

ExaHyPE Guidebook

http://www.exahype.eu

Version 1.0

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Preamble

ExaHyPE stands for an "Exascale Hyperbolic PDE Engine", where the term "PDE Engine" represents the novel idea of a software suite comparable to a game engine. However, instead of offering all the neccessary functions to render 3D scenes, manage the gameplay and all that (as a game engine would do), our PDE Engine offers similar ways to solve particular systems of Partial Differential Equations.

This document details

- how some "simple" demonstrators are ran,
- how a new application can be kicked off,
- and also details and documents how the program suite is working and meant to be used.

To read more about the project, we refer to the official website http://www.exahype.eu as well as the objectives at the EU's cordis page.

ExaHyPE is a collection of open source tools and mainly written in C, C++, FOR-TARN, Java, Matlab and Python.

Who should read this document

This guidebook is written similar to a tutorial in a hands-on style. It addresses users of ExaHyPE. It is not meant to help developers or replace code documentation. Using the guidebook requires a decent knowledge of the application domain modelled via a hyperbolic equation system. It does not require deep programming knowledge.

Everything in this guidebook runs out-of-the-box by following the written text only. There are however few additional steps that advanced users might want to try out. Those do not come along with very detailed step-by-step descriptions. They are marked with an (optional) postfix in the title. Standard or new users should just skip these sections.

February 2, 2017 The ExaHyPE team

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Part I.

ExaHyPE installation and demonstrator applications

1. Setup and Installation

1.1. Dependencies and prerequisites

ExaHyPE comes along with very few dependencies:

- ExaHyPE source code is C++ code. For serial codes, plain C++ does the job. All examples from this guidebook run and have been tested with GCC 4.2 and Intel 12 or later. Earlier compiler versions might work. There are no further dependencies or libraries required.
- You may prefer to write parts of your ExaHyPE code in Fortran. In this case, you need a Fortran code. ExaHyPE itself does not require Fortran.
- If you want ExaHyPE to exploit your multi- or manycore computer, you have to have Intel's TBB or OpenMP. Both come along with recently new Intel compilers.
- If you want to run ExaHyPE on a distributed memory cluster, you have to have MPI installed. ExaHyPE uses only very basic MPI routines. In our tests, basically any MPI version works.
- ExaHyPE's development environment relies on Java. We provide some jars but we do not test which versions they are built against. You can always build your own version of all development tools as long as you have a Java compiler. Again, ExaHyPE uses only very basic Java, so most versions should do.
- ExaHyPE's default build environment uses GNU Make.
- If you want to use ExaHyPE's optimised compute kernels, you have to have Intel's libxsmm¹

The guidebook assumes that you use a Linux system. It all should work on Windows and Mac as well, but we haven't tested it in detail. ExaHyPE also can not provide any support for these platforms. The code itself is minimalistic, i.e. in ExaHyPE's basic form no further libraries are required.

1.2. Obtaining ExaHyPE

ExaHyPE is available as source code only.

¹https://github.com/hfp/libxsmm

1.2.1. Downloading an official ExaHyPE distribution

ExaHyPE can be obtained from www.exahype.eu. Each release consists of at least three archives/files:

- 1. The actual ExaHyPE sources is a tar.gz archive. It contains the actual engine with all mesh organisation, computational kernels, load balancing components, and so forth.
- 2. ExaHyPE is based upon the PDE solver framework Peano (peano-framework.org) which provides the underlying adaptive mesh refinement (AMR) data structures as well as mesh traversal algorithms.
- 3. The engine is used through a Java toolbox that provides the opportunity to configure the engine to a particular setup. The sources for the latter typically are not required, but they are available from the ExaHyPE home page.
- 4. For some demonstrator applications, we provide additional archives comprising the actual application code.

A complete download/setup reads as follows:

```
> cd mywellsuiteddirectory
> wget http://www.exahype.eu/exahype.tar.gz
> wget http://sourceforge.net/projects/peano/files/peano.tar.gz
> wget http://www.exahype.eu/exahype.jar
> tar -xzf exahype.tar.gz
> ls
Applications ExaHyPE exahype.jar exahype.tar.gz peano peano.tar.gz
> tar -xzf peano.tar.gz -C peano
```

You might choose to maintain a different directory structure or rely on a previous Peano or ExaHyPE installation. In this case, you have to adopt pathes in your ExaHyPE scripts.

1.2.2. Downloading ExaHyPE's development branch

ExaHyPE is held in a git repository. Copy and paste this mini installation guide into your Linux terminal:

```
git clone git@gitlab.lrz.de:exahype/ExaHyPE-Engine.git
cd ExaHyPE-Engine/Peano
./checkout-update-peano.sh
cd ../Toolkit/
./build.sh
cd ../
ln -s Toolkit/dist/ExaHyPE.jar
```

These steps give you access to the latest ExaHyPE development version. The repository currently is closed source. If you require access, you have to get in touch with the ExaHyPE team.

1.3. Dry run of development tools

To check whether you are ready to program new applications with ExaHyPE, type in

```
> java -jar ExaHyPE.jar
```

This should give you the following welcome message:

The project has received funding from the European Unions Horizon 2020 research and innovation programme under grant agreement No 671698 (ExaHyPE). It is based upon the PDE framework Peano (www.peano-framework.org).

ERROR: Please provide input file as argument

If you don't see this message, there's a problem with the java based ExaHyPE toolbox.

1.4. Using a newer/other **Peano** version

ExaHyPE is based upon the PDE solver framework Peano (peano-framework.org). With the present scripts, you use the newest stable Peano release. As Peano is still improved, it might make sense to download a new archive from time to time.

ExaHyPE uses a couple of Peano toolboxes. These toolboxes are part of Peano's framework, but they are not by default included in the release. While normal Peano users have to download them manually, we provide a snapshot with ExaHyPE. These snapshots are help in ExaHyPE's Peano directory. If you want to try newer versions, download the corresponding toolboxes from Peano's webpage and extract them manually into ExaHyPE's Peano subdirectory.

If you use Peano in several projects, it might make sense to skip the download of the archive into ExaHyPE's Peano directory and instead add two symbolic links with 1n -s in the Peano directory to Peano's peano and tarch directory.

2. Demonstrator applications

We provide a small number of out-of-the-box ExaHyPE applications. They suit three purposes:

- 1. They allow users to assess whether their installation is working, and which size/characteristics of ExaHyPE codes their system is able to run. They act as technical assessment exercise.
- 2. They allow newbies to study particular technical concepts. As some demonstrator codes are minimalistic, it is easier for users to find out how certain things are realised than searching for features in large-scale applications.
- 3. Within the underlying EU H2020 ExaHyPE project, the team had committed to publish some grand challenge software. Our demonstrators cover (parts of) these grand challenge codes.

2.1. Euler equations with Finite Volumes

2.1.1. Preparation

We provide a complete Finite Volume implementation of a plain Euler solver realised with ExaHyPE. This solver solves exactly the same setups as the ADER-DG Euler solver and relies, as our ADER-DG basic variants, on a Rusanov solver. It is used by the ADER-DG variant as a limiter, too. With the Finite Volume code at hands, you can quickly assess the efficiency of ExaHyPE's ADER-DG scheme.

An archive provides you with all required sources, but you need the ExaHyPE kernel, the toolkit and Peano, too:

```
> wget http://www.exahype.eu/demonstrator-EulerFlowFVM.tar.gz
```

This archive has to be unzipped. It contains solely files modified to realise the solver. All glue code and all files that are typically generated by the toolkit, could be altered, but have not been altered for this particular application, are not contained in the archive either. We thus have to recreate them:

```
> mkdir ApplicationExamples
> wget http://www.exahype.eu/demonstrator-Euler-FiniteVolumes.tar.gz
> tar -xzvf demonstrator_EulerFlowFVM.tar.gz
> cd ..
> java -jar ../ExaHyPE.jar ApplicationExamples/EulerFlowFVM.exahype
```

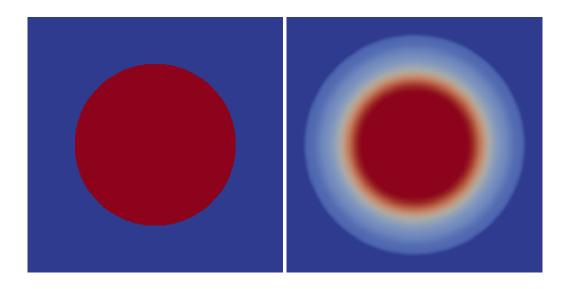
Finally, change into the directory ApplicationExamples/EulerFlowFVM and type in make. Depending on your environment (compilers, e.g.), you might have to adopt some environment variables, but the toolkit should give verbose information on all the various options.

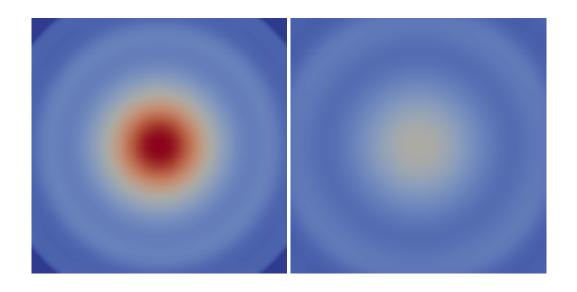
2.1.2. Run

Once the compile has been successful, you obtain an executable ExaHyPE-EulerFVM in your application-specific directory. ExaHyPE's specification files always act as both specification and configuration file, so you start up the code by handling it over the spec file again:

./ExaHyPE-EulerFVM ../EulerFlowFVM.exahype

A successful run yields a sequwence of vtk files that you can open with Paraview or VisIt, e.g. There are two quantitites plotted: The time encodes per vertex and quantity at which time step the data has been written. For these primitive tests with global time stepping, this information is of limited value. It however later makes a big difference if parts of the grid are allowed to advance in time asynchronous to other grid parts. The second quantity Q is a vector of the real unknowns. The underlying semantics of the unknowns is detailed in Section 4. For the time being, you may want to select first entry which is the density or the last quantity representing the local energy.





3. Source code documentation

ExaHyPE realises an "everything is in the code" philosophy. This guidebook give a high level overview and some references as well as recipes that do not align directly with a particular code snippet. Our papers detail the mathematical ideas, scientific outcomes and algorithmic concepts. Everything else is documented right inside the code.

Our paradigm is to document our code in the header files in JavaDoc syntax, i.e. documentation reads as

```
/**

*
*This is an ExaHyPE comment.

*
*/
```

No important code documentation is found inside the actual source code. It is always in the header. Typical header documentation comprises information alike

- what does a function do?
- how is a function to be used?
- how is the function's semantics realised?
- which alternatives have been considered (and probably discarded throughout the development process)?
- what bugs did arise, how have they been fixed, and why did the drop in in the first place?

Accessing the documentation

Modern integrated development environments (IDEs) such as Eclipse parse header files and extract our documentation automatically. They then are able to display documentation on-the-fly within the editor. This is our major motivation to stick to the /** . . . */ syntax and to the "everything is documented in the header" convention.

If you prefer not to use an IDE, the ExaHyPE project extracts all documentation from all source code parts automatically each and every night and creates a webpage (Figure 3.1) from this information. The webpage is available through

exahype.eu¹ and provides, besides hyperlinks and sketches of algorithmic concepts, a search engine.

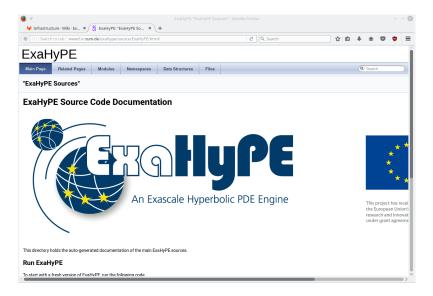


Figure 3.1.: The ExaHyPE source code documentation webpage that is updated every night.

ExaHyPE's adaptive meshing is based upon the framework Peano. You find both Peano and its source code documentation at www.peano-framework.org.

Create all documentation locally

The webpage generation is based upon the open source tool Doxygen (www.doxygen.org). If you prefer to have all source code documentation in HTML form on your local computer, you may prefer to change into ExaHyPE's ExaHyPE source directory and type in

doxygen exahype.doxygen-configuration

By default, no particular application is made part of the source code documentation. All HTML pages refer to the pure engine. Also, we do not document any toolbox/feature from Peano. It is however easy to augment your local documentation by these details. For this, you just extend the source/parsed files in the configuration file exahype.doxygen-configuration.

¹Should the official page be down, you may access the documentation via its direct link http://www5.in.tum.de/exahype/source/ExaHyPE/html.

Part II.

Developing new **ExaHyPE** applications

4. Preparing a new **ExaHyPE** development project

ExaHyPE is written for high performance computing experiments. Our philosophy is write one code specification per experiment/machine/setup configuration and sacrifice flexibility in exchange for performance. Because of this, ExaHyPE specification files act on the one hand as configuration files that are passed into the executable for a run. On the other hand, a specification file tailors the executable, i.e. is used to generate some source code. The compiler can, at hands of the specification, optimise aggressively in several places. ExaHyPE prefers to run the compiler more often rather than working with one or few generic executables.

