DS4003 Optimization Methods

Assignment Individual Project: Standard Form of Linear

Programming — 2022 Spring

Student No.: Student Name:

Practical projects: in this project, you are expect to

- 1. familiar with the Python Optimization package.
- 2. familiar with the standard form of linear programming
- 3. be able to transform a linear programming problem to the standard from so that the python linprog can be applied
- 4. all problems should be solved with the **Jupyter notebook** and export itas PDF.

Reference

1. NumPy:SciPy:Optimize:linprog

2. D. G. Luenberger, Yinyu Ye, Linear and Nonlinear Programming, Spinger, Chapter 1.

A standard form of linear programming problem can be formulated as

$$\min_{x} c^{T} x$$
such that
$$A_{ub} x \leq b_{up}$$

$$A_{eq} x = b_{eq}$$

$$\ell < x < u$$
(1)

where x is a vector of decision variables; c, b_{up} , b_{eq} , ℓ and u are vectors; and A_{up} and A_{eq} are matrices.



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1. (10 points) Read the linprog guide example and complete following questions.

$$\max_{x_1, x_2, x_3, x_4} 29x_1 + 45x_2$$

such that

$$x_{1} - x_{2} - 3x_{3} \leq 5$$

$$2x_{1} - 3x_{2} - 7x_{3} + 3x_{4} \geq 10$$

$$2x_{1} + 8x_{2} + x_{3} = 60;$$

$$4x_{1} + 4x_{2} + x_{4} = 60$$

$$0 \leq x_{1}$$

$$0 \leq x_{2} \leq 5$$

$$x_{3} \leq 0.5$$

$$-3 \leq x_{4}$$

- (a) (7 points) Transform the problem to the standard form (1) of linear programming. Specify that c, A_{up} , A_{eq} , b_{up} , b_{eq} , ℓ and u.
- (b) (3 points) Exclude the python code in the guide.
- 2. (20 points) Consider the following problem

$$\max x_1 + 4x_2 + x_3$$
 subject to $:2x_1 - 2x_2 + x_3 = 4$
$$x_1 - x_3 = 1$$

$$x_2 \ge 0, x_3 \ge 0$$

- (a) (14 points) Convert the following problem to standard form.
- (b) (6 points) Solve it with linprog
- 3. (30 points) Follow the steps of in question 1. Solve the following to linear programming program

$$\min x + 2y + 3z$$

subject to:

$$2 < x + y < 3$$

$$4 \le x + z \le 5$$

(Hints: you can use addition variables to make the equality constraints.)

- (a) (21 points) Convert the following problem to standard form.
- (b) (9 points) Solve it with linprog



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4. (30 points) A large textile firm has two manufacturing plants, two sources of raw material, and three market centers. The transportation costs between the sources and the plants and between the plants and the markets are as follows

	plant A	plant B
source 1	¥100/ton	¥150/ton
source 2	¥200/ton	¥150/ton

	market 1	market 2	market 3
plant A	¥400/ton	¥200/ton	¥100 /ton
plant B	¥300/ton	¥400 /ton	200/ton

Ten tons are available from source 1 and 15 tons from source 2. The three market centers require 8 tons, 14 tons and 3 tons. The plants have unlimited processing capacity.

- (a) (20 points) Formulate the problem of finding the shipping patterns from sources to plants to markets that minimizes the total transportation cost.
- (b) (10 points) Solve the problem with linprog.