



Intelligent controller for hybrid force and position control of robot manipulators using RBF neural network

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Abstract

In this paper, an intelligent controller is developed for hybrid force and position control of robot manipulators in the presence of external disturbances and the model uncertainties. The proposed controller consists of a model based controller and neural network based model free controller with an adaptive bound part. A non linear function of model dynamics is identified by employing a radial basis function neural network. The role of adaptive bound part is to estimate the bounds on model disturbances, friction term and neural network reconstruction error. The Lyapunov function candidate is used to prove the stability of the proposed controller and to show that the errors are asymptotically convergent. Finally numerical simulation results are presented for two link robot manipulator to show excellent performance of the proposed controller in comparison to other control schemes such as model based computed torque control and neural network based model free controller.

Keywords Hybrid force and position control · Constrained robot manipulator · Disturbances · Neural network · Asymptotically stable

1 Introduction

There are many industrial applications such as grinding, fine polishing, contour following, deburring and assembly in which the robot end effector comes in the contact with the environment. During the execution of such types of tasks, the control objective is to regulate the contact forces exerted by manipulator end effector on the environment while simultaneously regulating the position of end effector. Such type of control problem i.e. the hybrid force and position control of robotic manipulators has been a subject of interest in the literature of control system. Raibert and Craig [1] developed the hybrid position/force controller to control manipulator end effector trajectory by using force sensor. Lozano and Brogliato [2] presented a hybrid position/force controller to control the redundant mechanical robot manipulator. By extending the work of [1] Yoshikawa and Sudou [3] developed a dynamic hybrid control problem for constrained robot

with an undefined constraint surface. Kwan [4] developed a robust adaptive sliding control method for force/motion control of constrained manipulator with motor dynamics. Kouya et al. [5] introduced an adaptive position/force controller by utilizing the strict feedback back-stepping method which depends on passivity. De Queiroz et al. [6] proposed an adaptive controller for rigid robot manipulator to control force and position during constrained motion without velocity measurement. Cheah et al. [7] proposed an adaptive force/motion controller which worked well without the exact knowledge of Jacobian matrix, dynamics and kinematics. Filaretov and Zuev [8] developed a control scheme without force sensors to control force and position of rigid robot manipulator. Kouya [9] designed a hybrid force/position controller for constrained manipulators with uncertainty. Roy and Whitcomb [10] designed an adaptive force control method for robot arm which comes into contact with surface of unknown linear compliances. In order to control hybrid position/force control of robot manipulators, Pliego-Jimenez and Arteaga-Perez [11] developed the hybrid position/force controller for robot manipulator in contact with uncertain constraint surface. In this scheme measured force end effector position are used to estimate the constraint surface. The calculation of complex regression matrices are required for these techniques, which is very tedious task. In recent times, neu-

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ral networks have achieved popularity among community of control system due to their learning ability. The neural network based controllers are being used to learn uncertainties or unknown non linear function. There are many researches in the literature of control system that take the benefit of NN to compensate the uncertainties [12,13]. Fanaei and Farrokhi [14] designed the robust and adaptive neuro-fuzzy controller to compensate the friction force between the end effector and the surface. Liu et al. [15] designed the force controller for robot manipulator based on fuzzy prediction for reference trajectory in the impedance model. Karayiannidis et al. [16] proposed an adaptive controller for robotic manipulator to deal with the problem of force and position control in a compliant surface. Bechlioulis et al. [17] presented NN based adaptive force and position controller with the uncertainties in the dynamical system. Kumar et al. [18] proposed an adaptive control method to deal with the problem of hybrid force/position control of robotic manipulators. Feedforward neural network is used to compensate the uncertainties existing in the dynamical system. Singh and Sukavanam [19] extended the work of [18] and developed a NN based robust adaptive controller by including external disturbances and achieved the stability of system. Mahjoub et al. [20] developed an adaptive sliding mode control using radial basis function neural network for underactuated robotic manipulators. Li et al. [21] designed a hybrid position/force controller based on neural network for constrained reconfigurable manipulators. Lee and Wang [22] developed the robust adaptive force and position tracking controller using fuzzy neural network for robot manipulators under unknown environment. Ghajar et al. [23] introduced hybrid position and force controller for constrained manipulators with contact friction between the robot end effector and surface. De Oliveira et al. [24] presented a dual mode control method for adjusting the RBF weights. Rani and Kumar [25] designed a neural network based hybrid force and position controller for constrained robot manipulators. But their controller may face singularity issue. In the present paper, controller scheme is designed to address the singularity issue of [25] and to improve the performance of the controller.

The novelty of the paper is the design of an asymptotically stable controller for hybrid force and position control of robot manipulators by utilizing model based techniques and neural network based model free technique. Generally, all neural network based hybrid force and position controllers require no information regarding system dynamics. But in practical situation, we are always available with partial information. For effective controller, it would be better to use this information. In the present paper, utilizing partial information about the system dynamics, we have proposed a controller consisting of the merits of model based technique and RBF neural network based model free technique. The disturbances, unstructured uncertainties and network approx-

imation errors are compensated with the adaptive bound part of the controller. The numerical simulations are performed to prove the better performance of the proposed controller, i.e. a hybrid controller consisting of model based controller together with RFNNN based model free controller, as compare to model based controller and FFNN based model free controller.

The paper is structured as: In Sect. 2, the details about the dynamical model and its decomposition is presented. The radial basis function neural network based controller is developed in Sect. 3. Section 4, deals with the stability analysis. Simulation studies is discussed in details in Sect. 5 and the concluding remarks are presented in Sect. 6.