An ExaHyPE specification is a text file where you specify exactly what you want to solve in which way. This file¹ is handed over to our ExaHyPE toolkit, a small Java application generating all required code. This code (also linking to all other required resources such as parameter sets or input files) then is handed over to a compiler. You end up with an executable that may run without the Java toolkit or any additional sources from ExaHyPE. It however rereads the specification file again for input files or some parameters, e.g. We could have worked with two different files, a specification file used to generate code and a config file, but decided to have everything in one place.

4.1. Setting up trivial demonstration project

A trivial project in ExaHyPE is described by the following specification file:

```
exahype-project TrivialProject
  peano-path = ./Peano/peano
  tarch-path = ./Peano/tarch
  multiscalelinkedcell-path = ./Peano/multiscalelinkedcell
  sharedmemoryoracles-path = ./Peano/sharedmemoryoracles
  exahype-path = ./ExaHyPE

output-directory = ./Applications/trivialproject

architecture = noarch

computational-domain
```

¹Some examples can be found in the Toolkit directory or on the ExaHyPE webpage. They have the extension exahype.

```
dimension = 2
width = 1.0, 1.0
offset = 0.0, 0.0
end-time = 10.0
end computational-domain
end exahype-project
```

Most parameters should be rather self-explanatory. You might have to adopt some of the paths. Note ExaHyPE supports both two- and three-dimensional setups. We hand the file over to the toolkit

```
java -jar ExaHyPE.jar examples/trivial-project-2d.exahype
```

and observe that the toolkit has created a new directory Applications/trivialproject. We change into this directory and type in

```
make
```

which gives us an executable. The toolkit plots additional information how to switch into debug versions of the code or how to switch to another compiler through environment variables. For most systems, the defaults should do. We finally run this first ExaHyPE application with

```
./ExaHyPE <yourpath>/trivial-project-2d.exahype
```

Within the section computational-domain, all entries except the dimension can be changed before application startup: If you change their value, there is no need to recompile or to rerun the toolkit again.

If you have to check from which settings your build has been created, you may always type in

```
./ExaHyPE --version
```

4.2. Introducing physics: 2d Euler flow

So far, the simulation run neither computes anything nor does it give you any output. We close this section with a brief demonstration how to realise a 2d Euler flow within ExaHyPE. ExaHyPE's fundamental idea is that the user specifies all PDEs she wants to solve within the specification file. We start with a solve of the compressible Euler equations via the ADER-DG method. For this type of solver, the engine needs to know how many unknowns the solved PDE has and which polynomial order shall be used. We do not have any material involved, so we set the field parameters to 0.

For the actual computations, there are three types of kernels (PDE solver realisations) that can be used within ExaHyPE. You can either write the whole solver yourself, you can make ExaHyPE realise the solver while you specify the flux update operations, or you can use a pre-defined ExaHyPE kernel which gives you the best performance. Available options are described and detailed in Chapter D. For

the time being, we use kernel = generic::fluxes::nonlinear, the generic kernels for non-linear PDEs, where PDE-specific functions, e.g. the flux function, yet have to be specified by us.

In the present example, we rely on the latter variant. We also stick to a regular grid simulation for the time being. The specification file then is

```
exahype-project MyEuler

[...]

output-directory = ./Applications/guidebook-chapter-2
architecture = noarch

solver ADER-DG MyEulerSolver
  unknowns = 5
  parameters= 0
  order = 3
  kernel = generic::fluxes::nonlinear
  language = C
  end solver

end exahype-project
```

We run the toolkit and end up with a new directory Applications/guidebook-chapter-2. Within this directory, there is a file MyEulerSolver.cpp that we have to complete as follows:

```
#include "MyEulerSolver.h"
MyEuler::MyEulerSolver::MyEulerSolver(int nodesPerCoordinateAxis,
  double maximumMeshSize,
  exahype::solvers::Solver::TimeStepping timeStepping,
  std::unique_ptr<exahype::profilers::Profiler> profiler):
exahype::solvers::ADERDGSolver("MyEulerSolver", 5, 0,
  nodesPerCoordinateAxis, maximumMeshSize, timeStepping,
  std::move(profiler)) {
}
int MyEuler::MyEulerSolver::getMinimumTreeDepth() const {
 return 3;
}
// ...
void Euler::MyEulerSolver::adjustedSolutionValues(...) {
 if (tarch::la::equals(t, 0.0)) {
   const double GAMMA = 1.4;
   Q[0] = 1.;
```

Actually, only proper initial conditions have to be provided. The remainder is pre-generated.

To set the initial conditions, we need to implement two of the pregenerated functions: We specify that we want to adjust the solution values at time t=0 in function hasToAdjustSolutionValues and then set initial conditions via the function adjustedSolutionValues. We clarify the semantics of the arguments of hasToAdjustSolutionValues and adjustedSolutionValues in Chapter 5. For the time being, we compile and run the code.

4.3. A remark on material parameters

In ExaHyPE, we do not really distinguish unknowns that are subject to a PDE from parameters on the user side. If you have 4 unknowns and 3 (material) parameters, all functions just seem to handle 4+3=7 variables. We only distinguish the values in the script file as we obviously do not want to run any PDE kernel (unknown update) on top of the material parameters. For them, we restrict to a subset of all the variables—namely the first 4 in the example above. To the user, we do not distinguish material parameters from unknowns. When you set up the initial condition, e.g., you will be passed 7 unknowns.

4.4. Introducing Plots

Still, the simulation does not give any output besides status messages on the terminal. We have to add appropriate plotters. ExaHyPE offers a couple of predefined export mechanisms. Within each solver section, we may use an arbitrary number of plotters to pipe the result at certain time steps into files. We start with

•••

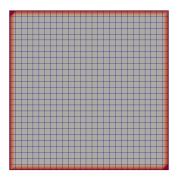


Figure 4.1.: Exemplary grid

```
solver ADER-DG MyEulerSolver
unknowns = 5
parameters= 0
order = 3
kernel = generic::fluxes::nonlinear
language = C

plot vtk::binary MyPlotter
unknowns = 5
time = 0.0
repeat = 0.02
output = ./solution
select = {}
end plot
end solver
...
```

and postpone a detailed explanation to later chapters. For the time being, it is sufficient to note that this operation writes VTK binary files (they can be read in by Paraview or VisIt, e.g.) into files named solution... .vtk. The first file is written at time 0, i.e. at startup time. From hereon, we obtain a new snapshot every 0.02 simulation intervals.

Once you have inserted the plotter into your specification file, invoke the toolkit again, compile the code and run the simulation. You obtain a sequence of files yielding images similar to the grid shown in figure 4.1.

ADER-DG solvers with user-defined kernels

In this chapter, we introduce ExaHyPE's kernels that allow the user to specify flux and eigenvalue functions for the kernels (for linear problems), but leaves everything else to ExaHyPE. The resulting code can run in parallel and scale, but its single node performance might remain poor, as we do not rely on ExaHyPE's high performance kernel. Therefore, the present coding strategy is well-suited for rapid prototyping of new solvers. To outline the steps a user has to perform to define his own fluxes and state-depending initial values, we again consider the compressible Euler equations with d=2. This is the example we also used in Chapter 4.

For the Euler equations

$$\frac{\partial}{\partial t}\mathbf{Q} + \mathbf{\nabla} \cdot \mathbf{F}(\mathbf{Q}) = 0 \quad \text{with} \quad \mathbf{Q} = \begin{pmatrix} \rho \\ \mathbf{v} \\ E \end{pmatrix} \quad \text{and} \quad \mathbf{F} = \begin{pmatrix} \mathbf{v} \\ \frac{1}{\rho}\mathbf{v} \otimes \mathbf{v} + pI \\ \frac{1}{\rho}\mathbf{v} \left(E + p\right) \end{pmatrix}$$

supplemented by initial values $\mathbf{Q}(0) = \mathbf{Q}_0$ and appropriate boundary conditions, we rewrite the conserved quantities \mathbf{Q} and fluxes \mathbf{F} into an equation over five state unknowns

$$\mathbf{Q} = \begin{pmatrix} Q_0 \\ Q_1 \\ Q_2 \\ Q_3 \\ Q_4 \end{pmatrix} = \begin{pmatrix} \rho \\ v_x \\ v_y \\ v_z \\ E \end{pmatrix}$$

which are discretised over Ω .

Here, ρ denotes the mass density, $\mathbf{v} \in \mathbb{R}^d$ denotes the velocity vector, E denotes the energy, and p denotes the fluid pressure. For our 2d setup, the velocity in z-direction v_z is set to zero.

Introducing the adiabatic index γ , the fluid pressure is here defined as

$$p = (\gamma - 1) \left(E - \frac{1}{2} \mathbf{v}^2 / \rho \right).$$

A corresponding specification file euler-2d. examype for this setup is

exahype-project Euler2d

peano-path = ./Peano/peano
tarch-path = ./Peano/tarch

```
multiscalelinkedcell-path = ./Peano/multiscalelinkedcell
 sharedmemoryoracles-path = ./Peano/sharedmemoryoracles
 exahype-path = ./ExaHyPE
 output-directory = ./ApplicationExamples/EulerFlow
 architecture = noarch
 computational-domain
   dimension = 2
   width = 1.0, 1.0
   offset = 0.0, 0.0
   end-time = 0.4
 end computational-domain
 solver ADER-DG MyEulerSolver
   variables = 5
   parameters = 0
   order = 3
   maximum-mesh-size = 0.1
   time-stepping = global
   kernel = generic::fluxes::nonlinear
   language = C
   plot vtk::binary MyPlotter
     variables = 5
     time = 0.0
     repeat = 0.05
     output = ./solution
     select = {}
   end plot
 end solver
end exahype-project
```

The script sets some paths in the preamble before it specifies the computational domain and the simulation time frame in the environment computational-domain.

In the next lines, a solver of type ADER-DG is specified and assigned the name MyEulerSolver. The kernel type of the solver is set to generic::fluxes::nonlinear. This tells the ExaHyPE engine that we do not provide it with problem specific and highly optimized ADER-DG kernels. Instead we tell it to use some generic partially optimized ADER-DG kernels that can be applied to virtually any hyperbolic problem. In this case, the user is only required to provide the ExaHyPE engine with problem specific flux (and eigenvalue) definitions.

Within the solver environment, there is also a plotter specified. The specified plotter is configured to write binary VTK output by setting its identifier to vtk::binary. The plotter is further configured to write out a snapshot of the solution of the associated solver every 0.05 time intervals. The first snapshot is set to be written at time t=0. The above plotter statement creates a plotter file MyPlotter

that allows you to alter the plotter's behaviour.

Once we are satisfied with the parameters in our ExaHyPE specification file, we hand it over to the ExaHyPE toolkit:

```
java -jar <mypath>/ExaHyPE.jar Euler2d.exahype
```

5.1. Study the generated code

We obtain a new directory (equalling output-directory from the specification file) and change into this file. It contains a makefile, some helper files, and a new class MyEulerSolver. This new class was generated according to the solver entry ADER-DG MyEulerSolver that we have specified in our script.

Class MyEulerSolver is divided into three source code files: First, there is a header that we might want to extend later on. For the time being, it suits our needs. There is further an implementation file with an addendum _generated. This is a file we should never edit since it is overwritten every time we use the toolkit to generate code for our problem. Finally, there is another implementation file that we will use to realise the actual solver behaviour. Here, we will specify the aforementioned user defined flux and eigenvalue definitions that are necessary if we want to use the generic ADER-DG kernels.

Before we start to do so, it might be reasonable to compile the overall code once and to doublecheck whether we can visualise the resulting outputs. This should all be straightforward. Please verify that any output you visualise holds only zero values since the initial values are set to zero at the moment.

If you translate in debug mode or with assertions, ExaHyPE might even stop with an assertion.

5.2. Setting up the experiment

To set up the experiment, we open the implementation file MyEulerSolver.cpp of the class MyEulerSolver. There is one routine adjustedSolutionValues that allow us to setup the initial grid. The implementation of the initial values might look as follows¹:

```
void Euler2d::MyEulerSolver::adjustedSolutionValues(
  const double *const x,
  const double w,
  const double t,
  const double dt,
  double *Q
) {
  if (tarch::la::equals( t,0.0,1e-15 )) {
    const double GAMMA = 1.4;
```

¹The exact names of the parameters might change with newer ExaHyPE versions and additional parameters might drop in, but the principle always remains the same.

The above routine enables us to specify time dependent solution values. It further enables us to add source term contributions to the solution values. While the routine itself is more or less self-explaining, we nevertheless highlight a few details:

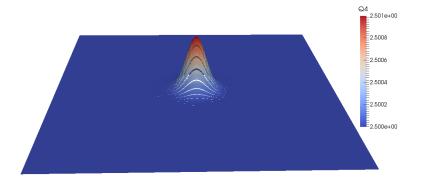
- We only want to impose initial conditions so we check if the time t is zero with respect to some tolerance in the first line of the routine.
- While the unknown pointer Q itself does not give any hint about the actual size of the array it points at, we know by construction that we have five unknowns per grid point and thus choose the iteration space accordingly. Note that as usual for C type languages indexing of the array starts with zero.
- The spatial position x is given as a pointer to a double array of size dimension which you have previously specified in the script euler-2d.exahype. Note that the indexing of the arrays starts here of course also with zero.

