

Hierarchical Force and Positioning Task Specification for Indirect Force Controlled Robots

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Abstract—Indirect force control (IFC) architectures are a common approach for dealing with unknown environments. What all IFC schemes have in common is that the relation between the set point and the actual configuration of the robot is determined by a mechanical relationship (e.g., a mass–spring–damper system). In this paper, we propose a set-point generation method for IFC schemes, enabling intuitive specification of mixed force and positioning tasks on joint and Cartesian levels. In addition, the formulation of equality and inequality tasks is supported and a passivity-based stability proof is formulated using the concept of virtual energy storage. The resulting task programming interface is demonstrated on a 7-degree-of-freedom robot, running a joint space impedance controller. One sample task demonstrates the application of the developed approach and highlights the basic features.

Index Terms—Compliant robots, robot control, robot programming.

I. MOTIVATION

Compliant control involving force and positioning tasks has been investigated elaborately in the last decades. A popular approach to realize compliance is provided by indirect force controllers, where the motion and interaction forces of the physical robot are indirectly controlled by moving a virtual robot, which is coupled to the physical robot via a virtual mechanical relationship. Fig. 1 depicts the basic idea. The most popular variation of **an indirect force control** (IFC) is the well-known impedance control paradigm, introduced by Hogan in his seminal paper [1], but also simpler variants, like stiffness control or an ordinary proportional-derivative controller with compensation of the gravitational torques and sufficiently low proportional gain. This control scheme also has nice stability properties that are basically independent from the environmental dynamics. Furthermore, series elastic actuator (SEA) robots, which are equipped with physical springs in their joints, can also be considered as IFC's.

The set-point selection for the virtual robot is also referred to as **virtual trajectory generation** and while there is an extensive amount of work, having the purpose of improving the accuracy of the virtual mechanical relationship or proposing different extensions or variations for IFC's (for impedance control in particular), the literature covering pure virtual trajectory generation is very sparse.

This paper is meant to fill the gap between the low-level control design and high-level application programming by introducing an ad-

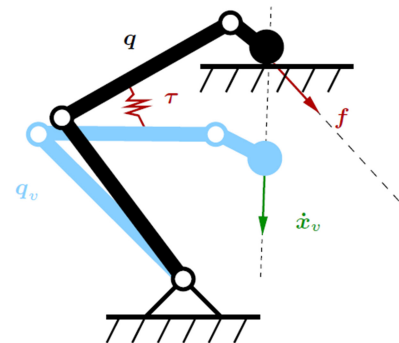


Fig. 1. Motion and interaction forces of the physical manipulator (black) are controlled indirectly by generating set points for the virtual manipulator (blue). For joint space compliance, the direction of applied forces is, in general, not aligned with the Cartesian position deviation.

ditional control layer, which we call set-point generator (SPG). The purpose of the SPG is to provide set points for the virtual manipulator according to the specified tasks, using only information on the current joint state. These tasks are defined by the application programmer via a task specification interface, where a set of hierarchically ordered force and positioning subtasks on joint and Cartesian level is determined. To our best knowledge, there is no work treating virtual set-point generation for joint level IFC's in order to achieve mixed force and positioning tasks without additional sensory feedback, like force or vision.

In [2], we proposed an approach to compose mixed force and positioning interaction tasks for a robotic manipulator under joint space IFC using recursive null-space mapping. In [3], we extended the formalism to support inequality tasks by applying a sequence of quadratic programs (QP). In this paper, we offer a more general formulation with a formal stability proof and additional experimental validation.

The remainder of this paper is structured as follows. Section II provides an overview on the fundamental ideas and approaches on which our work is based and summarizes the main contributions. In Section III, a simplified method of realizing force and positioning tasks for indirect force controlled robots is introduced, which is used in Section IV to implement a hierarchically structured set of equality and inequality tasks. A passivity-based stability proof can be found in Section V. The experimental results are presented in Section VI, and Section VII concludes the paper.

II. STATE OF THE ART AND CONTRIBUTION

A. Indirect Force Control

The major contributions regarding IFC have the intention to improve the performance of the controller itself or to introduce different variants and extensions [4]–[6]. Several investigations have also been made targeting the construction of compliances optimized for specific tasks [7], [8].

Considering applications, conventional trajectory planning approaches are often applied, and the IFC is used to compensate for

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This paper has supplementary downloadable material available at <http://ieeexplore.ieee.org>, provided by the author. This material consists of a video that shows some exemplary applications using the proposed task specification formalism, implemented on a Kuka LBR-IV lightweight arm. The general potential of the framework is shown by implementing various joint and Cartesian tasks, including force and positioning components.

