

Math 115E Activity 16

Chapter 5
Factoring Quadratics Part 2

How to factor quadratic equations

Quadratic factoring when $a = 1$:

When factoring, the form $x^2 + bx + c$ can be factored as $(x + m)(x + n)$

Start with real numbers m and n so: they both multiply to c and both add to b . There is not a value in front of either x

Quadratic factoring when $a \neq 1$:

When factoring, the form $ax^2 + bx + c$ can be factored as $(px + m)(qx + n)$

Start with two real numbers such that: multiply to $a \cdot c$ and yet add to b then we re-group the terms and factor

Example: We want to solve $3x^2 - 11x + 10 = 0$ by factoring

Step 1: Find the factors of $3 * 10 = 30$ that add up to -11 , (Write the factors if needed)

Step 2: The factors of 30 are: $\pm(1, 30), \pm(2, 15), \pm(3, 10), \pm(5, 6)$,
so the pair that adds to -11 is -5 and -6

Step 3: Rewrite the quadratic:

$$3x^2 + (-6x - 5x) + 10 = 0$$

Step 4: Regroup so that each group has a common factor: $(3x^2 - 6x) + (-5x + 10) = 0$

Step 5: Factor out a common term:

$$(3x)(x - 2) - 5(x - 2) = 0$$

Step 6: Factor again with the $x - 2$ term:

$$(3x - 5)(x - 2) = 0$$

Step 7: Solve for x , so we get $3x - 5 = 0$ and $x - 2 = 0$, giving us $x = \frac{5}{3}$ and $x = 2$

DONE: So starting with $3x^2 - 11x + 10 = 0$, we get $(3x - 5)(x - 2) = 0$

NOTE: If we aren't able to factor out a common term or we don't get the same expression in both parentheses in Step 5, then go back to Step 3 and swap the factor pair.

Factor the following quadratic equations

#1 $x^2 + 9x + 14 = 0$

#7 $9x^2 - 27x + 18 = 0$

#2 $x^2 - 8x + 7 = 0$

#8 $4x^2 - 13x + 10 = 0$

#3 $x^2 + x - 30 = 0$

#9 $2x^2 - 13x - 7 = 0$

#4 $3x^2 + 10x + 8 = 0$

#10 $4x^2 + 20x + 25 = 0$

#5 $2x^2 - 9x + 10 = 0$

#11 $3x^2 - 19x + 20 = 0$

#6 $2x^2 - 6x - 20 = 0$

#12 $8x^2 - 6x - 9 = 0$

How to use the Quadratic Formula

The Quadratic Formula:

If we are given any polynomial, which may not be factorable, in the form $ax^2 + bx + c = 0$

We can solve this by using the quadratic formula $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

We will either get 0, 1 or 2 solutions for the x-values

Example: We want to solve $3x^2 - 11x + 10 = 0$ by using the Quadratic Formula

Step 1: Identify the given coefficients: $a = 3, b = -11, c = 10$

Step 2: Plug these into the formula: $x = \frac{-(-11) \pm \sqrt{(-11)^2 - 4(3)(10)}}{2(3)}$

Step 3: Simplify as much as we can $x = \frac{-11 \pm \sqrt{121 - 120}}{6} \rightarrow x = \frac{11 \pm 1}{6}$

Step 4: Obtain the solutions: $x = \frac{11 \pm 1}{6}$, so $x_1 = \frac{11 + 1}{6} = \frac{12}{6} = 2$ and $x_2 = \frac{11 - 1}{6} = \frac{10}{6} = \frac{5}{3}$

DONE: So starting with $3x^2 - 11x + 10 = 0$, we get $x = \frac{5}{3}$ and $x = 2$, which is the same as before!

Solve the following quadratic equations

$$\#1 \quad x^2 + 9x + 14 = 0$$

$$\#7 \quad 4x^2 - 13x + 10 = 0$$

$$\#2 \quad x^2 + 4x + 2 = 0$$

$$\#8 \quad 4x^2 + 20x + 25 = 0$$

$$\#3 \quad x^2 + 2x - 1 = 0$$

$$\#9 \quad 10x^2 + 10x - 10 = 0$$

$$\#4 \quad x^2 + x - 30 = 0$$

$$\#10 \quad 8x^2 - 6x - 9 = 0$$

$$\#5 \quad 2x^2 - 6x + 3 = 0$$

$$\#11 \quad 4x^2 - 12x + 3 = 0$$

$$\#6 \quad 2x^2 - 9x + 10 = 0$$

$$\#12 \quad 2x^2 + 5x - 4 = 0$$