The routine adjustedSolutionValues must always be paired with the routine has—ToAdjustSolution that specifies when and in which grid cell we want to adjust solution values:

```
bool Euler2d::MyEulerSolver::hasToAdjustSolution(
   const tarch::la::Vector<DIMENSIONS,double>& center,
   const tarch::la::Vector<DIMENSIONS,double>& dx,
   double t
) {
   if (tarch::la::equals( t, 0.0 ,1e-15 )) {
     return true;
   }
   return false;
}
```

The routine's arguments center and dx refer to the center point of the cell and to its extent in each coordinate direction. The simulation time is here again denoted by t.

We conclude our experimental setup with a compile run and a first test run. This time we get a meaningful image and definitely not a program stop for an assertion, as we have set all initial values properly. However, nothing happens so far; which is not surprising given that we haven't specified any fluxes yet.



5.3. Realising the fluxes

To realise the fluxes, we have to fill the functions flux and eigenvalues in file MyEulerSolver.cpp with code. As we rely on the kernel mode generic::fluxes::nonlinear, ExaHyPE autonomously realises all steps of ADER-DG and only calls back to the solver for the flux and eigenvalue evaluations.

```
void Euler2d::MyEulerSolver::flux(
 const double* const Q,
 double** F
) {
 double* f = F[0];
 double* g = F[1];
 const double GAMMA = 1.4;
 const double irho = 1.0/Q[0];
 const double p = (GAMMA-1)*(Q[4] -0.5*(Q[1]*Q[1] + Q[2]*Q[2]) *irho);
 f[0] = Q[1];
 f[1] = irho*Q[1]*Q[1] + p;
 f[2] = irho*Q[1]*Q[2];
 f[3] = irho*Q[1]*Q[3];
 f[4] = irho*Q[1]*(Q[4]+p);
 g[0] = Q[2];
 g[1] = irho*Q[2]*Q[1];
 g[2] = irho*Q[2]*Q[2] + p;
 g[3] = irho*Q[2]*Q[3];
 g[4] = irho*Q[2]*(Q[4]+p);
```

```
void Euler2d::MyEulerSolver::eigenvalues(
  const double* const Q,
  const int normalNonZeroIndex,
  double* lambda
```

```
const double GAMMA = 1.4;

double irho = 1.0/Q[0];
double p = (GAMMA-1)*( Q[4] -0.5* (Q[1]*Q[1] + Q[2]*Q[2]) *irho );

double u_n = Q[normalNonZeroIndex+1] *irho;

double c = std::sqrt(GAMMA *p *irho);

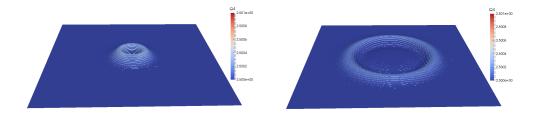
lambda[0] = u_n-c;

lambda[1] = u_n;
lambda[2] = u_n;
lambda[3] = u_n;

lambda[4] = u_n+c;
}
```

The implementation of function flux is again very straightforward. The code basically mimics the definition of the flux tensor $\mathbf{F}(\mathbf{Q}) = (\mathbf{f}(\mathbf{Q}), \mathbf{g}(\mathbf{Q}))^T$. As the creators of the Euler2d project, we naturally know the size of the parameters Q ,f, and g which is identical to the number of state unknowns. The same holds for the size of the array of eigenvalues the pointer lambda appearing in the signature and body of function eigenvalues refers to which is also identical to the number of state unknowns.

The normal vectors that are involved in ExaHyPE's ADER-DG kernels always coincide with the (positively signed) Cartesian unit vectors. Thus, the eigenvalues function is only supplied with the index of the single component that is non-zero within these normal vectors. In function eigenvalues, the aforementioned index corresponds to the parameter normalNonZeroIndex. A rebuild and rerun should yield results similar to



5.4. Setting up the Boundary Conditions

ExaHyPEoffers a generic API to implement any kind of *local* boundary conditions, ie. conditions to solve the Riemann problem at the simulation boundary which do not need to communicate with other cells. That is, you can easily implement

- Outflow boundary conditions (also sometimes referred to as "Null boundary Conditions" or "None boundary conditions").
- Exact boundary conditions
- Reflection symmetries

While you currently cannot implement any of

- Periodic Boundary Conditions
- Rotational symmetries around specific axis

The signature to implement your boundary conditions reads

```
void Euler::MyEulerSolver::boundaryValues(
   const double* const x, const double t, const double dt,
   const int faceIndex, const int normalNonZero,
   const double* const fluxIn,const double* const stateIn,
   double* fluxOut, double* stateOut)
   {
    ...
```

As you can read of the const keyword, you are offered plenty of variables while you are asked to set the fluxOut and stateOut, you can make use of all others. They offer you: The position and time as well as the local timestep of the cell in question where to provide boundary conditions to solve the local Riemann problem, the state and flux of the last cell inside the simulation domain and the two variables faceIndex and normalNonzero to answer the questions at which boundary side we currently are. The face index decodes as

```
0-left, 1-right, 2-front, 3-back, 4-bottom, 5-top or as an expression, \label{eq:continuous} \texttt{faceIndex} = 2*(\texttt{facenormaldirection"}1) + \frac{\texttt{cellboundarynormal}*\texttt{facenormal}+1}{2} ie.
```

This was just copied and pasted by Dominic via Sven. Todo: Make this nicer

5.5. Adding some runtime constants

There are various ways to add application-specific constants to your code. If you want to have them in the specification file, ExaHyPE allows you to add a constants section to your solver. Please note that our parser is not particular powerful, i.e. the parameters in the constants' brackets may not have any whitespaces.

```
solver ADER-DG MyParameterisedEulerSolver
  variables = 5
  parameters = 0
  order = 3
  maximum-mesh-size = 0.5
  time-stepping = global
  kernel = generic::fluxes::nonlinear
  language = C
  constants = {rho:0.4567,gamma:-4,alpha:4.04e-5,file:output}
end solver
```

If you rerun the toolkit now, you'll get a modified constructor that accepts a ParserView object which you can query for the constants.

It is now a convenient exercise to make your simulation code run several solvers simultanously in the code. For this, add multiple solver sections to the specification file. If all solvers solve the same PDE, it is a natural choice to make one solver invoke fluxes, initial conditions, ... from the other solvers. ExaHyPE does not support (yet, i.e. in this chapter) a feature to reuse one solver multiple times. As you have different solver sections in your specification file, you can make them tackle different constants. This way, you save grid construction overhead (the actual grid holding the solvers is maintained only once), and you typically increase the arithmetic intensity of your code. It thus should scale better.

5.6. Time stepping strategies

ExaHyPE provides various time stepping schemes for both the ADER-DG solvers and the Finite Volume solvers. You can freely combine them for the different solvers in your specification file. Please note that some schemes require you to recompile your code with the flag -DSpaceTimeDataStructures as they need lots

of additional memory for their realisation. At the same time, it would be stupid to invest that much memory, i.e. to increase the memory footprint, if these flags were defined all the time.

If you combine various time stepping schemes, please note that the most restrictive scheme determines your performance. ExaHyPE has time stepping schemes that try to fuse multiple time steps, e.g., and thus is particularly fast on distributed memory machines where synchronisation between time steps can be skippted. However, if you also have a solver with a tight synchronisation in your spec file, these optimisations automatically have to be switched off.

global

The global time stepping scheme makes each cell advance in time per iteration with a given time step Δt irrespective of its spatial resolution. If one cell in the domain finds out that Δt harms its CFL condition, all cells in the domain are rolled back to their last time step, Δt is reduced, and the time step is ran again. If a time step finds out that it has been too restrictive, the code carefully increases Δt for the next time step. So the scheme is a global scheme that does not anticipate any adaptive pattern (small cells usually are subject to more restrictive CFL conditions than coarse cells). However, the time step size is adaptively chosen. This implies that all ranks have to communicate once per time step, i.e. the scheme induces a tight synchronisation.

globalfixed

The global fixed time stepping scheme runs one time step of type global which determines a global Δt . From hereon, it uses this Δt for all subsequent time steps. If it turns out that the CFL condition is harmed through Δt later on throughout the simulation, no action is taken. In return, the scheme allows ExaHyPE to desynchronise all the ranks. This is among the fastest schemes available in the code. Furthermore, as the code knows the time step size and knows the time intervals between two plots a priori, it typically runs multiple time steps in one rush, i.e. you will not receive one terminal plot per time step, but most terminal outputs will summarise multiple time steps.

Finite Volume solvers with user-defined kernels

In this chapter, we work with ExaHyPE's Finite Volume code where we again specify the flux and eigenvalue functions ourselves. For the actual Finite Volume scheme, we rely on MUSCL and leave this implementation to ExaHyPE. While such a scheme is clearly inferior to ADER-DG (at least in the ExaHyPE philosophy), it offers an excellent limiter. However, for the time being, we realise it as stand-alone solver.

For a Finite Volume solver, we add a new Finite-Volumes solver section:

```
solver Finite-Volumes MyFVEulerSolver
variables = 5
parameters = 0
patch-size = 3
maximum-mesh-size = 0.1
time-stepping = global
kernel = generic::MUSCL
language = C
end solver
```

Different to an ADER-DG solver, we have a patch-size here instead of an order flag. All other parameters are basically the same. We support most plotters for both ADER-DG and finite volumes.

If you rerun the toolkit, this addendum will yield a MyFVEulerSolver class with routines that have to be implemented by the user. We again stick to the Euler equations here as an example and realise them as

```
void EulerFVM::MyFVEulerSolver::adjustedSolutionValues(
   const double* const x,
   const double w,
   const double t,
   const double dt, double* Q
) {
   if (tarch::la::equals(t, 0.0)) {
     const double GAMMA = 1.4;
     Q[0] = 1.;
     Q[1] = 0.;
     Q[2] = 0.;
     Q[3] = 0.;
     Q[4] =
     1. / (GAMMA -1) +
```

@todo Should be easy to follow without any ADER-DG knowledge @todo Define patch

```
void EulerFVM::MyFVEulerSolver::eigenvalues(
  const double* const Q,
 const int normalNonZeroIndex,
 double* lambda
) {
  const double GAMMA = 1.4;
 double irho = 1.0 / Q[0];
  double p = (GAMMA -1) *(Q[4] -0.5 *(Q[1] *Q[1] + Q[2] *Q[2]) *irho);
  double u_n = Q[normalNonZeroIndex + 1] *irho;
  double c = std::sqrt(GAMMA *p *irho);
 lambda[0] = u_n -c;
 lambda[1] = u_n;
 lambda[2] = u_n;
 lambda[3] = u_n;
 lambda[4] = u_n + c;
}
```

```
void EulerFVM::MyFVEulerSolver::flux(
 const double* const Q,
 double** F
) {
 const double GAMMA = 1.4;
 const double irho = 1.0 / Q[0];
 const double p =
     (GAMMA -1) *(Q[4] -0.5 *(Q[1] *Q[1] + Q[2] *Q[2]) *irho);
 double* f = F[0];
 double* g = F[1];
  // f
 f[0] = Q[1];
 f[1] = irho *Q[1] *Q[1] + p;
 f[2] = irho *Q[1] *Q[2];
 f[3] = irho *Q[1] *Q[3];
 f[4] = irho *Q[1] *(Q[4] + p);
 // g
 g[0] = Q[2];
 g[1] = irho *Q[2] *Q[1];
 g[2] = irho *Q[2] *Q[2] + p;
```

```
g[3] = irho *Q[2] *Q[3];
g[4] = irho *Q[2] *(Q[4] + p);
}
```

Please note that the Finite Volume solvers are not realised via cells but via patches: ExaHyPE's cells act as meta data structure into whose we embed patches of patch-size×patch-size or patch-size×patch-size patch-size, respectively. This fact is hidden from the user at the moment, but it gains importance once we make the finite volume solver act as limiter.

7. ADER-DG with Finite Volume limiting

The ADER-DG scheme with Finite Volume limiting combines the high-order approximation properties of the ADER-DG method in sufficiently regular parts of the domain with robustness of the Finite Volumes method in parts of the domain where shocks and contact discontinuities dominate the solution.

@todoDominic,pleasecomplete

In ExaHyPE, empty solver code for the ADER-DG method with Finite Volumes limiting can be generated by specifying a LimitingADERDG solver environment in the ExaHyPE specification file. This could e.g. look as follows:

```
[..]
solver Limiting-ADER-DG MySolver
 variables = 5
 parameters = 0
 order = 3
 maximum-mesh-size = 0.05
 time-stepping = global
 kernel = generic::fluxes::nonlinear
 language = C
 limiter-kernel = generic::Godunov
 limiter-language = C
 dmp-relaxation-parameter = 0.0001
 dmp-difference-scaling = 0.001
 [..]
end solver
[..]
```

Unlike to the pure ADER-DG and Finite Volumes method, we have to specify two kernels for the limiting ADER-DG solver – one for the ADER-DG method (kernel, language) and one for the Finite Volumes method employed for the limiting (limiter-kernel, limiter-language). Of couse, we can choose any of the kernels that are available for the pure ADER-DG or pure Finite Volumes method.

The last two parameters, dmp-relaxation-parameter and dmp-difference-scaling, are tuning parameters to relax a discrete maximum principle (DMP). The DMP plays a key role role in detecting troubled cells – cells that need limiting.