Color versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

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contact uncertainty and unexpected collisions, e.g., [9]–[11]. In these works, the occurring interaction forces are not considered explicitly. The only works explicitly dealing with virtual trajectory generation aim at pure force tracking or are part of a customized approach to a specific problem. In [12]–[16] and [17], force tracking in impedance control for industrial applications is treated, considering a Cartesian impedance controller. The focus of these works lies on setting proper virtual trajectories to adapt to the unknown environmental stiffness.

B. Task Specification

The first concept of assembling a mixed force and positioning main task from different subtasks was derived in conjunction with the task frame formalism [18] and further developed in [19]–[21]. A force or positioning subtask is assigned to every direction of the specified task frame, and a hybrid force/position controller is used to track the desired trajectories or set points simultaneously. Tasks are denoted as artificial constraints. A survey on such constraint-based task specification formalisms can be looked up in [22]. As the hybrid force position control scheme is used as the underlying low-level control, the task geometry has to be known in advance or estimated online as in [23] and [24].

C. Multitask Programming With Inequality Constraints 不等式约束

Due to computational limitations, only equality tasks are considered in the classical approaches for redundancy resolution. There exists a vast number of resolving joint level inequality constraints, e.g., [25] and [26], or handling specific inequality constraints, like collision/singularity avoidance, which has been treated in the past via the gradient projection method [27]. Flacco *et al.* introduced an algorithm to incorporate joint angle, velocity, and acceleration limits and exploit them as well as possible to achieve a Cartesian task by scaling it appropriately [28]. A unified approach is presented in [29], where general inequality tasks are treated on every priority level in a stack-of-tasks framework. In recent contributions, QP methods are used to find an optimal solution for the inverse kinematic problem with a given task hierarchy [30], [31]. The QP formulation is also exploited on the dynamics level to resolve the hyperredundancy of humanoid robots (e.g., [32] and [33]). To our best knowledge, there is no application in the context of set-point generation for IFC.

D. Contribution

The goal of this paper is to derive a task programming scheme for a general joint level IFC setup. The intention is not to present another IFC variation or force controller, instead an additional control layer between the IFC and the task level is introduced, which generates the appropriate set points for an IFC, depending on the specified tasks. In this paper, a simple underlying IFC scheme is assumed, which emulates a spring–damper system while canceling the torques due to gravity τ_g , realizing the relation

$$\tau = K(q_v - q) - D\dot{q} + \tau_g \quad (1)$$

between the robot torques τ and the deviation of virtual and actual joint configuration (q_v and q , respectively). K and D are constant, diagonal, positive-definite matrices parameterizing the virtual spring and damper in each joint. Nevertheless, more robust or advanced IFC schemes can be used with this approach.

This additional layer brings the following advantages.

- 1) Force and positioning equality and inequality tasks on joint and Cartesian level are captured with one unifying formalism. 一个统一形式
- 2) Intuitive, yet powerful task programming without requiring detailed information of the underlying structure, while the inherent compliance of the IFC is preserved. 保存 维持

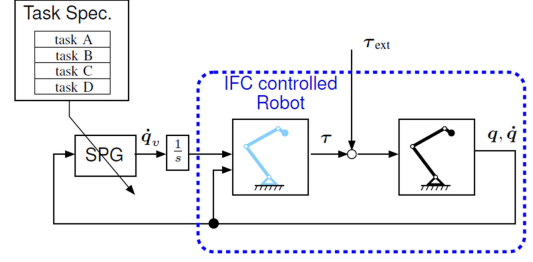


Fig. 2. Overview of the full IFC system. The IFC–robot block (blue-dashed box) is considered a black box, which returns the robot state and takes set-point commands for the virtual robot as input. These set points are transformed to torque commands, usually depending on a virtual mechanical relationship between the virtual and the physical robot. The set points are provided by the SPG, depending on the specified subtasks in the task specification block and the robot state. The external torques τ_{ext} are due to contact with the environment or humans.

- 3) By treating the IFC–robot entity as a general abstraction layer (see Fig. 2) and assuming no additional sensor information, the developed approach is basically hardware independent as long as the robot features an IFC interface, including SEA robots.
- 4) As neither modification nor detailed information of the underlying IFC is required, the proposed formalism is a suitable approach for dealing with so-called closed architectures, where only limited access (i.e., an IFC interface) to the robot is granted.

III. GENERALIZED FORCE AND POSITION REGULATION IN IFC CONTEXT

A. Robotic Foundations

The configuration of a manipulator with n degrees of freedom is uniquely defined by a set of n generalized coordinates q that are for revolute joints usually the joint angles. The Cartesian pose x of any desired frame attached to the robot can be computed from q by applying the forward kinematics map 关节角

$$x = \begin{pmatrix} p \\ o \end{pmatrix} \quad (2)$$

where $p \in \mathbb{R}^3$ denotes the position and o the orientation of the frame. The unit and dimension of o depend on the chosen orientation representation.

