A title with some math: x = 1

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Abstract...

Co	ontents	
1	Introduction	1
2	Methods & Datasets 2.1 Observables 2.2 Total GCE Luminosity 2.3 GCE Spacial distribution 2.4 Luminosity Functions 2.5 Sensitivity Models	1 1 1 3 3 4
3	Results	6
4	Future Sensitivity	6
5	Conclusion	6
Α	Conversion Between GCE Luminosity and Flux	6

1 Introduction

2 Methods & Datasets

2.1 Observables

To fit the luminosity functions described in section 2.4, we will use three observables: the total flux of the GCE $F_{\rm GCE}$, the ratio of the total flux to the flux visible from point sources resolved by $Fermi\ R_{\rm r}$, and the number of resolved point sources $N_{\rm r}$. We fix the first observable at $F_{\rm GCE} = 1.295 \times 10^{-9}\,{\rm erg\,s^{-1}}$ according to the methods outlined in section 2.2. We allow the other two observables to vary as functions of the parameters of the luminosity functions.

We will also discuss a third feature of a potential MSP population in the GC: the total number of MSPs $N_{\rm GCE}$, resolved or unresolved. This number is not measurable, but serves as a useful reference to gauge the physicality of any population of MSPs. *Mention that it's expected to be around 40,000*.

2.2 Total GCE Luminosity

Since an estimate of the total flux of the GCE is necessary for our data, we extract the total flux from several previous analyses of spectra using the following three methods and compare them. The spectral analyses we study here are refs. [1, 4, 5, 9??]. Each reference reports the total flux $F_{\gamma}(E)$ observed in an energy bin centered on E. The spectra from these sources are reported in figure 1

Describe the sources: what's similar between them, what's different.

We use compare three methods of extracting the total GCE flux from these analyses. The first method is direct numerical integration of the spectra provided by each source. This method is most sensitive to the data measured by *Fermi* and does not attempt to abstract over it with a smooth function.

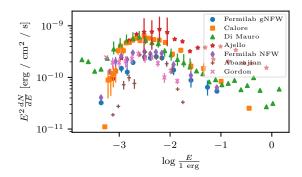


Figure 1.

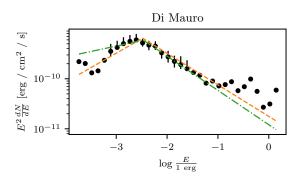


Figure 2.

However, numerical integration cannot account for the spectrum lying outside of Fermi's spectrum of sensitivity, and it may be oversensitive to experimental error. Therefore, we also consider a broken law fit to the data, of the same form as the NPTF luminosity function: eq. 2.4. It has four parameters: a constant of proportionality, the turnover flux F_b , and the slopes above and below the turnover flux n_2 and n_1 . This function can then be analytically integrated over all flux values to get the total flux of the GCE. Many of the analyses cited above only report error bars on some points, because error bars on the other points are too large. We therefore fit only to the points with error bars reported. Mention the specific range fitted over.

Unfortunately, for some analyses, the number of points reported with error bars is only slightly larger than the number of parameters of the broken power law function. To ensure that the fit result is less prone to statistical deviations of a small number of points, we use a third method in addition to the above two. Ref. [4] provides their fit parameters for their GCE flux spectral data: $F_{\rm b} = n_1 = -1.42, n_2 = 2.63$. Check for sign errors in the original. Also get the flux they provide. The third fitting method is to fix these three broken power law parameters at these values and allow only the overall normalization to vary.

An example of all three of these fitting methods applied to reference [5] is shown in figure 2.

In practice,

Just double check that I normalized the power law correctly in parse spectrum.py.

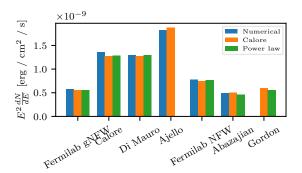


Figure 3.

2.3 GCE Spacial distribution

$$\rho_{\text{NFW}}(r) = \left(\frac{r}{r_s}\right)^{-\gamma} \left(1 + \frac{r}{r_s}\right)^{-3-\gamma} \tag{2.1}$$

where $\gamma = 1.2$ and $r_s = 20$ kpc for this work.

2.4 Luminosity Functions

Previous work has interpreted this MSP model. Ref. [9] has proposed an exponentially damped power law luminosity function

$$P_{\text{Power law}}(L) = L^{-\alpha} \exp\left(-\frac{L}{L_{\text{max}}}\right) \left[\Gamma\left(1 - \alpha, \frac{L_{\text{min}}}{L_{\text{max}}}\right) L_{\text{max}}^{1-\alpha}\right]^{-1}.$$
 (2.2)

The function has been normalized so that $P_{\text{Power law}}(L)$ represents the probability that a given MSP has luminosity L. This luminosity function restricts the range of luminosities to $[L_{\min}, \infty)$, where L_{\min} , L_{\max} , and α are free parameters. The following should probably be moved to the introduction, where Fermilab's research is described. This reference found that $(1 \times 10^{29} \, \text{erg s}^{-1}, 1 \times 10^{35} \, \text{erg s}^{-1}, 1.94)$ is required reproduced observations. They find that this model admits three million MSPs in the GCE, which differs from estimates based on the physical properties of observed MSPs that estimate the number of MSPs at the Galactic center at the order of 40,000 [?].