The toolkit will then generate implementation files for one ADER-DG solver and for one Finite Volumes solver. No additional implementation files for the limiting ADER-DG solver itself are generated. Instead, the ADER-DG and Finite Volumes solver are coupled with each other in the initSolvers(. . .) routine in file KernelCalls.cpp

Note that is often not practical to start directly with generating the empty Limiting-ADER-DG solver classes and to implement them from scratch. An ExaHyPE application de-

velopment workflow that works well together with the toolkit might instead look as follows:

- First implement a simple Finite Volumes solver MySolver_FV in project folder MyProject. Verify that shock problems can be solved by your Finite Volumes solver.
- Next implement a pure ADER-DG solver MySolver_ADERDG in the same folder. Verify that rarefaction problems can be solved with high-order accuracy by your ADER-DG method.
- Finally couple both implementations with each other by specifying a solver MySolver in the specification file and running the toolkit. The toolkit will not overwrite the two implementations MySolver_FV and MySolver_ADERDG. Make sure to remove the other two solvers from the specification file if you only want to run the limiting ADER-DG solver.

Often it is further important to test the numerical (initial) solution for physical admissibility, e.g., if a density is positive. The troubled cell indicator of ExaHyPE's ADER-DG scheme with Finite Volumes limiting thus does not only rely on the DMP but makes use of an physical admissbility detection (PAD).

The PAD will be used if you extend your MySolver_ADERDG.h and MySolver_ADERDG.cpp files by the following lines:

```
MySolver_ADERDG.h:
[..]
bool physicalAdmissibilityDetection(const double* const QMin,
   const double*const QMax) override;
[..]
```

```
MySolver_ADERDG.cpp:
Γ..1
bool MyProject::MySolver_ADERDG::physicalAdmissibilityDetection(const double*
const QMin,const double* const QMax) {
 // This is an example for the compressible Euler equations.
 // Modify it according to your needs.
 if (QMin[0] < 0.0) return false; // (min) density should not be negative</pre>
 if (QMin[4] < 0.0) return false; // (min)energy should not be negative
 for (int i=0; i<5; ++i) {
   if (!std::isfinite(QMin[i])) return false; // min velocities should
                                               // be finite
   if (!std::isfinite(QMax[i])) return false; // max velocities should
                                               // be finite
 return true;
}
[..]
```

7.1. Effects of the limiter

After each timestep, the limiter will examine all cells and mark the troubled cells and their neighbours. A cell is troubled if for any conserved quantity, its maximum is greater than the maximum of the cell or its neighbors before the steps, likewise for the minimum. The extrema are approximated by examining the quantities at the Gauss-Legendre and the Gauss-Lobatto ones to include the boundary values.

Additionally, a cell might be marked as troubled if the solution in the cell is not physically admissible.

If any cell was marked, a Finite Volume steps takes place on them using the saved values from before the ADER-DG steps or saved healthy values from a previous limiter intervention. Once the Finite Volumes solutions are computed, they are used to recompute and update a new ADER-DG solution on the marked cells. If the cells was troubled or the cell was a neighbors of a troubled cell and becomes troubled after this limiter step, the Finite Volume healthy value are saved for the next time to be used if required.

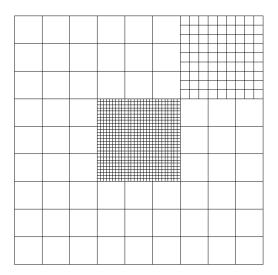
8. Adaptive mesh-refinement

In this chapter, we demonstrate the steps to perform for using ExaHyPE's adaptive mesh refinement. To this end, we consider again an ADER-DG solver for the compressible Euler equations (Ch. 5).

In the following sections, we assume that the reader has performed all steps in Ch. 5 and is able to run the example given there on a uniform mesh.

8.1. Static mesh adaptivity: A geometry-based refinement criterion

Let us start with a simple geometry-based refinement criterion. In our example, we consider a uniform mesh of 9×9 cells on the unit cube (use e.g. maximum-mesh-size=0.1). We additionally want to perform one level of adaptive refinement in the region $[0.666,1] \times [0.666,1]$ and two levels of adaptive refinements in region $[0.333,0.666] \times [0.333,0.666]$:



To facilitate the desired adaptive mesh refinement, we augment the function refinementCriterion(...) in our MyEulerSolver.cpp file as given below: (No modification of the project's specification file is necessary.)

```
exahype::solvers::Solver::RefinementControl
Euler::MyEulerSolver::refinementCriterion(
   const double* luh, const tarch::la::Vector<DIMENSIONS, double>& center,
   const tarch::la::Vector<DIMENSIONS, double>& dx, double t,
   const int level) {
```

```
if (dx[0] > getMaximumMeshSize()/3.)
  if (center[0] > 0.666)
    if (center[1] > 0.666)
      return exahype::solvers::Solver::RefinementControl::Refine;

if (dx[0] > getMaximumMeshSize()/9.)
    if (center[0] > 0.333 && center[0] < 0.666)
      if (center[1] > 0.333 && center[1] < 0.666)
        return exahype::solvers::Solver::RefinementControl::Refine;

return exahype::solvers::Solver::RefinementControl::Keep;
}</pre>
```

The line $dx[0] > getMaximumMeshSize()/X controls here the maximum refinement level in this area. A division of getMaximumMeshSize() by 3 means that we only allow one refinement level, a division by <math>3^2$ means we allow a maximum refinement level of two, and so on.

If we run the simulation, we should get plots similar to the ones given below:

8.2. Dynamic mesh adaptivity: A density-based refinement criterion

9. **ExaHyPE** FORTRAN

This part is yet to be written.

10. Multiple, simultaneously running, coupled solvers

This part is yet to be written.

Part III. Upscaling and tuning **ExaHyPE**

11. Shared memory parallelisation

ExaHyPE currently supports shared memory parallelisation through Intel's Threading Building Blocks (TBB) and OpenMP. We recommend using the TBB variant that is typically one step ahead of the OpenMP support. To make an ExaHyPE project use multi- and manycore architectures, please add a shared-memory configuration block to your specification file:

```
shared-memory
  strategy = dummy
  cores = 4
  properties-file = sharedmemory.properties
end shared-memory
```

Rerun the ExaHyPE toolkit afterwards, and recompile your code. For the compilation, we assume that the environment variables TBB_INC and TBB_SHLIB are set¹. If you use OpenMP, your compiler has to support OpenMP. The toolkit checks whether the environment variables are properly set and gives advise if this is not the case.

Whenever you configure your project with shared memory support, the **default** build variant is a shared memory build (with TBB or OpenMP, respectively). However, you always are able to rebuild without shared memory support or a different shared memory model just by manually redefining environment variables and by rerunning the makefile. There is no need to rerun the toolkit again. Also note that all arguments within the shared-memory environment are read at startup time. If you change the core count, there's no need to recompile. The same statements holds for the other parameters.

For users familiar with OpenMP, we emphasise that we do set the thread count manually within the code. OpenMP requires, per default, all users to control the thread count via environment variables. In ExaHyPE, the value of the environment variable and the value in the config file thus should match. You'll obtain a warning otherwise.

The dummy strategy as displayed above is a reasonable starting point to assess whether your code is correctly translated and started. While the field cores is self-explaining, the properties file is neglected for the dummy strategy. If you use a more sophisticated strategy, it however makes a difference. More sophisticated strategies are subject of discussion next.

¹ TBB_INC=-I/mypath/include and TBB_SHLIB="-L/mypath/lib64/intel64/gcc4.4 -ltbb" are typical environment values.

Table 11.1.: Parameter choices for the multicore configuration. All values are read at program startup. There is no need to rerun the toolkit if you change any of them.

Parameter	Options	Description
strategy	dummy autotuning sampling	The shared memory efficiency is very sensitive to a multitude of parameters that threshold the size of minimal problems deployed to one task, decide which code fragments shall run in parallel, and so forth. Three shared memory strategies for these parameters are provided at the moment. dummy uses some default values that have proven to be reasonably robust and yield acceptable speed. sampling tests different choices and plots information on well-suited variants to the terminal. autotuning tries to find the best choice on-the-fly.
cores	> 0	Number of cores that shall be used.
properties-file	filename	The sampling and the autotuning strategy can write their results into files and reuse these results in follow-up runs. If no (valid) file is provided, they both start from scratch and without any history. If the file name is empty or invalid, no output data is dumped. The entry is ignored if you use the dummy strategy.

11.1. Tailoring the shared memory configuration

Shared memory performance can be very sensitive to machine-specific tuning parameters: Peano, ExaHyPE's AMR code base, relies on static problem subpartitioning and thus needs precise instructions which problem sizes for particular parts of the code are convenient. We thus encourage high performance applications to tailor ExaHyPE's shared memory parallelisation to get the most out of their machine.

Key ingredient to do so is the usage of a different strategy than the dummy plus the configuration/properties files read by these strategies. All non-dummy strategies load tuning parameters from the properties file. If a file is specified but does not exist, they fall back to default/empty settings as detailed below. If your application terminates correctly, all strategies pipe updated information back into the properties file. This way, knowledge can be reused in the next run or runtime characteristics can be analysed.

It is obvious that proper property files depend on the machine you are using. They reflect your computer's properties. Yet, note that very good property files also depend on the

- choice of cores to be used,
- MPI usage and balancing,
- application type, and even
- input data/simulation scenario.

It thus might make sense to work with various property files for your experiments that depend on your simulation characteristics.

Autotuning

Our most convenient shared-memory tailoring relies on the autotuning strategy. Autotuning starts with serial configurations for all program parts. Once it has obtained a reasonable accurate estimate of how long each program part runs, it tries to deploy various parts of the code among multiple cores. We typically start with two cores, four cores, and so forth unless subproblems consist of large arrays that immediately can be broken up into more chunks. If a problem decomposition improves the runtime, the oracle continues to break it up into even smaller chunks to exploit more cores until the decomposition either does not improve the runtime anymore or even makes the performance worse. In this case, we roll back to the last reasonable configuration. This means that first runs might be really slow, but the runtime improves throughout the development.

The autotuning switches off per code segment automatically as soon as it has to believe that best-case parameters are found. As a result, timing overheads are reduced. As any configuration might correspond to a local runtime minimum, the autotuning restarts the search from time to time. This restart is randomised.

Peano provides a Python script to translate all measurements into a big HTML table. The script is located within Peano/sharedmemoryoracles. If you invoke it without parameters, you obtain a detailed usage message.

If a properties file does exist at startup already, ExaHyPE loads this property file, i.e., the autotuning starts from the previous properties dump. This way, long-term learning can be split among various program invocations.

- As the autotuning reads text configuration files, it is possible to configure the autotuning manually with proper parameter choices and to switch off the actual autotuning at the same time. Switching off is also done within the text files. You might for example search for optimal choices with the sampling and then feed these values into the autotuning. The format of the properties file is documented as comment within the file itself.
- The autotuning requires your OS to offer real-time timers. We have encountered various situations, notably on Intel KNL, where timers seem not to work properly. In this case, the autotuning works if and only if a properties file from another machine is handed in, i.e., a configuration from a different machine is used. Please note that disfunctional autotuning might mess up your properties files. In this case, they have to be replaced with copies from a different machine prior to each run.
- Large simulation runs seem to yield runtime data that varies strongly. It thus requires the autotuning to measure quite some time before code regions are identified that scale. We recommend to run autotuning first on small problem setups. The dumped properties files then can be reused by larger runs. If ExaHyPE is passed an autotuning configuration from a small run, it extrapolates measurements therein as initial data for the autotuning and then continues to optimise further.

Configuration sampling and manual tuning

To get the whole picture which code fragments perform in which way on your machine, you might want to run the sampling strategy. However, the parameter space is huge, i.e. getting a valid picture might require several days. The output of the sampling is written into the specified properties file and then allows you to identify global best case parameters.

Peano provides a Python script to translate all measurements into graphs. The script is located within Peano/sharedmemoryoracles. If you invoke it without parameters, you obtain a detailed usage message.

If a properties file does exist at startup already, ExaHyPE loads this propery file, i.e., the statistics are incremently improved. This way, a long-term statistical analysis can be split among various program invocations.

11.2. Hybrid parallelisation

If you want to combine shared memory parallelisation with MPI, nothing has to be done in most cases. However, the tailoring of a reasonable number of ranks per node plus a efficient number of threads per rank can be tedious. You cannot expect that a hybrid code shows the same shared memory speedup as a code that is parallelised with shared memory only.

ExaHyPE supports multithreaded MPI and most MPI implementations nowadays support multithreaded calls. However, we found that most applications do not benefit from hyperthreaded MPI or even are slowed down. It thus is disabled by default in ExaHyPE. If you want to use hyperthreaded MPI in your code, please comment the line

PROJECT_CFLAGS+=-DnoMultipleThreadsMayTriggerMPICalls

in your autogenerated makefile out.

If you use autotuning with MPI on p ranks, please note that ExaHyPE disables the learning on all ranks besides rank p-1. While rank p-1 reads in the properties file and tries to improve parameters specified therein, all remaining ranks do read the properties file, too. They however do not alter the file's settings.

Once your code terminates, rank p-1 dumps any (improved) parameter choice. If you use grain size sampling, rank p-1 dumps its statistics. The statistics from all other ranks are not dumped persistently. If your rank p-1 successively improves the setting in the properties file, better parameter findings automatically will be available to the other ranks in the next program run.