To control the motion of the robot in a reactive way, the derivative of (2)

$$\dot{x} = \begin{pmatrix} \dot{p} \\ \omega \end{pmatrix} = \frac{\partial x(q)}{\partial q} \dot{q} = J(q) \dot{q} \quad (3)$$

with ω as the angular velocity of the end-effector frame and J as the manipulator's base Jacobian can be used.

Another useful property of J is the static wrench transmission that relates the three-dimensional end-effector forces f and moments m to joint torques $\tau = J^T h$, where $h = (f^T \ m^T)^T$ denotes the end-effector wrench. If τ is due to an external wrench at the end effector, the Moore–Penrose pseudoinverse [34] of the transposed base Jacobian can be used to compute it from the torques:

$$h = J^+ \tau. \quad (4)$$

A more general formulation, considering dynamic components in τ , was proposed by Khatib in [35]. With the mass matrix M , this so-called dynamically consistent pseudoinverse $(JM^{-1}J^T)^{-1}JM^{-1}$ should be used instead of J^+ in (4) and all related equations to improve the

external wrench estimation. Still, in this paper the Moore–Penrose pseudoinverse was used in a quasi-static approximation in order to avoid using the mass matrix, requiring additional knowledge of the robotic hardware. This is done according to the assumption that the major components of τ are related to the external wrench, while dynamics can be neglected.

B. Task Variables

Consider a pure IFC interface like (1). Neither position q nor the full interaction torque τ can be controlled directly, hence we declare the following replacement task variables:

- 1) q_v —virtual joint space position;
- 2) $x_v = g(q_v)$ —virtual Cartesian pose (i.e. end effector);
- 3) $\tau_s = K(q_v - q)$ —static interaction joint torques;
- 4) $h_s = J^{T+}\tau_s = J^{T+}K(q_v - q)$ —static interaction wrench.

These variables have a close relation to the actual variables of interest (q, x, τ, h) but with a direct relation to q_v .

C. Generalized Task Control

To execute multiple tasks simultaneously, we need a generalized task control scheme. If the robot is redundant with respect to the task, local inversion of the differential relation between task variable and actuating variable (q_v) is the most common approach. The main advantages are the simplicity of task design, the possibility of a sensor-based execution, and the easy integration of multiple tasks with priorities [36]. This differential relation is captured by the so-called task Jacobian.

1) *Deriving the Task Jacobians:* In the following, we will derive the task Jacobians for the four task variables defined in the previous section.

a) *Joint Position:* For the joint position q_v , the task Jacobian is simply the $n \times n$ identity matrix I_n

$$\dot{q}_v = I_n \dot{q}_v. \quad (5)$$

b) *Cartesian Pose:* For the Cartesian pose, the instantaneous kinematics relation (3) is used:

$$\dot{x}_v = J_v \dot{q}_v \quad (6)$$

with $J_v = J(q_v)$ denoting the Jacobian of the virtual manipulator.

c) *Joint Torque:* Taking the time derivative of τ_s and reformulating gives us

$$\dot{\tau}_s + K\dot{q} = K\dot{q}_v.$$

It can be noted that an additional dependence on the joint velocity of the physical robot \dot{q} prevents a straight-forward linear formulation as in (5) and (6). Therefore, a new differential torque task variable β_τ is defined, which compensates for the effects of \dot{q} :

$$\beta_\tau = \dot{\tau}_s + K\dot{q}$$

$$\beta_\tau = K\dot{q}_v.$$

d) *Wrench:* With the time derivative of (4), we get

$$\dot{h}_s = J^{T+}\dot{\tau}_s + J^{T+}\dot{\tau}_s.$$

By assuming only moderate joint velocities, we neglect the term with the derivative of the Jacobian, resulting in

$$\dot{h}_s = J^{T+}\dot{\tau}_s = J^{T+}K(\dot{q}_v - \dot{q}).$$

Again, a compensated differential wrench task variable β_f can be defined and a differential relation stated

$$\beta_f = \dot{h}_s + J^{T+}K\dot{q} \quad (7)$$

$$\beta_f = J^{T+}K\dot{q}_v. \quad (8)$$

This relation is only valid for Jacobians, which are sufficiently far away from singularities, due to the inversion in (8).

To unify the four task variables, we define the general m -dimensional task variable σ , so that the general compensated differential task variable β and general $m \times n$ task Jacobian can be defined as

$$\beta = \dot{\sigma} + \gamma(\dot{q})$$

$$\beta = A\dot{q}_v$$

where $\gamma(\dot{q})$ is the respective compensation for \dot{q} .

2) *Trimmed Task Space:* Objectives do not have to be necessarily defined in the full task space. Often, only a particular subspace is relevant, and the released degrees of freedom can be used to achieve other tasks. The base of this subspace can be denoted by a set of orthonormal vectors, which form the columns of a matrix S . With σ being defined in the subspace frame, the basic task Jacobians have to be transformed to the subspace coordinates via $A := S^T A$.

