Regression

Put your name here
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Introduction

In this assignment we will learn how to run a regression analysis. Regression provides a model for the linear relationship between two numerical variables.

Instructions

Presumably, you have already created a new project and downloaded this file into it. From the Run menu above, select Run All to run all existing code chunks.

When prompted to complete an exercise or demonstrate skills, you will see the following lines in the document:

ANSWER ____

These lines demarcate the region of the R Markdown document in which you are to show your work.

Sometimes you will be asked to add your own R code. That will appear in this document as a code chunk with a request for you to add your own code, like so:

Add code here

Be sure to remove the line # Add code here when you have added your own code. You should run each new code chunk you create by clicking on the dark green arrow in the upper-right corner of the code chunk.

Sometimes you will be asked to type up your thoughts. That will appear in the document with the words, "Please write up your answer here." Be sure to remove the line "Please write up your answer here" when you have written up your answer. In these areas of the assignment, please use contextually meaningful full sentences/paragraphs (unless otherwise indicated) and proper spelling, grammar, punctuation, etc. This is not R code, but rather a free response section where you talk about your analysis and conclusions. You may need to use inline R code in these sections.

When you are finished with the assignment, knit to PDF and proofread the PDF file **carefully**. Do not download the PDF file from the PDF viewer; rather, you should export the PDF file to your computer by selecting the check box next to the PDF file in the Files pane, clicking the More menu, and then clicking Export. Submit your assignment according to your professor's instructions.

Load Packages

We load the standard mosaic package as well as the openintro package for the bdims data, the reshape2 package for the tips data, and the MASS package for the Rubber data. The broom package gives us tidy output.

library(openintro)
library(reshape2)
library(MASS)

```
library(broom)
library(mosaic)
```

Research question

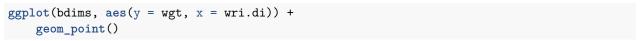
Can you predict someone's weight from their wrist diameter?

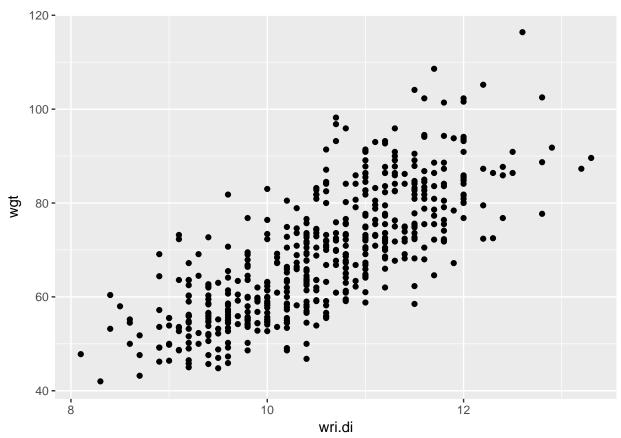
Regression

When we have a linear relationship between two numerical variables, it's helpful to model this relationship with an actual straight line. Such a line is called a regression line, or a best-fit line, or sometimes a least-squares line.

The mathematics involved in figuring out what this line should be is more complicated than we cover in this course. But R will do all the complicated calculations for us.

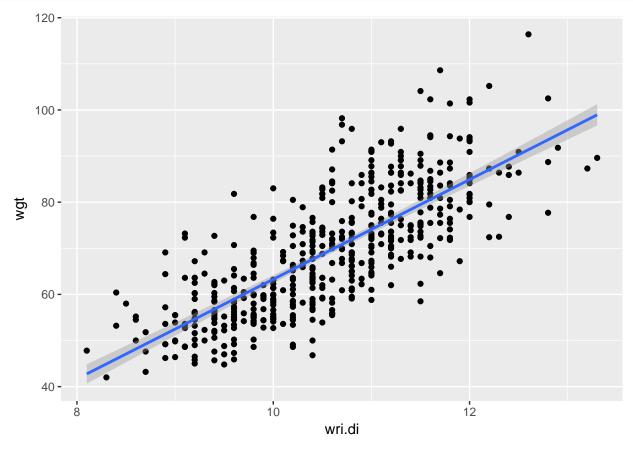
Let's look at a scatterplot of data from the bdims data set. These measurements come from 507 physically active individuals (a mix of males and females). The weight wgt is measured in kilograms and the wrist diameter wri.di is measured in centimeters as the sum of both wrists.





If certain conditions are met, we can graph a regression line; just add a geom_smooth layer to the scatterplot:

```
ggplot(bdims, aes(y = wgt, x = wri.di)) +
   geom_point() +
   geom_smooth(method = "lm")
```



The method = "lm" argument is telling ggplot to use a "linear model".