Ref. [6] proposes a power law luminosity function of

$$P_{\text{Log normal}}(L) = \frac{\log_{10} e}{\sigma \sqrt{2\pi} L} \exp\left(-\frac{(\log_{10} L - \log_{10} L_0)^2}{2\sigma^2}\right),\tag{2.3}$$

where L_0 and σ are free parameters. The ref. fits this model to data from globular cluster (GCL) data, yielding values $L_0 = 8.8 \times 10^{33} \,\mathrm{erg \, s^{-1}}$ and $\sigma = 0.62$. It predicts thousands of MSPs to occupy the GCE if the entire excess is to be explained by MSPs.

Ref. [8] proposes several more intricate luminosity functions, derived from a model of the pulsars themselves. They find that the same model may be used for resolved, globular cluster MSPs in the Galactic disk and unresolved MSPs at the Galactic center. We use their luminosity function generated for the galactic disk. It closely resembles a log normal luminosity function as in equation 2.3, where $L_0 = 1.61 \times 10^{32} \,\mathrm{erg \, s^{-1}}$ and $\sigma = 0.700$.

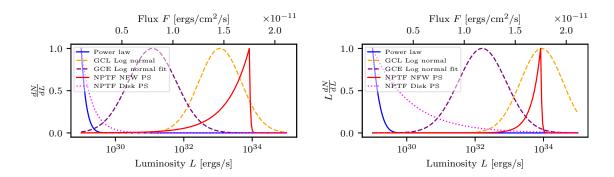


Figure 4. *Left:* Power law, GCL log normal, GCE log normal, and NPTF luminosity functions for MSPs in the GCE, vertically rescaled. *Right:* Same plot as *left* but weighted by luminosity.

Finally, ref. [7] proposes a broken-power law luminosity function of

$$P_{\text{NPTF}}(L) = \left(\frac{(1 - n_1)(1 - n_2)}{L_b(n_1 - n_2)}\right) \begin{cases} (L/L_b)^{-n_1} & L < L_b \\ (L/L_b)^{-n_2} & L > L_b \end{cases}$$
(2.4)

where the free parameters n_1 , n_2 , and L_b were found via a Non-Poissonian Template Fitting model (NPTF) to be $(18.2, -0.66, 8.66 \times 10^{33} \, \mathrm{erg \, s^{-1}})$ for an NFW-squared-distributed population of MSPs named NFW PS. The pxxxaper proposes a second luminosity function named Disk PS with parameters $(17.5, 1.4, 3.34 \times 10^{35} \, \mathrm{erg \, s^{-1}})$, which is unnormalizable except when a minimum luminosity of pulsars L_{\min} is introduced. We set $L_{\min} = 1 \times 10^{29} \, \mathrm{erg \, s^{-1}}$, which is the same minimum pulsar luminosity used by ref. [9]. The turnover luminosity L_{b} was given as a photon flux value in units of photons per centimeter squared per second; the process used to convert from photon flux to luminosity is detailed in the methods section.

All the above-mentioned luminosity functions are shown in figure 4.

2.5 Sensitivity Models

The *Fermi* telescope does not detect every pulsar in the GC; background emission obscures dimmer pulsars, and statistical effects cause some bright sources to be unresolved. We make use of three sensitivity models to model these factors.

The first, and simplest, is a step function luminosity model. It asserts that all point sources with $L > L_{\rm th}$ are resolved, and none with $L < L_{\rm th}$. Here, $L_{\rm th} = 10^{34}\,{\rm erg\,s^{-1}}$. This sensitivity model is the one used by ref. [9] to obtain the parameters of the power law luminosity function described in the paragraph after eq. 2.2. The four properties we intend to measure are then given by

$$L_{\rm GCE} = N_{\rm GCE} \int_{L_{\rm min}}^{\infty} LP(L)dL , \qquad L_{\rm r} = N_{\rm GCE} \int_{L_{\rm th}}^{\infty} LP(L)dL ,$$

$$N_{\rm r} = N_{\rm GCE} \int_{L_{\rm th}}^{\infty} P(L)dL , \qquad (2.5)$$

where N_{GCE} is a normalization constant, fixed by requiring that L_{GCE} reproduces the flux F_{GCE} observed. The conversion between L_{GCE} and F_{GCE} is outlined in appendix A.

The second sensitivity model acknowledges the effect of background flux on resolvability and uses a position-dependent flux threshold $F_{th}(b, l)$ published by the Fermi team [2, 3]

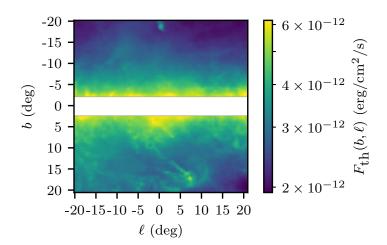


Figure 5. Position-dependent flux thresholds required to resolve an MSP, published by refs. [2, 3].