2 Dynamics of constrained robot manipulators

The general equation of motion for n link revolute constrained robot is expressed as [19]

$$B(q)\ddot{q} + C_m(q, \dot{q})\dot{q} + G(q) + F_f(\dot{q}) + D = \tau - \tau_e \quad (1)$$

where $B(q) \in R^{n \times n}$ symbolizes the inertia matrix. $C_m(q, \dot{q}) \in R^{n \times n}$ stands for the centripetal-coriolis matrix. $G(q) \in R^n$ represents the gravity effects. $F_f(\dot{q}) \in R^n$ stands for the friction effects. $D \in R^n$ is a bounded disturbance. $\tau \in R^n$ is the torque input vector and $\tau_e \in R^n$ is the interaction torque.

The link position, velocity and acceleration are denoted by q , \dot{q} and \ddot{q} respectively.

Property 1 The matrix $B(q)$ is symmetric and positive definite and satisfies the following inequality:

$$a_1 \|\xi\|^2 \leq \xi^T B(q) \xi \leq a_2 \|\xi\|^2 \quad \forall \xi \in R^n \quad (2)$$

where a_1 and a_2 are positive constant.

Property 2 The matrix $(\dot{B}(q) - 2C_m(q, \dot{q}))$ is skew symmetric matrix i.e for any $z \in R^n$, we have

$$z^T (\dot{B}(q) - 2C_m(q, \dot{q})) z = 0 \quad (3)$$

Some useful assumptions for the development of the controller are taken as:

Assumption 1 We assume that $(\|F_f(\dot{q})\| \leq b + c\|\dot{q}\|)$, where b and c are positive constants.

Assumption 2 $(\|D\| \leq e)$, where e is positive constant.

The relation between interaction torque (τ_e) and interaction force ($\bar{F} \in R^m$) is defined as follows

$$\tau_e = O^T(q) \bar{F} \quad (4)$$

where Jacobian matrix $O(q)$ belongs to $R^{m \times n}$.

The kinematic equation of robot is defined by

$$x = f(q) \quad (5)$$

where position vector of the end-effector is $x \in R^m$ and the kinematic transformation of robot is $f(q)$.

By taking derivative of Eq. (5), we have

$$\dot{x} = O(q)\dot{q} \quad (6)$$

In the task space, force ($\bar{F} \in R^m$) and environment deformation i.e. $(x - x_c)$ are related by

$$\bar{F} = \bar{S}(x - x_c) \quad (7)$$

where ($\bar{S} \in R^{m \times m}$) is constant stiffness matrix and $x_c \in R^m$ is the point of contact.

Equation (7) can be rearranged as:

$$\bar{F} = \begin{bmatrix} F \\ F' \end{bmatrix} = \begin{bmatrix} S \\ S' \end{bmatrix} (x - x_c) \quad (8)$$

where $F \in R^l$, $F' \in R^{n-l}$, $S \in R^{l \times m}$ ($l \leq m$) and l is the dimension of subspace where force can be controlled. In this way, we can control $(m - l)$ cartesian position, l forces and $(n - m)$ redundant joints velocities.

2.1 Decomposition of dynamical model

In this subsection, we decompose the robot dynamics (1) into position S^-x , force F and redundant joint subspace O^-q using the identities:

$$I = O^+O + O^- \quad (9)$$

$$I = S^+S + S^- \quad (10)$$

where

$$O^+ = O^T[OO^T]^{-1} \quad (11)$$

$$S^+ = S^T[SS^T]^{-1} \quad (12)$$

$$O^- = I - O^T[OO^T]^{-1}O \quad (13)$$

$$S^- = I - S^T[SS^T]^{-1}S \quad (14)$$

where O^+ and S^+ are penrose pseudo inverses and O^- , S^- are idempotent matrices.

Using Eqs. (9) and (5), \dot{q} is decomposed as

$$\dot{q} = O^+O\dot{q} + O^-\dot{q} = O^+\dot{x} + O^-\dot{q} \quad (15)$$

Using Eqs. (10) and (8), \dot{x} is decomposed as

$$\dot{x} = S^+S\dot{x} + S^-\dot{x} = S^+\dot{F} + S^-\dot{x} \quad (16)$$

Differentiating Eq. (6), we have

$$\ddot{x} = O\ddot{q} + \dot{O}\dot{q} \quad (17)$$

Taking Eqs. (9) and (17), \ddot{q} can be decomposed as

$$\ddot{q} = O^+O\ddot{q} + O^-\ddot{q} = O^+(\ddot{x} - \dot{O}\dot{q}) + O^-\ddot{q} \quad (18)$$

Differentiating Eq. (16), we get

$$\ddot{x} = S^+S\ddot{x} + S^-\ddot{x} = S^+\ddot{F} + S^-\ddot{x} \quad (19)$$

Using Eqs. (15–19) in Eq. (1), we get

$$\begin{aligned} & B(O^+(S^+\ddot{F} + S^-\ddot{x} - \dot{O}\dot{q}) + O^-\ddot{q}) \\ & + C_m(O^+(S^+\dot{F} + S^-\dot{x}) \\ & + O^-\dot{q}) + G(q) + F_f(\dot{q}) + D = \tau - \tau_e \end{aligned} \quad (20)$$

Equations (20) and (1) are equivalent equations and clearly Eq. (20) is a decomposition of position, force and redundant joints velocity.

