## OPTIMIZED STRATIFICATION PROJECT - (7/22/18)

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Section 1.Descriptive Statistics

The variable of interest is 'INVENTORY'.

The total number of units in the population is 9762.

> nrow(df) [1] 9762

The **true population total** is 1754954823.

> sum(df\$inventory)
[1] 1754954823

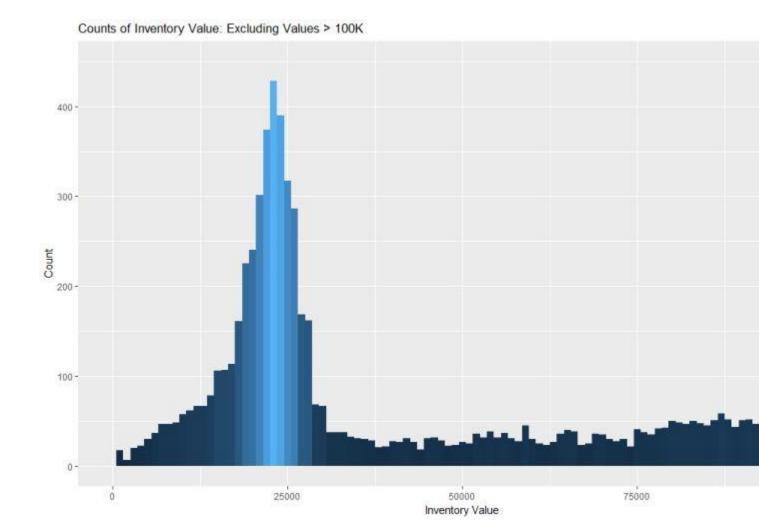
The true population standard deviation is 1573358.

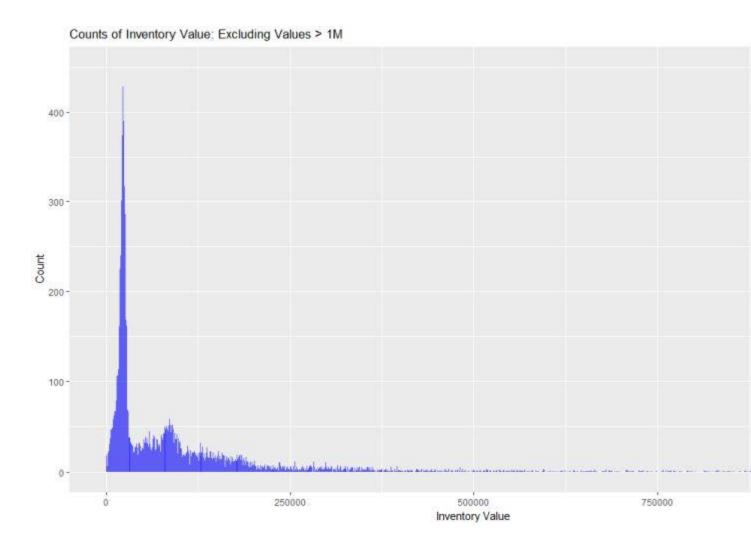
> sd(df\$inventory)
[1] 1573358

The **true population mean** is 179774.1.

> mean(df\$inventory)
[1] 179774.1

Histograms of the variable of interest are shown below:





Section 2. Stratification Using Sales(Inventory)

- 2.1 Description of the process followed in forming sampling strata for the population using the Inventory variable:
  - Description of the number and range of values chosen for the certainty stratum and the criteria used for including units in the certainty stratum.

Particularly when dealing with severely right-skewed data, best analytic practices suggest assigning the highest-valued records to the certainty stratum to minimize sampling variance. Cf. <a href="https://enablement.acl.com/helpdocs/analytics/13/user-guide/en-us/Content/da\_sampling\_data/classical\_variables\_sampling.htm#navlink-5">https://enablement.acl.com/helpdocs/analytics/13/user-guide/en-us/Content/da\_sampling\_data/classical\_variables\_sampling.htm#navlink-5</a>.

Deciding how many of the highest-valued records to assign was determined according to a custom-made optimization wrapper function designed to minimize the overall coefficient of variation (relative root mean squared error) produced when applying the generalized Lavallee-Hidiroglou stratification method for skewed populations.

Cf. Lavallée, P. and Hidiroglou, M. (1988). On the stratification of skewed populations, Survey Methodology, 14, 33-43.

The Lavallee-Hidiroglou stratification method is implemented using the strat.LH() function from the 'Stratification' R package. The function implements Kozak's Random Search method.

Cf. Kozak, M. (2004). Optimal Stratification Using Random Search Method in Agricultural Surveys, Statistics in Transition, 6, 5, 797-806.

For an explanation of Lavallee-Hidiroglou stratification and Kozak's Random Search method,

Cf. Sebnem, Er. (2011). Computational Methods for Optimum Stratification: A Review, Int. Statistical Inst.: Proc. 58<sup>th</sup> World Statistical Congress, 2011, Dublin (Session STS058).

As shown in Sebnem (2011), the Lavallee-Hidiroglou stratification method works as follows:

Lavallée & Hidiroglou tries to find such values (Lavallée & Hidiroglou (1988), pp.36)

$$(18) b_1 < b_2 < \dots < b_{L-1}$$

that minimizes n considering a take-all top stratum,

(19) 
$$n = N_L + \left(\sum_{h=1}^{L-1} N_h^2 \sigma_h^2 / a_h\right) \left(N^2 \mu^2 C V^2 + \sum_{h=1}^{L-1} N_h \sigma_h^2\right)^{-1}.$$

given the level of precision (CV) and the specified allocation scheme represented by  $a_h$  (Lavall Hidiroglou (1988), pp.36).

In their paper Lavallée & Hidiroglou (1988) mainly consider X-proportional power allocation:

(20) 
$$a_h = \frac{(W_h \mu_h)^p}{\sum_{h=1}^{L-1} (W_h \mu_h)^p}$$

where 0 . Putting (20) in (19)

(21) 
$$n = NW_L + \frac{N\left[\sum_{h=1}^{L-1} (W_h \sigma_h)^2 (W_h \mu_h)^p\right] \left[\sum_{h=1}^{L-1} (W_h \mu_h)^p\right]}{NCV^2 \mu^2 + \sum_{h=1}^{L-1} W_h \sigma_h^2}.$$

As shown in Sebnem (2011), Kozak's Random Search method works as follows:

Kozak's (2004) Random Search Method tries to find such values

$$(22) b_1 < b_2 < \cdots < b_{L-1}$$

that minimizes the objective function considering a take-all top stratum with Neyman allocation

(23) 
$$n = N_L + \left(\sum_{h=1}^{L-1} W_h \sigma_h\right)^2 \left(\mu^2 C V^2 + \frac{1}{N} \sum_{h=1}^{L-1} W_h \sigma_h^2\right)^{-1};$$

under the constraints  $N_h \ge 2$  for h = 1, 2, ..., L and  $2 \le n_h \le N_h$  for h = 1, 2, ..., L - 1, who is the minimizing sample size required to achieve the given precision CV of the mean estimate of straffication when the strata boundaries are  $\mathbf{b} = (b_1, b_2, ..., b_{L-1})^T$ .

Kozak's (2004) random search method chooses an initial set of strata boundaries and calculate function values of n. Then for a certain number of iterations the following steps are repeated:

 Generate the set of boundaries b' by choosing one stratum boundary b<sub>h</sub> and changing follows:

(24) 
$$b_h' = b_h + j$$

where j is the random integer,  $j \in \langle -p; -1 \rangle \cup \langle 1; p \rangle$  and p is a given integer according to the of the population.

