Functional Programming Starting Haskell

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Let's get started!

Haskell Demo

- Let's say we want to buy a game in the USA and we have to convert its price from USD to EUR
- A definition gives a name to a value
- Names are case-sensitive, must start with lowercase letter
- Definitions are put in a text file ending in .hs

Examples.hs

dollarRate = 1.3671

Using the definition

• Start the Haskell interpreter GHCi

```
> stack ghci
```

Configuring GHCi with the following packages:
GHCi, version 8.0.2: http://www.haskell.org/ghc/ :? for h
Loaded GHCi configuration from /private/var/folders/t4/skr
Prelude>

Load the file

```
Prelude> :1 Examples.hs
[1 of 1] Compiling Main (Examples.hs, interproblem, modules loaded: Main.
```

*Main>

Use the definition

```
*Main> dollarRate
1.3671
*Main> 53 * dollarRate
72.4563
```

A function to convert EUR to USD

Examples.hs dollarRate = 1.3671 -- |convert EUR to USD usd euros = euros * dollarRate

- line starting with --: comment
- usd: function name (defined)
- euros: argument name (defined)
- euros * dollarRate: expression to compute the result

Using the function

- load into GHCi
 - as before or
 - ▶ use :r to reload
- *Main> usd 1
- 1.3671
- *Main> usd 73
- 99.7983

Converting back

Write a function euro that converts back from USD to EUR!

```
*Main> euro (usd 73)
73.0
*Main> euro (usd 1)
1.0
*Main> usd (euro 100)
100.0
```

Converting back

Write a function euro that converts back from USD to EUR!

```
*Main> euro (usd 73)
73.0
*Main> euro (usd 1)
1.0
*Main> usd (euro 100)
100.0
```

Your turn

Testing properties

Is this function correct?

A reasonable property of euro and usd

```
prop_EuroUSD x = euro (usd x) == x
== is the equality operator
*Main> prop_EuroUSD 79
True
*Main> prop_EuroUSD 1
True
```

Testing properties

Is this function correct?

A reasonable property of euro and usd

```
prop_EuroUSD x = euro (usd x) == x
== is the equality operator
```

*Main> prop_EuroUSD 79

True

*Main> prop_EuroUSD 1

True

Does it hold generally?

Aside: Testing by Writing Properties

Convention

Function names beginning with prop_ are properties we expect to be True

Writing properties in a file

- Tells us how functions should behave
- Tells us what has been tested
- Lets us repeat tests after changing a definition

Testing

At the beginning of Examples.hs

import Test.QuickCheck

A widely used Haskell library for automatic random testing

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May need to install it first ...

stack install QuickCheck

Running tests

```
*Main> quickCheck prop_EuroUSD

*** Failed! Falsifiable (after 10 tests and 1 shrink):
7.0
```

- Runs 100 randomly chosen tests
- Result: The property is wrong!
- It fails for input 7.0

Running tests

```
*Main> quickCheck prop_EuroUSD

*** Failed! Falsifiable (after 10 tests and 1 shrink):
7.0
```

- Runs 100 randomly chosen tests
- Result: The property is wrong!
- It fails for input 7.0

Check what happens for 7.0!

What happens for 7.0

- *Main> usd 7 9.5697
- *Main> euro 9.5697
- 6.9999999999999

The Problem: Floating Point Arithmetic

- There is a tiny difference between the initial and final values
 - *Main> euro (usd 7) 7 -8.881784197001252e-16
- Calculations are only performed to about 15 significant figures
- The property is wrong!

Fixing the problem

- NEVER use equality with floating point numbers!
- The result should be nearly the same
- The difference should be small smaller than 10E-15

Comparing Values

```
*Main> 2<3
```

True

*Main> 3<2

False

Defining "Nearly Equal"

• Can define new operators with names made up of symbols

In Examples.hs

$$x == y = x - y < 10e-15$$

*Main> 3 ~== 3.000001

True

*Main> 3 ~== 4

True

Defining "Nearly Equal"

Can define new operators with names made up of symbols

In Examples.hs

$$x = y = abs(x - y) < 10e-15 * abs x$$

```
*Main> 3 ~== 3.000001
```

True

True

Fixing the property

In Examples.hs

```
prop_EuroUSD' x = euro (usd x) ~== x
```

```
*Main> prop_EuroUSD' 3
True

*Main> prop_EuroUSD' 56
True

*Main> prop_EuroUSD' 7
True
```

Name the price

Let's define a name for the price of the game we want in Examples.hs price = 79

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```
After reload: Ouch!

*Main> euro price

<interactive>:57:6:

    Couldn't match expected type 'Double' with actual type 'In the first argument of 'euro', namely 'price'
    In the expression: euro price
    In an equation for 'it': it = euro price
```

Every Value has a type

The :i command prints information about a name

```
*Main> :i price
price :: Integer
   -- Defined at ...
*Main> :i dollarRate
dollarRate :: Double
   -- Defined at ...
```

More types

```
*Main> :i True
data Bool = ... | True -- Defined in 'GHC.Types'
*Main> :i False
data Bool = False | ... -- Defined in 'GHC.Types'
*Main> :i euro
euro :: Double -> Double
    -- Defined at...
*Main> :i prop_EuroUSD'
prop_EuroUSD' :: Double -> Bool
    -- Defined at...
```

• True and False are data constructors

Types matter

- Types determine how computations are performed
- A type annotation specifies which type to use

```
*Main> 123456789*123456789 :: Double
1.524157875019052e16
*Main> 123456789*123456789 :: Integer
15241578750190521
```

- Double: double precision floating point
- Integer: exact computation
- GHCi must know the type of each expression before computing it.

Type checking

- An algorithm infers (works out) the type of every expression
- Checks that all types match before running the program

Our example

```
*Main> :i price
price :: Integer
   -- Defined at...
*Main> :i euro
euro :: Double -> Double
   -- Defined at...
*Main> euro price
<interactive>:70:6:
    Couldn't match expected type 'Double' with actual type 'In
    In the first argument of 'euro', namely 'price'
    In the expression: euro price
    In an equation for 'it': it = euro price
```

24 / 27

Why did it work before?

*Main> euro 79 57.78655548240802 *Main> 79 :: Integer

79

- Numeric literals are **overloaded**: they can be used with several types
- Giving the number a name fixes its type

```
*Main> 79 :: Double
79.0
*Main> price :: Integer
79
*Main> price :: Double
<interactive>:76:1:
    Couldn't match expected type 'Double' with actual type 'In
    In the expression: price :: Double
    In an equation for 'it': it = price :: Double
```

Fixing the problem

A definition can be given a type signature which specifies its type

```
In Examples.hs

| -- | price of the game in USD |
|-- | price' :: Double |
| price' = 79
```

```
*Main> :i price'
price' :: Double
  -- Defined at...
*Main> euro price'
57.78655548240802
```

Questions?