12. Distributed memory parallelisation

ExaHyPE's distributed memory parallelisation is done with plain MPI. We rely on the 1.3 standard with the pure C bindings. To make an ExaHyPE project use mpi, please add a distributed-memory configuration block to your specification file:

```
distributed-memory
  identifier = static_load_balancing
  configure = {greedy,FCFS}
  buffer-size = 64
  timeout = 120
end distributed-memory
```

Rerun the ExaHyPE toolkit afterwards, and recompile your code. For the compilation, we assume that a proper MPI compiler is available.

Whenever you configure your project with distributed memory support, the **default** build variant is a distributed memory build. However, you always are able to rebuild without distributed memory support by manually redefining environment variables and by rerunning the makefile. There is no need to rerun the toolkit again. Also note that all arguments within the distributed-memory environment are read at startup time.

The parameter timeout specifies how long a node shall wait (in seconds) before it triggers a time out if no message has arrived. If half of the time has elapsed, it furthermore writes a warning. This is a very useful variable to identify deadlocks as well as communication inefficiencies. Set the value to zero if you don't want to use the time out detection.

The parameter buffer-size specifies how many messages Peano shall internally bundle into one MPI message. This operation allows you to tailor your application behaviour w.r.t. latency and bandwidth requirements. The fewer messages you bundle, i.e. the small this value, the faster messages are sent out and other ranks might not have to wait for them. The more messages you bundle the lower the total communication overhead. Please note that some Infiniband implementations tend to deadlock, if this value is too small as they are swamped with lots of tiny messages. We found 64 to be a reasonable first try.

The required/permitted values in the configure field depend on the identifier chosen and thus are enlisted below in the respective tables (cf. table 12.1).

Argument	Values	Semantics
greedy	none	Uses a greedy split strategy to decompose the underlying spacetree. Subpartitions do not join again. The individual ranks do not synchronise with each other. What might be a hot spot on a rank A might not matter overall as rank B has so much more work to do. So this scheme is fast and stupid but might yield non-optimal partitions right from the start.
hotspot	none	The ranks do synchronise with each other. This variant is the most conservative one and introduces quite some grid construction overhead as the load balancing has to plug into the grid construction. It should however yield better partitions than the greedy partitioning scheme.
FCFS	none	If an MPI rank want to split its domain, it sends a request for an additional MPI rank to rank 0. All requests on rank 0 are answered in FCFS fashion which minimises the answer latency but might yield unfair decompositions: ranks with a very low latency towards rank 0 are more likely to be served than others. You may not combine FCFS and fair.
fair	none	All requests sent to rank 0 are collected for a couple of ms and then answered such that those ranks with the lowest number of workers so far get new workers first. The answering latency is slightly higher than for FCFS but the distributions tend to be fairer. This variant expects the user to specify ranks_per_node, too. You may not combine FCFS and fair.
ranks_per_node	≥1	Ignored if fair is not specified. It instructs the load balancing how many ranks are placed on one node.

Table 12.1.: MPI variant static_load_balancing

12.1. On ranks_per_node

This flag is used by the fair/hotspot load balancing strategies. It instructs the load balancing how many ranks are placed on one node. The balancing uses this information in two ways:

- 1. Out of the first ranks_per_node, only the very first rank is used for the global master and the global load balancing code. The rationale is as follow: The load balancing is a single point of contact. Every node that wants to fork, has to ask at the global master for free ranks. So it is critical that the global master has a low latency. I thus sacrifice one node and run only the global master there to allow it to have the whole MPI IO exclusively. We accept that ranks_per_node-1 ranks are wasted.
- 2. If n ranks request for one worker each for a level ℓ , the load balancing tries to make each node, i.e. every ranks_per_nodeth rank, serve this request. Notably, the ranks responsible for the coarests tree levels are assigned to the ranks ranks_per_node, $2 \cdot \text{ranks_per_node}$, $3 \cdot \text{ranks_per_node}$, and so forth. The idea is that jobs are homogeneously distributed among the nodes and no node runs risk to run out of memory. Furthermore, if the grid is reasonably regular, also the load should be reasonably distributed among the nodes.

If you plot scalability results, you have to rescale your x-axis corresponding to ranks_per_node. If you want to use all cores on the first node, please make MPI deploy ranks_per_node + ranks_per_node-1 ranks to this node.

12.2. Hybrid parallelisation

Please see Section 11.2 for details how MPI and the shared memory parallelisation interplay.

13. Optimisation

13.1. High-level tuning

ExaHyPE realises few high level optimisations that you can switch on and off at code startup through the specification file. To gain access to these optimisations, add a paragraph

```
optimisation
...
end optimisation
```

at the end of your specification file. It requires a sequence of parameters in a fixed order as they are detailed below.

Step fusion. Each time step of an ExaHyPE solver consists of three phases: computation of local ADER-DG predictor (and projection of the prediction onto the cell faces), solve of the Riemann problems at the cell faces, and update of the predicted solution. We may speed up the code if we fuse these four steps into one grid traversal. To do so, we set fuse-algorithmic-steps. Permitted values are on and off.

The fusion is using a moving average kind time step size estimate. If we detect a-posteriori that this estimate has violated the CFL condition, we have to rerun the predictor phase of the ADER-DG scheme with a time step size that does not violate the CFL condition. In our implementation, such a CFL-stable time step size is available after the ADER-DG time step has been performed.

We offer to rerun the predictor phase of the ADER-DG scheme with this CFLstable time step size weighted by a factor

fuse-algorithmic-steps-factor. This problem-dependent factor must be chosen greater zero and smaller to/equal to one. A value close to one might lead to more predictor reruns during a simulation but to less additional numerical diffusion.

```
optimisation
  fuse-algorithmic-steps = off
  fuse-algorithmic-steps-factor = 0.99
   ...
end optimisation
```

Batching of time steps. If you use fixed, adaptive or anarchic time stepping, Peano can guess from an evaluation of the CFL condition how many grid sweeps (global time steps) are required to advanced all patches such that the next plotter becomes

active or we meet the simulation's termination time. Each grid sweep/global time step might update only a few patches and their permitted time step size again might change throughout the simulation run. So we can only predict. For MPI's speed is it advantageous if multiple time steps are triggered in one rush—this way, ranks that have already finished its traversal know whether they can immediately continue with the subsequent time step. To allow so, you have to set fuse-algorithmic-steps-factor to a value from (0,1(. Setting it to zero switches off this feature. The semantics is as follows: The code computes how many time steps it expects to be required to reach the next plotter or final simulation time, respectively. This value is scaled with fuse-algorithmic-steps-factor and the resulting number of time steps then are ran. A factor of around 0.5 has to be proven to be good starting point.

```
optimisation
...
timestep-batch-factor = 0.5
end optimisation
```

Skip reduction of global data. If you allow the code to run multiple iterations in one batch, it makes sense to tell ExaHyPE that there is no need to restrict any data (such as minimal time steps) while a batch is processed. It is usually sufficient (unless you need this data explicitly) to restrict global data after the last grid update sweep has terminated. The flag skip-reduction-in-batched-time-steps switches the reduction on or off. Permitted values are on and off. The value is always requried even though you might not allow the code to batch time steps. In this case, it is ignored.

```
optimisation
...
timestep-batch-factor = 0.5
skip-reduction-in-batched-time-steps = on
end optimisation
```

Restrict adaptivity pattern. For many setups, it makes sense to disable the dynamic AMR from time to time; when multiple iterartions are batched and the code runs a fixed number of iterations or when the previous grid iteration did not identify any refinement and thus we have to expect that the probability of a refinement in the subsequent iteration is low, e.g. Often, the CFL condition in local time stepping requires the code to perform N grid sweeps and it is sufficient if the grid is adopted afterwards. This can speed up the code in many cases. To tell ExaHyPE to throttle the dynamic adaptivity, set the flag to on.

```
optimisation
   ...
   disable-amr-if-grid-has-been-stationary-in-previous-iteration = on
end optimisation
```

Modify storage precision. ExaHyPE internally can store data in less-than-IEEE precision. This can reduce the memory footprint of the code signficantly. To allow ExaHyPE to do so, the user has to specify through double-compression which accuracy actually is required. If the field is set to zero, ExaHyPE works with full double precision and no compression is activated.

While the data is compressed, ExaHyPE nevertheless computes with double precision always. Consequently, data has to be converted forth and back: Any compressed data is converted into IEEE precision before any arithmetic operation and later on compressed before it is written back to the main memory. This process is costly, though we can spawn it into background threads. This is particularly convenient if you have idle cores 'left' and controlled via the flag spawn-double-compression-as-background-thread.

```
optimisation
...
   double-compression = 0.0
   spawn-double-compression-as-background-thread = off
end optimisation

optimisation
...
   disable-amr-if-grid-has-been-stationary-in-previous-iteration = on
end optimisation
```

13.2. Optimised Kernels

ExaHyPEoffers optimised compute kernels. Given a specification file, the toolkit triggers the code generator to output optimised compute kernels for this specific setup.

Prerequisites The code generator exhibits two dependencies. First, the code generator requires Python 3. Second, it relies on Intel's libxsmm generator driver. You therefore have to clone the libxsmm repository https://github.com/hfp/libxsmm and build your local generator driver

```
make generator
```

to obtain the executable in path/to/libxsmm/bin/libxsmm_gemm_generator.

Specification file The path to libxsmm have to be given in the specification file under the path to ExaHyPE:

```
exahype-project MyEulerFlow
...
exahype-path = ./ExaHyPE
libxsmm-path = ./Libxsmm
output-directory = ./ApplicationExamples/EulerFlow
...
```

Architecture	Meaning
noarch	unspecified
wsm	Westmere
snb	Sandy Bridge
hsw	Haswell
knc	Knights Corner (Xeon Phi)
knl	Knights Landing (Xeon Phi)

Table 13.1.: Supported flags

Microarchitecture The optimised kernels explicitly use the instruction set available on the target processor. You therefore have to define its microarchitecture in the specification file. The specification file terms the processor architecture just architecture. The supported options for this flag are given in table 13.1. You can identify the microarchitecture of your processor through amplxe-gui, an analysis tool part of Intel VTune Amplifier. Alternatively, you can obtain the 'model name' via

cat /proc/cpuinfo

and search for it on http://ark.intel.com.

Set the architecture flag to 'noarch' if the microarchitecture of your processor is not supported. You will nevertheless obtain semi-optimised kernels. The default makefile utilises the flags march=native (gcc) respectively xHost (icc). The compiler queries what hardware features are available and optimises the kernels to some degree.

Part IV. Working with **ExaHyPE**'s output

14. ExaHyPE program output

In this section, we discuss how to tailor the ExaHyPE program output to your needs. We focus on direct output such as terminal messages. Information on supported output file formats can be found in Chapter 15 while real on-the-fly postprocessing such as the computation of global integrals is picked up in Chapter 16.

14.1. Logging

ExaHyPE creates a large number of log files and log messages; notably if you build in debug or assert mode. Which data actually is written to the terminal can be controlled via a file exahype.log-filter. This file has to be held in your executable's directory. It specifies exactly which class of ExaHyPE is allowed to plot or not. The specification works hierarchically, i.e. we start from the most specific class identifier and then work backwards to find an appropriate policy.

```
# Level Trace Rank Black or white list entry
# (info or debug) (-1 means all ranks)

debug tarch -1 black
debug peano -1 black
info tarch -1 black
info peano -1 black
info peano::utils::UserInterface -1 white
info exahype -1 white
```

If no file exahype.log-filter is found in the working directory, a default configuration is chosen by the code. Please note that a some performance analyses requires several log statements to be switched on. We refer to Peano's handbook, the usage descriptions of the analysis postprocessing scripts and the respective guidebook sections for details.

By default, Peano pipes all output messages to the terminal, and many developers thus pipe such output into a report file. Alternatively, you can add a

```
log-file = mylogfile.log
```

statement to your specification file right after the architecture flag. If such a statement exists ExaHyPE pipes the output into the respective log files. Furthermore, one log file is used per grid sweep if you translate with assertions or in debug mode where lots of information is dumped. This enables you to search for particular information of a particular grid sweep. Once you translate your code with

MPI support, each rank writes a log file of its own. This way, we avoid garbage in the output files if multiple MPI ranks write concurrently as well as congestion on the IO terminal.

14.2. Grid statistics

By default, ExaHyPE does not plot statistics about the grid such as used mesh widths. There are multiple reasons why we refrain from this:

- ExaHyPE makes the compute grid host the solution but often chooses on purpose finer grids for efficiency reasons.
- Most applications can derive information about the actual compute grids used from the output files and a generic plot thus would be redundant.
- In MPI, ExaHyPE tries to avoid global communication whereever possible, i.e. any global grid statistics written out can be corrupted. If you use plot routines, all data is consistent, but this comes at the price of some additional synchronisation.

For many codes it makes, at least throughout the development phase, however sense to track grid statistics such as used mesh sizes and vertex counts. To enable it, please translate your code with the option -DTrackGridStatistics. For this, we propose to add the line

```
PROJECT_CFLAGS+=-DTrackGridStatistics
```

to you makefile. Following a recompile, you obtain data similar to

```
48.5407 info step 13 t_min =0.0229621
48.5407 info dt_min =0.00176632
48.5408 info memoryUsage =639 MB
48.5408 info inner cells/inner unrefined cells=125479/59049
48.5408 info inner max/min mesh width=[5,5]/[0.0617284,0.0617284]
48.5408 info max level=6
```

15. Plotting

In this chapter, we start with an overview over various output formats supported by ExaHyPE. In a second part, we discuss how to pass selections over to the simulation engine. Often, you are not interested in the whole domain or all variables, so notifying the code base about the regions of interests allows the code to stream out only the data actually required which makes it faster. We wrap up with some remarks how to modify/postprocess variables on-the-fly before they are written. An all time classic of such an in-situ postprocessing is the conversion of conservative into primitive variables of the elimination of helper variables from the output.

