

1. (a) $A \rightarrow B$ (x) $[1 \rightarrow 2, 1 \rightarrow 3, 1 \rightarrow 4]$
- (b) $A \rightarrow C$ (v) $[1 \rightarrow 2, 2 \rightarrow 2]$
- (c) $B \rightarrow A$ (v) $[2 \rightarrow 1, 3 \rightarrow 1, 4 \rightarrow 1, 5 \rightarrow 2]$
- (d) $B \rightarrow C$ (v) $[2 \rightarrow 2, 3 \rightarrow 2, 4 \rightarrow 2, 5 \rightarrow 2]$
- (e) $C \rightarrow A$ (x) $[2 \rightarrow 1, 2 \rightarrow 2]$
- (f) $C \rightarrow B$ (x) $[2 \rightarrow 2, 2 \rightarrow 3, 2 \rightarrow 4, 2 \rightarrow 5]$
- (g) $AB \rightarrow C$ (v) $[1, 2 \rightarrow 2, 13 \rightarrow 2, 14 \rightarrow 2, 25 \rightarrow 2]$
- (h) $AC \rightarrow B$ (x) $[12 \rightarrow 2, 12 \rightarrow 3, 12 \rightarrow 4]$
- (i) $BC \rightarrow A$ (v) $[22 \rightarrow 1, 32 \rightarrow 1, 42 \rightarrow 1, 52 \rightarrow 2]$

2. (a) $A \rightarrow B, B \rightarrow C$ then $A \rightarrow C$ is correct (v)

(b) $AB \rightarrow C$ then $A \rightarrow C$ is incorrect (x)

course ~~class~~, student ~~de~~ determine the teacher, but only the ~~out~~ course can not determine teacher.

(c) correct.

(d) If $A \rightarrow C$ and $B \rightarrow C$ and $ABC \rightarrow D$, then $A \rightarrow D$ is incorrect. Because $A \rightarrow C, B \rightarrow C$ and interpret the $C \rightarrow D$ but not $A \rightarrow D$.



3. $R(A, B, C, D, E)$

$A \rightarrow B$, $B \rightarrow D$, so $A \rightarrow D$, and $CD \rightarrow E$, so $AC \rightarrow E$
So $\{AC\}^+ = \{ABCDE\} = R$.

$B \rightarrow D$, $CD \rightarrow E$ so $BC \rightarrow E$, and $E \rightarrow A$, so $BC \rightarrow A$.
So $\{BC\}^+ = \{ABCDE\} = R$.

$CD \rightarrow E$, $E \rightarrow A$, $A \rightarrow B$ so $CD \rightarrow A$, $CD \rightarrow B$.

So $\{CD\}^+ = \{ABCDE\} = R$.

$E \rightarrow A$, $A \rightarrow B$, $B \rightarrow D$, so $E \rightarrow B$, $E \rightarrow D$.

So $\{CE\}^+ = \{ABCDE\} = R$.

candidate key is $\{AC\}$ $\{BC\}$ $\{CD\}$ $\{CE\}$.

a) $A \rightarrow BCD$, $D \rightarrow E$, so $\{A\}^+ = \{ABCDE\}$

$F \rightarrow GH$, so $\{AF\}^+ = \{ABCDEFGH\} = R$

so candidate key is $\{AF\}$.

b) $A \rightarrow BCD$, ~~$A \rightarrow E$~~ , so $A \rightarrow AD \rightarrow E$.

So $AD \rightarrow E$ is ~~canon~~ redundant, change to $\{A \rightarrow E\}$

$F \rightarrow GH$, so $F \rightarrow H$.

So $EF \rightarrow H$ is redundant. change to $\{F \rightarrow H\}$

Then the canonical cover is $\{A \rightarrow BCD, A \rightarrow E, F \rightarrow H\}$.



4. (a) $A \rightarrow C$, $B \rightarrow D$, so $\{AB\}^+ = \{ABCD\}$

$B \rightarrow D$, $DE \rightarrow F$, so $BE \rightarrow F$.

so $\{ABE\}^+ = \{ABCDEFG\} = R$.

~~so~~ $\{ABE\}$ is a candidate key

cb) A is a key and ~~att~~ attribute ~~is~~ is one both right and left side in the new dependent.

So we ~~now~~ have $\{A \rightarrow B, A \rightarrow C, DE \rightarrow F, B \rightarrow D\}$ now
 $\{A\}^+ = \{ABCD\}$, so if A can determine the E , we
can infer the $\{A\} \rightarrow \{F\}$. So the new dependency
is $\{A \rightarrow E\}$ or $\{C \rightarrow E\}$ or $\{B \rightarrow E\}$ or $\{D \rightarrow E\}$

6. $F_1 = \{A \rightarrow B, B \rightarrow C\} \rightarrow$ it can imply the $A \rightarrow C$
 $F_2 = \{A \rightarrow B, A \rightarrow C\} \rightarrow$ it can not imply the $B \rightarrow C$

$\nsubseteq F_3 = \{A \rightarrow B, AB \rightarrow C\} \rightarrow$ it can imply the $A \rightarrow C$
but it can~~not~~^{not} imply the $B \rightarrow C$.