S serves for two purposes here. First, it can be used as a selection matrix to select relevant directions of the full task space, similar to the selection matrix in hybrid force and position control [37]. Second, a coordinate transformation can be incorporated in S to formulate the task (partially) in a convenient coordinate system. It follows that S is either $6 \times m$ or $n \times m$, depending on whether σ is defined in Cartesian or in joint space.

3) *Generalized Controller:* The simplest way to bring the task variable σ continuously to a desired state σ_d is by using the task error $\tilde{\sigma} = \sigma_d - \sigma$ to formulate a general proportional task level controller

$$\dot{\sigma}_{\text{cmd}} = \Lambda \tilde{\sigma} + \dot{\sigma}_{\text{ff}} \quad (9)$$

where $\dot{\sigma}_{\text{ff}}$ denotes a feedforward term and Λ a diagonal gain matrix. The main purpose of $\dot{\sigma}_{\text{ff}}$ is to allow a direct specification of the differential task variable. The desired compensated task variable is then

$$\beta_d = \dot{\sigma}_{\text{cmd}} + \gamma(\dot{q}).$$

IV. SIMULTANEOUS POSITION AND FORCE CONTROL IN IFC

With the generalized task control presented in the previous section, we can apply some of the most common redundancy resolution techniques to combine different tasks.

In [2], it was shown how equality tasks could be realized in an IFC context by applying hierarchical null-space mapping, and in [3], the approach was extended to inequality tasks via a QP-based formulation. As the stability proof presented in this paper requires limitation of \dot{q}_v , the more general QP approach is briefly recapitulated.

Instead of having one desired value for the task variable σ_d , we specify lower and upper bounds (σ_m and σ_M) as a desired range for σ , what can be defined as an inequality task or constraint $\sigma_m \leq \sigma \leq \sigma_M$. An equality task σ_d can be specified by setting $\sigma_m = \sigma_M = \sigma_d$.

The global limits are transformed to local limits on the differential task variable $\dot{\sigma}_{\text{cmd}_m} \leq \dot{\sigma} \leq \dot{\sigma}_{\text{cmd}_M}$, where

$$\dot{\sigma}_{\text{cmd}_m} = \Lambda(\sigma_m - \sigma) + \dot{\sigma}_{m\text{ff}}$$

$$\dot{\sigma}_{\text{cmd}_M} = \Lambda(\sigma_M - \sigma) + \dot{\sigma}_{M\text{ff}}.$$

As in (9), a feedforward term $\dot{\sigma}_{m\text{ff}}$, respectively, $\dot{\sigma}_{M\text{ff}}$ can be specified for both bounds. The according limits on β are

$$\beta_m = \dot{\sigma}_{\text{cmd}_m} + \gamma(\dot{q})$$

$$\beta_M = \dot{\sigma}_{\text{cmd}_M} + \gamma(\dot{q}).$$

The main advantage compared to other common approaches, like artificial potential fields [38], is that a clear inequality constraint is specified, hence no switching or priority shifting is required. Also, the limit can be reached in finite time, hence the full range of possible motions is exploited [30].

The set of subtasks can be formulated as a sequence of QPs, where every problem is solved in an optimal way, without altering the quality of the solution for the previous tasks. Starting with the highest priority level, for every subtask, the following QP problem is stated:

$$\min. \quad \frac{1}{2} \mathbf{s}^T \mathbf{s} + \frac{1}{2} \rho \dot{\mathbf{q}}_v^T \dot{\mathbf{q}}_v \quad (10)$$

$$\text{s.t.} \quad \beta_m \leq \mathbf{A} \dot{\mathbf{q}}_v - \mathbf{s} \leq \beta_M \quad (11)$$

$$\bar{\beta}_m + \bar{\mathbf{s}}^* \leq \bar{\mathbf{A}} \dot{\mathbf{q}}_v \leq \bar{\beta}_M + \bar{\mathbf{s}}^* \quad (12)$$

$$\dot{\mathbf{q}}_{v_m} \leq \dot{\mathbf{q}}_v \leq \dot{\mathbf{q}}_{v_M} \quad (13)$$

where $\bar{\bullet}$ indicates the augmented vector or matrix of all the higher priority tasks. The cost function (10) contains a vector of slack variables \mathbf{s} , which is balanced against the virtual joint velocities with the regularization parameter $\rho \in \mathbb{R}^+$, which is important for the numerical stability of the process [39].

