## **Equations**

1. 
$$P = \frac{dW}{dt} = IV$$

$$2. I = \frac{dq}{dt}$$

3. 
$$V = \frac{W}{q}$$

4. 
$$R = \frac{\rho L}{A}$$

5. Ohm's Law: 
$$V = IR$$

6. Coulomb's Law: 
$$\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{r}$$

7. Kirchhoff's Loop Law: 
$$\sum V_i = 0$$
 (around a closed loop)

8. Kirchhoff's Current Law: 
$$\sum I_i = 0$$
 (going into a node)

9. Conductance: 
$$G = \frac{1}{R}$$

10. Equivalent resistance: 
$$R_{eq} = \frac{V_{test}}{I_{test}}$$

11. Series capacitance: 
$$\frac{1}{C_{total}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

12. Parallel capacitance: 
$$C_{total} = C_1 + C_2 + \dots$$

13. Series inductor: 
$$L_{total} = L_1 + L_2 + \dots$$

14. Parallel inductor: 
$$\frac{1}{L_{total}} = \frac{1}{L_1} + \frac{1}{L_1} + \dots$$

15. 
$$I_{cap} = C \frac{dV}{dt}$$

16. 
$$V_{ind} = L \frac{dI}{dt}$$

17. Energy stored in capacitor: 
$$\frac{1}{2}CV^2$$

18. Energy stored in inductor: 
$$\frac{1}{2}LI^2$$

$$v_c(\infty) + (v_c(t_0) - v_c(\infty)) e^{(\frac{-1}{RC})(t-t_0)}$$

20. Current in RL circuit:

$$I_L(\infty) + (I_L(t_0) - I_L(\infty)) e^{(\frac{-R}{L})(t-t_0)}$$

- 21. Impedance of a capacitor:  $\frac{-j}{\omega C}$
- 22. Impedance of an inductor:  $j\omega L$
- 23. Equivalent impedance for impedances in series:

$$Z_{eq} = \sum_{i}^{n} Z_{i}$$

24. Equivalent impedance for impedances in parallel:

$$\frac{1}{Z_{eq}} = \sum_{i=1}^{n} \frac{1}{Z_i}$$

25. RMS value of signal: 
$$S_{rms} = \sqrt{\frac{1}{T} \int_{t_0}^{t_0+T} s^2(t) dt}$$

26. Maximum power extracted in DC circuits: 
$$\frac{Vth^2}{4R_{th}}$$

27. Maximum power extracted in AC circuits: 
$$\frac{|\tilde{V}_{th}|^2}{8R_{th}}$$

28. Average power: 
$$P_{avg} = \frac{V_m I_m}{2} \cos(\theta_v - \theta_i)$$

29. Reactive power: 
$$V_{ar} = Im(\frac{1}{2}\tilde{V}\tilde{I}^*)$$

30. Apparent power: 
$$P_{app} = \frac{|V_{rms}|^2}{|z|}$$

31. Coupling coefficient in coupled circuit: 
$$k = \frac{L_{12}}{\sqrt{L_1 L_2}}$$

32. Voltage in magnetically coupled coils:

$$v_1(t) = L_1 \frac{di_1(t)}{dt} + L_{12} \frac{di_2(t)}{dt}$$
$$v_2(t) = L_1 \frac{di_2(t)}{dt} + L_{12} \frac{di_1(t)}{dt}$$

33. Voltage in ideal transformer:

$$\begin{split} \frac{v_2(t)}{v_1(t)} &= \frac{N_2}{N_1} \\ \frac{i_2(t)}{i_1(t)} &= -\frac{N_1}{N_2} \end{split}$$

34. Terminated transformer circuit equations:

$$\begin{split} \tilde{V}_1 &= \frac{\tilde{V}_2}{n} \\ \tilde{I}_{out} &= \frac{\tilde{I}_{in}}{n} \\ \tilde{V}_{in} &= Z_{in} \tilde{I}_{in} + \tilde{V}_1 \\ \tilde{V}_2 &= Z_{out} \tilde{I}_{out} \\ \tilde{V}_2 &= Z_{out} \frac{\tilde{I}_{in}}{n} \\ \frac{\tilde{V}_{in}}{\tilde{I}_{in}} &= Z_{in} + \frac{Z_{out}}{n^2} \end{split}$$

35. Energy stored in magnetically coupled circuit:

$$E = \frac{1}{2}L_1i_1^2 + \frac{1}{2}L_2i_2^2 + L_{12}i_1i_2$$

- 36. Equilibrium in pn junction:  $pn = n_i^2$
- 37. Current in pn junction:

$$J_N = q\mu_n n E_x + q D_n \frac{dn}{dx}$$
$$J_P = -q D_p \frac{dp}{dx} + q \mu_p p E_x$$

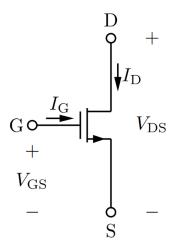
38. Width of depletion region:

$$W = \left[\frac{2\epsilon_r \epsilon_0}{q} \left(\frac{N_A + N_D}{N_A N_D}\right) V_{bi}\right]^{1/2}$$

39. Built-in potential:  $V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A N_D}{n_i^2} \right)$ 

40. Current through an ideal diode:  $I = I_0(e^{qV_A/kT} - 1)$ 

41. Schematic of a MOSFET:



42. Transistor equations:

$$\begin{split} V_{DS} &= V_D - V_S \\ V_{GS} &= V_G - V_S \\ V_T &= V_G - V_D \\ I_D &= \mu_n C_{ox} \left(\frac{W}{L}\right) \left[ (V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right] \\ &= k \left[ (V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right], V_{DS} \le V_{GS} - V_T, V_D \le V_G - V_T \\ I_D &= \mu_n C_{ox} \left(\frac{W}{L}\right) \left[ \frac{1}{2} (V_{GS} - V_T)^2 \right] \\ &= k \left[ \frac{1}{2} (V_{GS} - V_T)^2 \right], V_{DS} \ge V_{GS} - V_T, V_D \ge V_G - V_T \end{split}$$

- 43. Condition for CSA distortion less than 10%:  $V_G < 0.2(V_G V_T)$
- 44. Gain of a CSA:  $A = -R_D k(V_G V_T) = -g_m R_D$

To find Thevenin voltage and Norton current:

- $(R_{eq})$  Turn off all independent sources (dependent sources remain unchanged) and calculate the resulting resistance at the desired port. Notice that you may have to apply the i-v test if resistors cannot be combined through series and parallel connections, or if the circuit includes dependent sources.
- $(V_{th})$  Leave the desired port open-circuited (i.e. no load connected) and find the voltage across it.
- $(I_N)$  Short-circuit the desired port (i.e. connect a short circuit across the port) and find the current through it.