Ve 280

Programming and Elementary Data Structures

Linked List

Learning Objectives:

Understand what is a linked list and when to use it

Know how to implement a (singly) linked list

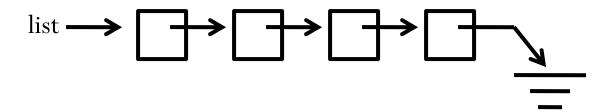
Understand what is doubly-linked list and when to use it

Outline

- Introduction to Linked List
- Implementation of Linked List
- Double-Ended Linked Lists

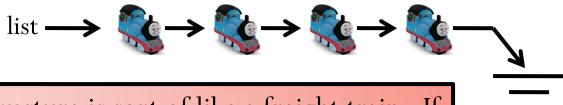
Introduction

- Expandable arrays are only one way to implement storage that can grow and shrink over time.
- Another way is to use a **linked structure**.
- A linked structure is one with a series of zero or more data containers, connected by pointers from one to another, like:



Introduction

- Expandable arrays are only one way to implement storage that can grow and shrink over time.
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- A linked structure is one with a series of zero or more data containers, connected by pointers from one to another, like:



A linked structure is sort of like a freight train. If you need to carry more freight, you get a new boxcar, connect it to the train, and fill it. When you don't need it any more, you can remove that boxcar from the train.

Introduction

- Suppose we wanted to implement an abstract data type for a mutable list of integers, represented as a linked structure.
- This ADT will be similar to the list_t type from project two, except that list t is **immutable**:
 - Once a list_t object was created, no operations on that list would ever change it.

Introduction

• There are three operations that the list must support:

```
bool isEmpty();
  // EFFECTS: returns true if list is empty,
  //
              false otherwise
void insert(int v);
  // MODIFIES: this
  // EFFECTS: inserts v into the front of the list
class listIsEmpty {}; // An exception class
int remove();
  // MODIFIES: this
  // EFFECTS: if list is empty, throw listIsEmpty.
              Otherwise, remove and return the first
  //
  //
              element of the list
```

Introduction

• For example, if the list is (1 2 3), and you remove (), the list will be changed to (2 3), and remove returns 1.

```
int remove();
  // MODIFIES: this
  // EFFECTS: if list is empty, throw listIsEmpty.
  // Otherwise, remove and return the
  // first element of the list
```

• If you then insert (4), the list changes to (423).

```
void insert(int v);
   // MODIFIES: this
   // EFFECTS: inserts v into the front of the list
```

What would be the impact of using Linked List instead of an array for defining IntSet?

Select all the correct answers.

- A. It is not possible to redefine IntSet with Linked List.
- **B.** Some operations (among query, insert, remove) of IntSet would be faster if we were to use Linked List instead of an array.
- C. Some operations (among query, insert, remove) of IntSet would be slower if we were to use Linked List instead of an array.
- D. IntSet would be more memory efficient.

Outline

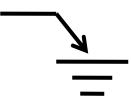
- Introduction to Linked List
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Implementation

• To implement linked list, we need to pick a concrete representation for the node in the list.

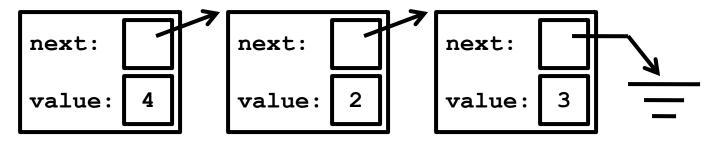
```
struct node {
  node *next;
  int value;
};
```

- The invariants on these fields are:
 - The value field holds the integer value of this element of the list.
 - The **next** field points to the next node in the list, or NULL if the node is the last one in the list.
- NULL means "pointing at nothing". Its value is "0", written as:



Implementation

• The concrete representation of the list (4 2 3) is:



- The basic idea of implementation is that each time an int is inserted into the list, we'll create a new node to hold it.
- Each time an int is removed from the (non-empty) list, we'll save the value of the first node, destroy the first node, and return the value.

Implementation

• We'll use the following (private) data members:

• The rep invariant is that "first" points to first node of the sequence of nodes representing this IntList, or NULL if the list is empty.

