
repo\\assignment2\\output shellsort.txt", words, indices, num words);
  sort_and_measure_shell_bubble(words, indices, num_words, bubblesort, "Bubble Sort");
  write\_words("C:\Users\john2\OneDrive\Desktop\uofc\c\ENSF-604-assignment-files)
repo\\assignment2\\output_bubblesort.txt", words, indices, num_words);
  return 0;
}
```

Program output

All three output files have the same content

```
0045
 1045
 145
 200
 2024-05-30
 245
 376
 476
 576
ac123
ama1123
ama11231
ama11232
calgary
delta233
delta2331
delta2332
edmonton
otawa
toronto
wj1230
wj12301
wj12302
```

Execution screenshot

Part II

Exercise A

7. 2^(N/2)

2/N Decreasing as N gets bigger
 37 Constant. Not growing
 √N Smaller than N
 N Linear
 N log(N) log(N) is not a constant and it is growing. This is greater than N
 N^2 N grows faster than log(N)

exponential growth is the fastest

Exercise B

(1) O(N) one loop n times
(2) O(N^2) two loop n times. n^2
(3) $O(N^3)$ one loop n times. Another loop n^2 times. It sums to n^3 .
(4) $O(N^2)$ two loops n times. n^2 . This is slightly smaller than (2) because j and k may be less than n. The big O notation is still $O(N^2)$
(5) $O(N^3)$ three loops n times. n^3 . but slightly smaller than (3), because the j and are less than n for a lot of the iteration. The big O notation is still $O(N^2)$
(6)
O(N^3) three loops n times. n^3.