## Use case

theta\_dot\_pan\_real =

## Pan axis

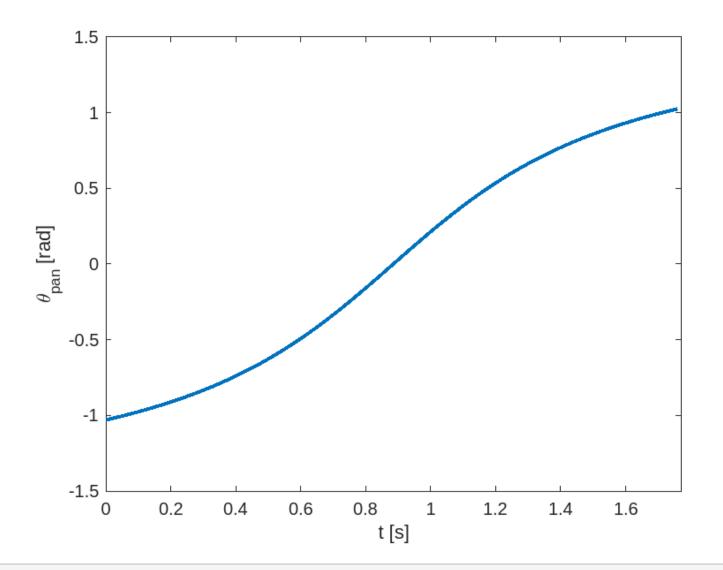
```
syms W L V_y V_x d x_0 t theta_pan theta_dot_pan H a b c theta_tilt_sym theta_tilt_real
         = [W L V_y V_x d theta_pan theta_dot_pan H];
s_real = [20 40 0 22.6 2 theta_pan theta_dot_pan 7];
x = (V_x * t - 1/2 * L);
y = (d + 1/2 * W);
theta_pan_sym = atan( x / y )
theta_pan_sym =
theta_dot_pan_sym = diff(theta_pan_sym)
theta_dot_pan_sym =
\frac{V_x}{\left(\frac{\left(\frac{L}{2} - V_x t\right)^2}{\left(\frac{W}{2} + d\right)^2} + 1\right) \left(\frac{W}{2} + d\right)}
t_max_sym = L/V_x
t_max_sym =
theta_pan_real = subs(theta_pan_sym, s, s_real)
theta_pan_real =
atan\left(\frac{113 t}{60} - \frac{5}{3}\right)
theta_dot_pan_real = subs(theta_dot_pan_sym, s, s_real)
```

```
\frac{113}{60\left(\frac{\left(\frac{113\,t}{5} - 20\right)^2}{144} + 1\right)}
```

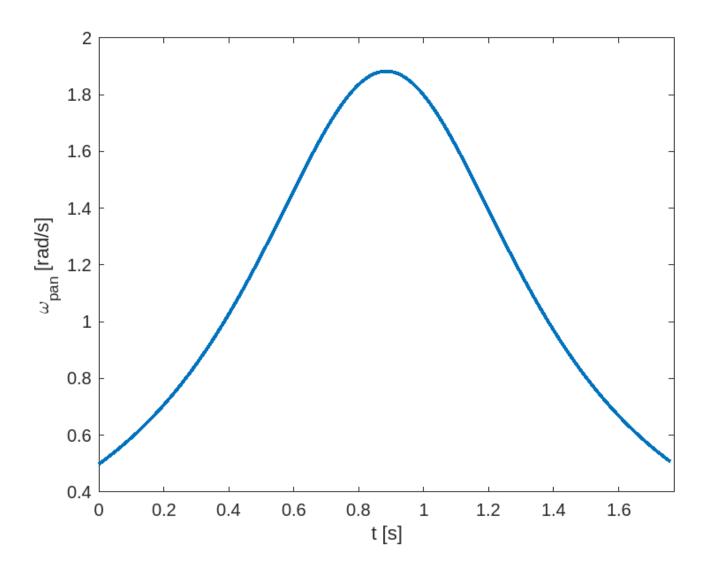
```
t_max = double(subs(t_max_sym, s, s_real))
```