Linked List Traversal

• With the "first" pointer, we can traverse the linked list.

```
int IntList::getSize() {
// Effect: return # of items in this list
  int count = 0;
  node *current = first;
  while(current) {
                                    Traverse
    count++;
                                    through the list.
    current = current->next;
  return count;
```

Implementation

• Here are the public methods we have to implement:

```
class IntList {
  node *first;
public:
 bool isEmpty();
  void insert(int v);
  int remove();
  IntList();
                              // default ctor
  IntList(const IntList& 1); // copy ctor
  ~IntList();
                              // dtor
  // assignment
  IntList &operator=(const IntList &1);
```

Implementation

- We will implement the "operational" methods first, assuming that the representation invariants hold.
- After that, we'll go back and implement the default constructor and the **Big Three** to make sure that:
 - The invariants hold during object creation.
 - All dynamic resources are accounted for.
- A list is empty if there is no node in the list, or first is NULL:

```
bool IntList::isEmpty() {
  return !first;
}
```

Implementation

- When we insert an integer, we start out with the "first" field pointing to the current list:
 - That list might be empty, or it might not, but in any event "first" must point to a valid list thanks to the rep invariant.
- The first thing we need to do is to create a new node to hold the new "first" element:

```
void IntList::insert(int v) {
  node *np = new node;
```

Question: Can we declare a **local** object instead of a **dynamic** one? I.e., declare:

node n;

Implementation

- Next, we need to establish the invariants on the new node.
- This means setting the value field to ∨, and the next field to the "rest of the list" this is precisely the start of the current list:

```
void IntList::insert(int v) {
  node *np = new node;
  np->value = v;
  np->next = first;
  ...
}
```

Implementation

• Finally, we need to reestablish the representation invariant: first currently points to the second node in the list, and must point to the first node of the new list instead:

```
void IntList::insert(int v) {
  node *np = new node;
  np->value = v;
  np->next = first;
  first = np;
```

We have accomplished the work of the method, and all invariants are now true, so we are done.

Implementation

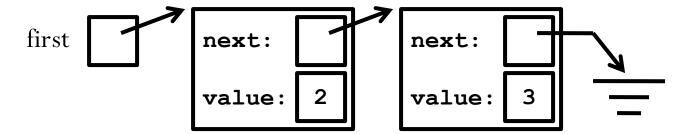
• Finally, we need to reestablish the representation invariant: first currently points to the **second** node in the list, and must point to the first node of the new list instead:

```
void IntList::insert(int v) {
  node *np = new node;
  np->value = v;
  np->next = first;
  first = np;
}
Notice that this matter what the is, as long as the
```

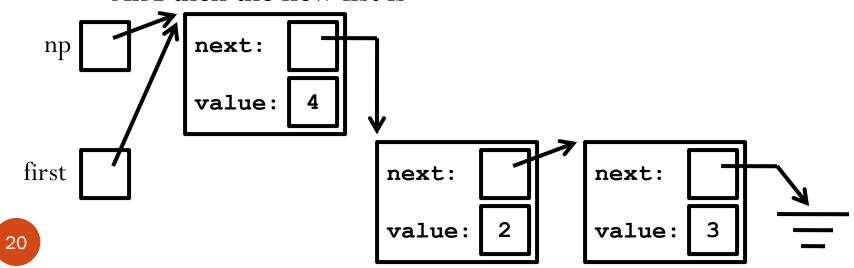
Notice that this works no matter what the current list is, as long as the invariant holds (see next slides).

Example

- Suppose we are inserting a 4.
- The list might already have elements:

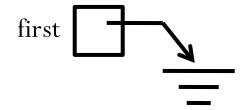


• And then the new list is

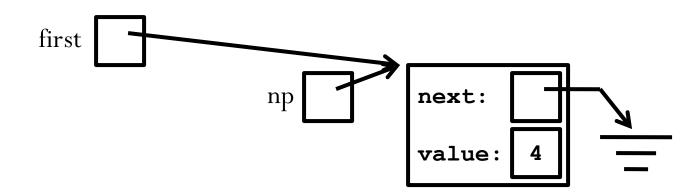


Example

- Suppose we are inserting a 4.
- The list might be empty:



• And the new list is



Implementation

- Removal is a bit trickier since there are lots of things we need to accomplish, and they have to happen in precisely the right order.
- If the first item is removed, this violates the invariant on "first", which we have to fix:

```
int IntList::remove() {
    ...
    first = first->next;
    ...
}
```

Implementation

first = first->next;

- If we are removing the first node, we must delete it to avoid a memory leak.
- Unfortunately, we can't delete it before advancing the "first" pointer (since first->next would then be undefined).
- But, **after** we advance the "first" pointer, the node to be removed is an orphan, and can't be deleted.
- We solve this by introducing a local variable to remember the "old" first node, which we will call the victim.