- Calculate the function value of n'.
- If the constraints are satisfied and n' < n, the new set of boundaries bh' are accepted.</li>

The custom wrapper function (written in R) iterated through several sizes of highest-valued certainty strata before arriving at an optimum overall coefficient of variation (CV) value of **0.003779453**, using **110 records** with the highest inventory value. The values of these 110 records allocated to the certainty stratum **ranged from 1372514.04 to the maximum 105379553.91**.

o Description of the process for deciding on the number of non-certainty strata.

The same custom wrapper function served to jointly optimize the number of non-certainty strata, arriving at the number 10.

• Table showing a row for each stratum, with the stratum number, number of units, and range of values.

The optimal configuration of highest-valued records and number of non-certainty strata is shown below, with stratum numbers, number of units (Nh) and their respective ranges of values (bh):

```
print(Optim_Config)
Given arguments:
x = df$inventory
n = 500, Ls = 10, takenone = 0, takeall = 0
allocation: q1 = 0.5, q2 = 0, q3 = 0.5
model = none
algo = Kozak: minsol = 1000, idopti = nh, minNh = 2, maxiter = 10000,
              maxstep = 100, maxstill = 500, rep = 5, trymany = TRUE
Strata information:
                  type rh
                                       bh
                                                 E(Y)
                                                          Var(Y)
                                                                   Nh
                                                                       nh
                                                                        79 0.02
stratum 1
                                 36703.82
                                            21229.61
             take-some
                       1
                                                        41103797 4346
stratum 2
                                            55039.89
                                                        99472460 1054
                                                                        30 0.03
             take-some
                        1
                                 71986.24
                                                        79086957 1334
                                                                        33 0.02
stratum 3
             take-some
                                106848.40
                                            88032.43
                                151201.78
stratum 4
             take-some
                        1
                                           128117.76
                                                       158852979
                                                                  852
                                                                        30 0.04
             take-some
                                           176507.24
stratum 5
                                210748.83
                                                       257069766
                                                                  730
                                                                        33 0.05
stratum 6
                         1
                                295186.09
                                           251081.23
                                                       612253308
                                                                  416
                                                                        29 0.07
             take-some
                                413551.11
                                            343819.24 1063090418
                                                                          0.09
stratum 7
             take-some
                        1
                                                                  361
                                                                        33
stratum 8
             take-some
                       1
                                614205.40
                                           499757.45 3131901977
                                                                  248
                                                                        39
                                                                          0.16
stratum 9
             take-some 1
                                974662.93
                                           756680.65 8825392705
                                                                  176
                                                                       47 0.27
stratum 10
                       1 |
                             105379553.90 1193526.37 9217654279
                                                                  135
                                                                       37 0.27
             take-some
               certain 1 |
                                         - 5476606.91
                                                                  110 110 1.00
Total
                                                                 9762 500 0.05
Total sample size: 500
Anticipated population mean: 179774.1
Anticipated CV: 0.003779453
Note: CV=RRMSE (Relative Root Mean Squared Error) because takenone=0.
```

2.2 Neyman allocation of units to a stratified sample of size 500.

The Neyman allocation of sample strata followed the procedure shown below. The sample sizes come from the 'nh' vector of the 'Optim\_Config' object returned by the stratification::strata.LH() function. The size of the certainty stratum is appended before performing the sampling procedure.

```
> Ney_Samp_12_merged <- Ney_Samp_12_merged[order(Ney_Samp_12_merged$Stratum),</pre>
```

2.3 Selection of 5 stratified samples using Neyman allocation.

After preparing the population data frame (as shown below), the procedure above was used to select the 5 samples used by the analysis.

```
> #Preparing the data frame################################
options(digits=15)
    min(df[order(df$inventory, decreasing=T)[1:110],]$inventory)
[1] 1372514.035
    #Returns 1372514.035
    df$Stratum <- NA
   df$Stratum[df$`inventory` < 36703.82] <- 1
df$Stratum[(df$`inventory` < 71655.62) & (df$`inventory` >= 36703.82)] <- 2
df$Stratum[(df$`inventory` < 106848.40) & (df$`inventory` >= 71655.62)] <-</pre>
    df$Stratum[(df$`inventory` < 151104.80) & (df$`inventory` >= 106848.40)] <-</pre>
    df$Stratum[(df$`inventory` < 209954.79) & (df$`inventory` >= 151104.80)] <-</pre>
    df$Stratum[(df$`inventory` < 295186.09) & (df$`inventory` >= 209954.79)] <-</pre>
    df$Stratum[(df$`inventory` < 413551.11) & (df$`inventory` >= 295186.09)] <-</pre>
    df$Stratum[(df$`inventory` < 614205.40) & (df$`inventory` >= 413551.11)] <-</pre>
    df$Stratum[(df$\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inven
    df$Stratum[(df$`inventory` < 1372514.04) & (df$`inventory` >= 974662.93)] <</pre>
    df$Stratum[(df$`inventory` < 105379553.91) & (df$`inventory` >= 1372514.04)
    <- 11
    #Check if any NAs in Stratum column
    any(is.na(df$Stratum))
[1] FALSE
   #Assign column for Finite Population Correction
  df$Num <- NA
   df$Num[df$Stratum == 1] <- 4346
   df$Num[df$Stratum == 2] <- 1047
   df$Num[df$Stratum == 3] <- 1341
    df$Num[df$Stratum == 4] <- 851
    df$Num[df$Stratum == 5]
    df$Num[df$Stratum == 6] <- 424
    df$Num[df$Stratum == 7] <-</pre>
```

```
> df$Num[df$Stratum == 8] <- 248
> df$Num[df$Stratum == 9] <- 176
> df$Num[df$Stratum == 10] <- 135
> df$Num[df$Stratum == 11] <- 110</pre>
```

2.4 Estimations of Inventory for each sample: the population mean, the standard error of the mean, the 95% confidence interval for the mean, the population total, the standard error for the total, and the 95% confidence interval for the total.

	Mean_Estimate	Mean_SE	Mean_95%_CI	Includes_True_Mean	Total_Estimate	Total_SE	Total_95%_C
Stratified_Test 1	169756.5	3452.98	[162988.75, 176524.17]	NO	1657162518	33707961	[1591096127.57, 17232
Stratified_Test 2	171029.2	3328.93	[164504.66, 177553.81]	NO	1669587375	32496969	[1605894485.29, 17332
Stratified_Test 3	170941.7	3432.96	[164213.25, 177670.19]	NO	1668733078	33512528	[1603049730.45, 17344
Stratified_Test 4	180661.4	4638.57	[171569.94, 189752.80]	YES	1763616255	45281715	[1674865723.84, 18523
Stratified_Test 5	188972.1	4634.39	[179888.87, 198055.35]	NO	1844745764	45240921	[1756075189.22, 19334
Stratified_No_Lonely_PSU 1	185135.8	4675.96	[175971.11, 194300.55]	YES	1807295958	45646764	[1717829943.82, 18967
Stratified_No_Lonely_PSU 2	179848.5	4643.22	[170747.97, 188949.05]	YES	1755681140	45327086	[1666841683.02, 18445
Stratified_No_Lonely_PSU 3	184075.6	4733.82	[174797.44, 193353.68]	YES	1796945611	46211566	[1706372606.51, 18875
Stratified_No_Lonely_PSU 4	182583.6	5040.98	[172703.45, 192463.72]	YES	1782380940	49210021	[1685931070.09, 18788
Stratified_No_Lonely_PSU 5	170758.0	3455.04	[163986.30, 177529.80]	NO	1666940099	33728064	[1600834307.76. 17330
SRS	314438.5	203292.38	[-84007.23, 712884.27]	YES*	157219259	101646191	[-42003614.45, 35644
Stratified_LH-Optimized 1	173299.0	7965.95	[157686.07, 188912.04]	YES	1691745349	77763647	[1539331402.05, 18441
Stratified_LH-Optimized 2	170343.7	7660.28	[155329.87, 185357.61]	YES	1662895555	74779635	[1516330162.61, 18094
Stratified_LH-Optimized 3	175205.2	7810.02	[159897.81, 190512.53]	YES	1710352871	76241440	[1560922394.72, 18597
Stratified_LH-Optimized 4	174342.7	8034.61	[158595.18, 190090.28]	YES	1701933736	78433884	[1548206147.84, 18556
Stratified LH-Optimized 5	170959.9	7684.90	[155897.78, 186022.04]	YES	1668910633	75020020	[1521874096.22, 18159

