

Lesson 3: Factoring Quadratics when $a = 1$

Quadratics in the form $x^2 + bx + c$

$$y = a(x - r)(x - s)$$

When we're factoring quadratics, we create two factors: $(x \text{ + } r)$ and $(x \text{ + } s)$

$r + s = b$ and $r \times s = c$ (in this case, r and s are integers)

Some trends to watch for:

- If b and c are both positive, then: $(x+r)(x+s)$
- If b and c are both negative, then: $(x-r)(x+s)$, but $r > s$
- If b is positive and c is negative, then: $(x+r)(x-s)$, where $r > s$
- If b is negative and c is positive, then $(x-r)(x-s)$

* If there is a common factor, first divide it out!

Ex 1 use the constant (c) and coefficient (b) to factor:

$$ax^2 + bx + c$$

$$x^2 + 10x + 24$$

$$= (x + 4)(x + 6)$$

$$= x^2 + 6x + 4x + 24$$

$$= x^2 + 10x + 24$$

Both b and c are positive, so:

Both r and s are also positive.

To find ^{and s} r you need two numbers that add to: 10

and multiply to:

$$24$$

$$\begin{array}{r} 24 \\ \diagup \quad \diagdown \\ 1 \times 24 \\ 2 \times 12 \\ 3 \times 8 \\ \hline 4 \times 6 = 24 \\ \hline 4 + 6 = 10 \end{array}$$

Try using the acronym M A N (Multiply to equal "c", Add to equal "b", the Numbers are)

$$M: 24$$

$$A: 10$$

$$N: 4 \text{ and } 6$$

Ex 2: Factor out the GCF first, before factoring the quadratic

$$\begin{aligned} \text{a) } 6x^3 - 42x^2 - 48x \\ &= 6x(x^2 - 7x - 8) \\ &= 6x(x - 8)(x + 1) \end{aligned}$$

* don't forget to find the **GCF** first and take it out!

$$\begin{aligned} M &: -8 \\ A &: -7 \\ N &: -8, 1 \end{aligned}$$

$$\begin{array}{c} -8 \\ \swarrow \quad \searrow \\ (-8) \quad (+1) \end{array}$$

Check by expanding:

$$\begin{aligned} &6x(x - 8)(x + 1) \\ &= 6x(x^2 + 1x - 8x - 8) \\ &= 6x(x^2 - 7x - 8) \\ &= 6x^3 - 42x^2 - 48x \end{aligned}$$

$$b) 4x^3 - 8x^2 - 60x$$

$$= 4x(x^2 - 2x - 15)$$

-2

-15

$$\begin{array}{rcl} -15 & + & 1 = -14 \\ -5 & + & 3 = -2 \\ \hline \end{array}$$

$$\therefore y = 4x(x-5)(x+3)$$

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