Implementation

• After creating the Victim, we can then delete the node **after** it is skipped by first.

```
int IntList::remove() {
  node *victim = first;
  ...
  first = victim->next;
  ...
    Note: equivalent to
    delete victim;    first = first->next;
    ...
}
```

Implementation

- However, removing the first node is only half of the work.
- We must also return the value that was stored in the node.
- This is also tricky:
 - We can't return the value first and then delete the node, since then the delete wouldn't happen.
 - Likewise, if we delete the node first, the contained value is lost.
- So, we use **another** local variable, result, to remember the result that we will eventually return.

Implementation

Now that we have the result variable, the method becomes:

```
int IntList::remove() {
  node *victim = first;
  int result;
  first = victim->next;
  result = victim->value;
  delete victim;
  return result;
```

Implementation

• Finally, we need to cope with an empty list, and throw an exception if we have one:

```
int IntList::remove() {
  node *victim = first;
  int result;
  if (isEmpty()) {
    listIsEmpty e;
    throw e;
  first = victim->next;
  result = victim->value;
  delete victim;
  return result;
```

Exercise

• Note that for victim, we initialize it when it is declared, but we don't for result.

• Question:

Why didn't we initialize result to victim->value?

```
int IntList::remove() {
  node *victim = first;
  int result;
  if (isEmpty()) {
    listIsEmpty e;
    throw e;
  }
  first = victim->next;
  result = victim->value;
  delete victim;
  return result;
}
```

Exercise

• Slightly more efficient (one assignment less when the list is empty!)

```
int IntList::remove() {
  if (isEmpty()) {
    listIsEmpty e;
    throw e;
  node *victim = first;
  first = victim->next;
  int result = victim->value;
  delete victim;
  return result;
```

Implementation

- Now let's work on the maintenance methods:
 - Constructors
 - Assignment operator
 - Destructor
- The default constructor is easy:
 - We just have to establish the representation invariant for an empty list:

```
IntList::IntList()
: first(0)
{}
```

Implementation

- Likewise, the destructor is easy.
- We have to destroy each node in the list before the list itself is destroyed.
- Actually, we already have a mechanism to destroy a single node – it's a side effect of remove ().
- So, we call remove () until the list is empty, ignoring remove () 's result.
- We put this functionality into another private method, called removeAll().

Implementation

• Here is the destructor and its helper:

```
void IntList::removeAll() {
  while (!isEmpty()) {
    remove();
IntList::~IntList() {
  removeAll();
```

?

Do you agree that the copy operation can be performed as follows?

```
IntList::IntList(const IntList &1): first (0) {
   if (!1.first) return;
   node *current = 1.first;
   while(current) {
      this->insert(current->value);
      current = current->next;
   }
}
```

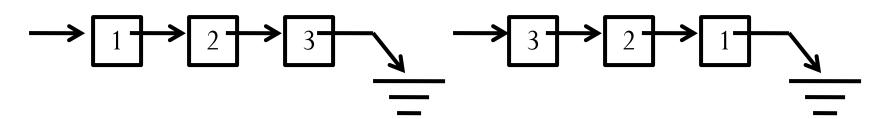
Select all the correct answers.

- A. Yes, all the values are copied.
- **B.** No, some values are not copied.
- C. No, even if all the values are copied.
- **D.** In fact, sometimes it works.



Implementation

- The copy constructor is tricky.
- The naive approach would be to walk the list from front to back, and insert each element that we find into the list.
- However, this gives us a list **in reverse order**, because we always insert a new element at the beginning of the list.



• What we would prefer is to be able to walk the list backward.

Implementation

- Since there's no convenient way to walk the list backwards, we'll instead write a helper function that will **recursively** walk the list till the end.
- When we unwind the recursion, we can insert the elements from "back" to "front", which gives us the right answer:

```
void IntList::copyList(node *list) {
  if (!list) return; // Base case

copyList(list->next);
  insert(list->value);
}
copyList is a private member function
```

Implementation

```
void IntList::copyList(node *list) {
  if (!list) return; // Base case
  copyList(list->next);
  insert(list->value);
                       Assuming the current list is empty
```

• copyList() must be a private method, since it deals with the concrete representation, not the abstraction.

Implementation

- With copyList(), the copy constructor and assignment operator are pretty easy.
- For the copy constructor, make sure we start with an empty list, and then call copyList():

```
IntList::IntList(const IntList &1)
: first (0)
{
   copyList(l.first);
}
```

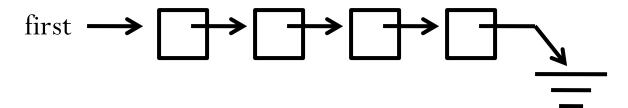
Implementation

• The assignment operator ensures that there is no self-assignment, destroys the current list, then copies the new one:

Outline

- Introduction to Linked List
- Implementation of Linked List
- Double-Ended Linked Lists

- What if we wanted to insert something at the end of the list?
- Intuitively, with the current representation, we need to walk down the list until we found "the last element", and then insert it there.