Of all possible lines, the blue line comes the closest to each point in the scatterplot. If we wiggled the line a little bit, it might get closer to a few points, but the net effect would be to make it further from other points. This is the mathematically optimal line of best fit. The gray region around the line is called a confidence band; the "true" population regression line is likely to lie inside this gray area.

What is the equation of this line? In your algebra class you learn that a line takes the form y = mx + b where m is the slope and b is the y-intercept. Statisticians write the equation in a slightly different form:

$$\hat{y} = b_0 + b_1 x.$$

The intercept is b_0 and the slope is b_1 . We use \hat{y} instead of y because when we plug in values of x, we do not get back the exact values of y from the data. The line, after all, does not actually pass through most (if any) actual data points. Instead, this equation gives us "predicted" values of y that lie on the regression line. These predicted y values are called \hat{y} .

To run a regression analysis, we use the 1m command in R. (1m stands for "linear model".) As usual, we then use the tidy command to make the output a little cleaner. There is one tiny change we'll make to the tidy command: unlike previous hypothesis tests we've seen, the tidy command for 1m does not automatically include a confidence interval. So we'll need to add an argument conf.int = TRUE.

```
wgt_wrist_lm <- lm(wgt ~ wri.di, data = bdims)
wgt_wrist_tidy <- tidy(wgt_wrist_lm, conf.int = TRUE)
wgt_wrist_tidy</pre>
```

Interpreting the coefficients

2 10.00916 11.60174

Look at the output of the tidy command above.

The estimate column of the output gives us the intercept and slope for the model regression line.

```
wgt_wrist_tidy$estimate[1]
```

```
## [1] -44.77

wgt_wrist_tidy$estimate[2]
```

```
## [1] 10.80545
```

The intercept is -44.7700047 and the slope is 10.8054466.

Therefore, the equation of the regression line could be written

term estimate std.error statistic

1 (Intercept) -44.77000 4.2900420 -10.43580

$$\hat{y} = -44.77 + 10.81x.$$

When we report the equation of the regression line, we typically use words instead of \hat{y} and x to make the equation more interpretable in the context of the problem. For example, for this data, we would write the equation as

$$\widehat{weight} = -44.77 + 10.81wrist.$$

The slope b_1 is always interpretable. This model predicts that one unit of increase in the x-direction corresponds to a change of 10.81 units in the y-direction. Let's phrase it this way, using inline code:

The model predicts that an increase of one cm in wrist diamater corresponds to a weight increase of 10.8054466 kg.

The intercept b_0 is a different story. There is always a literal interpretation:

The model predicts that someone with a wrist diameter of zero will weigh -44.7700047 kg.

It is true that the model makes that prediction, so the preceding sentence is technically correct. However, that prediction is nonsensical. Aside from the fact that it is impossible for a wrist to have zero diameter and impossible for a weight to be negative, this is *extrapolation*—in other words, a prediction outside the range of the data.

The rest of the tidy output involves inference on the two parameters (intercept and slope). We'll get back to that later.

Checking conditions

We need to be careful here. We have not checked any conditions; therefore, it is inappropriate to fit a regression line at this point. Once the line is seen, it cannot easily be "unseen", and it's crucial that you don't trick your reader into believing there is a linear relationship before checking the conditions that justify that belief.

The regression line we saw above makes no sense unless we know that regression is appropriate. The conditions for running a regression analysis include all the conditions you checked for a correlation analysis: "Random" and "10%" to ensure a good sample, "Linear association" to make sure our association follows a linear pattern, and an "Outlier" check because outliers can be bad. Let's check what he have so far:

- Random
 - We are not told how the sample was collected, so we can't say if it's a representative sample of all
 physically active individuals. We'll proceed with caution.
- 10%
 - Surely 507 people are less than 10% of all physically active people.
- Linear association
 - The scatterplot showed a clear linear relationship between wrist diameter and weight.
- Outliers
 - There are no apparent outliers in the scatterplot.

However, there is an additional condition to check to ensure that our regression model is appropriate. We need to check for...

• Patterns in the residuals

We discuss this below.

Residuals

Residuals are the vertical distances from each data point to the regression line. More formally, we're saying that the residual e is given by the following formula:

$$e = y - \hat{y}$$
.

We know that some of the points are going to lie above the line (positive residuals) and some of the points will lie below the line (negative residuals). What we need is for there not to be any pattern among these residuals.