A table showing the results of the analysis is shown above. The first 5 rows show the results of a stratified sampling procedure which used a 'lonely PSU' adjustment, allocating a single record to the highest-valued certainty stratum. The second set of 5 rows show the results of a stratified sampling procedure which did not employ a 'lonely PSU' adjustment, allocating two records to the highest-valued certainty stratum. The 11<sup>th</sup> row shows the results of an unstratified simple random sampling (SRS) procedure. Altogether, the first 11 rows represent a performance comparison to the results output by a stratified sampling design that employs the generalized Lavallee-Hidiroglou stratification method for skewed populations, allocating the 110 highest-valued records to the certainty stratum as determined by the optimization procedure. Although this strategy did result in broader confidence intervals and larger values of standard error (incurred by including more of the highly variant higher-valued records in the certainty stratum), it also resulted in a more accurate estimation, successfully including the population mean and total 100% of the time.

Using the generalized Lavallee-Hidiroglou stratification method for 5 sampling procedures, the mean of the estimate of mean, its standard error, as well as the mean of the estimate of total and its standard error are shown below:

```
> #Mean of the Total and Mean Estimates and their Standard Errors (across Sam
ples assuming the Sizes allocated by LH Optimization)
>
> m.est_of_mean <- mean(173299.05, 170343.74, 175205.17, 174342.73, 170959.91)
> m.est_of_mean
[1] 173299.05
> m.est_of_mean_SE <- mean(7965.95, 7660.28, 7810.02, 8034.61, 7684.90)
> m.est_of_mean_SE
[1] 7965.95
> m.est_of_total <- mean(1691745349.49, 1662895554.54, 1710352871.10, 1701933 735.66, 1668910633.11)
> m.est_of_total
[1] 1691745349.49
> m.est_of_total_SE <- mean(77763647.01, 74779635.28, 76241439.93, 78433884.0 0, 75020019.78)
> m.est_of_total_SE
[1] 77763647.01
```

2.5. Estimates of mean and total compared to the true values of mean and total.

When using the 'lonely PSU' adjustment (allocating a single record to the highest-valued certainty stratum), the confidence intervals of the estimations included the true values only 20% of the time.

When not using the 'lonely PSU' adjustment (allocating two records to the highest-valued certainty stratum), the confidence intervals of the estimations included the true values 80% of the time.

When applying optimized stratification using the generalized Lavallee-Hidiroglou method, (allocating 110 records to the highest-valued certainty stratum), the confidence intervals of the estimations included the true values 100% of the time.

2.6 Results of performing the analysis without stratification.

When no stratification procedure was applied, and a simple random sampling (SRS) of the population data was used, the confidence intervals of the estimations failed entirely to include the true values, capturing it 0%\* of the time. More precisely, the true mean was included by a completely uninformative confidence interval, ranging from [-84007.23, 712884.27]—when corrected for nonsensical values, [0, 712884.27]. Despite the similarly enormous confidence interval of the SRS estimate of total ([-42003614.45, 356442133.11], or [0, 356442133.11], it still failed to capture the true value.

## Section 4. Conclusion

Stratification can greatly enhance the precision of one's estimates. Dealing with highly skewed data presents particular challenges when determining the optimal partitioning of strata. Applications of the Lavallee-Hidiroglou method outperformed the geometric method when minimizing the overall coefficient of variation (relative root mean squared error) to obtain the most precise estimates. Wrapping the L-H function in a custom-written optimization function facilitated the process of identifying the most performant

configuration of parameters (including the number of records to include in the certainty stratum, and the number of strata to create). Although including the highest-valued records of this strongly right-skewed data in the certainty stratum resulted in larger standard error and broader confidence intervals than were obtained when limiting the number of these highly variant records to only one or two, it also resulted in better estimations, capturing the true values of mean and total 100% of the time.

## References

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## Appendix. R Code

```
library(readxl)
library(Hmisc)
library(plotrix)
library(ggplot2)
library(stratification)
library(sampling)
library(PracTools)
library(survey)
library(gridExtra)
#read individual sheet to dataframe object
df <- readxl::read_excel('projectData.xlsx',sheet='projectData')</pre>
head(df)
summary(df)
nrow(df)
#Returns: 9762
sum(df$inventory)
#Returns: 1754954823
```

```
mean(df$inventory)
#Returns: 179774.1
sd(df$inventory)
#Returns: 1573358
plotrix::std.error(df$inventory)
#Returns: 15924.22
Hmisc::describe(df)
#Histogram of inventory, excluding values above 100K
ggplot(df,aes(x=inventory)) + geom_histogram(binwidth=1000,aes(fill=..count..)) +
 xlab('Inventory Value') + ylab('Count') + ggtitle('Counts of Inventory Value: Excluding Values > 100K'
 xlim(c(0, 100000)) + ylim(c(0, 450))
#Histogram of inventory, excluding values above 1M
ggplot(df,aes(x=inventory)) + geom_histogram(binwidth=1000,fill='blue',alpha=0.6) +
 xlab('Inventory Value') + ylab('Count') + ggtitle('Counts of Inventory Value: Excluding Values > 1M') -
 xlim(c(0, 1000000)) + ylim(c(0, 450))
#Using highest valued Inventory records as the certainty stratum
# CF. https://enablement.acl.com/helpdocs/analytics/13/user-guide/en-us/Content/da sampling data/class.
#NB: The stratification::strata.LH() function below accepts an index vector as input to the argument spec
cert_vec <- list(top_certainty_vec <- c(which(df$inventory==max(df$inventory))),</pre>
```

```
top20_certainty_vec <- df[order(df$inventory, decreasing=T)[1:20],]$coID,
                                     top50_certainty_vec <- df[order(df$inventory, decreasing=T)[1:50],]$coID,
                                     top80_certainty_vec <- df[order(df$inventory, decreasing=T)[1:80],]$coID,
                                     top90_certainty_vec <- df[order(df$inventory, decreasing=T)[1:90],]$coID,
                                     top100 certainty vec <- df[order(df$inventory, decreasing=T)[1:100],]$coID,
                                     top110_certainty_vec <- df[order(df$inventory, decreasing=T)[1:110],]$coID,</pre>
                                     top120_certainty_vec <- df[order(df$inventory, decreasing=T)[1:120],]$coID,</pre>
                                     top150 certainty vec <- df[order(df$inventory, decreasing=T)[1:150],]$coID,
                                     top200_certainty_vec <- df[order(df$inventory, decreasing=T)[1:200],]$coID)</pre>
#NB: Must define cert vec in global environment before passing to minCV() function below. For common sco
     CF. https://stackoverflow.com/questions/28601959/error-object-not-found-in-nested-functions
#Generalized Lavallee-Hidiroglou Method -- applying Kozak's (2004) Algorithm###################################
# CF. https://www.rdocumentation.org/packages/stratification/versions/2.2-5/topics/strata.LH
#Function Optimizing the number of sampled strata and the best performing certainty stratum from the vec-
#NB:
                 Passing the vector c(0.5, 0, 0.5) to the 'alloc' argument of the stratification::strata.LH() fund
                 Passing 'none' to the 'model' argument assumes that Y=X, i.e. that the variable being stratified
minCV <- function(lo_Ls, hi_Ls, cert_vec){</pre>
    CV.list<-numeric()</pre>
    min.CV <- 999
    min.i <- 99
    min.j <- 99
    for (i in lo_Ls:hi_Ls){
        for (j in 1:length(cert vec)){
             k <- tryCatch(stratification::strata.LH(x=df$\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inven
                                                                 certain=cert_vec[j], model="none", algo="Kozak")$RRMSE,
                                           warning=function(w){
```

