

# *Notes for ECE 36800 - Data Structures and Algorithms*

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## *Course Introduction*

Provides insight into the use of data structures. Topics include stacks, queues and lists, trees, graphs, sorting, searching, and hashing. The learning outcomes are:

- Advanced programming ideas, in practice and in theory
- Data structures and their abstractions: Stacks, lists, trees, and graphs
- Fundamentals of algorithms and their complexities: Sorting, searching, hashing, and graph algorithms
- Problem Solving

## *Introduction to Data Structures & Algorithms*

Data Structures are methods of organizing information for ease of manipulation. Examples:

1. Dictionary
2. Check-out line or queues
3. Spring-loaded plate dispenser or stacked
4. Organizational Chart or tree

These are associated with methods known as algorithms to be manipulated

Algorithms are methods of doing something. Examples:

1. Multiplying two numbers
2. Making a sandwich
3. Getting dressed

The topics of interest within them are:

- Correctness
- Efficiency in time and space

## *Asymptotic Notation*

The questions to be asked about an algorithm are the following:

- Is it correct?
- Is it as fast as possible?
- How many machine instructions (in terms of  $n$ ) does it take?

Let us take the following algorithm to add the numbers from 1 to  $n$ :

```
total = 0;
for (i=1:n)
    total = total + i;
return total
```

The cost will be:

Cost	Frequency	Function
$C_1$	1	Assign initial value
$C_2$	$n+1$	For loop iterations and exit
$C_3$	$n$	Number additions
$C_4$	1	Return value

The total is then:

$$C_1 * 1 + C_2(n + 1) + C_3(n) + C_4(1) = (C_2 + C_3)n + (C_1 + C_2) + C_4$$

However the  $O(n)$  will only be  $n$ , as the constants and coefficients of these will be deprecated, as we will come to understand in more detail as this topic continues.

Let us take another example of some code that has a

$$\begin{aligned}
 T(n) &= n^2 + 10^7 n + 10^{10} \\
 T(10^{11}) &= 10^{22} + 10^{18} + 10^{10} \\
 T(2 * 10^{11}) &= 4 * 10^{22} + 2 * 10^{18} + 10^{10} \\
 \Rightarrow \frac{T(2 * 10^{11})}{T(10^{11})} &\approx 4 = \left( \frac{2 * 10^{11}}{10^{11}} \right)^2
 \end{aligned}$$

This goes to show that this algorithm has an  $O(n) = n^2$ , and all coefficients and lower order terms that are a part of the complexity are largely irrelevant for large  $n$  values. This is why this is called **asymptotic notation**.

Another example of a simple algorithm is

```

total = 0;
for (i=1:n):
    if (((i*i%3)==0) || ((i*i%7)==0)):
        total = total+i*i;
return total;

```

Which has a cost table that looks like the following:

Cost	Frequency	Function
$C_1$	1	Assign initial value
$C_2$	$n+1$	For loop iterations and exit
$C_3$	$n$	Number of $i\%3$ comparisons
$C_4$	$n - \lfloor \frac{n}{3} \rfloor$	Number of $i\%7$ comparisons
$C_5$	$\lfloor \frac{n}{3} \rfloor + \lfloor \frac{n}{7} \rfloor - \lfloor \frac{n}{21} \rfloor$	Number of additions
$C_6$	1	Returning value

It can be noted that  $O(n) = n$  for this function, despite all the other complexities in the algorithm. However, it is important to know how to calculate  $T(n)$  as well.

Now, let us look at something more complicated, matrix multiplication.

```

for (i=1:n):
    for (j=1:n):
        C_ij = 0;
        for (k=j:i):
            C_ij = C_ij+A_ik*B_kj
return C

```

This has a cost table that looks like the following:

Cost	Frequency	Function
$C_1$	$n+1$	First loop
$C_2$	$\sum_{i=1}^n (i+1)$	Second loop
$C_3$	$\sum_{i=1}^n \sum_{j=1}^i 1$	Number of assigns
$C_4$	$\sum_{i=1}^n \sum_{j=1}^i (i-j+2)$	Third loop
$C_5$	$\sum_{i=1}^n \sum_{j=1}^i \sum_{k=j}^i 1$	Number of assigns to matrix
$C_6$	1	Returning value