(figure 5). Here, I could talk about how to convert between flux and luminosity and then use the mean of this map to assess how accurate 1e34 ergs/s actually is.. To calculate the four properties of GC MSP populations, we use

$$\begin{split} F_{\text{GCE}} &= \int_{\Omega} d\Omega \int_{0}^{\infty} s^{2} ds A \rho_{NFW}^{2}(r) \int_{L_{\text{min}}}^{\infty} dL \frac{L}{4\pi s^{2}} P(L) \,, \\ N_{\text{GCE}} &= \int_{\Omega} d\Omega \int_{0}^{\infty} s^{2} ds A \rho_{NFW}^{2}(r) \,, \\ F_{\text{r}} &= \int_{\Omega} d\Omega \int_{0}^{\infty} s^{2} ds A \rho_{NFW}^{2}(r) \int_{4\pi s^{2} F_{\text{th}}(b,\ell)}^{\infty} dL \frac{L}{4\pi s^{2}} P(L) \,, \\ N_{\text{r}} &= \int_{\Omega} d\Omega \int_{0}^{\infty} s^{2} ds A \rho_{NFW}^{2}(r) \int_{4\pi s^{2} F_{\text{th}}(b,\ell)}^{\infty} dL P(L) \,. \end{split} \tag{2.6}$$

Here, Ω represents the 20° × 20° region of interest with |b| < 2° cut out, and A is the coefficient of equation 2.1, fixed by forcing F_{GCE} to equal the observed value. In equation 2.6 represents the distance to the galactic center from the point of integration, and is determined by the law of cosines: $r^2 = s^2 + r_c^2 - 2r_c s \cos \ell$.

The third and final sensitivity model takes into account the statistical fluctuation of photons from point sources. Ref. [8] models the probability that a point source with average flux F is resolved as

$$P_{\rm r}(F) = \frac{1}{\sigma_{\rm th} F \sqrt{2\pi}} \exp\left(-\frac{(\ln F - (F_{\rm th}(\ell, b) - K_{\rm th}))^2}{2\sigma_{\rm th}^2}\right)$$
(2.7)

where $K_{\rm th}$ and $\sigma_{\rm th}$ were determined via an MCMC fit to globular cluster MSPs. What are the values? The observables are calculated simply by multiplying the integrand of the luminosity integral in equation 2.6 by $P_r(L/4\pi s^2)$ for $F_{\rm r}$ and $N_{\rm r}$. (Not for $F_{\rm GCE}$, because we do not require that the $F_{\rm GCE}$ flux be resolved.)

- 3 Results
- 4 Future Sensitivity
- 5 Conclusion

A Conversion Between GCE Luminosity and Flux

Copy most of this from the January summary, if I include it.

Acknowledgments

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Note added. This is also a good position for notes added after the paper has been written.

References

- [1] Kevork N. Abazajian, Nicolas Canac, Shunsaku Horiuchi, and Manoj Kaplinghat. Astrophysical and Dark Matter Interpretations of Extended Gamma-Ray Emission from the Galactic Center. *Phys. Rev. D*, 90(2):023526, 2014.
- [2] S. Abdollahi et al. Fermi Large Area Telescope Fourth Source Catalog. Astrophys. J. Suppl., 247(1):33, 2020.
- [3] J. Ballet, T. H. Burnett, S. W. Digel, and B. Lott. Fermi Large Area Telescope Fourth Source Catalog Data Release 2. 5 2020.
- [4] Francesca Calore, Ilias Cholis, and Christoph Weniger. Background Model Systematics for the Fermi GeV Excess. *JCAP*, 03:038, 2015.
- [5] Mattia Di Mauro. Characteristics of the Galactic Center excess measured with 11 years of Fermi-LAT data. Phys. Rev. D, 103(6):063029, 2021.
- [6] Dan Hooper and Tim Linden. The gamma-ray pulsar population of globular clusters: Implications for the GeV excess. *JCAP*, 2016(08), 8 2016.
- [7] Samuel K. Lee, Mariangela Lisanti, Benjamin R. Safdi, Tracy R. Slatyer, and Wei Xue. Evidence for Unresolved γ -Ray Point Sources in the Inner Galaxy. *Phys. Rev. Lett.*, 116(5):051103, 2016.
- [8] Harrison Ploeg, Chris Gordon, Roland Crocker, and Oscar Macias. Comparing the Galactic Bulge and Galactic Disk Millisecond Pulsars. *JCAP*, 12:035, 2020.
- [9] Yi-Ming Zhong, Samuel D. McDermott, Ilias Cholis, and Patrick J. Fox. Testing the Sensitivity of the Galactic Center Excess to the Point Source Mask. *Phys. Rev. Lett.*, 124(23):231103, 2020.