So F_2 is equivalent to the F_3



7. ca) $\{A \rightarrow B\} \quad [1 \rightarrow 2, 5 \rightarrow 2]$
 $\{C \rightarrow B\} \quad [3 \rightarrow 2, 4 \rightarrow 2, 6 \rightarrow 2]$
 $\{A \oplus C \rightarrow B\} \quad [13 \rightarrow 2, 14 \rightarrow 2, 53 \rightarrow 2, 56 \rightarrow 2]$
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cb) $F = \{A \rightarrow B, C \rightarrow B, AC \rightarrow B\}$
 candidate key = $\{A^C\}$ ~~is~~ because $\{AC\}^+ = F$
 So $\{A\}$ and $\{C\}$ is not candidate

So it violates BCNF, R is decomposed to
 $R_1 = \{AB\} \quad R_2 = \{AC\}$
 so the result is $\{AB\}, \{AC\}$

8. ca) $\{AB\} = \{ABCD \oplus E\} = R$.
 as $\{AB \rightarrow BC\} \{BC \rightarrow CD\} \{CD \rightarrow DE\}$
 $\{BC\} = \{ABCDE\} = R$.
 as $\{BC \rightarrow CD\} \{CD \rightarrow DE\} \{DE \rightarrow A\}$

~~$\{BCD\} = R$~~

$\{BDE\} = \{ABCDE\} = R$.

So $\{AB\}, \{BC\}, \{BDE\}$ are candidate keys for R.



(b) $\{CD \rightarrow E\} \{DE \rightarrow A\}$ is ~~not~~ violations

(c) $R_1 = \{CDE\}$
 $R_2 = \{ABCD\}$ not ~~do~~ violate the BCNF.

(d) $R_1 = \{DEA\}$
 $R_2 = \{BCDE\}$ $DE \rightarrow A$ ~~is~~ ~~do~~ violates the BCNF
 $R_3 = \{CDE\} \{BCD\}$.

(e) ~~A~~ $CD \rightarrow E$ ~~not~~ violates 3NF.

~~$R_1 = \{BC \rightarrow DEA\}$~~

$F_c = \{AB \rightarrow C, BC \rightarrow D, CD \rightarrow E, DE \rightarrow A\}$

$R_1 = \{ABC\}$ $R_2 = \{BCD\}$ $R_3 = \{CDE\}$

$R_4 = \{ADE\}$



(a) $F = \{ \text{stuID} \rightarrow \text{stuName}, \text{profID} \rightarrow \text{profOffice} \}$

(b) $\{ \text{stuID}, \text{profID}, \text{course} \}^+ = R$.

candidate key: $\{ \text{stuID}, \text{profID}, \text{course} \}$

(c) $\text{stuID} \rightarrow \text{stuName}$ violate the BCNF.

So the $R_1 = \{ \text{stuID}, \text{stuName} \}$

$R_2 = \{ \text{stuID}, \text{profID}, \text{course}, \text{profOffice} \}$.

violate because $\text{profID} \rightarrow \text{profOffice}$

$R_3 = \{ \text{profID}, \text{profOffice} \}$

$R_4 = \{ \text{profID}, \text{stuID}, \text{course} \}$

for R_4 , candidate key is $\{ \text{profID}, \text{stuID}, \text{course} \}$.

So the result is R_1, R_3, R_4

(d) $F = \{ \text{stuID} \rightarrow \text{stuName}, \text{profID} \rightarrow \text{profOffice},$

$\text{stuID} \rightarrow \text{profID}, \text{course}, \text{profID} \rightarrow \text{course} \}$
new

(e) $\text{stuID} \rightarrow \text{profID}, \text{profID} \rightarrow \text{profOffice}, \text{profID} \rightarrow \text{course}$

So $\text{stuID} \rightarrow \text{profOffice}$, ~~student~~ $\text{stuID} \rightarrow \text{course}$.

~~$\{ \text{stuID} \}^+ = R$~~ $\{ \text{stuID} \}^+ = R$, $\{ \text{stuID} \}$ is candidate key.

(f) $\text{profID} \rightarrow \text{profOffice}$ violates the BCNF

$R_1 = \{ \text{profID}, \text{profOffice} \}$

$R_2 = \{ \text{profID}, \text{stuID}, \text{course} \}$

candidate key for R_2 is $\{ \text{stuID} \}$.



studID \rightarrow course (\checkmark)

profID \rightarrow course violates BCNF.

$R_3 = \{ \text{profID}, \text{course} \}$.

$R_4 = \{ \text{studID}, \text{profID} \}$.

So the result is $\left\{ \begin{array}{l} \text{studID}, \text{profID} \\ \text{studID}, \text{course} \\ \text{profID}, \text{course} \\ \text{profID}, \text{profoffice} \end{array} \right\} \Rightarrow \{ \text{studID}, \text{profID}, \text{course} \}$

10.

(1) $\{AB\}^+ = \{ABC EFD\} \neq R$.

$\{B\}^+ = \{BEFCDA\}$

$\{G\}^+ = \{G\}$.

$\{AB\}$ is not a surkey

(2) $\{B\}^+ = \{ABCDEF\}$

$\{BG\}^+ = \{ABCDEF G\} = R$

$\{CFG\}^+ = \{ABCDEF EG\} = R$ ①

$\{CDG\}^+ = \{ABCDEF G\} = R$ ②

because $\left\{ \begin{array}{l} CF \rightarrow CD, CD \rightarrow B \\ CD \rightarrow B \end{array} \right.$ ① ②

So $\{BG\}$, $\{CFG\}$, $\{CDG\}$ are candidate keys.



(3)

$B \rightarrow C, B \rightarrow E$ and $CE \rightarrow F$

can imply $B \rightarrow CE \rightarrow F$

so $B \rightarrow F$ ~~is~~ should be deleted.

Then $B \rightarrow C, B \rightarrow E, B \rightarrow F$ can be written as $B \rightarrow CE$.

so the $F_c = \{AB \rightarrow C, B \rightarrow CE, CF \rightarrow D, CD \rightarrow B, C \rightarrow A\}$

