

Notes for ECE 20002 - Electrical Engineering Fundamentals II

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These are lecture notes for spring 2024 ECE 20002 at Purdue. Modify, use, and distribute as you please.

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Course Introduction

Continuation of Electrical and Computer Engineering Fundamentals I. The course addresses mathematical and computational foundations of circuit analysis (differential equations, Laplace Transform techniques) with a focus on application to linear circuits having variable behavior as a function of frequency, with emphasis on filtering. Variable frequency behavior is considered for applications of electronic components through single-transistor and operational amplifiers. The course ends with a consideration of how circuits behave and may be modeled for analysis at high frequencies.

Learning Objectives:

1. Analyze 2nd order linear circuits with sources and/or passive elements
2. Compute responses of linear circuits with and without initial conditions via one-sided Laplace transform techniques
3. Compute responses to linear circuits using transfer function and convolution techniques
4. Analyze and design transistor amplifiers at low, mid and high frequencies

ECE 20001 Review

Sinusoidal Signal (voltage and current) involve phasors, which bring complex numbers to the forefront. When in Sinusoidal Steady State (SSS):

$$Z_R = R$$

$$Z_L = j\omega L$$

$$Z_C = \frac{1}{j\omega C}$$

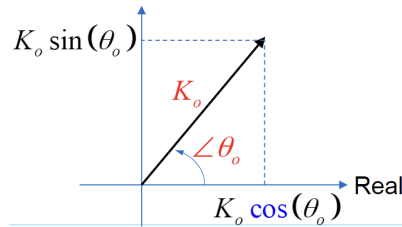
This can in turn be represented as as the following function:

$$x(t) = K_0 \cos(\omega t + \theta_0)$$

Which can be transformed into the following form:

$$\begin{aligned} K_0 e^{j(\omega t + \theta_0)} &= K_0 e^{j\theta_0} \\ &= K_0 (\cos(\theta_0) + j\sin(\theta_0)) \\ &= K_0 \angle \theta_0 \end{aligned}$$

This can be represented as the following in the cartesian plane:



Thus, these forms can be summed as following:

$x(t)$	\mathbf{X}
$K \cos(\omega t)$	K
$K \sin(\omega t) = K \cos(\omega t)$	$-Kj$
$\cos(\omega t) - \sin(\omega t)$	$1 + j$
$a \cos(\omega t) + b \sin(\omega t)$	$a - bj$

This is especially useful for circuit analysis methods such as KCL and KVL. The methods of conversion between polar and phasor are:

$$z = a + bj$$

$$z = \rho \angle \theta$$

$$\rho = |z| = \sqrt{a^2 + b^2}$$

$$\theta = \text{phase}(z) = \tan^{-1}\left(\frac{b}{a}\right)$$

These conversions and operations alongside KCL and KVL, can allow us to create a system of differential equations that will allow us to

solve almost any circuit. However, we don't like ODEs, so we have developed methods to get around this.

We know that at SSS, the following equations are valid.

$$V_R = RI_R$$

$$V_L = j\omega LI_L$$

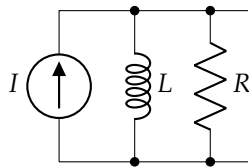
$$V_C = \frac{1}{j\omega C} I_C$$

$$i_L(t) = i_L(0) + \frac{1}{L} \int v_L dt$$

$$V_C(t) = V_C(0) + \frac{1}{C} \int i_C dt$$

This can be used to solve most SSS circuits, using the aforementioned strategies, alongside strategies like current and voltage division.

Example:



$$I_L = \frac{Z_L}{Z_R + Z_L} * I = \frac{j\omega L}{R + j\omega L} * I$$

$$I_R = \frac{Z_R}{Z_R + Z_L} * I = \frac{R}{R + j\omega L} * I$$