3 Control system development

In this section, we design the control scheme. Let us define the filtered tracking error r as

$$r = O^+[S^+(\dot{F} - v_f) + S^-(\dot{x} - v_x)] - O^-\dot{\tilde{q}} \quad (21)$$

where

$$v_f = \dot{F}_s - \lambda\tilde{F}, v_x = \dot{x}_s - \lambda\tilde{x} \quad (22)$$

$$\tilde{F} = F - F_s, \tilde{x} = x - x_s, \tilde{q} = q - q_s \quad (23)$$

where $\lambda > 0$ and F_s, x_s, q_s are desired values of F, x, q .

Now differentiating Eq. (21) and using Eqs. (22) and (23), we can write Eq. (20) in terms of r as

$$B\dot{r} + C_m r = \tau - \tau_e - h(y) - F_f - D \quad (24)$$

where $h(y) = B(O^+[S^+v_f + S^-\dot{v}_x - \dot{O}\dot{q}] + O^-\ddot{q}_d - z) + C_m(O^+[S^+v_f + S^-\dot{v}_x] + O^-\dot{q}_d) + G$ is a non linear function. Here $z = \frac{dO^+}{dt}[S^+(\dot{F} - v_f) + S^-(\dot{x} - v_x)] + \frac{dO^-}{dt}\dot{\tilde{q}}$. We write the function $h(y)$ as summation of two parts one corresponding to known dynamics and another corresponding to unknown dynamics as follows

$$h(y) = \hat{h}(y) + \tilde{h}(y) \quad (25)$$

where

$$\begin{aligned}\hat{h}(y) = & \hat{B}(O^+[S^+v_f + S^-v_x - \dot{O}\dot{q}] + O^-\ddot{q}_d - z) \\ & + \hat{C}_m(O^+[S^+v_f + S^-v_x] + O^-\dot{q}_d) + \hat{G}\end{aligned}\quad (26)$$

and

$$\begin{aligned}\tilde{h}(y) = & \tilde{B}(O^+[S^+v_f + S^-v_x - \dot{O}\dot{q}] + O^-\ddot{q}_d - z) \\ & + \tilde{C}_m(O^+[S^+v_f + S^-v_x] + O^-\dot{q}_d) + \tilde{G}\end{aligned}\quad (27)$$

and the vector y is given by $y = [r^T, \bar{F}^T, q^T, \dot{q}^T]$.

3.1 Radial basis function neural network (RBFNN)

RBF neural network is utilized to identify a non linear function of model dynamics and it is defined as follows:

$$\tilde{h}(y) = W^T \zeta(y) + \varepsilon(y) \quad (28)$$

where $W \in R^{P \times n}$ symbolizes the matrix of weights of neural network, $\varepsilon(y) : R^{3n+1} \rightarrow R^n$ denotes NN reconstruction error with $\|\varepsilon(y)\| \leq \varepsilon_P$ for some ε_P and $\zeta(y) : R^{3n+1} \rightarrow R^P$ is a smooth basis function defined as

$$\zeta_i(y) = \exp\left(-\frac{\|(y - c_i)\|^2}{\sigma_i^2}\right) \quad i = 1, 2, \dots, P \quad (29)$$

where $c_i \in R^{3n+1}$ and $\sigma_i \in R$ are centers and width of nodes and P is the no. of nodes of NN.

Using Eqs. (25) and (28) in Eq. (24), we get

$$B\dot{r} = -C_m r + \tau - \tau_e - \hat{h}(y) - W^T \zeta(y) - \varepsilon(y) - F_f - D \quad (30)$$

3.2 Adaptive bound

In this subsection, we use Assumptions 1, 2 and bound of $\varepsilon(y)$, such that:

$$\|F_f(\dot{q}) + D + \varepsilon(y)\| \leq b + c\|\dot{q}\| + e + \varepsilon_P \quad (31)$$

Now we define $\beta = b + c\|\dot{q}\| + e + \varepsilon_P$ as an adaptive bound and it can be rewritten as

$$\beta = [1 \ \|\dot{q}\| \ 1 \ 1] [b \ c \ e \ \varepsilon_P]^T = Q^T (\|\dot{q}\|) \phi \quad (32)$$

where $Q \in R^k$ is known vector of joint velocity and $\phi \in R^k$ is a parameter vector, where k is positive fixed number.

To achieve the desired control objective, the **controller** is proposed as:

$$\tau = \tau_e + \hat{h}(y) - K_g r + \hat{W}^T \zeta(y) - \frac{\hat{\beta}^2 r}{\hat{\beta} \|r\| + \delta} \quad (33)$$

where gain matrix $K_g \in R^{n \times n}$ is a positive matrix, $\hat{\beta} = Q^T \hat{\phi}$, $\hat{\phi}$ and \hat{W} are estimated values of parameter vector

and neural network weights respectively and $\dot{\delta} = -\gamma \delta$, $\delta(0) =$ designed constant > 0 , $\gamma > 0$.

Using τ given by Eq. (33) in Eq. (30), we get

$$B\dot{r} = -(K_g + C_m)r - \tilde{W}^T \zeta(y) - (F_f + D + \varepsilon(y)) - \frac{\hat{\beta}^2 r}{\hat{\beta} \|r\| + \delta} \quad (34)$$

where $\tilde{W} = W - \hat{W}$

4 Stability analysis

In this section, we analysis the system stability using following theorem.

