

State: We are interested in the true proportion of video game players (p) among U.S. adults.

Plan: We construct a one-sample z -interval for a population proportion at confidence level $C = 0.9$.

- Randomness: A random sample of U.S. adults is taken.
- Independence: Since the number of U.S. adults $\geq 10n = 10(2001) = 20010$, by the 10% rule, independence can be assumed.
- Normality: Since $n\hat{p} = 2001(0.49) = 980.49$, $n(1 - \hat{p}) = 2001(1 - 0.49) = 1020.51 \geq 10$, by the Large Counts Rule, \hat{p} is approximately normally distributed.

Do:

$$\begin{aligned} z_{\alpha=0.1}^* &= 1.645 \\ \text{SE} &= \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}} = \sqrt{\frac{0.49(1 - 0.49)}{2001}} = 0.011 \\ \text{ME} &= z^* \text{SE} = 0.018 \end{aligned}$$

$$90.0\% \text{ Confidence Interval} = \hat{p} \pm \text{ME} = 0.49 \pm 0.018 = (0.472, 0.508).$$

Conclude: We are 90.0% confident that the interval (0.472, 0.508) captures the true proportion of video game players among U.S. adults.