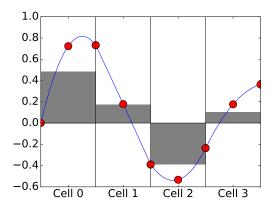
Most output formats of ExaHyPE are standardised output formats such as VTK. There are a number of Open-Source tools available to interactively watch, inspect and render these files. Popular choices are *ParaView* and *Visit*. These programs are available for many operating systems and also typically present on vizualization nodes in scientific clusters.

15.1. DG polynomials in the **ExaHyPE** output

As ExaHyPE involves the Discontinous Galerkin method, it aims to output not only cell-averaged data for each cell, but instead the data on all the polynomial supporting points. For instance, for a second order DG approximation in 1D, your output contains three data points per cell and thus holds almost three times more data than with a cell-averaging output method. The chosen output format allows you to exactly reconstruct the polynomials as they are available during an ExaHyPE run.

In shock-free simulations, this output format introduces a certain redundancy, as values at the cell boundaries are given out ("plotted") two times. However, these points provides additional information as soon as discontinuities appear, cf. figure 15.1.

While a visualization software might use the data to reconstruct the polynomial, we don't expect this to happen in every-day visualisations. This has two reasons: First, it is an expensive computation. Second, it needs information about the grid structure which is present in the VTK files that is not so easily extractable. We provide a VTK hands on in the next pages to show how to access these information.



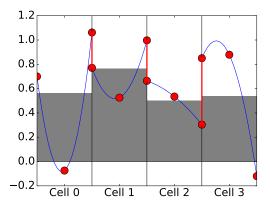


Figure 15.1.: A sketch of ExaHyPE's output point structure in a 1D example with four cells and a polynomial degree of 2. In each example, the polynomial degree is plotted. The shaded regions indicate the cell average. In the regular case of a continous solution, there are two data points at the cell boundaries with exactly the same value. In the vicinity of shocks (discontinuities), as sketched in an exaggerated manner on the right, the different values for two points at the same grid value becomes obvious. The output is thus a double-valued function.

15.2. Overview of supported data output formats

The text below lists all available plotter types. They are distinguished by their identifier in the specification file. While the number of plotters and their type have to be fixed at compile time—if you want to introduce a new plotter, you have to rerun the ExaHyPE toolkit and rebuild your code—all other parameters are read at runtime. A plotter always has to specify how many variables are written through the unknowns statement. By default, these are the first unknowns unknowns from your solver. If unknowns is greater than the unknowns of the solver, you also obtain the material parameters if there are material parameters.

Volumetric plotters

We currently support the following combinations for volumetric data (snapshots):

$$\mathsf{vtk} \; \times \; \left\{ \begin{array}{l} \mathsf{Legendre} \\ \mathsf{Cartesian} \end{array} \right\} \; \times \; \left\{ \begin{array}{l} \mathsf{Vertices} \\ \mathsf{Cells} \end{array} \right\} \; \times \; \left\{ \begin{array}{l} \mathsf{Ascii} \\ \mathsf{Binary} \end{array} \right\}$$

vtk::Cartesian::vertices::ascii Dumps the whole simulation domain into one VTK file. If you use multiple MPI ranks, each ranks writes into a file of its own. The plotter uses ASCII, i.e. text format, so these files can be large. output has to be a valid file name where a rank and time step identifier can be appended. The plotter always adds a .vtk postfix. Through the select statement, you can use spatial filters. if you add values such as select = {left:0.4,right:0.6,bottom:0.2,

top:0.8, front:0.2, back:0.5}, you get only data overlapping into this box. As VTK does not natively support higher order polynomials, the solution is projected onto a grid, and the solution values are sampled on this grid. In this case, we use a Cartesian grid and the values are sampled at the grid vertices.

vtk::Cartesian::vertices::binary Same as vtk::Cartesian::vertices::ascii, but the files internally hold binary data rather than ASCII data. All written files should thus be slightly smaller.

vtk::Cartesian::cells::ascii See vtk::Cartesian::vertices::ascii. Solution values are sampled as cell values instead of vertex values.

vtk::Cartesian::cells::binary Binary variant of plotter with identifier
vtk::Cartesian::cells::ascii.

vtk::Legendre::vertices::ascii See counterpart with Cartesian instead of Legendre. Mesh values are not sampled at Cartesian mesh points but at Legendre points.

vtk::Legendre::vertices::binary See counterpart with Cartesian instead of Legendre. Mesh values are not sampled at Cartesian mesh points but at Legendre points.

vtk::Legendre::cells::ascii See counterpart with Cartesian instead of Legendre. Mesh values are not sampled at Cartesian mesh points but at Legendre points.

vtk::Legendre::cells::binary See counterpart with Cartesian instead of Legendre. Mesh values are not sampled at Cartesian mesh points but at Legendre points.

Non-volumetric plotters

probe::ascii This option probes the solution over time, i.e. you end up with files specified by the field output that hold a series of samples in one particular point of the solution. The code adds a .probe postfix to the file name. This option should be used to plot seismograms, e.g. For this data format is ascii, the file holds one floating point value per line per snapshot in text format. To make the plotter know where you want to probe, please add a line alike

```
select = \{x:0.3,y:0.3,z:0.3\}
```

to your code. If you run your code with MPI, the probe output files get a postfix -rank-x that indicates which rank has written the probe. Usually, only one rank writes a probe at a time. However, you might have placed a probe directly at the boundary of two ranks. In this case, both ranks do write data. If dynamic load

balancing is activated, the responsibility for a probe can change over time. If this happens, you get multiple output files (one per rank) and you have to merge them manually. Please note that output files are created lazily on-demand, i.e. as long as no probe data is available, no output file is written. The probe file contains data from all variables specified in the plotter. It furthermore gives you the time when the snapshot had started and the actual simulation time at the snapshot location when data had been written. As ExaHyPE typically runs adaptive or local time stepping, a snapshot is triggered as soon as all patches in a simulation domain have reached the next snapshot time. At this point, some patches might already have advanced in time. This is why we record both snapshot trigger time and real time at the data point.

15.3. Filtering

By default, ExaHyPE offers two types of built-in filtering: You can use the select statement to impose spatial constraints on the output data, and you can constrain the number of variables written.

The spatial selection mechanism is described above. We built it into the ExaHyPE kernel as IO has a severe performance impact. It synchronises the involved MPI ranks. If we know that only variables of a certain region are of interest, only ranks responsible for these regions have to be synchronised, i.e. the resulting code is faster.

With a restriction on only a few output parameters, you can reduce the output data file and thus reduce the pressure on the memory system. By default, the first k unknowns are streamed if k unknows are to be written. However, you can use the postprocessing techniques discussed below to plot other unknowns from your unknown set.

15.4. Parameter selection and conversion

If you want to plot only a few parameters of your overall simulation, you have to invest a little bit of extra work. First, adopt your plotter statements such that the unknowns statement tells the toolkit exactly how many variables you want to write. Typically, you plot fewer variables than the unknowns of your actual PDE. However, there might be situations where you determine additional postprocessing data besides your actual data and you then might plot more quantities than the original unknowns.

Once you have tailored the unknowns quantity, you rerun the toolkit and you obtain classes alike MySolver_Plotter0. These classes materialise the individual solvers as written down in your specification file and they are enumerated starting from 0. Open your plotter's implementation file and adopt the function there that maps quantities from the PDE onto your output quantities. By default, this mapping is the identity (that's what the toolkit generates). However, you might prefer to do some conversations such as a conversion of conservative to primitive

variables. Or you might want to select the few variables from the PDE solver that you are actually interested in.

Below is an example:

```
solver ADER-DG MyEulerSolver
  variables = 5
  parameters = 0
  order = 3
  maximum-mesh-size = 0.1
  time-stepping = global
  kernel = generic::fluxes::nonlinear
  language = C

plot vtk::Cartesian::ascii MySolutionPlotter
  variables = 2
  time = 0.0
  repeat = 0.05
  output = ./solution
  select = {}
  end plot

...
```

Originally, we did plot all five variales. Lets assume we are only interested in Q0 and Q4. We therefore set variables in the plotter to 2 and modify the corresponding generated plotter:

```
void MyEulerSolver_Plotter0::mapQuantities(
    const tarch::la::Vector<DIMENSIONS, double>& offsetOfPatch,
    const tarch::la::Vector<DIMENSIONS, double>& sizeOfPatch,
    const tarch::la::Vector<DIMENSIONS, double>& x,
    double* Q,
    double* outputQuantities,
    double timeStamp
) {
    outputQuantities[0] = Q[0];
    outputQuantities[1] = Q[4];
}
```

16. Postprocessing

16.1. On-the-fly computation of global metrics such as integrals

The plotter sections in the specification file allow you to write unknowns=0. For this exercise use for example In this case, the toolkit creates a plotter and hands over to this plotter all discretisation points. However, it neglects all return data, i.e. nothing is plotted.

To compute the global integral of a quantity, you might want to use the vtk::Cartesian::ascii plotter but set the unknowns to zero. Whenever your plotter becomes active, ExaHyPE calls your startPlotting operation. Add a local attribute m to your class and set it to zero in the start function. In your conversation routines, you can now accumulate the L2 integral in m, while you use finishPlotting write the result to the terminal or into a file of your choice, e.g. If you alter the start and finish routine, please continue to call the parent operation, too.

We illustrate the realisation at hands of a simple computation of the global L_2 norm over all quantities of a simulation. For this, we first add a new variable to the class:

```
class MyEulerSolver_Plotter0: public ...
private:
    // We add a new attribute to the plotter.
    double _globalL2Accumulated;
public:
    MyEulerSolver_Plotter0();
    virtual ~MyEulerSolver_Plotter0();
...
```

Next, we set this quantity to zero in the plotter initialisation, we accumulate it in the mapping operation and we write the result to the terminal when the plotting finishes.

```
void MyEulerSolver_Plotter0::startPlotting(double time) {
    // Reset global measurements
    _globalL2Accumulated = 0.0;
}

void MyEulerSolver_Plotter0::finishPlotting() {
    _globalL2Accumulated = std::sqrt(_globalL2Accumulated);
```

```
std::cout << "my_global_value_=_" << _globalL2Accumulated << std::endl;</pre>
void MyEulerSolver_Plotter0::mapQuantities(
   const tarch::la::Vector<DIMENSIONS, double>& offsetOfPatch,
   const tarch::la::Vector<DIMENSIONS, double>& sizeOfPatch,
   const tarch::la::Vector<DIMENSIONS, double>& x,
   double* Q,
   double* outputQuantities,
   double timeStamp
) {
 // There are no output quantities
 assertion( outputQuantities==nullptr );
 // Now we do the global computation on Q but we do not write anything
 // into outputQuantities
 const NumberOfLagrangePointsPerAxis = 4; // Please adopt w.r.t. order
 const NumberOfUnknownsPerGridPoint = 5; // Please adopt
 double scaling = tarch::la::volume(
   sizeOfPatch* (1.0/NumberOfLagrangePointsPerAxis)
 for (int iQ=0; iQ<NumberOfUnknownsPerGridPoint; iQ++) {</pre>
   _globalL2Accumulated += Q[iQ] *Q[iQ] *scaling;
 }
}
```

As we have set the number of plotted unknowns to zero, no output files are written at all. However, all routines of MyEulerSolver_Plotter0 are invoked, i.e. we can compute global quantities, e.g. Some remarks on the implementation:

- It would be nicer to use the plotter routines of Peano when we write data to the terminal. This way, we can filter outputs via a filter file, i.e. at startup, and Peano takes care that data from different ranks is piped into different log file and does not mess up the terminal through concurrent writes.
- Most L_2 computations do scale the accumulated quantity with $\frac{1}{N}$ where N is the number of data points. Such an approach however fails for adaptive grids. If we scale each point with the mesh size, we automatically get a discrete equivalent to the L_2 norm that works for any adaptivity pattern. The volume function computes h^d for a vectorial h. See the documentation in tarch::la.
- The abovementioned version works if you use a Cartesian plotter where ExaHyPE's solution already is projected onto regular patches within each cell (subsampling). There are other plotters that allow you to evaluated the unknowns directly in the Lagrange points. The scaling of the weights then however has to be chosen differently.

Plotting is expensive as ExaHyPE switches off multithreading for plotting always. It thus makes sense not to invoke a plotter too often—even if you can handle the produced data of a simulation.

16.2. Reduction of global quantities over all MPI ranks

The code snippets so far are unaware of any MPI parallelisation. ExaHyPE does disable any shared memory parallelisation if you decide to plot—so ensure that there is a reasonable time in-between any two plots, even if they do only derive a single scalar—but it does not automatically synchronise the plotters between any two MPI ranks at any time.

We try to make ExaHyPE minimalistic and easy to handle, maintain and learn. Predefined reduction routines—reduction means all MPI ranks combine their results into one final piece of data on one rank—would contradict this objective and require us to come up with a comprehensive list of possibly required reductions. So we decided to make the programming of reductions simple rather than offering as many as possible reductions out-of-the-box.