Theorem *If the control input τ given by Eq. (33) for the robot dynamics (1) and adaptation laws for NN weights and adaptive bound are selected as given by Eqs. (35) and (36) respectively, then the controller is stable as well as the filtered tracking error r and henceforth the position error S^-x , force error \bar{F} and the redundant velocity error $O^- \dot{q}$ converges to zero as $t \rightarrow \infty$*

$$\dot{\hat{W}} = -\Gamma_W \zeta(y) r^T \quad (35)$$

$$\dot{\hat{\phi}} = \Gamma_\phi Q \|r\| \quad (36)$$

where $\Gamma_W = \Gamma_W^{-1} \in R^{N \times N}$, $\Gamma_\phi = \Gamma_\phi^{-1} \in R^{k \times k}$

Proof Consider the following Lyapunov function candidate:

$$L = \frac{1}{2} r^T B r + \frac{1}{2} \text{tr}(\tilde{W}^T \Gamma_W^{-1} \tilde{W}) + \frac{1}{2} \text{tr}(\tilde{\phi}^T \Gamma_\phi^{-1} \tilde{\phi}) + \frac{\delta}{\gamma} \quad (37)$$

where $\tilde{W} = W - \hat{W}$ and where $\tilde{\phi} = \phi - \hat{\phi}$

Taking derivative of the Lyapunov function w.r.t, we have

$$\dot{L} = \frac{1}{2} r^T \dot{B} r + r^T B \dot{r} + \text{tr}(\tilde{W}^T \Gamma_W^{-1} \dot{\tilde{W}}) + \text{tr}(\tilde{\phi}^T \Gamma_\phi^{-1} \dot{\tilde{\phi}}) + \frac{\dot{\delta}}{\gamma} \quad (38)$$

Now using the Eq. (34) and the facts $\dot{\tilde{W}} = -\dot{\hat{W}}$, $\dot{\tilde{\phi}} = -\dot{\hat{\phi}}$ and $\dot{\delta} = -\delta\gamma$, we get the following expression

$$\begin{aligned}\dot{L} = & \frac{1}{2} r^T \dot{B} r + r^T \left(-K_g r - C_m r - \tilde{W}^T \zeta(y) \right. \\ & \left. - (F_f + D + \varepsilon(y)) \right. \\ & \left. - \frac{\hat{\beta}^2 r}{\hat{\beta} \|r\| + \delta} \right) - \text{tr}(\tilde{W}^T \Gamma_W^{-1} \dot{\hat{W}}) - \text{tr}(\tilde{\phi}^T \Gamma_\phi^{-1} \dot{\hat{\phi}}) - \delta\end{aligned}\quad (39)$$

Using Eqs. (35) and (36) in Eq. (39), we have

$$\begin{aligned}\dot{L} = & \frac{1}{2}r^T \dot{B}r - r^T K_g r - r^T C_m r - r^T \tilde{W}^T \zeta(y) \\ & - r^T (F_f + D + \varepsilon(y)) - \frac{\hat{\beta}^2 r^T r}{\hat{\beta} \|r\| + \delta} \\ & + \text{tr}(\tilde{W}^T \Gamma_W^{-1} \Gamma_W \zeta(y) r^T - \text{tr}(\tilde{\phi}^T \Gamma_\phi^{-1} \Gamma_\phi Q \|r\|) - \delta\end{aligned}\quad (40)$$

$$\begin{aligned}\dot{L} = & \frac{1}{2}r^T (\dot{B} - 2C_m)r - r^T K_g r - r^T (F_f + D + \varepsilon(y)) \\ & - \frac{\hat{\beta}^2 \|r\|^2}{\hat{\beta} \|r\| + \delta} - \text{tr}(\tilde{\phi}^T Q \|r\|) - \delta\end{aligned}\quad (41)$$

Using Property 2, we have

$$\begin{aligned}\dot{L} = & -r^T K_g r - r^T (F_f + D + \varepsilon(y)) \\ & - \frac{\hat{\beta}^2 \|r\|^2}{\hat{\beta} \|r\| + \delta} - \text{tr}(\tilde{\phi}^T Q \|r\|) - \delta\end{aligned}\quad (42)$$

Now using Eqs. (31) and (32), we find that

$$\begin{aligned}-r^T (F_f + D + \varepsilon(y)) & \leq \|r\| \|F_f + D + \varepsilon(y)\| \leq \|r\| \beta \\ & = \|r\| Q^T \phi = \|r\| Q^T (\tilde{\phi} + \hat{\phi})\end{aligned}\quad (43)$$

Using inequality given by Eq. (43) in Eq. (42), we get

$$\begin{aligned}\dot{L} \leq & -r^T K_g r + \|r\| Q^T (\tilde{\phi} + \hat{\phi}) - \frac{\hat{\beta}^2 \|r\|^2}{\hat{\beta} \|r\| + \delta} \\ & - \text{tr}(\tilde{\phi}^T Q \|r\|) - \delta\end{aligned}\quad (44)$$

