

# Functional Programming

## Laziness

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# Laziness

- Haskell does not evaluate function arguments unless they are demanded to calculate the function's result
- Data structures are only evaluated as much as they are needed

# Infinite lists

```
nat :: [Integer]
nat = [0..] -- cheating!

ones :: [Integer]
ones = undefined

-- |create an infinite list of argument value
repeat' :: a -> [a]
repeat' a = undefined
```

# Fibonacci numbers

```
fib :: [Integer]
fib = undefined
```

# Sieve of Eratosthenes

```
primes :: [Integer]
primes = undefined
```

# The minimum tree

## A binary tree type

A variant of binary trees has information only at the nodes.

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data BTree = Leaf Int | Branch BTree BTree
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- Write a function `mintree` that replaces the value at each leaf by the minimum value of all leaves in the tree.
- **Only one traversal of the tree is allowed!**