

Lesson 4: Quadratics in Vertex Form

By the end of today you should be able to:

- Recognize the vertex form of a quadratic
- Apply transformations to the graph of $y = x^2$

Vertex Form: A Quadratic function in the form
vertex is (h,k) .

$$y = a(x - h)^2 + k, \text{ where the}$$

To graph a quadratic when it is vertex form, you must apply the transformations (movements up or down, left or right, stretches or compressions and reflections) to the original graph ($y = x^2$)

Example 1: use a data table to graph the function
graph your data.

$$y = 2(x + 3)^2 + 5 \text{ and then}$$

x	y
-5	5
-4	7
-3	13
-2	
-1	
0	
1	

$$2(-3+3)^2 + 5$$

$$2(0)^2 + 5$$

$$y = 2(-2+3)^2 + 5$$

$$= 2 + 5 = 7$$

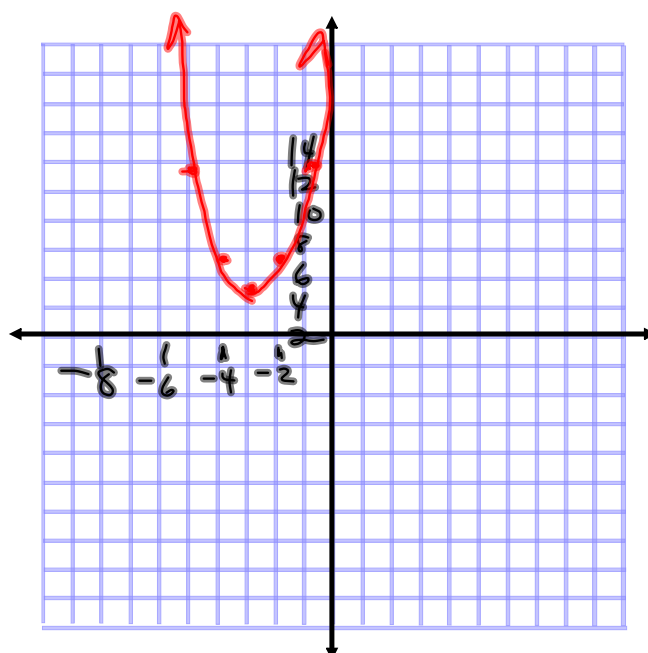
$$y = 2(-1+3)^2 + 5$$

$$= 2(4) + 5$$

$$= 13$$

$$y = 2(-4+3)^2 + 5$$

$$= 2 + 5 = 7$$



Example 2: using reasoning to graph quadratics in vertex form. Graph

$$y = -3(x - 2)^2 - 7$$

move right 2 units.

Step 1: create a table of values for $y = x^2$

Step 2: There is a vertical stretch by a factor of 3 and a reflection in the x-axis.

Make a table of values for $y = -3x^2$

Step 3: the x values increase by 2 since $h=2$, the y values decrease by 7, since $k=-7$. Make a table of values that has all of your x values increasing by 2 and all of your y values decreasing by 7 (use the table you made in step 2 as your starting point because it has been stretched and reflected).

STEP 1: $y = x^2$

x	y
2	4
1	1
0	0
-1	1
-2	4

STEP 2: $y = -3x^2$

x	y
2	-12
1	-3
0	0
-1	-3
-2	-12

STEP 3:

x	y
4	-19
3	-10
2	-7
1	-10
0	-19