top5\_certainty\_vec <- df[order(df\$inventory, decreasing=T)[1:5],]\$coID,
top10\_certainty\_vec <- df[order(df\$inventory, decreasing=T)[1:10],]\$coID,</pre>

```
message("Warning: LH Algo failed. Some sampled strata < mininum Nh")</pre>
                                                                NA})
                 if(is.na(k)){
                       next
                 }
                 cat('Coefficient of Variation (RRMSE): ', k, '\n')
                 cat('Selected Number of Strata: ', i, '\n')
                 cat('Index of Certainty Stratum: ', j, '\n')
                 CV.list <- append(CV.list, k)</pre>
                 cat('All Coefficients of Variation: \n', CV.list, '\n')
                 min_val <- min(CV.list, na.rm=TRUE)</pre>
                 if (min.CV > min val){
                      min.CV <- min_val</pre>
                      min.i <- i
                      min.j <- j
                 }
           }
      }
     result_list <- list('Minimum_CV'=min.CV, 'Best_LS'=min.i, 'Best_CertStratum'=min.j)</pre>
     return(result_list)
}
best_results <- minCV(5, 10, cert_vec)</pre>
best_results$Minimum_CV
best_results$Best_LS
best_results$Best_CertStratum
#Best Stratification Configuration: Lavallee-Hidiroglou (1988) Method and Kozak's (2004) Algorithm######
Optim_Config <- stratification::strata.LH(x=df$\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventory\inventor
                                                                                    certain=cert_vec[9], model='none', algo='Kozak')
```

```
print(Optim_Config)
plot(Optim_Config)
#Performance Comparison: Gunning and Horgan (2004) Geometric Stratification Method
Optim_Geo <- stratification::strata.geo(x=df$\inventory\inventory\inventory\inventor\), n=500, Ls=8, alloc=c(0.5, 0, 0.5),
               certain=cert_vec[9], model="none")
print(Optim_Geo)
plot(Optim_Geo)
#Identify boundary separating highest-valued certainty stratum from other strata
options(digits=15)
min(df[order(df$inventory, decreasing=T)[1:110],]$inventory)
#Returns 1372514.035
#Assign Strata
df$Stratum <- NA
df$Stratum[df$`inventory` < 36703.82] <- 1</pre>
df$Stratum[(df$\inventory\\ < 71655.62) & (df$\inventory\\ \>= 36703.82)] <- 2
```

```
df$Stratum[(df$`inventory` < 106848.40) & (df$`inventory` >= 71655.62)] <- 3</pre>
df$Stratum[(df$\inventory\) < 151104.80) & (df$\inventory\) >= 106848.40)] <- 4</pre>
df$Stratum[(df$`inventory` < 209954.79) & (df$`inventory` >= 151104.80)] <- 5</pre>
df$Stratum[(df$`inventory` < 295186.09) & (df$`inventory` >= 209954.79)] <- 6</pre>
df$Stratum[(df$\inventory\) < 413551.11) & (df$\inventory\) >= 295186.09)] <- 7</pre>
df$Stratum[(df$\inventory\) < 614205.40) & (df$\inventory\) >= 413551.11)] <- 8</pre>
df$Stratum[(df$`inventory` < 974662.93) & (df$`inventory` >= 614205.40)] <- 9
df$Stratum[(df$`inventory` < 1372514.04) & (df$`inventory` >= 974662.93)] <- 10</pre>
df$Stratum[(df$`inventory` < 105379553.91) & (df$`inventory` >= 1372514.04)] <- 11</pre>
#Check if any NAs in Stratum column
any(is.na(df$Stratum))
#Assign column for Finite Population Correction
df$Num <- NA
df$Num[df$Stratum == 1] \leftarrow 4346
df$Num[df$Stratum == 2] <- 1047
df$Num[df$Stratum == 3] \leftarrow 1341
df$Num[df$Stratum == 4] <- 851
df$Num[df$Stratum == 5] <- 723
df$Num[df$Stratum == 6] \leftarrow 424
df$Num[df$Stratum == 7] <- 361
df$Num[df$Stratum == 8] <- 248
df$Num[df$Stratum == 9] <- 176
df$Num[df$Stratum == 10] <- 135</pre>
df$Num[df$Stratum == 11] <- 110</pre>
#Check if any NAs in df
any(is.na(df))
#Specify vector of population stratum sizes, appending certainty stratum
Nh <- append(Optim Config$Nh, 110)
#Specify vector of population stratum standard deviations, appending 1 for certainty stratum
Sh <- append(sqrt(Optim_Config$varh), 1)</pre>
```

#NB: Appending 1 as the certainty stratum standard deviation may result in an underestimation of varian

```
The results of procedures #12-16 accept the stratum sample sizes determined by LH-Optimization,
'certainty' stratum.
#Neyman Allocation to determine strata sizes in sample of size n = 500
PracTools::strAlloc(n.tot=500, Nh=Nh, Sh=Sh, alloc='neyman')
#Returns sample stratum sizes of (100, 38, 43, 39, 41, 39, 43, 50, 60, 47, 0)
#Run the allocation again for a sample of size 499, reserving 1 unit for the certainty stratum
Nh <- Optim Config$Nh
Sh <- sqrt(Optim_Config$varh)</pre>
PracTools::strAlloc(n.tot=499, Nh=Nh, Sh=Sh, alloc='neyman')
#Returns sample stratum sizes of (101, 37, 43, 39, 41, 38, 43, 50, 60, 47)
#Adjusted Neyman Allocation, including certainty stratum
Ney_Alloc <- c(101, 37, 43, 39, 41, 38, 43, 50, 60, 47, 1)
#PASS 1 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- IMPLEMENTING LONELY PSU ADJUSTMENT
#Set Random Sampling Seed
set.seed(222)
#Sampling using Neyman Allocation
Ney_Samp_1 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc, method="srswor")</pre>
```