Since $\hat{\beta} = Q^T \hat{\phi}$, we have the following expression from Eq. (44)

$$\begin{aligned}\dot{L} \leq & -r^T K_g r + Q^T \tilde{\phi} \|r\| + Q^T \hat{\phi} \|r\| - \frac{(Q^T \hat{\phi})^2 \|r\|^2}{Q^T \hat{\phi} \|r\| + \delta} \\ & - \text{tr}(\tilde{\phi}^T Q \|r\|) - \delta\end{aligned}\quad (45)$$

$$\dot{L} \leq -r^T K_g r + Q^T \hat{\phi} \|r\| - \frac{(Q^T \hat{\phi})^2 \|r\|^2}{Q^T \hat{\phi} \|r\| + \delta} - \delta\quad (46)$$

$$\dot{L} \leq -r^T K_g r - \frac{\delta^2}{Q^T \hat{\phi} \|r\| + \delta}\quad (47)$$

$$\dot{L} \leq -\alpha_{\min} \|r\|^2\quad (48)$$

where α_{\min} is minimum singular value of matrix K_g . Since we have $L(r(t), \tilde{W}, \tilde{\phi}) > 0$ and Eq. (48) gives $\dot{L}(r(t), \tilde{W}, \tilde{\phi}) \leq 0$, from this we have r, \tilde{W} and $\tilde{\phi}$ and hence $\hat{W}, \hat{\phi}$ are bounded. Now we define a new function $\theta(t) = \alpha_{\min} \|r\|^2 \leq -\dot{L}$ and taking integration of this w.r.t

time, we have

$$\int_0^t \theta(t) dt \leq L(0) - L(t) = L(r(0), \tilde{W}, \tilde{\phi}) - L(r(t), \tilde{W}, \tilde{\phi})\quad (49)$$

Since $L(r(0), \tilde{W}, \tilde{\phi})$ is bounded function and $L(r(t), \tilde{W}, \tilde{\phi})$ being bounded and decreasing function, we find that

$$\lim_{t \rightarrow \infty} \int_0^t \theta(t) dt < \infty\quad (50)$$

Further using Eqs. (21) and (7), we get

$$r = O^+[S^+(\dot{S}x - v_f) + S^-(\dot{x} - v_x)] + O^-\dot{\tilde{q}}\quad (51)$$

Using Eq. (10), we have

$$r = O^+[\dot{x} - S^+v_f - S^-v_x] + O^-\dot{\tilde{q}}\quad (52)$$

$$r = O^+\dot{x} - O^+(S^+v_f + S^-v_x) + O^-\dot{q} - O^-q_d\quad (53)$$

Using Eq. (15), we have

$$r = \dot{q} - O^+(S^+v_f + S^-v_x) - O^-q_d\quad (54)$$

Since we have considered that the joints are revolute, therefore O^+, O^-, S^+, S^-, F, x are bounded. Therefore, v_f and v_x given by Eq. (22) are bounded. Thus q_d and \dot{q} are bounded. If we take the derivative of r in Eq. (54) and using Property 1, one can find that \dot{r} and hence $\dot{\theta}(t)$ is bounded. It shows that $\theta(t)$ is uniform continuous and from Barbalat's Lemma [26] $\lim_{t \rightarrow \infty} \theta(t) = 0 \Rightarrow r \rightarrow 0$ as $t \rightarrow \infty$. This proves that the system is asymptotically stable. Now, multiplying Eq. (21) by SO , we have

$$SO r = \dot{F} - v_f \rightarrow 0\quad (55)$$

Now multiplying Eq. (21) by O , we get

$$Or = S^-(\dot{x} - v_x) \rightarrow 0\quad (56)$$

Using Eqs. (21), (54) and (55), we get

$$O^-\dot{\tilde{q}} \rightarrow 0\quad (57)$$

Thus, taking into consideration Eqs. (55), (56), (22) and (23), we have $\dot{F} + \lambda \tilde{F} \rightarrow 0$ and $S^-\dot{\tilde{x}} + \lambda S^-\tilde{x} \rightarrow 0$. Hence the position error $S^-\tilde{x}$, force error \tilde{F} as well as redundant joints velocity $O^-\dot{\tilde{q}}$ tends to zero. \square

5 Simulation studies

In this section, the simulation results are provided for a two link rigid robot manipulator whose mathematical model is expressed as

$$\begin{bmatrix} B_{11} & B_{12} \\ B_{21} & B_{22} \end{bmatrix} \begin{bmatrix} \ddot{q}_1 \\ \ddot{q}_2 \end{bmatrix} + \begin{bmatrix} C_{m11} & C_{m12} \\ C_{m21} & C_{m22} \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix} + \begin{bmatrix} G_1 \\ G_2 \end{bmatrix} + \begin{bmatrix} F_{f1} \\ F_{f2} \end{bmatrix} + \begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} \tau_1 \\ \tau_2 \end{bmatrix} + O^T \bar{F} \quad (58)$$

where

$$\begin{aligned} B_{11} &= l_2^2 m_2 + l_1^2 (m_1 + m_2) + 2l_1 l_2 m_2 \cos(q_2) \\ B_{12} &= l_2^2 m_2 + l_1 l_2 m_2 \cos(q_2) \\ B_{21} &= l_2^2 m_2 + l_1 l_2 m_2 \cos(q_2) \\ B_{22} &= l_2^2 m_2 \\ C_{m11} &= -l_1 l_2 m_2 \sin(q_2) \dot{q}_2 \\ C_{m12} &= -l_1 l_2 m_2 \sin(q_2) (\dot{q}_1 + \dot{q}_2) \\ C_{m21} &= l_1 l_2 m_2 \sin(q_2) \dot{q}_1 \\ C_{m22} &= 0 \\ G_1 &= l_1 g_0 (m_1 + m_2) \cos(q_1) + l_2 m_2 g_0 \cos(q_1 + q_2) \\ G_2 &= l_2 m_2 g_0 \cos(q_1 + q_2) \\ F_f(q) &= 5.3 \dot{q}_1 + 2.4 \dot{q}_2 \\ D_1 &= 80 \cos(2t) \text{ and } D_2 = 80 \sin(2t) \end{aligned}$$

The parameters given as $\hat{m}_1 = 15.61 \text{ kg}$, $\hat{m}_2 = 11.36 \text{ kg}$, $\hat{l}_1 = 0.432 \text{ m}$, $\hat{l}_2 = 0.432 \text{ m}$ are masses and lengths of link 1 and 2 respectively with $g_0 = 9.8 \text{ m/s}^2$.