Reducing data from all MPI ranks is a popular task in distributed memory programming. Therefore, MPI offers a collective operation to do this. The term collective here means that all MPI ranks are involved. The term collective also reasons why we may not use MPI collectives in ExaHyPE. Our dynamic load balancing, notably in combination with dynamic mesh refinement, may remove MPI ranks from the computation at any time; just to use them for other tasks later on that are urgent. You can never rely that really all MPI ranks do work (though most of the time, all of them will do). As a result, we have to program the reduction manually. We discuss how to do this by means of the summation of values from all plotters running on MPI ranks at a certain time.

• If you have code parts that you want not to be translated if no MPI is activated, protect it via

```
#ifdef Parallel
...
#endif
```

• ExaHyPE runs plotters only on "active" MPI ranks. If an MPI rank currently is not used by the (dynamic) load balancing, no plotter ever is started on this rank. At the same time, ExaHyPE's Peano code base identifies a *global master* rank. This rank is always working. If you have to reduce data, it is convenient always to reduce all data on the global master. At any point, you can find out whether you are on the global master via

```
#include "tarch/parallel/Node.h"
...
if (tarch::parallel::Node::getInstance().isGlobalMaster()) {
...
}
```

Please note that isGlobalMaster() is always defined. If you run without MPI, it always returns true as there is only one instance of ExaHyPE running.

• Peano, which is ExaHyPE's grid management engine, uses literally hundreds of different message types running through the network at any time simultaneously. It is important that we do not interfer with any ExaHyPE core messages if we postprocess data. To ensure this, we propose to *tag* messages, i.e. to give them a label to say "these are for my postprocessing" only. Peano offers a tagging mechanism that we use here.

Our proposed reduction now realises the following three ideas:

- 1. We do all the reduction at the end of finishPlotting where we can assume that the reduced data per rank is available.
- 2. If we run on any rank that is not the global master, finishPlotting sends its data to the global master.
- 3. The global master's finishPlotting runs over all ranks that are not idling around and collects the data from them.

```
#include "tarch/parallel/Node.h"
#include "tarch/parallel/NodePool.h"
void MyEulerSolver_Plotter0::finishPlotting() {
// All the stuff we have done before comes here
// ...
const int myMessageTagUseForTheReduction =
 tarch::parallel::Node::getInstance().reserveFreeTag(
  "MyEulerSolver_Plotter0::finishPlotting()" );
double myValue = ...;
if (tarch::parallel::Node::getInstance().isGlobalMaster()) {
 double receivedValue;
 for (
  int rank=1;
  rank<tarch::parallel::Node::getInstance().getNumberOfNodes(); rank++</pre>
  if ( !tarch::parallel::NodePool::getInstance().isIdleNode(rank) ) {
   MPI_Recv( &receivedValue, 1, MPI_DOUBLE, rank,
    myMessageTagUseForTheReduction,
    tarch::parallel::Node::getInstance().getCommunicator(),
    MPI_STATUS_IGNORE );
   myValue += receivedValue;
```

```
}
}
else {
MPI_Send( &myValue, 1, MPI_DOUBLE,
   tarch::parallel::Node::getGlobalMasterRank(),
   myMessageTagUseForTheReduction,
   tarch::parallel::Node::getInstance().getCommunicator()
);
}

tarch::parallel::Node::getInstance().releaseTag(
   myMessageTagUseForTheReduction);
}
```

The reserveFreeTag operation stems from Peano. We are supposed to tell the function which operation has invoked it, as this is a quite useful piece of information for MPI debugging. The last line of the code snippet returns this tag again, so it might be reused later on. Our snippet demonstrates the reduction at hands of the double variable double. An extension to non-double and vector types should be straightforward for developers having rudimentary knowledge of MPI.

The class Node is a singleton—it exists only once—representing an MPI rank. The class NodePool is a singleton, too, and holds all of Peano's load balancing information. Notably is knows which ranks are idling. We use those two classes here.

Our code snippet sends the value of myValue to the global master if we run into the routine on a rank which is not the global master itself. If the plotter is invoked on the global master, we run over all the ranks that do exist. Per rank, we ask the node pool whether the rank is idling. If it is not, we know that it will send data to the global master and we receive these data.

Part V. **ExaHyPE** design & rationale

17. **ExaHyPE** architecture

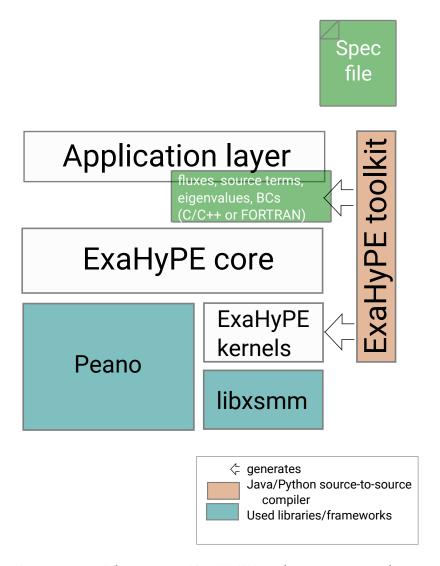


Figure 17.1.: The generic ExaHyPE architecture at a glance

ExaHyPE is a solver engine (Figure 17.1), i.e. the sole code can not solve any problem. Domain-specific code has to integrate into ExaHyPE to make it a working simulation code. All these code fragments that are PDE-specific are summarised in ExaHyPE as application layer.

To write an ExaHyPE code, users typically start from a specification file. We use a green colour in our cartoon to highlight that this file is to be written completely by the ExaHyPE user. The specification file is passed to the ExaHyPE toolkit that

creates lots of glue code and empty application-specific classes where the user has to fill in flux functions, eigenvalue computations, and so forth (green again). The generated glue code and these empty templates that are to be befilled make up the aforementioned *application layer*. Usually, there is no need to modify any glue, but the user is free to do so.

The core ExaHyPE code is now an application based upon the software Peano that brings together the application-specific code fragments and the dynamically adaptive Cartesian mesh. It also controls Peano's parallelisation. Peano itself is a 3rd party component and not part of the original ExaHyPE project. We thus colour it here. ExaHyPE tailors its generic features towards ADER-DG.

In the simplest version, the sketched architecture now is complete. One of ExaHyPE's key ideas however is to use tailored, extremely optimised code snippets whenever it comes to the evaluation of fluxes, eigenvalues, space-time predictors, and so forth. If the user decides to run for these optimised variant in the specification file, the toolkit skips the creation some application-specific emtpy templates that are to be befilled. Instead, it creates domain- and architecture-specific code fragments (*kernels*) that are now invoked whenever we run into computationally demanding program phases.

These generated fragments are typically not to be edited and are an essential part of ExaHyPE (and therefore white) and of ExaHyPE's identity. While the ExaHyPE core relies on Peano, the generated kernels use Intel's libxsmm which is the second 3rd party building block in the basic ExaHyPE architecture.

Obviously, our architecture as described so far still is simplistic and rudimentary; too rudimentary for most real-world applications. We hence expect most applications to extend and connect it to futher software fragments. An example is given in Figure 17.2. However, such links to other products are not part of the core ExaHyPE architecture and concept, as we try to keep it as simple and free of dependencies as possible.

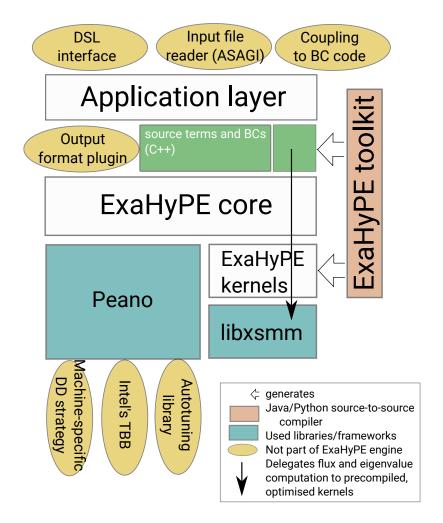
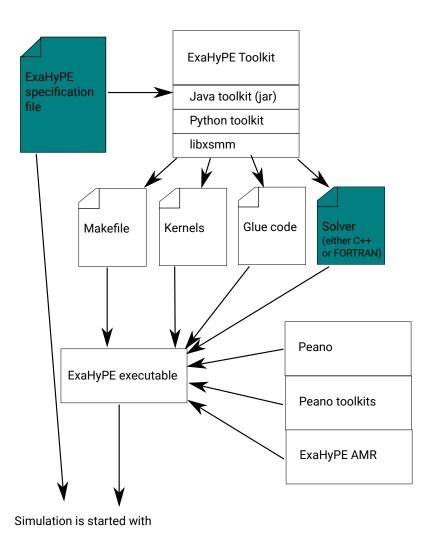


Figure 17.2.: Any ExaHyPE application tailors/uses/adopts the generic architecture to its needs. The present snapshot shows a sophisticated seismology ExaHyPE code that couples the simulation engine to 3rd party software and provides a domain specific language (DSL) in the top layer, delegates all flux and eigenvalue computations to predefined, optimised kernels generated by the toolkit and using libxsmm, and internally relies on Intel's TBBs, Peano's autotuning and Peano's generic domain decomposition to speed the code up.

18. **ExaHyPE** workflow



./MyExaHyPEApplication spec-file

Figure 18.1.: A typical ExaHyPE workflow.

The typical workflow when working with the ExaHyPE engine is graphically displayed in Figure 18.1 and described in the following:

1. The user writes a specification file (text format) that holds all required data ranging from paths, which parallelisation to use, computational domain up to a specification which kind of solvers will exist and which numerical schemes they realise.

- 2. This specification file is handed over to the ExaHyPE toolkit which is a Java tool. It internally relies on Python scripts and invokes the libxsmm generator driver as well. A local build of the libxsmm's code generation driver is therefore a prerequisite for using optimised kernels.
- 3. The toolkit yields a couple of files (Makefile, glue code, helper files, ...). Among them is also one C++ implementation class per solver that was specified in the specification file. The output directory in the specification file defines where all these generated files go to.
- 4. a) Within each C++ implementation file, the user can code solver behaviour such as initial conditions, mesh refinement control, and so forth.
 - b) The whole build environment is generated. A simple make thus at any time should create the ExaHyPE executable.
- 5. If you run your ExaHyPE executable, you have to hand over the specification file again. Obviously, many entries in there (simulation time or number of threads to be used) are not evaluated at compile time but at startup. You don't have to recompile your whole application if you change the number of threads to be used.

To summarise, the blueish text files in Figure 17.1 are the only files you typically have to change yourself. All the remainder is generated and assembled according to the specification file.

Driven by the choice in the specification file, ExaHyPE chooses either generic kernels or optimised kernels. If you switch between the generic and the optimised kernels, you have to use the toolkit to regenerate the glue code.

Part VI.

Appendix

A. The **ExaHyPE** toolbox

The ExaHyPE toolbox is a small Java toolkit. It acts as sole interface for users, i.e. non-developers. We decided to realise it in Java for several reasons:

- 1. We can realise lots of syntax checks without blowing up the C++ code.
- 2. We have to generate code fragments in ExaHyPE. The order of the methods chosen for example has an impact on kernel calls and mapping variants. This is easy in Java.
- 3. We prefer not to have several interfaces. With a Java front-end, we can directly generate the configuration rather than parsing configurations again.

A.1. Rebuilding the toolbox

To (re-)build the toolbox, change into the source directory of the toolkit and type in

make all

Alternatively, you can invoke the makefile with make target where target is from

- createParser. Recreates the Java parser. ExaHyPE's Java parser relies on SableCC. The parser has to be regenerated if and only if you change the grammar or you have to rebuild the tool without a previous build.
- compile. Translate the toolkit.
- dist. Pack the translated files into one jar file.
- clean. Clean up the compiled and temporary files.

A.2. Troubleshooting

Our toolkit is based upon ant as build environment. It seems that newer Linux/-Java versions are often incompatible with precompiled ant versions (OpenSUSE, e.g., has problems). In this case, you might have to switch to superuser and to select an older Java version manually:

```
update-alternatives --config java
```

In most cases, we however found it more convenient to recompile the toolkit.

B. Frequently asked developer questions

• MPI plus TBB deadlocks or is very slow

On several systems, we have encountered problems when we tried to use multithreaded MPI. As a result, we disable multithreaded MPI usage by default in the makefile (switch -DnoMultipleThreadsMayTriggerMPICalls). You might want to try to enable multithreaded MPI again with -DMultipleThreadsMayTriggerMPICalls, but we cannot guarantee that it works properly. It is trial & error depending on your compiler/MPI/cluster choice.

How can I use ExaHyPE's logging

ExaHyPE uses Peano's technical architecture (tarch) and the logging therein. For a detailed documentation of this technical architecture (besides logging, there's also a small linear algebra library in there that allows you to write down C++ code in a MATLAB-like notation) please consult the Peano cookbook. For the simple logging, please add a static field to year header

```
static tarch::logging::Log _log;
```

initialise it and then use the logInfo macro:

```
tarch::logging::Log MyParticularClass::_log( "MyParticularClass" );

[...]

void MyParticularClass::myRoutine() {
   double myA = 1.2345;

   logInfo( "myRoutine()", "variable_myA_has_the_value_" << myA );

[...]
}</pre>
```

From hereon, you can also filter your own log messages with the filter file.