See results of sampling procedures #1-10 below, which serve as a performance comparison, assigni

```
#Drop duplicated column
Ney_Samp_1 <- Ney_Samp_1[, !duplicated(colnames(Ney_Samp_1))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney Samp 1)[2] <- "coID"</pre>
Ney_Samp_1_merged <- merge(x = df, y = Ney_Samp_1)</pre>
#sort by Stratum
Ney_Samp_1_merged <- Ney_Samp_1_merged[order(Ney_Samp_1_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_1 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_1_merged, fpc = ~Num)</pre>
#Adjust for single-PSU certainty stratum
options(survey.lonely.psu = "certainty")
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_1)
#Returns:
                         mean
                                     SE
         inventory 169756.4553944 3452.97697
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_1))
#Returns:
                         2.5 %
                                    97.5 %
         inventory 162988.744885283 176524.165903571
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_1)
#Returns:
                        total
                                     SE
         inventory 1657162517.56 33707961.22347
```

```
confint(survey::svytotal(~`inventory`, design = mydesign_1))
#Returns:
                       2.5 %
                                     97.5 %
         inventory 1591096127.57013 1723228907.55066
#DOES NOT CONTAIN TRUE VALUE of 1754954822.94687########
#PASS 2 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- IMPLEMENTING LONELY PSU ADJUSTMENT
#Set Random Sampling Seed
set.seed(223)
#Sampling using Neyman Allocation
Ney_Samp_2 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_2 <- Ney_Samp_2[, !duplicated(colnames(Ney_Samp_2))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_2)[2] <- "coID"</pre>
Ney_Samp_2_merged <- merge(x = df, y = Ney_Samp_2)</pre>
#sort by Stratum
Ney_Samp_2_merged <- Ney_Samp_2_merged[order(Ney_Samp_2_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_2 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_2_merged, fpc = ~Num)</pre>
```

#Confidence interval of the estimate of total

```
#Adjust for single-PSU certainty stratum
options(survey.lonely.psu = "certainty")
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_2)
#Returns:
                     mean
                                SE
      inventory 171029.233252 3328.92537
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_2))
                    2.5 %
#Returns:
                                 97.5 %
# inventory 164504.659423391 177553.807080663
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_2)
#Returns:
                    total
      inventory 1669587375.006 32496969.44308
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_2))
#Returns:
                   2.5 %
                                97.5 %
      inventory 1605894485.29115 1733280264.72143
```

#PASS 3 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- IMPLEMENTING LONELY PSU ADJUSTMENT

```
#Set Random Sampling Seed
set.seed(224)
#Sampling using Neyman Allocation
Ney_Samp_3 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_3 <- Ney_Samp_3[, !duplicated(colnames(Ney_Samp_3))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_3)[2] <- "coID"</pre>
Ney_Samp_3_merged <- merge(x = df, y = Ney_Samp_3)</pre>
#sort by Stratum
Ney_Samp_3_merged <- Ney_Samp_3_merged[order(Ney_Samp_3_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_3 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_3_merged, fpc = ~Num)</pre>
#Adjust for single-PSU certainty stratum
options(survey.lonely.psu = "certainty")
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_3)
#Returns:
                                      SE
                        mean
          inventory 170941.7207444 3432.95716
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_3))
#Returns:
                                       97.5 %
                        2.5 %
          inventory 164213.248356339 177670.193132409
```

```
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_3)
#Returns:
                    total
        inventory 1668733077.907 33512527.76587
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_3))
#Returns:
                    2.5 %
                                 97.5 %
       inventory 1603049730.45458 1734416425.35857
#PASS 4 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- IMPLEMENTING LONELY PSU ADJUSTMENT
#Set Random Sampling Seed
set.seed(225)
#Sampling using Neyman Allocation
Ney_Samp_4 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_4 <- Ney_Samp_4[, !duplicated(colnames(Ney_Samp_4))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_4)[2] <- "coID"</pre>
Ney_Samp_4_merged <- merge(x = df, y = Ney_Samp_4)</pre>
```

```
#sort by Stratum
Ney_Samp_4_merged <- Ney_Samp_4_merged[order(Ney_Samp_4_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_4 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_4_merged, fpc = ~Num)</pre>
#Adjust for single-PSU certainty stratum
options(survey.lonely.psu = "certainty")
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_4)
#Returns:
                         mean
                                     SE
         inventory 180661.3660204 4638.56949
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_4))
#Returns:
                        2.5 %
                                        97.5 %
         inventory 171569.936881626 189752.795159095
#CONTAINS TRUE VALUE of 179774.106017914#################
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_4)
#Returns:
                        total
         inventory 1763616255.091 45281715.35415
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_4))
#Returns:
                        2.5 %
                                           97.5 %
         inventory 1674865723.83843 1852366786.34309
```

```
#PASS 5 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- IMPLEMENTING LONELY PSU ADJUSTMENT
#Set Random Sampling Seed
set.seed(226)
#Sampling using Neyman Allocation
Ney_Samp_5 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_5 <- Ney_Samp_5[, !duplicated(colnames(Ney_Samp_5))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_5)[2] <- "coID"</pre>
Ney_Samp_5_merged <- merge(x = df, y = Ney_Samp_5)</pre>
#sort by Stratum
Ney_Samp_5_merged <- Ney_Samp_5_merged[order(Ney_Samp_5_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_5 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_5_merged, fpc = ~Num)</pre>
#Adjust for single-PSU certainty stratum
options(survey.lonely.psu = "certainty")
```

#Neyman stratified mean estimate and SE

#Returns:

survey::svymean(~`inventory`, design = mydesign\_5)

mean

SE

```
inventory 188972.1127207 4634.39056
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_5))
#Returns:
                   2.5 %
                                  97.5 %
# q
       inventory 179888.874126264 198055.351315211
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_5)
#Returns:
                    total
# inventory 1844745764.38 45240920.6795
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_5))
#Returns:
                      2.5 %
                                   97.5 %
  inventory 1756075189.22059 1933416339.53909
```

#DOES NOT CONTAIN TRUE VALUE of 1754954822.94687#########

#PASS 6 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- NO LONELY PSU CERTAINTY STRATUM ADJUSTMEN

#Run the allocation again for a sample of size 498, reserving 2 units for the certainty stratum

```
Nh <- Optim_Config$Nh
Sh <- sqrt(Optim_Config$varh)</pre>
PracTools::strAlloc(n.tot=498, Nh=Nh, Sh=Sh, alloc='neyman')
#returns sample stratum sizes of (101, 37, 43, 39, 41, 38, 42, 50, 60, 47)
#adjusted Neyman Allocation, including certainty stratum
Ney_Alloc_2 <- c(101, 37, 43, 39, 41, 38, 43, 50, 60, 47, 2)
#Set Random Sampling Seed
set.seed(227)
#Sampling using Neyman Allocation
Ney_Samp_6 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_2, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_6 <- Ney_Samp_6[, !duplicated(colnames(Ney_Samp_6))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_6)[2] <- "coID"</pre>
Ney_Samp_6_merged <- merge(x = df, y = Ney_Samp_6)</pre>
#sort by Stratum
Ney_Samp_6_merged <- Ney_Samp_6_merged[order(Ney_Samp_6_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_6 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_6_merged, fpc = ~Num)</pre>
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_6)
#Returns:
                          mean
          inventory 185135.8284971 4675.96438
```

```
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_6))
#Returns:
                    2.5 %
                               97.5 %
# inventory 175971.106721974 194300.550272168
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_6)
                    total
#Returns:
                                  SE
# inventory 1807295957.788 45646764.26414
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_6))
#Returns:
                    2.5 %
       inventory 1717829943.81991 1896761971.7569
```

