Design and Analysis of Algorithms

L09: Fundamental Data Structures

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Resources

Text book I: Levitin

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Fundamental Data Structures

- Primarily support 4 kinds of operations
 - Insert (or add) an item
 - Search (or find) an item
 - Find minimum is specific case
 - Delete (or remove) an item
 - Delete minimum is specific case
 - Modify (or update)
- Cost (efficiency) of the operation depends on underlying data structure in use.
- Unsorted array:
 - Insert: O(I), Search O(n)
- Sorted array
 - Insert: O(log n), Search: O(log n)

Fundamental Data Structures

- Choosing a data structure
 - Determine the operations you need to perform,
 - How much cost to be paid for operation
- Examples:
 - Email:
 - Insert, delete, search
 - No modify/update
 - Class attendance
 - Insert (fastest), modify and search (rarely),
 - No delete operation
 - Contacts (or address book)
 - All 4 operations
 - Search should be fastest

Fundamental Data Structures

- Lists
 - Arrays, Linked Lists, Strings
- Stacks
- Queues
- Priority queues
- Trees and Binary trees
- Graphs
- Sets
- Dictionaries

Lists

- Arrays
 - A sequence of n items of same types
 - Stored continguously in memory
 - Elements are accessed by element index
 - Single dimensional, multi-dimensional array
- Linked List
 - A sequence of n items (nodes)
 - Node has two kind of information
 - Some data corresponding to node
 - One or more links to other nodes
 - Singly linked list
 - Doubly linked list

Stacks

- Storing items in a way that only top item is accessible
 - Also called LIFO
- Operations:
 - Push (Add)
 - Pop (Delete)
 - Read
 - Search ?? (not inside the stack)
 - IsEmpty
 - IsFull?
- Typically implemented as array (or even list)

Queues

- Storing items in a way that only first (head) and last (tail) item is accessible
 - Also called FIFO
- Operations:
 - Enqueue (Add)
 - At the rear
 - Dequeue (Delete)
 - At the front

Priority Queues

- A data structure that maintains items (elements) such that each is associated with
 - A key (or priority) value
- Operations
 - Finding item with highest priority (find min)
 - Deleting the item with highest priority (delete min)
 - Inserting a new element (with its own priority)
- Examples:
 - Scheduling a job on computer

Graphs

- A graph $G = \langle V, E \rangle$ is defined by a pair of two sets:
 - A finite set V of items called vertices, and
 - A set E of vertex pairs called edges.
- Graphs are of two types
 - Undirected Graphs
 - Given a graph of n nodes, max edges?
 - Directed graphs
- Other graph categorization
 - Complete Graph
 - Dense Graph
 - Sparse graphs

Graph Representation

- Adjacency matrix
 - n x n boolean matrix if |V| is n.
 - The element on the ith row and jth column is 1
 - If there's an edge from ith vertex to the jth vertex
 - Otherwise 0.
 - The adjacency matrix of an undirected graph is symmetric.
- Adjacency linked lists
 - A collection of linked lists, one for each vertex;
 - contain all the vertices adjacent to the list's vertex.
- Weighted graphs: edges with weights
- Q: which data structure would you use if the graph is a 100-node star shape?

Graph Properties

- Path from node u to v
 - A sequence of adjacent (connected by an edge) vertices that starts with u and ends with v.
 - -Simple path: all edges of a path are distinct.
 - -Q: what happens when edges are not distinct?
- -Conencted graphs
 - For every pair of its vertices u and v
 - There exists a path from u to v.
- subgraph
 - A subset V' of V, with all of its edge corresponding to V'
 - \bullet if $u \in V'$, $v \in V'$, and $(u,v) \in E$, then $(u,v) \in E'$
- Connected component
 - The maximum connected subgraph of a given graph.
- Strongly connected components (for directed graphs)

Graphs: Acyclicity

- Cycles in a graph G=(V,E)
 - A simple path of positive length that starts from a vertex and ends at same vertex
- Cyclic graphs
 - A graph having cycles
- Acyclic graphs
 - A graphh without cycles
 - Direced acyclic graphs

Trees & Forest

- Tree is a connected acyclic graph
- Forest: A graph that has no cycles but necessarily not connected
 - There may exist 2 nodes u and v for which no path exist between them
- Every two vertices of tree
 - There exists exactly one path between these nodes
- Rooted tree:
 - Identify a vertex of tree and deginate is as root
 - Levels in a rooted tree
 - Root is level 0,
 - Directly connected nodes from root are at level 1.

Rooted Trees

- Ancestors
 - For any vertex v in a tree T, all the vertices on the simple path from root to that vertex are called ancestors of v
- Descendants
 - All the vertices for which a vertex v is an ancestor are said to be descendants of v.
- Parent, child and siblings
 - If (u, v) is the last edge of the simple path from the root to vertex v, u is said to be the parent of v and v is called a child of u.
 - Vertices that have the same parent are called siblings.
- Leaves
 - A vertex without children is called a leaf.

Rooted Trees

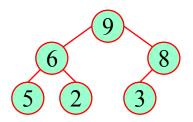
- Subtree
 - A vertex v with all its descendants is called the subtree of T rooted at v.
- Depth of a vertex
 - The length of the simple path from the root to the vertex.
- Height of a tree
 - The length of the longest simple path from the root to a leaf.

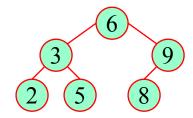
Ordered Trees

- Ordered trees
 - An ordered tree is a rooted tree in which all the children of each vertex are ordered.
- Binary trees
 - A binary tree is an ordered tree in which every vertex has no more than two children and each children is designated s either a left child or a right child of its parent.
- Binary search trees
 - Each vertex is assigned a number.
 - A number assigned to each parental vertex is larger than all the numbers in its left subtree and smaller than all the numbers in its right subtree.
- $\lfloor \log_2 n \rfloor \le h \le n 1$, where h is the height of a binary tree and n the size.

Ordered Trees

 Q:Which of the following tree is ordered tree and which one is binary search tree?





Summary

- Lists
- Stacks
- Queues
- Priority Queues
- Graphs
- Trees
- Ordered trees
- Sets
- Dictionaries