We take the contact force $F = \kappa(x - x_{1c})$ in the x_1 direction where $\kappa = 10^4$ and $x_{1c} = 0.61 \text{ m}$.

The desired trajectory is taken as $x_{2s} = 0.5[1 - \exp(-t)]$ in x_2 direction.

The desired force is taken as $F_s = 20[1 - 0.5 \sin(t)]$.

Also, $S^+ = \frac{1}{\kappa}$, $S^- = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$, $O^+ = O^{-1}$ and $O^- = 0$. The controller parameters are $\lambda = 100$, $K_g = 200I_2$.

RBFNN is constructed using 10 nodes, the central positions c_i takes values from $[-2, 2]^7$ and the spread factors are taken as $\sigma_i = 0.2$. The matrices in the weight updates law are $\Gamma_W = 10I_{10}$ and $\Gamma_\phi = 5I_4$.

The simulation is exposed for 10 seconds. To show the effectiveness of the proposed control scheme, the simulation studies have been performed with three different controllers i.e. computed torque type model based controller [12], FFNN based model free controller [18] and the proposed controller, i.e. a hybrid controller consisting of model based controller together with RFNN based model free controller, in a comparative manner. The Figs. 1 and 2 are produced to show the tracking of desired and actual force in Fig. 1 as well force tracking in Fig. 2 respectively, with all the three different

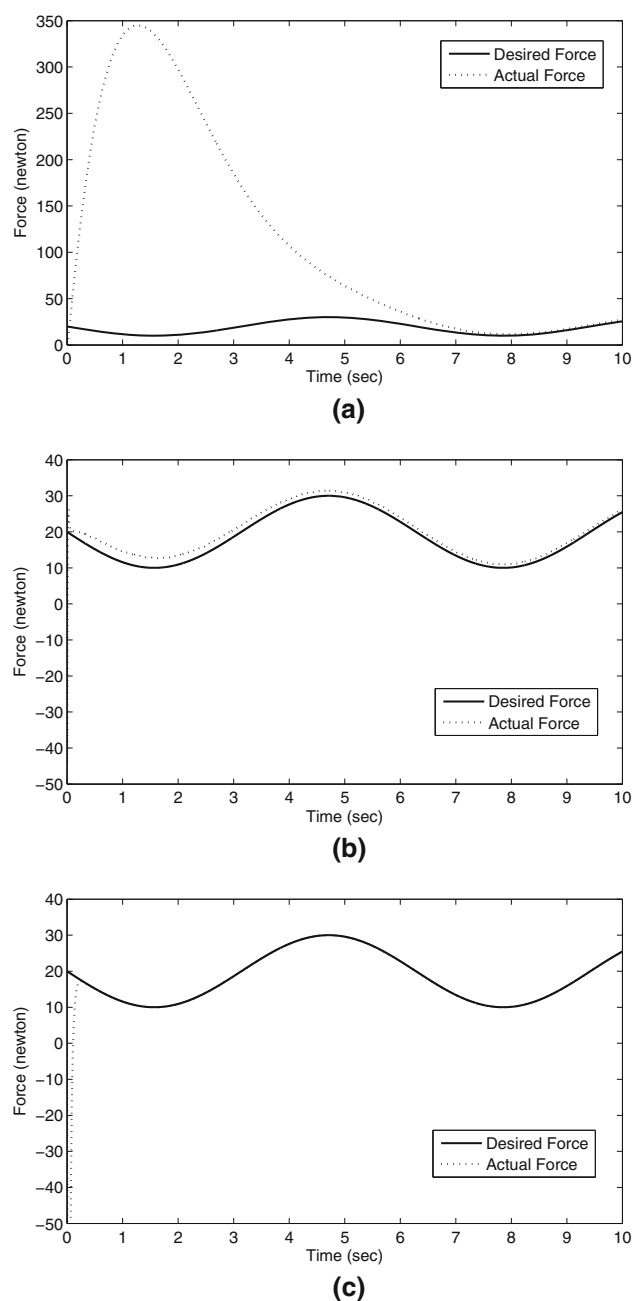
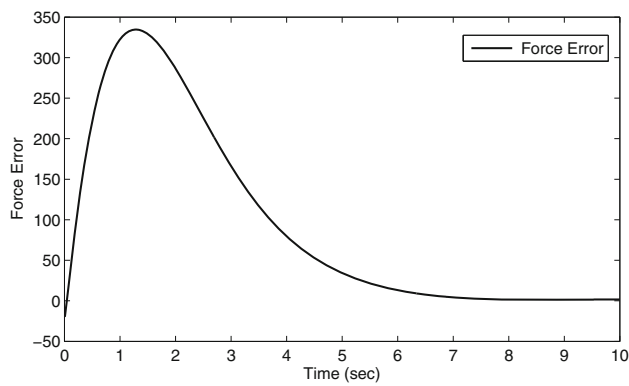
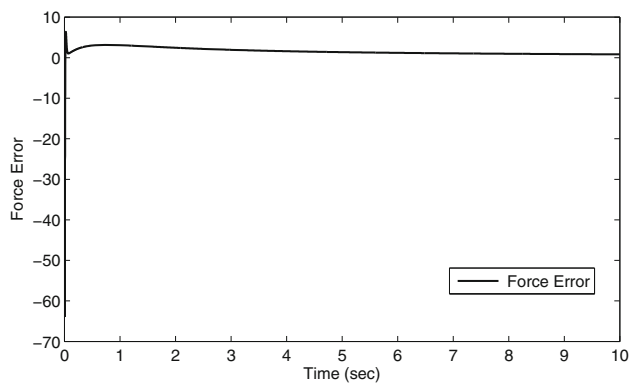