 $t_{max} = 1.7699$ 

```
theta_pan = @(time) subs(theta_pan_real, t, time);
theta_dot_pan = @(time) subs(theta_dot_pan_real, t, time);
t_vals = 0:0.01:t_max
plot(t_vals, theta_pan(t_vals), LineWidth=2)
xlim([0 t_max])
xlabel('t [s]')
ylabel('\theta_{pan} [rad]')
exportgraphics(gcf, '../figures/reference_theta_pan.png')
```



```
plot(t_vals, theta_dot_pan(t_vals), LineWidth=2)
xlim([0 t_max])
xlabel('t [s]')
ylabel('\omega_{pan} [rad/s]')
exportgraphics(gcf, '../figures/reference_omega_pan.png')
```



## Tilt axis

```
syms H a b c

z = @(t) a*t^2 + b*t + c;

eqs = [
    z(0) == 0;
    z(t_max/2) == H;
    z(t_max) == 0;
]
```

eqs =

$$\begin{pmatrix} c = 0\\ \frac{10000 \, a}{12769} + \frac{100 \, b}{113} + c = H\\ \frac{40000 \, a}{12769} + \frac{200 \, b}{113} + c = 0 \end{pmatrix}$$

[A B] = equationsToMatrix(eqs, [a b c])

A =

$$\begin{pmatrix}
0 & 0 & 1 \\
\frac{10000}{12769} & \frac{100}{113} & 1 \\
\frac{40000}{12769} & \frac{200}{113} & 1
\end{pmatrix}$$

B =

 $\begin{pmatrix} 0 \\ H \\ 0 \end{pmatrix}$ 

sol = solve(eqs, [a b c])

sol = struct with fields:

a: -(12769\*H)/10000

b: (113\*H)/50

c: 0

sol.a

ans =

$$-\frac{12769\ H}{10000}$$

sol = subs(sol, s, s\_real)

sol = struct with fields:

a: -89383/10000

b: 791/50

c: 0

$$z = sol.a * t.^2 + sol.b * t + sol.c$$

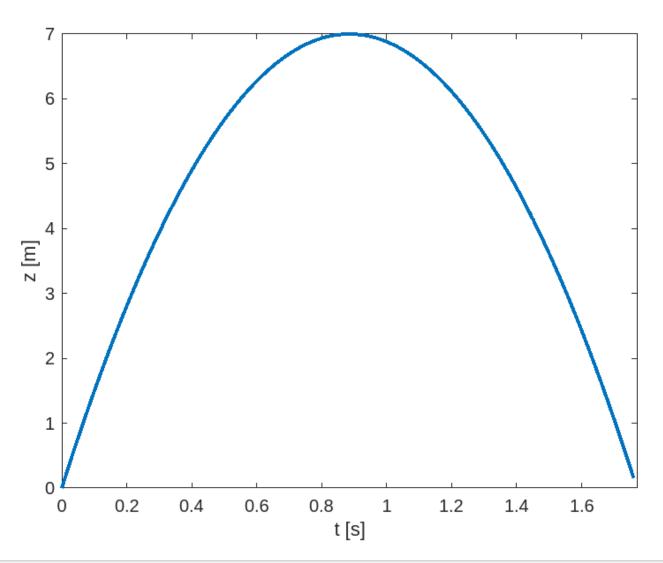
z =

$$\frac{791\,t}{50} - \frac{89383\,t^2}{10000}$$

latex(vpa(z,4))

ans =

```
plot(t_vals, subs(z, t, t_vals), LineWidth=2)
xlim([0 t_max])
xlabel('t [s]')
ylabel('z [m]')
```



