

Equations

1. $P = \frac{dW}{dt} = IV$
2. $I = \frac{dq}{dt}$
3. $V = \frac{W}{q}$
4. $R = \frac{\rho L}{A}$
5. Ohm's Law: $V = IR$
6. Coulomb's Law: $\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{r}$
7. Kirchhoff's Loop Law: $\sum V_i = 0$ (around a closed loop)
8. Kirchhoff's Current Law: $\sum I_i = 0$ (going into a node)
9. Conductance: $G = \frac{1}{R}$
10. Equivalent resistance: $R_{eq} = \frac{V_{test}}{I_{test}}$
11. Series capacitance: $\frac{1}{C_{total}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$
12. Parallel capacitance: $C_{total} = C_1 + C_2 + \dots$
13. Series inductor: $L_{total} = L_1 + L_2 + \dots$
14. Parallel inductor: $\frac{1}{L_{total}} = \frac{1}{L_1} + \frac{1}{L_2} + \dots$
15. $I_{cap} = C \frac{dV}{dt}$
16. $V_{ind} = L \frac{dI}{dt}$
17. Energy stored in capacitor: $\frac{1}{2} CV^2$
18. Energy stored in inductor: $\frac{1}{2} LI^2$
19. Voltage in RC circuit:
$$v_c(\infty) + (v_c(t_0) - v_c(\infty)) e^{(\frac{-1}{RC})(t-t_0)}$$
20. Current in RL circuit:
$$I_L(\infty) + (I_L(t_0) - I_L(\infty)) e^{(\frac{-R}{L})(t-t_0)}$$
21. Impedance of a capacitor: $\frac{-j}{\omega C}$
22. Impedance of an inductor: $j\omega L$
23. Equivalent impedance for impedances in series:
$$Z_{eq} = \sum_i^n Z_i$$
24. Equivalent impedance for impedances in parallel:
$$\frac{1}{Z_{eq}} = \sum_i^n \frac{1}{Z_i}$$
25. RMS value of signal: $S_{rms} = \sqrt{\frac{1}{T} \int_{t_0}^{t_0+T} s^2(t) dt}$
26. Maximum power extracted in DC circuits: $\frac{V_{th}^2}{4R_{th}}$
27. Maximum power extracted in AC circuits: $\frac{|\tilde{V}_{th}|^2}{8R_{th}}$
28. Average power: $P_{avg} = \frac{V_m I_m}{2} \cos(\theta_v - \theta_i)$
29. Reactive power: $V_{ar} = Im(\frac{1}{2} \tilde{V} \tilde{I}^*)$
30. Apparent power: $P_{app} = \frac{|V_{rms}|^2}{|z|}$
31. Coupling coefficient in coupled circuit: $k = \frac{L_{12}}{\sqrt{L_1 L_2}}$
32. Voltage in magnetically coupled coils:
$$v_1(t) = L_1 \frac{di_1(t)}{dt} + L_{12} \frac{di_2(t)}{dt}$$

$$v_2(t) = L_1 \frac{di_2(t)}{dt} + L_{12} \frac{di_1(t)}{dt}$$
33. Voltage in ideal transformer:
$$\frac{v_2(t)}{v_1(t)} = \frac{N_2}{N_1}$$

$$\frac{i_2(t)}{i_1(t)} = -\frac{N_1}{N_2}$$
34. Terminated transformer circuit equations:
$$\tilde{V}_1 = \frac{\tilde{V}_2}{n}$$

$$\tilde{I}_{out} = \frac{\tilde{I}_{in}}{n}$$

$$\tilde{V}_{in} = Z_{in} \tilde{I}_{in} + \tilde{V}_1$$

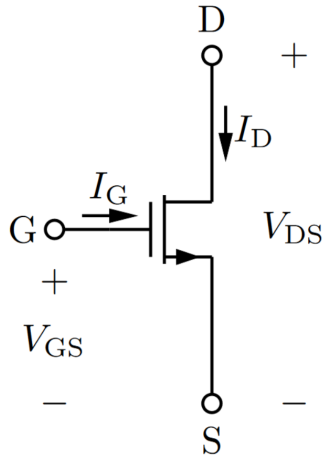
$$\tilde{V}_2 = Z_{out} \tilde{I}_{out}$$

$$\tilde{V}_2 = Z_{out} \frac{\tilde{I}_{in}}{n}$$

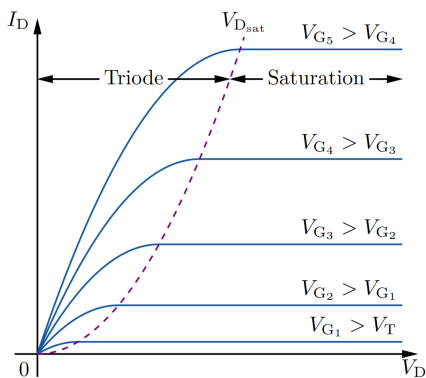
$$\frac{\tilde{V}_{in}}{\tilde{I}_{in}} = Z_{in} + \frac{Z_{out}}{n^2}$$
35. Energy stored in magnetically coupled circuit:
$$E = \frac{1}{2} L_1 i_1^2 + \frac{1}{2} L_2 i_2^2 + L_{12} i_1 i_2$$
36. Equilibrium in pn junction: $pn = n_i^2$
37. Current in pn junction:
$$J_N = q\mu_n n E_x + qD_n \frac{dn}{dx}$$

$$J_P = -qD_p \frac{dp}{dx} + q\mu_p p E_x$$
38. Width of depletion region:
$$W = \left[\frac{2\epsilon_r \epsilon_0}{q} \left(\frac{N_A + N_D}{N_A N_D} \right) V_{bi} \right]^{1/2}$$
39. Built-in potential: $V_{bi} = \frac{kT}{q} \ln \left(\frac{N_A N_D}{n_i^2} \right)$
40. Current through an ideal diode: $I = I_0 (e^{qV_A/kT} - 1)$

41. Schematic of a MOSFET:



42. $I_D - V_D$ characteristic graph:



43. Transistor equations:

$$V_{DS} = V_D - V_S$$

$$V_{GS} = V_G - V_S$$

$$I_D = \mu_n C_{ox} \left(\frac{W}{L} \right) \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

$$= k \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right], V_{DS} \leq V_{GS} - V_T, V_D \leq V_G - V_T$$

$$I_D = \mu_n C_{ox} \left(\frac{W}{L} \right) \left[\frac{1}{2} (V_{GS} - V_T)^2 \right]$$

$$= k \left[\frac{1}{2} (V_{GS} - V_T)^2 \right], V_{DS} \geq V_{GS} - V_T, V_D \geq V_G - V_T$$

44. Condition for CSA distortion less than 10%: $V_G < 0.2(V_G - V_T)$

45. Gain of a CSA: $A = -R_D k (V_G - V_T) = -g_m R_D$

To find Thevenin voltage and Norton current:

(R_{eq}) Turn off all independent sources (dependent sources remain unchanged) and calculate the resulting resistance at the desired port. Notice that you may have to apply the i-v test if resistors cannot be combined through series and parallel connections, or if the circuit includes dependent sources.

(V_{th}) Leave the desired port open-circuited (i.e. no load connected) and find the voltage across it.

(I_N) Short-circuit the desired port (i.e. connect a short circuit across the port) and find the current through it.