Your Name: October 28th 2025

Math 115E Activity 15

Chapter 5 Factoring Quadratics Part 2

How to factor quadratic equations

Quadratic factoring when a = 1:

When factoring, the form $x^2 + bx + c$ can be factored as (x + m)(x + n)Start with real numbers m and n so: they both multiply to c and both add to bThere is not a value in front of either x

Quadratic factoring when $a \neq 1$:

When factoring, the form $\mathbf{a}x^2 + bx + c$ can be factored as (px + m)(qx + n)Start with two real numbers such that: multiply to $\mathbf{a} \cdot c$ and yet add to b then we re-group the terms and factor

Example: We want to solve $3x^2 - 11x + 10$ by factoring

Step 1: Find the factors of 3 * 10 = 30 that add up to -11, (Write the factors if needed)

Step 2: The factors of 30 are: $\pm (1,30), \pm (2,15), \pm (3,10), \pm (5,6),$ so the pair that adds to -11 is -5 and -6

Step 3: Rewrite the quadratic:

$$3x^2 + (-6x - 5x) + 10 = 0$$

Step 4: Regroup so that each group has a common factor: $(3x^2 - 6x) + (-5x + 10) = 0$

Step 5: Factor out a common term:

$$(3x)(x-2) - 5(x-2) = 0$$

Step 6: Factor again with the x-2 term:

$$(3x - 5)(x - 2) = 0$$

Step 7: Solve for x, so we get 3x - 5 = 0 and x - 2 = 0, giving us $x = \frac{5}{2}$ and x = 2

DONE: So starting with $3x^2 - 11x + 10 = 0$, we get (3x - 5)(x - 2) = 0

NOTE: If we aren't able to factor out a common term or we dont get the same expression in both parentheses in Step 5, then go back to Step 3 and swap the factor pair.

Factor the following quadratic equations

$$#1 x^2 + 9x + 14 = 0$$

$$\#79x^2 - 27x + 18 = 0$$

$$\#2 \ x^2 - 8x + 7 = 0$$

$$\#8 \ 4x^2 - 13x + 10 = 0$$

$$\#3 \ x^2 + x - 30 = 0$$

$$\#9 \ 2x^2 - 13x - 7 = 0$$

$$\#4 \ 3x^2 + 10x + 8 = 0$$

$$\#10\ 4x^2 + 20x + 25 = 0$$

$$#5 \ 2x^2 - 9x + 10 = 0$$

$$\#11 \ 3x^2 - 19x + 20 = 0$$

$$\#6 \ 2x^2 - 6x - 20 = 0$$

$$\#12\ 8x^2 - 6x - 9 = 0$$

How to use the Quadratic Formula

The Quadratic Formula:

If we are given any polynomial, which may not be factorable, in the form $ax^2 + bx + c = 0$

We can solve this by using the quadratic formula $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

We will either get 0,1 or 2 solutions for the x-values

Example: We want to solve $3x^2 - 11x + 10$ by using the Quadratic Formula

Step 1: Identify the given coefficients: a = 3, b = -11, c = 10

Step 2: Plug these into the formula: $x = \frac{-(-11)\pm\sqrt{(-11)^2-4(3)(10)}}{2(3)}$

Step 3: Simplify as much as we can $x = \frac{-11 \pm \sqrt{121 - 120}}{6} \longrightarrow x = \frac{11 \pm 1}{6}$

Step 4: Obtain the solutions: $x = \frac{11 \pm 1}{6}$, so $x_1 = \frac{11 + 1}{6} = \frac{12}{6} = 2$ and $x_2 = \frac{11 - 1}{6} = \frac{10}{6} = \frac{5}{3}$

DONE: So starting with $3x^2 - 11x + 10 = 0$, we get $x = \frac{5}{3}$ and x = 2, which is the same as before!

Solve the following quadratic equations

$$\#1 \ x^2 + 9x + 14 = 0$$

$$\#7 \ 4x^2 - 13x + 10 = 0$$

$$\#2 \ x^2 + 4x + 2 = 0$$

$$\#8 \ 4x^2 + 20x + 25 = 0$$

$$\#3 \ x^2 + 2x - 1 = 0$$

$$#9 \ 10x^2 + 10x - 10 = 0$$

$$\#4 \ x^2 + x - 30 = 0$$

$$#10 8x^2 - 6x - 9 = 0$$

$$\#5 \ 2x^2 - 6x + 3 = 0$$

$$\#11 \ 4x^2 - 12x + 3 = 0$$

#6
$$2x^2 - 9x + 10 = 0$$

$$\#12\ 2x^2 + 5x - 4 = 0$$