Fig. 1 Desired and actual force tracking with **a** model based CT controller, **b** FFNN based model free controller, **c** proposed controller

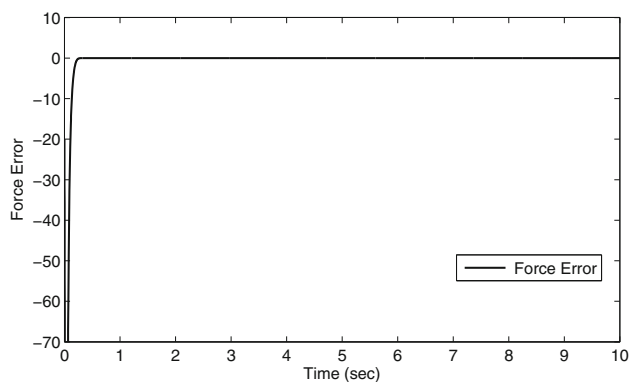
controllers. The end effector trajectory tracking is shown in Fig. 3 with all the three controllers. From these figures, it is clear that the CT controller is unable to deal with uncertainties and disturbances, FFNN based model free controller achieves the desired tracking but better performance is achieved with the proposed controller as is clear from the comparison of the Figs. 1, 1 and 3. From these figures, one can conclude that the performance is enhanced with the proposed controller. The joint trajectories and the joint velocities with



(a)



(b)



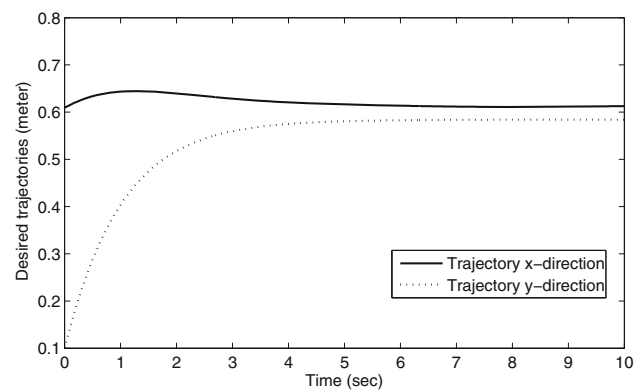
(c)

Fig. 2 Force tracking error with **a** model based CT controller, **b** FFNN based model free controller, **c** proposed controller

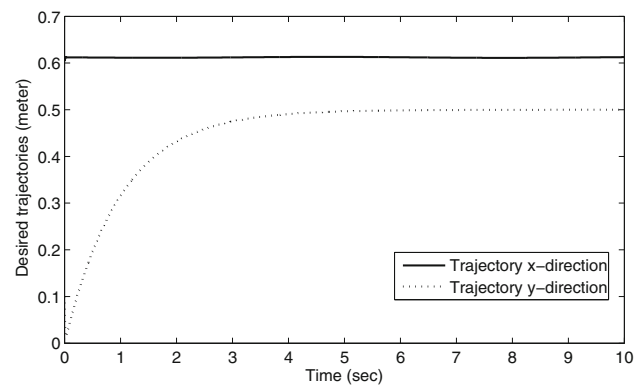
all the three controllers are shown by Figs. 4 and 5 respectively.

6 Conclusion

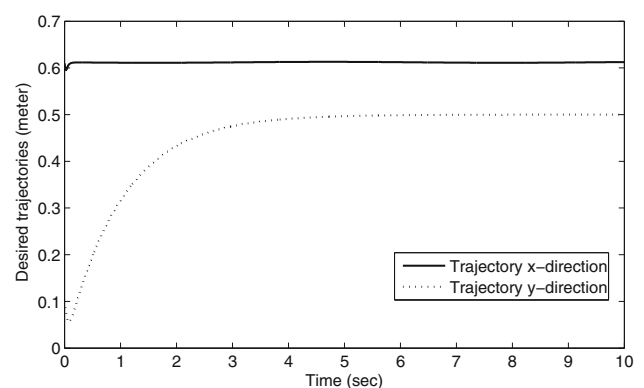
In this paper, a new intelligent control scheme is proposed for hybrid force and position control of robot manipulators. The control scheme utilized the merits of both the model



(a)



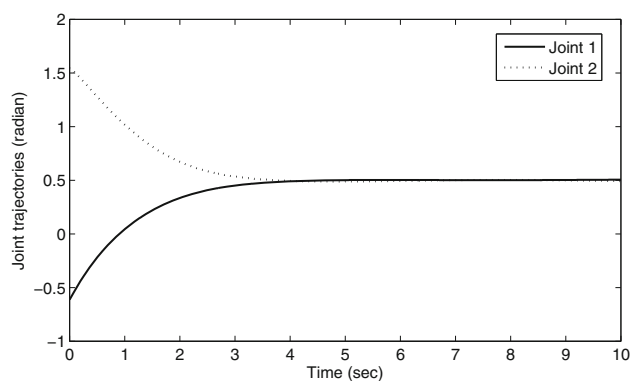
(b)



