

Multizestaw zadań

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1 Wikieł/C1.1n

1. Zadanie z Wikieł C 1.1n moja wersja nr [nrWersji]

Oblicz całkę

$$\int \frac{[a] \cdot [b]^x - [c] \cdot [d]^x}{[e]^x} dx.$$

Rozwiązanie (autor Justyna Chojecka , recenzent):

$$\begin{aligned} \int \frac{[a] \cdot [b]^x - [c] \cdot [d]^x}{[e]^x} dx &= \int \left(\frac{[a] \cdot [b]^x}{[e]^x} - \frac{[c] \cdot [d]^x}{[e]^x} \right) dx \\ &= \int \frac{[a] \cdot [b]^x}{[e]^x} dx - \int \frac{[c] \cdot [d]^x}{[e]^x} dx = [a] \int \frac{[b]^x}{[e]^x} dx - [c] \int \frac{[d]^x}{[e]^x} dx \\ &= [a] \int \left(\frac{[b]}{[e]} \right)^x dx - [c] \int \left(\frac{[d]}{[e]} \right)^x dx = \frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]} \right)^x - \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C \end{aligned}$$

Odpowiedź:

$$\frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]} \right)^x - \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$$

Test:

- A. $\frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]} \right)^x - \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$
- B. $\frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]} \right)^x - \frac{[d]}{\ln\left(\frac{[c]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$
- C. $-\frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]} \right)^x - \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$
- D. $\frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]} \right)^x - \frac{[c]}{\ln\left(\frac{[e]}{[d]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$
- E. $\frac{[a]}{\ln\left(\frac{[e]}{[b]}\right)} \left(\frac{[b]}{[e]} \right)^x + \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$
- F. $\frac{[a]}{\ln\left(\frac{[e]}{[b]}\right)} \left(\frac{[b]}{[e]} \right)^x - \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$
- G. $\frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]} \right)^x + \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]} \right)^x + C$

$$\text{H. } \frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]}\right)^x + \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]}\right)^x + C$$

$$\text{I. } -\frac{[a]}{\ln\left(\frac{[b]}{[e]}\right)} \left(\frac{[b]}{[e]}\right)^x + \frac{[c]}{\ln\left(\frac{[d]}{[e]}\right)} \left(\frac{[d]}{[e]}\right)^x + C$$

Test poprawna odpowiedź:

A