## CSCI2100C 2019-20: Assignment 4 Part 2\*

# This assignment is due at 11:59:59pm, 5th May 2020.

■ Q1. [38 marks] Consider the directed graph  $G_1$  as shown in Figure 1. Answer the following questions.

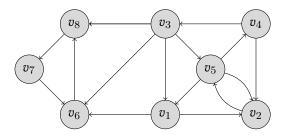


Figure 1. Directed graph for Q1

- (i). [4 marks] Calculate the out-degree of  $v_3$  and the in-degree of  $v_8$ . (Refer to CSCI2100C-Lecture22 Page 11)
- (ii). [8 marks] For  $G_1$ , show both its adjacency list representation and its adjacency matrix representation. (Refer to CSCI2100C-Lecture22 Pages 17-20)
- (iii). [10 marks] Traverse  $G_1$  using breadth-first search with  $v_1$  as the source, assuming that the out-neighbors of a node are visited in ascending order of ID. Show the process and the content of the queue Q step by step. You may use 0 to denote the color to be white, 1 to denote the color to be gray, and 2 to denote the color to be black. (Refer to CSCI2100C-Lecture22 Pages 24-28)
- (iv). [8 marks] According to the results of Part (iii), show the contents of minlength array and prev array respectively. (Refer to CSCI2100C-Lecture22 Pages 34-35)
- (v). [4 marks] Show how to get the minimum length path from the source  $v_1$  to  $v_4$  using the minlength array and prev array. Justify your answer.
- (vi). [4 marks] Draw the BFS tree. (Refer to CSCI2100C-Lecture22 Page 36)

<sup>\*</sup>Departmental Guideline for Plagiarism (Department of Systems Engineering and Engineering Management): If a student is found plagiarizing, his/her case will be reported to the Department Examination Panel. If the case is proven after deliberation, the student will automatically fail the course in which he/she committed plagiarism. The definition of plagiarism includes copying of the whole or parts of written assignments, programming exercises, reports, quiz papers, mid-term examinations and final examinations. The penalty will apply to both the one who copies the work and the one whose work is being copied, unless the latter can prove his/her work has been copied unwittingly. Furthermore, inclusion of others' works or results without citation in assignments and reports is also regarded as plagiarism with similar penalty to the offender. A student caught plagiarizing during tests or examinations will be reported to the Faculty office and appropriate disciplinary authorities for further action, in addition to failing the course.

■ Q2. [26 marks] A directed graph  $G_2$  is shown in Figure 2. Assume that we use depth-first search (DFS) to check if  $G_2$  is a DAG and the permutation of nodes to do DFS on  $G_2$  is  $(v_2, v_3, v_4, v_5, v_6, v_1, v_7)$ . During a DFS traversal, assume that the out-neighbors of a node are visited in ascending order of ID. Answer the following questions.

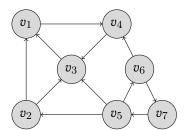


Figure 2. Directed Graph  $G_2$  for Q2

- (i). [7 marks] Show the first discovery time and finish time of each node. (Refer to CSCI2100C-Lecture24 Pages 5-6)
- (ii). [4 marks] Draw the DFS trees. (Refer to CSCI2100C-Lecture24 Page 7)
- (iii). [11 marks] Classify edges according to the interval of each node derived from Part (i). You should explicitly output the type of each edge. Justify your answer. (Refer to CSCI2100C-Lecture24 Page 8)
- (iv). [4 marks] Show why  $G_2$  is (or is not) a DAG using the results in Part (iii). Justify your answer. (Refer to CSCI2100C-Lecture24 Page 11)