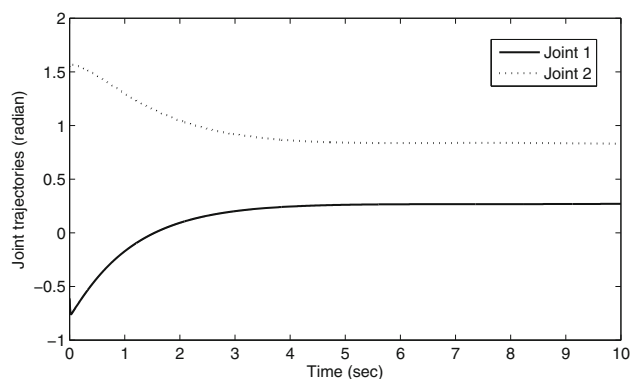
(c)

Fig. 3 End effector trajectory tracking with **a** model based CT controller, **b** FFNN based model free controller, **c** proposed controller

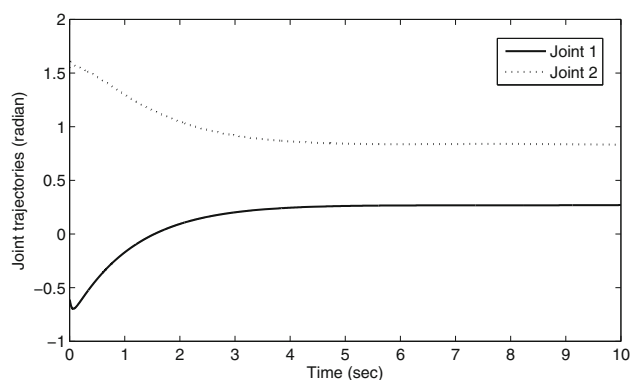
based computed torque type control and neural network based model free control techniques. The controller achieves not only the tracking of desired internal forces but also the tracking of end-effector trajectory effectively. The controller learns the uncertainties in online manner with the help of RBF neural network. The unknown bounds on uncertainties and the neural network approximation error are compensated effectively with the adaptive bound part of the controller. The Lyapunov stability theory is used to show that the proposed



(a)



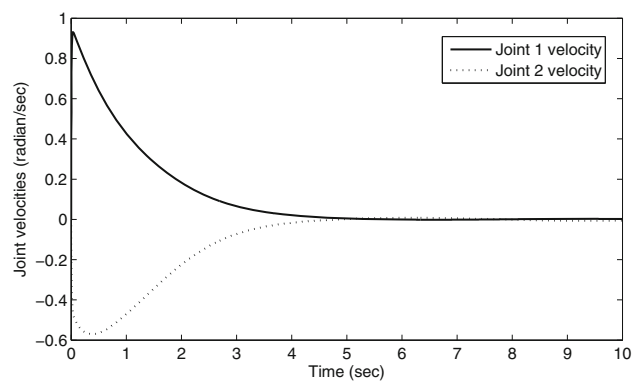
(b)



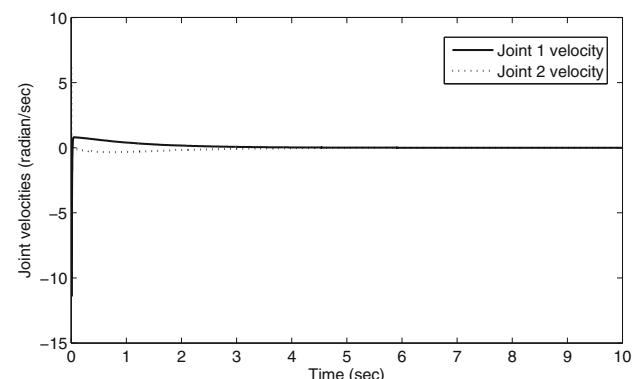
(c)

Fig. 4 Joint trajectories with **a** model based CT controller, **b** FFNN based model free controller, **c** proposed controller

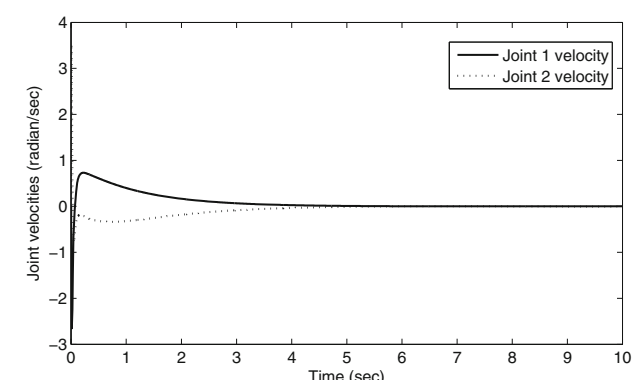
controller is stable and the errors converge asymptotically. Finally, through the numerical simulation, the effectiveness of proposed controller is proved in a comparative manner with model based and model free controllers. From overall analysis and simulation studies, it is concluded that the proposed controller is able to deal with uncertainties and disturbances in effective manner and the tracking performance is enhanced with the proposed controller as compare to the model based and model free controllers.



(a)



(b)



(c)

Fig. 5 Joint velocities with **a** model based CT controller, **b** FFNN based model free controller, **c** proposed controller

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