Minimizing a slack variable instead of the task error itself makes the current task inequality (11) a soft constraint, allowing violation of the task velocity bounds β_m and β_M in case the task is unfeasible. The second inequality constraint (12) is a hard constraint, which makes sure that the higher priority task velocity bounds, accumulated in the augmented vectors $\bar{\beta}_m$ and $\bar{\beta}_M$, are not violated more than the previously determined minimal slack variables $\bar{\mathbf{s}}^*$. Inequality (13) finally constraints the virtual joint velocity to stay within certain bounds, which are shaped to obey joint position, velocity, and acceleration limits ($\mathbf{q}_m, \mathbf{q}_M, \mathbf{v}_M$, and \mathbf{a}_M), using finite differences and the current commanded joint velocity $\dot{\mathbf{q}}_v$:

$$\dot{\mathbf{q}}_{v_m} = \max \left\{ \frac{\mathbf{q}_m - \mathbf{q}_v}{\Delta T}, -\mathbf{v}_M, (\mathbf{a}_M + \dot{\mathbf{q}}_v) \Delta T, -\sqrt{2\mathbf{a}_M(\mathbf{q}_v - \mathbf{q}_m)} \right\}$$

$$\dot{\mathbf{q}}_{v_M} = \min \left\{ \frac{\mathbf{q}_M - \mathbf{q}_v}{\Delta T}, \mathbf{v}_M, (-\mathbf{a}_M + \dot{\mathbf{q}}_v) \Delta T, \sqrt{2\mathbf{a}_M(\mathbf{q}_M - \mathbf{q}_v)} \right\}$$

assuming a constant sample time ΔT .

It has to be noted that the dynamically consistent pseudoinverse should be used here instead of \mathbf{J}^+ to cancel potential null-space torques, leading to uncontrolled motions of the robot. Alternatively, force tasks should be placed in the lowest priority level (without leaving any degrees of freedom for potential null-space torques). However, once the desired wrench is reached, the resulting differential commands are so small, that the uncontrolled null-space motion can be neglected.

V. STABILITY ANALYSIS

While it was shown in multiple works that the interconnection of an IFC block and a robot is stable (e.g., [40] and [41]) for external generation of set points, this is not necessarily the case if the SPG block is connected via a feedback loop to the system (see Fig. 2).

As the solution of the QP problem cannot be stated in a closed form, classic stability analysis cannot be applied here. Passivity theory has proven as a useful tool to handle such conditions.

A. Passivity and Stability

Being a sufficient stability condition, passivity is an intuitive approach to stabilize a nonlinear, partially unknown system. Instead of relying on a model, passivity theory makes assumptions on energetic properties to derive stability conditions. The system is energetically passive if the overall energy transmitted to the system E is bounded by a constant $c \in \mathbb{R}$, which depends on the initial energy

$$E \geq -c^2.$$

There exist multiple approaches to enforce passivity of a system, like the time-domain passivity control concept [42] or the energy bounding

algorithm [43]. In [44], a passive set-point modulation (PSPM) for a Cartesian impedance controlled manipulator is proposed. As this setup is very similar to our scenario, we apply the basic concepts to formulate a stability proof.

To make the system passive, Lee *et al.* [44] propose to implement a virtual energy reservoir, which stores the dissipated energy and use it to execute nonpassive actions. This is realized by augmenting the overall system with a virtual energy storage and modulate the desired set points to the IFC, so that the energy transferred to the virtual spring is limited by the amount of energy left in the reservoir.

B. Passive Set-Point Modulation

Let us analyze the energy flow for the IFC–SPG system of an individual joint

$$\tau = K \Delta q - D \dot{q} + \tau_g \quad (14)$$

where $\Delta q = (q_v - q)$ and K and D are the corresponding diagonal entries in the stiffness and damping matrices from (1). Specific joint indexing is omitted in the following for the sake of readability. It can be shown that the robot possesses open-loop energetic passivity with respect to the external torques, hence only the port between the SPG-IFC block and the robot needs to be considered. To prove the passivity with respect to the input–output pair $\{\tau, -\dot{q}\}$, it has to be shown that

$$-\int_0^T \tau \dot{q} dt \geq -c^2 \quad (15)$$

holds for every joint.

The potential energy stored in the virtual spring is

$$E_K = \frac{1}{2} K \Delta q^2$$

and the energy dissipated by the damper after time T is

$$E_D(t) = \int_0^T D \dot{q}^2 dt.$$

It is assumed that either the internal IFC controller runs at a high frequency or a physical spring is installed so that (14) is continuous. The SPG on the other hand is regarded as a discrete system, which provides set points with the frequency $1/\Delta T$. Hence, the IFC input \dot{q}_v is equivalent to setting a joint position increment δq_v with the sampling time ΔT

$$\delta q_v = \dot{q}_v \Delta T. \quad (16)$$

By taking the difference of the potential energy before and after the position increment, the energy increase at the discrete sampling point i due to the set-point setting can be computed as

$$\Delta E_K[i] = \frac{1}{2} K ((\Delta q[i] + \delta q_v)^2 - \Delta q[i]^2) \quad (17)$$

where $\bullet[i]$ denotes the respective quantity at the discrete time-step i . The sign of $\Delta E_K[i]$ is not determined, hence the set-point increment is a potentially not passive action. Besides that, the dissipated energy during the time interval ΔT by the damper can be written as

$$\Delta E_D[i] = \int_{t_i}^{t_i + \Delta T} D \dot{q}^2 dt$$

where t_i is the continuous time at the discrete sample point i .