- I get tons of warnings in the MPI part of the code that irritate me. Please add the statement -Wno-deprecated-declarations to the compile arguments in your makefile.
- How do I deal with vectors \vec{v} in the code? Peano, the underlying grid code for ExaHyPE, contains a small linear algebra library called tarch::la. It is used inside the ExaHyPE core all the place and also visible to the user-defined kernels (chapter 5). You may want to dig into the Peano Doygen

documentation to learn about the vector classes offered. You can, however, also use the method tarch::la::Vector::data() to access the raw C array, ie. to obtain a data* pointer. This allows you to easily connect any C++ vector library, ie. LAPACK, Eigen, Boost, GLM, Armadillo or you own one to your kernels. It also allows you to freely use Fortran functions in your kernels. This is frequently used in the project where tensorial computations are done.

• To be continued ...

C. Frequently asked user questions

• How do I modify the computational domain?

Open the specification file and alter the width. The entry specifies the dimensions of the computational domain. Please note that ExaHyPE only supports square/cube domains as it works on cube/square cells only. You might have to extend your problem's domain accordingly. width is read at startup time, i.e. there's no need to rerun any script or recompile once you have changed the entry. Just relaunch your simulation.

• How do I alter the time step size?

ExaHyPE implements two time stepping schemes (global time stepping and globally fixed time stepping). Per solver, you can choose a strategy. All schemes run a trial time step in the first iteration to evaluate the CFL condition and determine a reasonable time step size. All schemes besides globalfixed then continue to study the CFL constraints and adopt the time step size automatically. Only globalfixed fixes the time step size for the whole simulation period. All schemes use a security factor on the CFL condition, i.e. the admissible time step size is scaled before it is applied. This scaling is set by fuse-algorithmic-steps-factor in the optimisation block. Its value has to be small or equal to one. Besides this security factor, nothing has to be done by the user.

• How do I alter the time step size (advanced)?

You may however choose the time step size yourself if you do not rely on the generated kernels but write a whole solver yourself (see solver variant user::defined in Section 5) from scratch.

• Why do the time stamps in the plot output differ from the ones I have set in the specification file?

Plotting at specific times would require ExaHyPE to perform shorter time steps than prescribed by the CFL condition. It is well-known that this leads to long-term pollution of the numerical solution.

We thus plot as soon as the solver time (minimum over all cells) is greater or equal to the next plotting time.

• ExaHyPE did not create all the plots I requested. Why? It's very likely that more than one of the plotting times you specified did fall into a single time step interval of the corresponding solver.

In this case, see bullet point Why do the time stamps in the plot output differ from the ones I have set in the specification file?.

- How do I change the resolution dynamically? The dynamic AMR is realised along the same lines as the static refinement. You have to implement refinementCriterion in your solver which tells ExaHyPE where you want to refine. How this is realised—notably how all the ranks and cores synchronise—is hidden away from the user code and decided in the kernel.
- To be continued ...

D. Solver Kernels

Table $\overline{\text{D.1}}$ shows the kernel variants offered for the ADER-DG solver type. The last column indicates whether we offer FORTRAN support for these.

Kernel	Description	F
user::defined	Only function signatures are generated. All responsibility which and how kernels are realised is up to the user. We basically only hand over large double arrays. This is the lowest level of abstraction.	yes
generic::fluxes::nonlinear	Default ADER-DG routines are used, but they make no assumptions on the fluxes. The toolkit will ask you to provide fluxes, eigenvalues, and so forth which are then used within nested for loops generi- cally. This is the second level of abstraction and well- suited for fast prototyping.	yes
generic::fluxes::linear	Similar to generic::fluxes::nonlinear. Given the explicit notion of a linear flux, the underlying generic source code however is simpler. This variant is faster.	yes
optimised::fluxes::nonlinear	Equals generic::fluxes::nonlinear from a user's point of view. However, the underlying ADER-DG routines/loops all are optimised through libxsmm.	no
optimised::fluxes::linear	Optimised version of optimised::fluxes::nonlinear that removes any non-linear iteration.	no
kernel::euler2d	These are optimised kernels that solves the Euler equations in two or three dimensions. They mirror the example from Chapter 5. As we fix the PDE, no fluxes, eigenvalues, have to be written by the user and the resulting kernel is very aggressively optimised.	t.b.a.

Table D.1.: ADER-DG solver types

Table $\hbox{\bf D.2}$ displays the kernel variants offered for the the Finite-Volume solver type.

Kernel	Effect
user::defined	Only function signatures are generated. All responsibility which and how kernels are realised is up to the user. We basically only hand over large double arrays. This is the lowest level of abstraction.
t.b.d.	

Table D.2.: Finite-Volume solver types

E. Datastructures in the Optimised Kernels

This chapter provides an up-to-date documentation of the memory layout employed in the optimised solver kernels.

System Matrices The optimised kernels use padded structures and thereby differ from the generic code base. Padding, of course, depends on the target microarchitecture. It guarantees that the height of the matrices is always a multiple of the SIMD width.

All matrices are stored in column major order. Table E.1 lists the memory layout. The corresponding CodeGen files are DGMatrixGenerator.py and WeightsGenerator.py. The matrix dudx is only generated in the case of a linear PDE.

Matrix	Memory Layout	Size
Kxi iK1 dudx	[[Kxi];0] analogous to Kxi analogous to Kxi	(nDOF+Pad) × nDOF
FRCoeff FLCoeff	[FRCoeff] analogous to FRCoeff	$1 \times nDOF$
F0	[F0;0]	$1 \times (nDOF+Pad)$
equidistantGridProjector1d fineGridProjector1d	analogous to generic version analogous to generic version	

Table E.1.: Structure of the system matrices in the optimised kernels.

Quadrature Weights The solver kernels exhibit three distinct patterns of weights. Either occurrence is mapped onto a separate data structure.

- wGPN. Quadrature weights.
- aux = (/ 1.0, wGPN(j), wGPN(k) /). Combination of two weights, stored in weights2.
- aux = (/ wGPN(i), wGPN(j), wGPN(k) /). Combination of three weights, stored in weights3.

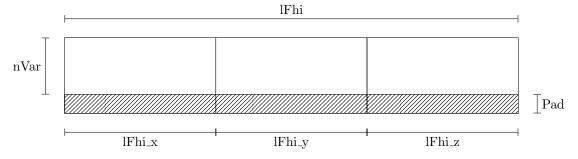
Table E.2 illustrates the memory layout for a 2D and 3D setup, respectively. In any case, the weights vectors are interpreted as linear, padded arrays. The pad width depends on the microarchitecture and ensures that the total length of the vectors is a multiple of the SIMD width. In the 2D case, the vectors weights1 and weights2 coincide because their computational pattern coincides.

Name	Memory Layout	Meaning
		2D
weights1	$[w_i, 0]$	quadrature weights + Pad
weights2	$[w_i, 0]$	quadrature weights + Pad
weights3	$[w_i w_j, 0]$	outer product of quadrature weights + Pad
		3D
weights1	$[w_i, 0]$	quadrature weights + Pad
weights2	$[w_i w_i, 0]$	outer product of quadrature weights + Pad
weights3	$[w_i w_j w_k, 0]$	all combinations of quadrature weights + Pad

Table E.2.: Variables holding combinations of quadrature weights employed in the optimised kernels.

Parameters and Local Variables Table E.3 lists the structure of the input/output parameters of the solver kernels and local variables used within the solver kernels. The parameters nDOFx, nDOFy and nDOFz denote the number of degrees of freedom in x-, y-, and z-direction, respectively. Analogously, nDOFt gives the number of degrees of freedom in time. All variables are linearised, i.e. one-dimensional arrays.

The parameter lFhi is decomposed into three tensors lFhi_x, lFhi_y, lFhi_z, all sized (nVar+Pad)·nDOF³



Name Ordering		Size			
rhs, rhs0 lFbnd lQbnd lqh (nonlinear) lqh (linear)	(nVar,nDOFx,nDOFy,nDOFz,nDOFt) (nDOFx, nDOFy, nVar) (nDOFx, nDOFy, nVar) (nVar, nDOFx, nDOFy, nDOFz,nDOFt+1)	nVar · nDOF ⁴ ((nDOFx · nDOFy)+Pad)· nVar ((nDOFx · nDOFy)+Pad)· nVar ((nVar+Pad)· nDOF ⁴ (nVar+Pad)· nDOF ³ ·(nDOF+1) (nVar+Pad)· nDOF ⁴ ·d			
lFh lFhi luh, lduh	(nVar, nDOFx, nDOFy, nDOFz,nDOFt,d) irregular (nVar, nDOFx, nDOFy, nDOFz)	(nVar+Pad)·nDOF ³ ·d (nVar · nDOF ³ nVar · nDOF ³			
	temporary variables				
QavL, QavR lambdaL, lambdaR	(nVar) (nVar)	(nVar+Pad) (nVar+Pad)			
auxiliary variables					
tmp.bnd s_m ("scaled matrix") s_v ("scaled vector")	(nDOFx, nDOFy, nVar) analogous to Kxi analogous to F0	((nDOFx · nDOFy)+Pad)· (nVar+Pad)			

Table E.3.: Data layout (Fortran notation) used in the optimised kernels.

Their internal ordering of the degrees of freedom depends on the direction.

- 1Fhi_x. (nVar, nDOFx, nDOFy, nDOFz)
- 1Fhi_y. (nVar, nDOFy, nDOFx, nDOFz)
- 1Fhi_z. (nVar, nDOFz, nDOFx, nDOFy)

Note that the structure of luh respectively lduh is chosen for compatibility with the generic kernels.

F. Remarks on output file formats

F.1. VTK

Our VTK support sticks to the VTK legacy format. This section is not supposed to replace the VTK file format description as it can be found in The VTK User's Guide available from Kitware free of charge. An excerpt of the relevant pages can be found at http://www.vtk.org/wp-content/uploads/2015/04/file-formats.pdf, e.g. This section complements the technical aspects with a user's point of view.

- **File format.** As VTK has no real support for block-structured adaptive meshes, ExaHyPE writes out all data as an unstructured mesh: the output file describes a graph. The graph is specified via three sections.
- **Section 1: Point coordinates.** In the first section of the VTK file, all points used by the mesh are specified. There is no particular on these points. Please see the introductory remarks in Chapter 15 on DG polynomials that clarify why some points can be found redundantly in the file. The only way the order plays a role is through the fact that it imposes an enumeration of the vertices starting with 0.
- **Section 2: Cells.** In a second part of the file, we specify all cells. Again, there is no particular order but the sequence in which the cells are enlisted defines an order. Each line in the file specifies on cell. VTK requires each cell definition to start with the number of vertices used to span the cell. As ExaHyPE restricts to block-Cartesian grids, this initial number always is either 4 or 8.
- Section 3: Cell types. The VTK file format requires a block where one enlists the cell type per cell entry. As we stick to cubes/squares in ExaHyPE, this section contains the same identifier (number) per cell and can be skipped if you want to postprocess the data yourself.
- **Point time step data.** After the cell types, you find the time steps of the point data. Per vertex, we track at which time stamp its data is written if your plotter has to write data. Otherwise, the section is omitted. Per vertex, we write one scalar. For global time stepping, all values are equal. For adaptive time stepping, they might differ as the data gives the real time stamp of the data, not the simulation time when the data has been written.
- **Point data.** After the time stamp, you find per vertex one vector holding all the vertex data.

- Cell time step data. Analogous to vertices.
- Cell data. Analogous to vertices.

If you have chosen a VTK binary format, all the section identifiers are still written in plain text, i.e. you can continue to open the output files as text files. The real data, i.e. the coordinates, the indices spanning a cell, the unknowns the are written binary and this binary stream is embedded into the text file.

requires texts about the file format. A first attemp is made in https://gitlab.lrz.de/exahype/ExaHyPE-Engine/wikis/fileformats and shall be resumed here.

Here we follow the display of cell and point data as defined in the VTK file format.

F.1.1. VTK cell data

Table F.1 describes the data present in a VTK file which was created with the vtk::*::cells::* stanza. A note on the ordering of the data rows: There is no obvious order one should assume. Instead, it is helpful to sort the data on own criteria after reading in.

Point ID	Points			Time	Cell ID	Cell Type	Q		
	X	y	Z			J F -	Q_0	Q_1	
0	0.00	0.00	0.00	0.01	0	Pixel	1.23	4.56	
1	0.01	0.00	0.00	0.01	1	Pixel	3.41	0.07	
2	0.01	0.01	0.00	0.01	2	Pixel	0.81	5.47	
•••					•••				

Table F.1.: The point and cell data tables in ExaHyPE's VTK cell data format

F.1.2. VTK point data

Table F.2 describes the data present in a VTK file which was created with the vtk::*::vertices::* stanza. A note on the ordering of the data rows: There is no obvious order one should assume. Instead, it is helpful to sort the data on own criteria after reading in.

Point ID		Points	i	Time	Q		
10111112	х	y	Z		Q_0	Q_1	
0	0.00	0.00	0.00	0.01	1.23	4.56	
1	0.01	0.00	0.00	0.01	3.14	0.07	
2	0.01	0.01	0.00	0.01	0.81	5.47	

Cell ID	Cell Type
0	Pixel
1	Pixel
2	Pixel
•••	

Table F.2.: The point and cell data tables in ExaHyPE's VTK point data format