#PASS 7 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- NO LONELY PSU CERTAINTY STRATUM ADJUSTMEN

#Set Random Sampling Seed
set.seed(228)

#Sampling using Neyman Allocation

```
Ney_Samp_7 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_2, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_7 <- Ney_Samp_7[, !duplicated(colnames(Ney_Samp_7))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_7)[2] <- "coID"</pre>
Ney_Samp_7_merged <- merge(x = df, y = Ney_Samp_7)</pre>
#sort by Stratum
Ney Samp 7 merged <- Ney Samp 7 merged[order(Ney Samp 7 merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_7 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_7_merged, fpc = ~Num)</pre>
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_7)
#Returns:
                          mean
         inventory 179848.508501 4643.21721
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_7))
                          2.5 %
                                            97.5 %
#Returns:
        inventory 170747.969987538 188949.047014456
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_7)
#Returns:
                         total
                                          SE
         inventory 1755681139.987 45327086.45115
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_7))
```

```
inventory 1666841683.01835 1844520596.95512
#PASS 8 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- NO LONELY PSU CERTAINTY STRATUM ADJUSTMEN
#Set Random Sampling Seed
set.seed(229)
#Sampling using Neyman Allocation
Ney_Samp_8 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_2, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_8 <- Ney_Samp_8[, !duplicated(colnames(Ney_Samp_8))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_8)[2] <- "coID"</pre>
Ney_Samp_8_merged <- merge(x = df, y = Ney_Samp_8)</pre>
#sort by Stratum
Ney_Samp_8_merged <- Ney_Samp_8_merged[order(Ney_Samp_8_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_8 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_8_merged, fpc = ~Num)</pre>
```

2.5 %

97.5 %

#Returns:

```
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_8)
#Returns:
                        mean
# inventory 184075.5593905 4733.82151
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_8))
                       2.5 %
                                        97.5 %
#Returns:
        inventory 174797.439716593 193353.679064313
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_8)
#Returns:
                      total
# inventory 1796945610.77 46211565.60562
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_8))
#Returns:
                      2.5 %
                                    97.5 %
        inventory 1706372606.51338 1887518615.02582
```

#PASS 9 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- NO LONELY PSU CERTAINTY STRATUM ADJUSTMEN

```
#Set Random Sampling Seed
set.seed(230)
#Sampling using Neyman Allocation
Ney_Samp_9 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_2, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_9 <- Ney_Samp_9[, !duplicated(colnames(Ney_Samp_9))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney Samp 9)[2] <- "coID"</pre>
Ney_Samp_9_merged <- merge(x = df, y = Ney_Samp_9)</pre>
#sort by Stratum
Ney_Samp_9_merged <- Ney_Samp_9_merged[order(Ney_Samp_9_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_9 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_9_merged, fpc = ~Num)</pre>
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_9)
#Returns:
                           mean
                                          SF
          inventory 182583.5832636 5040.97741
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_9))
#Returns:
                           2.5 %
                                              97.5 %
          inventory 172703.449097735 192463.717429423
#CONTAINS TRUE VALUE of 179774.106017914################
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_9)
                          total
#Returns:
                                             SE
```

```
inventory 1782380939.819 49210021.45333
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_9))
#Returns:
                      2.5 %
                                    97.5 %
        inventory 1685931070.09209 1878830809.54603
#PASS 10 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- NO LONELY PSU CERTAINTY STRATUM ADJUSTMEN
#Set Random Sampling Seed
set.seed(231)
#Sampling using Neyman Allocation
Ney_Samp_10 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_2, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_10 <- Ney_Samp_10[, !duplicated(colnames(Ney_Samp_10))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_10)[2] <- "coID"</pre>
Ney_Samp_10_merged <- merge(x = df, y = Ney_Samp_10)</pre>
#sort by Stratum
Ney_Samp_10_merged <- Ney_Samp_10_merged[order(Ney_Samp_10_merged$Stratum),]</pre>
```

```
#Neyman stratified design object
mydesign_10 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_10_merged, fpc = ~Num)</pre>
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_10)
#Returns:
                         mean
# inventory 170758.0515275 3455.03629
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_10))
#Returns:
                          2.5 %
                                           97.5 %
         inventory 163986.304831325 177529.798223672
#DOES NOT CONTAIN TRUE VALUE of 179774.106017914###########
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_10)
                          total
#Returns:
                                           SE
         inventory 1666940099.011 33728064.2754
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_10))
#Returns:
                          2.5 %
                                         97.5 %
         inventory 1600834307.7634 1733045890.25948
#DOES NOT CONTAIN TRUE VALUE of 1754954822.94687###########
```

#PASS 11: PERFORMANCE COMPARISON with UNSTRATIFIED SIMPLE RANDOM SAMPLING #Set Random Sampling Seed set.seed(1) #SRS of Size 500 srs\_df <- df[sample(nrow(df), 500), ]</pre> #SRS design object mydesign\_srs <- survey::svydesign(id = ~1, data = srs\_df)</pre> #SRS mean estimate and SE survey::svymean(~`inventory`, design = mydesign\_srs) #Returns: mean SE inventory 314438.5186579 203292.38226 #confidence interval of SRS mean estimate confint(survey::svymean(~`inventory`, design = mydesign\_srs)) #Returns: 2.5 % 97.5 % inventory -84007.2288961298 712884.266211934 #HUGE UNINFORMATIVE CONFIDENCE INTERVAL CONTAINS TRUE VALUE of 179774.106017914### #SRS estimate of total and SE survey::svytotal(~`inventory`, design = mydesign\_srs) #Returns: total SE

# inventory 157219259.329 101646191.1282

```
#Confidence interval of SRS estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_srs))
                                97.5 %
#Returns:
                     2.5 %
# inventory -42003614.4480649 356442133.105967
#HUGE UNINFORMATIVE CONFIDENCE INTERVAL STILL DOES NOT CONTAIN TRUE VALUE of 1754954822.94687###
#PASS 12 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- ASSUMING SAMPLE STRATUM SIZES ASSIGNED B'
#adjusted Neyman Allocation, assuming values provided by the LH optimization
Ney_Alloc_3 <- append(Optim_Config$nh, 110)</pre>
#Set Random Sampling Seed
set.seed(232)
#Sampling using Neyman Allocation
Ney_Samp_12 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_3, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_12 <- Ney_Samp_12[, !duplicated(colnames(Ney_Samp_12))]</pre>
```

```
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_12)[2] <- "coID"</pre>
Ney_Samp_12_merged <- merge(x = df, y = Ney_Samp_12)
#sort by Stratum
Ney_Samp_12_merged <- Ney_Samp_12_merged[order(Ney_Samp_12_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_12 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_12_merged, fpc = ~Num)</pre>
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_12)
#Returns:
                          mean
         inventory 173299.0523965 7965.95442
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_12))
#Returns:
                          2.5 %
                                           97.5 %
         inventory 157686.068638111 188912.036154827
#CONTAINS TRUE VALUE of 179774.106017914#################
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_12)
#Returns:
                          total
         inventory 1691745349.494 77763647.01153
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_12))
#Returns:
                          2.5 %
                                            97.5 %
         inventory 1539331402.04524 1844159296.94342
```

```
#adjusted Neyman Allocation, assuming values provided by the LH optimization
Ney_Alloc_3 <- append(Optim_Config$nh, 110)</pre>
#Set Random Sampling Seed
set.seed(233)
#Sampling using Neyman Allocation
Ney_Samp_13 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_3, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_13 <- Ney_Samp_13[, !duplicated(colnames(Ney_Samp_13))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_13)[2] <- "coID"</pre>
Ney_Samp_13_merged <- merge(x = df, y = Ney_Samp_13)
#sort by Stratum
Ney_Samp_13_merged <- Ney_Samp_13_merged[order(Ney_Samp_13_merged$Stratum),]</pre>
#Neyman stratified design object
```

mydesign\_13 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney\_Samp\_13\_merged, fpc = ~Num)