- That's not very efficient, because we have to go through every element to insert something at the tail.
- Instead, we'll change our concrete representation to track both the front and the back of our list.

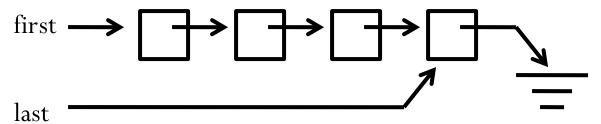
Double-ended list

• The new representational invariant has **two** node pointers:

```
class IntList {
  node *first;
  node *last;
  public:
  ...
};
```

- The invariant on first is unchanged.
- The invariant on last is:
 - last points to the last node of the list if it is not empty, and is NULL otherwise.

- So, in an empty list, both first and last point to NULL.
- However, if the list is non-empty, they look like this:



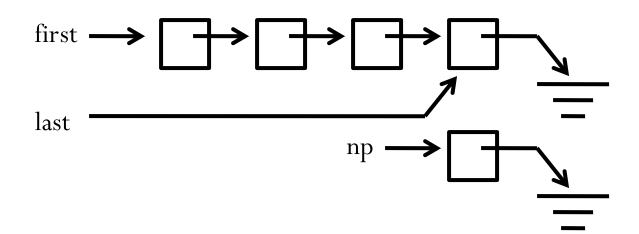
- Question: Adding this new data member, what methods should be changed?
 - <u>Answer</u>: remove, insert, and default/copy constructor should be re-written
- In lecture, we'll only write a new method, insertLast, which inserts a node at the tail of the linked list

Double-ended list

• First, we create the new node, and establish its invariants:

```
void IntList::insertLast(int v) {
  node *np = new node;
  np->next = NULL;
  np->value = v;
  ...
}
```

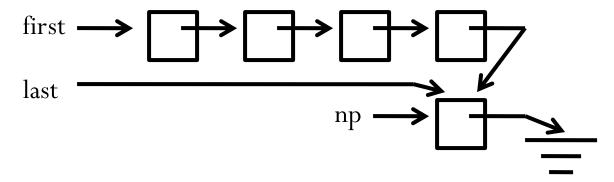
- To actually insert, there are two cases:
 - If the list is empty, we need to reestablish the invariants on first and last (the new node is both the first and last node of the list)
 - If the list is **not** empty, there are two broken invariants. The "old" last->next element (incorrectly) points to NULL, and the last field no longer points to the last element.



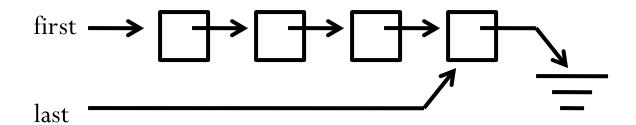
```
void IntList::insertLast(int v) {
  node *np = new node;
  np->next = NULL;
  np->value = v;
  if (isEmpty()) {
    first = last = np;
  else {
    last->next = np;
    last = np;
              first -
              last
```

Double-ended list

• This is efficient, but only for insertion.



• **Question**: Is removal **from the end** efficient or not? Why?



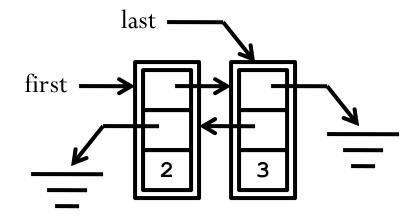
- To make removal from the end efficient, as well, we have to have a doubly-linked list, so we can go forward and backward.
- To do this, we're going to change the representation again.
- In our new representation, a node is:

```
struct node {
  node *next;
  node *prev;
  int value;
};
```

- The next and value fields are the same as before.
- The prev field's invariant is:
 - The prev field points to the previous node in the list, or NULL if no such node exists (e.g., the current node is the first node).

Double-ended list

- With this representation, an empty list is unchanged: both "first" and "last" are NULL.
- While the list (2, 3) would look like this:



• We will implement each method in project five.

Which of the following statements are true when comparing doubly-linked lists and singly-linked lists?

Select all the correct answers.

- A. Doubly-linked lists allows more operations.
- **B.** Doubly-linked lists make some operations more efficient.
- C. Doubly-linked lists make some operations less efficient.
- **D.** Doubly-linked lists double the memory requirement compared to singly-linked list.



Reference

- **Problem Solving with C++ (8th Edition)**, by *Walter Savitch*, Addison Wesley Publishing (2011)
 - Chapter 13.1 Nodes and Linked Lists