$$d = sqrt(x^2 + y^2)$$

d =

$$\sqrt{\left(\frac{L}{2} - V_x t\right)^2 + \left(\frac{W}{2} + d\right)^2}$$

theta\_tilt\_sym =

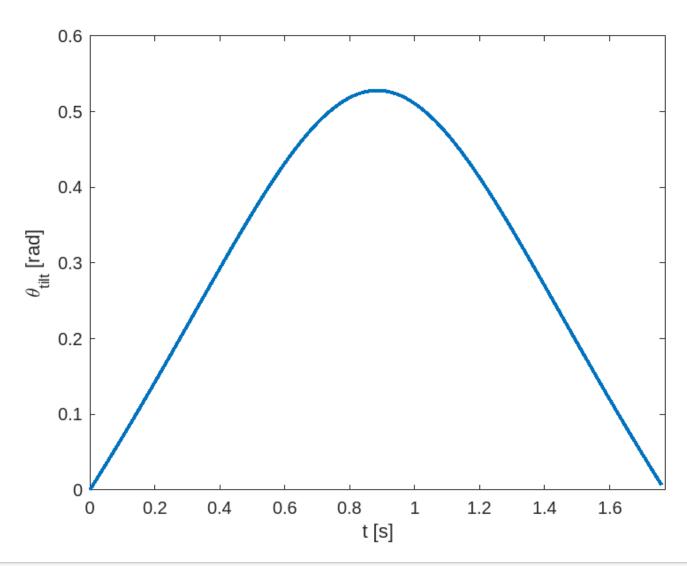
$$\operatorname{atan}\left(\frac{\frac{791 t}{50} - \frac{89383 t^2}{10000}}{\sqrt{\left(\frac{L}{2} - V_x t\right)^2 + \left(\frac{W}{2} + d\right)^2}}\right)$$

```
theta_tilt_real = subs(theta_tilt_sym, [s], [s_real])
```

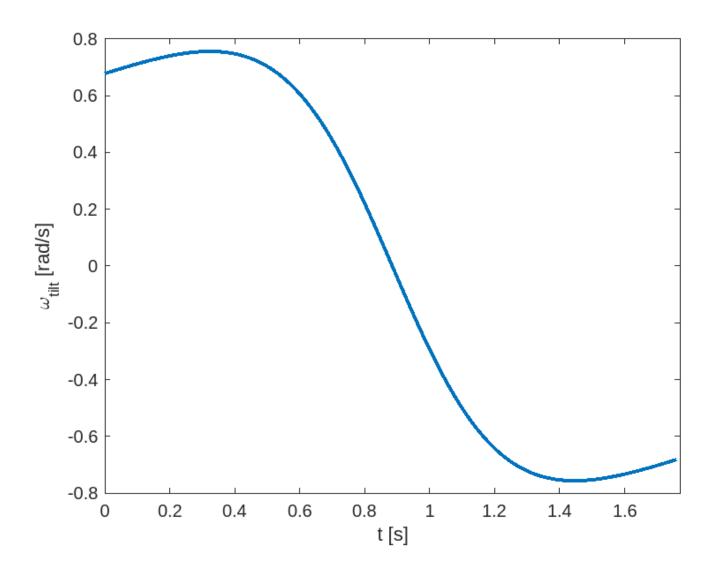
theta\_tilt\_real =

$$\frac{\frac{791 t}{50} - \frac{89383 t^2}{10000}}{\sqrt{\left(\frac{113 t}{5} - 20\right)^2 + 144}}$$

```
theta_dot_tilt_real = diff(theta_tilt_real);
plot(t_vals, subs(theta_tilt_real, t, t_vals), LineWidth=2)
xlim([0 t_max])
xlabel('t [s]')
ylabel('\theta_{tilt} [rad]')
exportgraphics(gcf, '../figures/reference_theta_tilt.png')
```



```
plot(t_vals, subs(theta_dot_tilt_real, t, t_vals), LineWidth=2)
xlim([0 t_max])
xlabel('t [s]')
ylabel('\omega_{tilt} [rad/s]')
exportgraphics(gcf, '../figures/reference_omega_tilt.png')
```



## **References for Simulink**

```
ref = @(time) double(subs([
    theta_dot_pan_real;
    theta_dot_tilt_real;
], t, time));
```

```
plot(t_vals, ref(t_vals), LineWidth=2)
xlim([0 t_max])
xlabel('t [s]')
ylabel('\omega [rad/s]')
legend(["Pan" "Tilt"])
```