#PASS 13 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- ASSUMING SAMPLE STRATUM SIZES ASSIGNED B'

```
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_13)
#Returns:
                         mean
# inventory 170343.7363795 7660.27815
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_13))
#Returns:
                        2.5 %
                                          97.5 %
  inventory 155329.867097901 185357.605661186
#CONTAINS TRUE VALUE of 179774.106017914################
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_13)
#Returns:
                       total
# inventory 1662895554.537 74779635.28079
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_13))
#Returns:
                       2.5 %
                                         97.5 %
        inventory 1516330162.60971 1809460946.4645
```

#PASS 14 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- ASSUMING SAMPLE STRATUM SIZES ASSIGNED B'

```
#adjusted Neyman Allocation, assuming values provided by the LH optimization
Ney_Alloc_3 <- append(Optim_Config$nh, 110)</pre>
#Set Random Sampling Seed
set.seed(234)
#Sampling using Neyman Allocation
Ney_Samp_14 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_3, method="srswor")</pre>
#Drop duplicated column
Ney_Samp_14 <- Ney_Samp_14[, !duplicated(colnames(Ney_Samp_14))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_14)[2] <- "coID"</pre>
Ney_Samp_14_merged <- merge(x = df, y = Ney_Samp_14)</pre>
#sort by Stratum
Ney_Samp_14_merged <- Ney_Samp_14_merged[order(Ney_Samp_14_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign 14 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_14_merged, fpc = ~Num)</pre>
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_14)
#Returns:
                          mean
                                          SE
          inventory 175205.17016 7810.02253
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_14))
#Returns:
                          2.5 %
                                             97.5 %
          inventory 159897.807284972 190512.533034961
```

```
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_14)
#Returns:
                   total
       inventory 1710352871.102 76241439.92664
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_14))
#Returns:
                     2.5 %
                                   97.5 %
# inventory 1560922394.7159 1859783347.48729
#PASS 15 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- ASSUMING SAMPLE STRATUM SIZES ASSIGNED B'
#adjusted Neyman Allocation, assuming values provided by the LH optimization
Ney_Alloc_3 <- append(Optim_Config$nh, 110)</pre>
#Set Random Sampling Seed
set.seed(235)
#Sampling using Neyman Allocation
Ney_Samp_15 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_3, method="srswor")</pre>
```

```
#Drop duplicated column
Ney_Samp_15 <- Ney_Samp_15[, !duplicated(colnames(Ney_Samp_15))]</pre>
#Rename ID column to match original data frame, for merging
colnames(Ney Samp 15)[2] <- "coID"</pre>
Ney_Samp_15_merged <- merge(x = df, y = Ney_Samp_15)</pre>
#sort by Stratum
Ney_Samp_15_merged <- Ney_Samp_15_merged[order(Ney_Samp_15_merged$Stratum),]</pre>
#Neyman stratified design object
mydesign_15 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_15_merged, fpc = ~Num)
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_15)
#Returns:
                        mean
                                       SF
         inventory 174342.7305529 8034.61217
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_15))
#Returns:
                         2.5 %
                                          97.5 %
         inventory 158595.180070016 190090.281035698
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_15)
#Returns:
                        total
        inventory 1701933735.657 78433884.00301
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_15))
#Returns:
                         2.5 %
                                           97.5 %
         inventory 1548206147.8435 1855661323.47048
```

```
#PASS 16 OF STRATIFIED SAMPLING ESTIMATION of MEAN and TOTAL -- ASSUMING SAMPLE STRATUM SIZES ASSIGNED B'
```

```
#adjusted Neyman Allocation, assuming values provided by the LH optimization
Ney_Alloc_3 <- append(Optim_Config$nh, 110)

#Set Random Sampling Seed
set.seed(236)

#Sampling using Neyman Allocation
Ney_Samp_16 <- sampling::strata(df, stratanames='Stratum', size=Ney_Alloc_3, method="srswor")

#Drop duplicated column
Ney_Samp_16 <- Ney_Samp_16[, !duplicated(colnames(Ney_Samp_16))]

#Rename ID column to match original data frame, for merging
colnames(Ney_Samp_16)[2] <- "coID"
Ney_Samp_16_merged <- merge(x = df, y = Ney_Samp_16)

#sort by Stratum
Ney_Samp_16_merged <- Ney_Samp_16_merged[order(Ney_Samp_16_merged$Stratum),]</pre>
```

```
#Neyman stratified design object
mydesign_16 <- survey::svydesign(id = ~1, strata = ~Stratum, data = Ney_Samp_16_merged, fpc = ~Num)
#Neyman stratified mean estimate and SE
survey::svymean(~`inventory`, design = mydesign_16)
#Returns:
                      mean
       inventory 170959.9091492 7684.90266
#Confidence interval of the mean estimate
confint(survey::svymean(~`inventory`, design = mydesign_16))
#Returns:
                      2.5 %
                                    97.5 %
# inventory 155897.77670773 186022.04159064
#Neyman stratified estimate of total and SE
survey::svytotal(~`inventory`, design = mydesign_16)
#Returns:
                      total
       inventory 1668910633.114 75020019.78265
#Confidence interval of the estimate of total
confint(survey::svytotal(~`inventory`, design = mydesign_16))
                     2.5 %
#Returns:
                                      97.5 %
# inventory 1521874096.22086 1815947170.00782
```

```
#Mean of the Total and Mean Estimates and their Standard Errors (across Samples assuming the Sizes allocations)
m.est of mean <- mean(173299.05, 170343.74, 175205.17, 174342.73, 170959.91)
#Returns: 173299.05
m.est of mean SE <- mean(7965.95, 7660.28, 7810.02, 8034.61, 7684.90)
#Returns: 7965.95
m.est_of_total <- mean(1691745349.49, 1662895554.54, 1710352871.10, 1701933735.66, 1668910633.11)
#Returns: 1691745349.49
m.est_of_total_SE <- mean(77763647.01, 74779635.28, 76241439.93, 78433884.00, 75020019.78)
#Returns: 77763647.01
val_df <- setNames(data.frame(matrix(ncol = 8, nrow = 16)),</pre>
              c('Mean Estimate','Mean SE','Mean 95% CI','Includes True Mean','Total Estimate','Total
rownames(val_df) <- c(paste('Stratified_Test',1:5), paste('Stratified_No_Lonely_PSU',1:5), 'SRS', paste(
val_df[,1] <- c(169756.46, 171029.23, 170941.72, 180661.37, 188972.11,</pre>
            185135.83, 179848.51, 184075.56, 182583.58, 170758.05,
```

```
314438.52,
                173299.05, 170343.74, 175205.17, 174342.73, 170959.91)