With $E_K(t)$ being the energy stored in the spring at time t , the energy equation can be stated as

$$-\int_0^T \tau \dot{q} dt - E_D(T) + \sum_{j=1}^i \Delta E_K[j] = E_K(T) - E_K(0)$$

and with (15), the IFC–SPG block for one joint is passive with respect to the input–output pair $\{\tau, -\dot{q}\}$ if

$$-\int_0^T \tau \dot{q} dt = E_K(T) - E_K(0) + E_D(T) - \sum_{j=1}^i \Delta E_K[j] \geq -c^2.$$

We start with a simple energy reservoir, which stores the dissipated energy from the damper and provides energy to the SPG, used to load the virtual spring. The discrete storage function is

$$E_r[i] = E_r[i-1] + E_D(t_i) - \Delta E_K[i]. \quad (18)$$

Now, for practical reasons, the following adjustments have to be done.

- 1) E_D cannot be computed due to missing information on the joint velocity between the sampling points and also missing future data. Therefore, the minimal dissipated energy $E_{D_{\min}}$ has to be used instead (see [44] for details on how to obtain $E_{D_{\min}}$).
- 2) Excessive energy accumulation might allow aggressive/dangerous behavior of the system, while theoretically still being passive. Therefore, the energy in the system is limited by a maximum capacity $E_{r_{\max}}$ for E_r , what is called energy ceiling in [44].
- 3) For highly dissipative environments, it is useful to transfer some energy to the system. This action also makes sure that the robot does not get stuck when all the energy in the storage is depleted. This is realized by adding the shuffling term $\Delta E_{\text{shuffle}}$ to the energy storage function (18).
- 4) With a depleted energy reservoir at $t = 0$, no motion would be possible in the beginning of the task, since any extension of the virtual spring would result in a violation of the passivity condition. To overcome this “takeoff” problem, the storage is initialized with the energy $E_r[0] = E_{r_{\text{init}}}$.

The new energy storage function with minimum dissipated energy and shuffling term is

$$E_r[i] = E_r[i-1] + \Delta E_{D_{\min}} + \Delta E_{\text{shuffle}} - \Delta E_K(t_i).$$

By requesting $E_r[i] \geq 0$, it is assured that the energy generated by the SPG is not larger than the energy dissipated in the IFC. This limitation can be directly incorporated into the existing SPG framework by adjusting the velocity limits on \dot{q}_v . From (16) and (17), new velocity limits can be derived

$$\dot{q}_{v_m} = \frac{1}{\Delta T} \left(-\sqrt{\frac{2}{K}(E_r[i-1] + \Delta E_{D_{\min}} + \Delta E_{\text{shuffle}})} + \Delta q^2 - \Delta q \right) \quad f. \quad \Delta q \leq 0 \quad (19)$$

$$\dot{q}_{v_M} = \frac{1}{\Delta T} \left(\sqrt{\frac{2}{K}(E_r[i-1] + \Delta E_{D_{\min}} + \Delta E_{\text{shuffle}})} + \Delta q^2 - \Delta q \right) \quad f. \quad \Delta q \geq 0. \quad (20)$$

The energy flow between the SPG, IFC, robot, and augmented energy reservoir is depicted in Fig. 3, where the robot is regarded as a system with $n+1$ ports. One for each joint connected to its IFC and one for the connection of the robot to the environment, with τ_{ext} as the external joint torques. Assuming a passive environment, only the energy flow between the robot and the controller has to be analyzed.

VI. EXPERIMENTAL RESULTS

In this paper, one exemplary task with different components, an uncertain task geometry, and the possibility for unexpected collisions

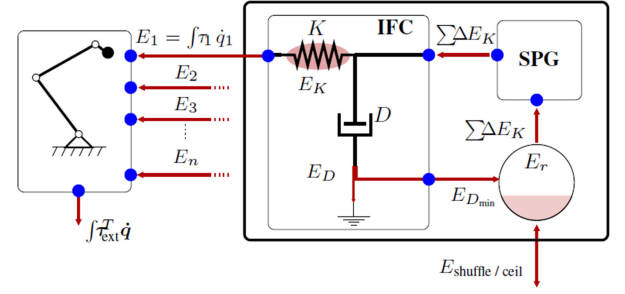


Fig. 3. Energy flow with the augmented energy reservoir. The energetic contribution of each joint ($E_1 \dots E_n$) is regarded separately and is transmitted to the robot from the virtual spring K in the IFC controller. The minimal dissipated energy $E_{D_{\min}}$ is stored in the virtual energy reservoir E_r and the SPG is only allowed to use the energy from this reservoir to load the spring, which is realized by the additional inequality constraints on the virtual joint velocity (19) and (20). By coupling the energy generation of the SPG to the virtual energy reservoir, the overall system is guaranteed to be passive, hence stable.

