

$$\begin{cases} \dot{\mathbf{I}} = \frac{\mathbf{V}_{s}}{L_{m}} - \frac{\mathbf{R}_{m}}{L_{m}} \mathbf{I} - \frac{\mathbf{K}_{e}}{L_{m}} \dot{\mathbf{G}} & \dot{\mathbf{G}}_{s} \\ \ddot{\mathbf{G}}_{g} = \frac{\mathbf{b}}{\mathbf{J}} \dot{\mathbf{G}}_{g} - \frac{\mathbf{K}_{i}}{\mathbf{J}} \mathbf{G} & \mathbf{I} \end{cases}$$

Let's create a state space model!

First we define our states and input

$$X = \begin{bmatrix} I \\ \dot{o}_{3} \end{bmatrix} \Rightarrow \dot{X} = \begin{bmatrix} \dot{I} \\ \ddot{o}_{3} \end{bmatrix}, \quad u = V_{3}$$

Then we fill in the model

$$\dot{X} = A_X + Bu = \begin{bmatrix} \dot{I} \\ \ddot{o}_g \end{bmatrix} = \begin{bmatrix} \frac{R_{u_1}}{L_{m_1}} - k_{v_2} \\ \frac{-k_{v_1}}{L_{m_2}} - \frac{k_{v_2}}{2} \end{bmatrix} \begin{bmatrix} I \\ \dot{o}_g \end{bmatrix} + \begin{bmatrix} \dot{L}_{m_2} \\ 0 \end{bmatrix} \vee_S$$

As the pan/tilt system has two axis, the model is exteded with two extra states. We can now describe both pan and tilt.