val_df[,2] <- c(3452.98, 3328.93, 3432.96, 4638.57, 4634.39,</pre>
                4675.96, 4643.22, 4733.82, 5040.98, 3455.04,
                203292.38,
                7965.95, 7660.28, 7810.02, 8034.61, 7684.90)
val_df[,3] <- c('[162988.75, 176524.17]','[164504.66, 177553.81]','[164213.25, 177670.19]','[171569.94,
                '[175971.11, 194300.55]','[170747.97, 188949.05]','[174797.44, 193353.68]','[172703.45,
                '[-84007.23, 712884.27]',
                '[157686.07, 188912.04]','[155329.87, 185357.61]','[159897.81, 190512.53]','[158595.18,
val_df[,4] <- c('NO','NO','NO','YES','NO',</pre>
                'YES', 'YES', 'YES', 'NO',
                'YES', 'YES', 'YES', 'YES')
val_df[,5] <- c(1657162517.56, 1669587375.01, 1668733077.91, 1763616255.09, 1844745764.38,
                1807295957.79, 1755681139.99, 1796945610.77, 1782380939.82, 1666940099.01,
               157219259.33,
                1691745349.49, 1662895554.54, 1710352871.10, 1701933735.66, 1668910633.11)
val df[,6] <- c(33707961.22, 32496969.44, 33512527.77, 45281715.35, 45240920.68,
                45646764.26, 45327086.45, 46211565.61, 49210021.45, 33728064.28,
                101646191.13,
                77763647.01, 74779635.28, 76241439.93, 78433884.00, 75020019.78)
val_df[,7] <- c('[1591096127.57, 1723228907.55]','[1605894485.29, 1733280264.72]','[1603049730.45, 17344
1852366786.34]','[1756075189.22, 1933416339.54]',
                [1717829943.82, 1896761971.76]','[1666841683.02, 1844520596.96]','[1706372606.51, 18875
1878830809.55]','[1600834307.76. 1733045890.26]',
                '[-42003614.45, 356442133.11]',
                '[1539331402.05, 1844159296.94]','[1516330162.61, 1809460946.46]','[1560922394.72, 18597
1855661323.47]','[1521874096.22, 1815947170.01]')
```

```
val_df[,8] <- c('NO','NO','NO','YES','NO',</pre>
                 'YES', 'YES', 'YES', 'NO',
                 'NO',
                 'YES', 'YES', 'YES', 'YES')
#Create grid of results values
val_tbl <- tableGrob(val_df)</pre>
#Helper function to find cells in grid
find_cell <- function(table, row, col, name="core-fg"){</pre>
 1 <- table$layout</pre>
 which(1$t==row & 1$1==col & 1$name==name)
}
#Coloring 'YES' cells resulting from the LH Optimized Stratification Method
ind <- find_cell(val_tbl, 13, 5, "core-bg")</pre>
val_tbl$grobs[ind][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind2 <- find_cell(val_tbl, 14, 5, "core-bg")</pre>
val_tbl$grobs[ind2][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind3 <- find_cell(val_tbl, 15, 5, "core-bg")</pre>
val_tbl$grobs[ind3][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind4 <- find_cell(val_tbl, 16, 5, "core-bg")</pre>
val_tbl$grobs[ind4][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind5 <- find_cell(val_tbl, 17, 5, "core-bg")</pre>
val_tbl$grobs[ind5][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind6 <- find_cell(val_tbl, 13, 9, "core-bg")</pre>
```

```
val_tbl$grobs[ind6][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind7 <- find_cell(val_tbl, 14, 9, "core-bg")</pre>
val_tbl$grobs[ind7][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind8 <- find_cell(val_tbl, 15, 9, "core-bg")</pre>
val_tbl$grobs[ind8][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind9 <- find_cell(val_tbl, 16, 9, "core-bg")</pre>
val_tbl$grobs[ind9][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
ind10 <- find_cell(val_tbl, 17, 9, "core-bg")</pre>
val_tbl$grobs[ind10][[1]][["gp"]] <- gpar(fill="darkolivegreen1", col = "darkolivegreen4", lwd=5)</pre>
#Coloring 'NO' cells resulting from the SRS method and from strafication methods allocating 1 or 2 record
ind11 <- find_cell(val_tbl, 2, 5, "core-bg")</pre>
val_tbl$grobs[ind11][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind12 <- find_cell(val_tbl, 3, 5, "core-bg")</pre>
val_tbl$grobs[ind12][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind13 <- find_cell(val_tbl, 4, 5, "core-bg")</pre>
val_tbl$grobs[ind13][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind14 <- find_cell(val_tbl, 6, 5, "core-bg")</pre>
val_tbl$grobs[ind14][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind15 <- find_cell(val_tbl, 11, 5, "core-bg")</pre>
val_tbl$grobs[ind15][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
```

```
ind16 <- find_cell(val_tbl, 2, 9, "core-bg")</pre>
val_tbl$grobs[ind16][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind17 <- find_cell(val_tbl, 3, 9, "core-bg")</pre>
val_tbl$grobs[ind17][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind18 <- find_cell(val_tbl, 4, 9, "core-bg")</pre>
val_tbl$grobs[ind18][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind19 <- find_cell(val_tbl, 6, 9, "core-bg")</pre>
val_tbl$grobs[ind19][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind20 <- find_cell(val_tbl, 11, 9, "core-bg")</pre>
val_tbl$grobs[ind20][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
ind21 <- find_cell(val_tbl, 12, 9, "core-bg")</pre>
val_tbl$grobs[ind21][[1]][["gp"]] <- gpar(fill="coral1", col = "coral4", lwd=5)</pre>
#Coloring 'YES' cells resulting from strafication methods allocating 1 or 2 records to the upper certain
ind22 <- find_cell(val_tbl, 5, 5, "core-bg")</pre>
val_tbl$grobs[ind22][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind23 <- find_cell(val_tbl, 7, 5, "core-bg")</pre>
val_tbl$grobs[ind23][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind24 <- find_cell(val_tbl, 8, 5, "core-bg")</pre>
val_tbl$grobs[ind24][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind25 <- find_cell(val_tbl, 9, 5, "core-bg")</pre>
val_tbl$grobs[ind25][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
```

```
ind26 <- find_cell(val_tbl, 10, 5, "core-bg")</pre>
val_tbl$grobs[ind26][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind27 <- find_cell(val_tbl, 5, 9, "core-bg")</pre>
val_tbl$grobs[ind27][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind28 <- find_cell(val_tbl, 7, 9, "core-bg")</pre>
val_tbl$grobs[ind28][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind29 <- find_cell(val_tbl, 8, 9, "core-bg")</pre>
val_tbl$grobs[ind29][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind30 <- find_cell(val_tbl, 9, 9, "core-bg")</pre>
val_tbl$grobs[ind30][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
ind31 <- find_cell(val_tbl, 10, 9, "core-bg")</pre>
val_tbl$grobs[ind31][[1]][["gp"]] <- gpar(fill="azure1", col = "azure4", lwd=5)</pre>
#Coloring the 'YES' cell resulting from the uninformative SRS method
ind32 <- find_cell(val_tbl, 12, 5, "core-bg")</pre>
val_tbl$grobs[ind32][[1]][["gp"]] <- gpar(fill="darkgrey", col = "black", lwd=5)</pre>
grid.draw(val_tbl)
#Create grid without coloring cells
#grid.arrange(val_tbl)
```