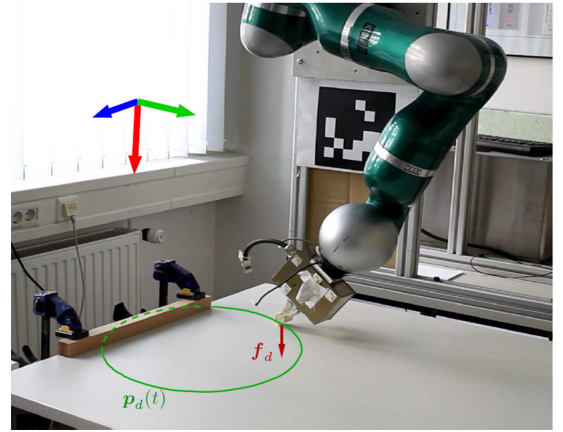


Fig. 4. Sample mixed components task with an obstacle, generating an unexpected perturbation. The main subtasks are to apply a constant interaction force and follow a circular trajectory. Different strategies to deal with unexpected perturbations are compared, relying on the IFC compliance, limiting the joint torques, and limiting the end-effector forces. The according data are plotted in Fig. 5.

TABLE I
SET OF SUBTASKS FOR CONSTRAINED TRAJECTORY FOLLOWING

task	type	σ_m	σ_M	S
1a,c	joint torque	$-50\text{Nm } I_7$	$50\text{Nm } I_7$	I_7
1b	joint torque	$-5\text{Nm } I_7$	$5\text{Nm } I_7$	I_7
2	Cart. pose	σ_{init}	σ_{init}	$\begin{bmatrix} 0_3 \\ I_3 \end{bmatrix}$
3a,b	wrench	$\begin{bmatrix} 10 \\ -10 \\ -10 \end{bmatrix}$ N	$\begin{bmatrix} 10 \\ 10 \\ 10 \end{bmatrix}$ N	$[1 \ 0 \ 0 \ 0 \ 0]^T$
3c	wrench	$\begin{bmatrix} 10 \\ -10 \\ -10 \end{bmatrix}$ N	$\begin{bmatrix} 10 \\ 10 \\ 10 \end{bmatrix}$ N	$\begin{bmatrix} I_3 \\ 0_3 \end{bmatrix}$
4	Cart. pose	$p_d(t)$	$p_d(t)$	$\begin{bmatrix} I_3 \\ 0_3 \end{bmatrix}$
5	joint position	0_{rad}	0_{rad}	I_7

is presented. The accompanying video shows some other realizations, using the proposed method.

