

Multizestaw zadań

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1 Wiekł/C1.1a

1. Zadanie z Wiekł C 1.1a moja wersja nr [nrWersji]

Oblicz całkę

$$\int \sqrt{x}([a] - x^2)^2 dx.$$

Rozwiązanie (autor Aleksandra Pasińska , recenzent):

$$\begin{aligned} \int \sqrt{x}([a] - x^2)^2 dx &= \int \sqrt{x}([aa] - [a2]x^2 + x^4) dx = \\ &= \int [aa]\sqrt{x} - [a2]x^2\sqrt{x} + x^4\sqrt{x} dx = \int [aa]x^{\frac{1}{2}} - [a2]x^2 \cdot x^{\frac{1}{2}} + x^4 \cdot x^{\frac{1}{2}} dx = \\ &= \int [aa]x^{\frac{1}{2}} - [a2]x^{\frac{5}{2}} + x^{\frac{9}{2}} dx = [aa] \int x^{\frac{1}{2}} dx - [a2] \int x^{\frac{5}{2}} dx + \int x^{\frac{9}{2}} dx = \\ &= [aa] \cdot \frac{2x^{\frac{3}{2}}}{3} - [a2] \cdot \frac{2x^{\frac{7}{2}}}{7} + \frac{2x^{\frac{11}{2}}}{11} = [aa] \cdot \frac{2x\sqrt{x}}{3} - [a2] \cdot \frac{2x^3\sqrt{x}}{7} + \frac{2x^5\sqrt{x}}{11} + C = \\ &= \frac{[aa2]x\sqrt{x}}{3} - \frac{[a22]x^3\sqrt{x}}{7} + \frac{2x^5\sqrt{x}}{11} + C \end{aligned}$$

Odpowiedź:

$$\frac{[aa2]x\sqrt{x}}{3} - \frac{[a22]x^3\sqrt{x}}{7} + \frac{2x^5\sqrt{x}}{11} + C$$

Test:

$$\begin{aligned} \text{A. } &\frac{[aa2]x\sqrt{x}}{3} - \frac{[a22]x^3\sqrt{x}}{7} + \frac{2x^5\sqrt{x}}{11} + C \quad \text{B. } -\frac{2x^5\sqrt{x}}{11} + C \quad \text{C. } \frac{[aa2]x\sqrt{x}}{3} - 2 + C \quad \text{D. } \frac{[aa2]x\sqrt{x}}{3} + C \\ \text{E. } &\frac{2x^5\sqrt{x}}{11} + C \quad \text{F. } \frac{[a22]x^3\sqrt{x}}{7} + \frac{2x^5\sqrt{x}}{11} + C \quad \text{G. } -\frac{[a22]x^3\sqrt{x}}{7} + \frac{2x^5\sqrt{x}}{11} + C \quad \text{H. } \frac{[aa2]x\sqrt{x}}{3} + \\ &\frac{2x^5\sqrt{x}}{11} + C \quad \text{I. } \frac{[aa2]x\sqrt{x}}{3} - \frac{[a22]x^3\sqrt{x}}{7} + C \end{aligned}$$

Test poprawna odpowiedź:

A