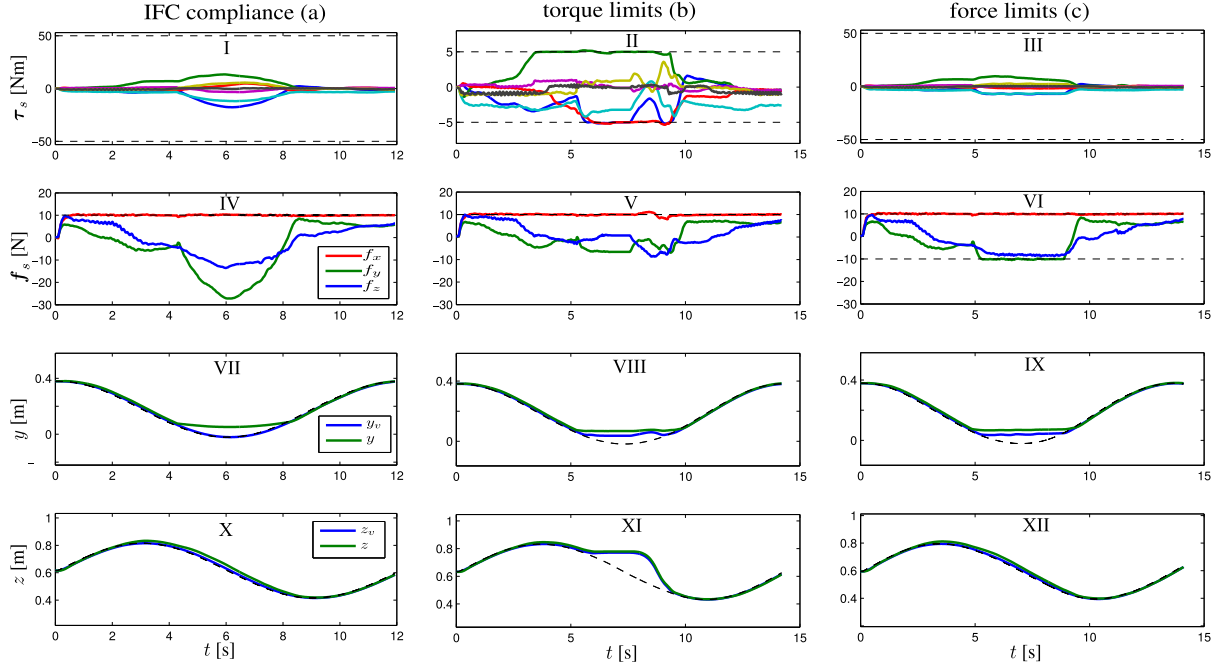


Fig. 5. Each column shows the propagation of the relevant task variables for three different task specifications from Table I. The interaction forces and torques are computed according to the static relations presented in Section III-B. For the trajectory following task, both the virtual and the physical positions of the end effector are plotted. In each graph, the dashed line represents the task constraints (desired value or limits). Left: the obstacle impedes the motion of the physical end effector along the y -axis (VII). This is compensated by the inherent compliance of the IFC, leading to additional interaction forces in the y - and z -direction (IV). Forces along y and z are not constrained by the task specification. This approach corresponds basically to a classical IFC application. Middle: the torque limits are lowered to $\pm 5 \text{ N} \cdot \text{m}$ in order to avoid large interaction torques (II). This prevents the virtual end effector from penetrating further into the obstacle (VIII). However, due to friction, in this case, the new torque limits are so conservative that at some point no motion is possible at all while the virtual end-effector penetrates the obstacle (XI). Right: another possibility is to explicitly limit the interaction forces instead of the torques, making it possible to tune the allowed forces in Cartesian space, to account for expected resistance, e.g., friction (VI).

A. Implementation Details and Hardware

The experiments have been carried out on our KUKA LBR-IV lightweight arm. The manipulator was running a joint space impedance controller, whose details can be found in [45]. This IFC controller emulates a physical mass-spring-damper system in every joint and has same behavior as a SEA-type robot. The rate of the discrete controller was 500 Hz and the stiffness was set to $\mathbf{K} = 200 \mathbf{I}_7 \text{ N} \cdot \text{m}/\text{rad}$. The task convergence factors $\mathbf{\Lambda}$ and the regularization factor $\rho = 0.01$ were chosen heuristically. The C++ QP library qpOASES [46], which is an implementation of [47], was used to carry out the optimization (10)–(13).

B. Constrained Trajectory Tracking

A generic mixed components task is executed, which is following a Cartesian trajectory on a table surface while applying a constant force on it. In addition, there is an obstacle blocking the way, which generates an unexpected perturbation. The setup is depicted in Fig. 4, and the main subtasks are summarized in Table I.

Three different task descriptions a, b, and c were applied to demonstrate some basic properties of our IFC approach and highlight the simplistic task programming interface. According to Table I, tasks 2, 4, and 5 are the same for all setups, which are

- 1) maintaining the initial orientation of the end effector \mathbf{o}_{init} (task 2);
- 2) following a time-dependent trajectory in the yz plane with the end effector (task 4);
- 3) maximizing the distance of the joints to their limits (task 5).

First, the force task is specified as an equality constraint along the x -axis only (specification a). Then, the torque limits are lowered to avoid large interaction torques (specification b). Finally, the force task is defined as an equality in its x -component and as an inequality in the y and z components to limit the interaction forces explicitly (specification c). The results are depicted in Fig. 5.

VII. CONCLUSION

We combined different methods from robot control to develop an additional layer between the task programming and the low-level indirect force controlled robot. The assumptions on the actual robotic hardware are very general, hence the formulated method is applicable on any IFC-like architecture or also SEA-type manipulators, which represent a physical realization of an IFC.

The following information is required from the IFC–robot system:

- 1) the kinematic parameters;
 - 2) optionally: the joint position, velocity, acceleration, and torque limits;
 - 3) the IFC joint stiffness \mathbf{K} ;
 - 4) the physical and virtual joint positions (\mathbf{q} and \mathbf{q}_v , respectively).
- A task is completely specified by providing
- 1) the task type (or task Jacobian \mathbf{A});
 - 2) the lower and upper bounds for the task variable σ_m and σ_M (or σ_d);
 - 3) the feedforward differential task variables $\dot{\sigma}_{m_{\text{ff}}}$ and $\dot{\sigma}_{M_{\text{ff}}}$;
 - 4) the convergence rate $\mathbf{\Lambda}$;
 - 5) the subspace matrix \mathbf{S} .

The resulting scheme allows the specification of a hierarchical set of equality and inequality tasks, consisting of force and positioning components on joint and Cartesian level. The reduced performance in terms of accuracy is deliberately accepted in tradeoff a permanently compliant behavior and to allow intuitive, yet powerful task programming in highly unstructured environments. Neither modification nor detailed information of the IFC is required, which makes the approach very general in terms of robotic hardware.

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