To calculate the residuals, we introduce a new function from the broom package. Whereas tidy serves up information about the parameters of interest (in this case, the intercept and the slope of the regression line), augment gives us extra information for each data point.

```
wgt_wrist_aug <- augment(wgt_wrist_lm)
head(wgt_wrist_aug)</pre>
```

```
##
                  .fitted
                                         .resid
      wgt wri.di
                            .se.fit
                                                       .hat
                                                              .sigma
## 1 65.6
            10.4 67.60664 0.3867199
                                     -2.006639 0.002017451 8.617911
## 2 71.8
            11.8 82.73426 0.6371288 -10.934265 0.005476013 8.604526
## 3 80.7
            10.9 73.00936 0.4088942
                                      7.690637 0.002255444 8.611549
## 4 72.6
            11.2 76.25100 0.4660527
                                     -3.650997 0.002930084 8.616836
                                     -1.773175 0.004450089 8.618012
## 5 78.8
            11.6 80.57318 0.5743536
## 6 74.8
            11.5 79.49263 0.5447794
                                     -4.692631 0.004003607 8.615830
           .cooksd .std.resid
## 1 0.00005501433 -0.2332990
```

```
## 2 0.00446470911 -1.2734648
## 3 0.00090385322 0.8942473
## 4 0.00026499134 -0.4246720
## 5 0.00009521952 -0.2064074
## 6 0.00059944407 -0.5461256
```

Examine the first few rows of output. The first two columns are the actual data values we started with. But now we've "augmented" the original data with some new stuff too. The third column—here called .fitted—is \hat{y} , or the point on the line that corresponds to the given x value. Let's check and make sure this is working as advertised.

The regression equation from above is

$$\widehat{weight} = -44.77 + 10.81wrist.$$

The first subject listed in row 1 has wrist diameter 10.4 cm. Plug that value into the equation above:

$$\widehat{weight} = -44.77 + 10.81(10.4) = 67.6.$$

The model predicts that a person with a wrist diameter of 10.4 will weigh 67.6 kg. The first number in the .fitted column is 67.60664, so that's correct.

Now skip over to the fifth column of the augment output, the one that says .resid. If this is the residual e, then it should be $y - \hat{y}$. Since y is the actual value of wgt and \hat{y} is the value predicted by the model, we should get for the first row of output

$$e = y - \hat{y} = 65.6 - 67.60664 = -2.00664.$$

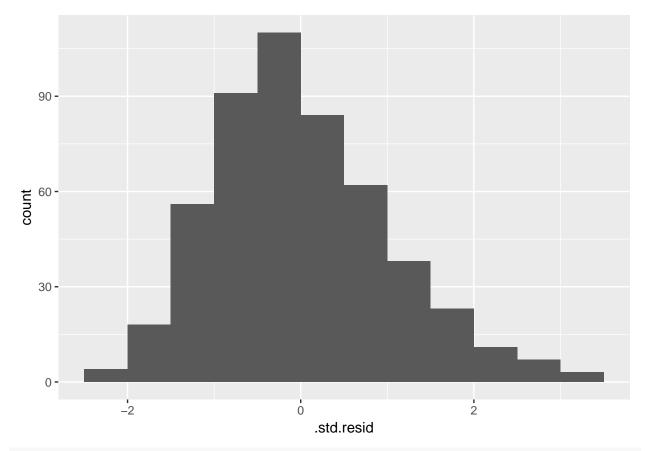
Yup, it works!

Skip to the last column of the output .std.resid. These are similar to z-scores for the residuals, so they're easy to interpret. One can examine either the raw residuals (stored in .resid) or the standardized residuals (.std.resid), but we'll do the latter.

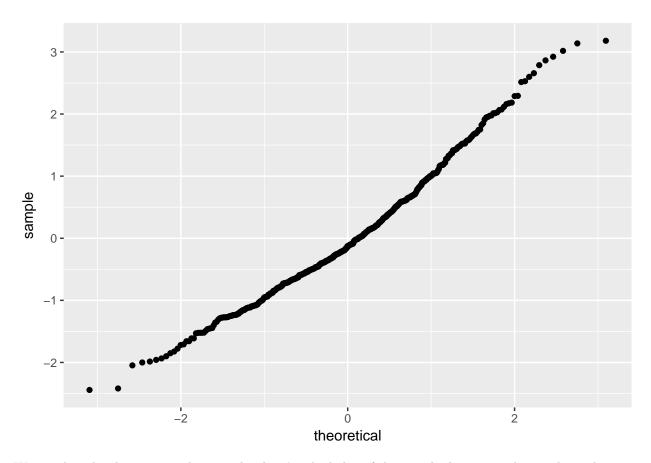
To check for patterns in the residuals, we'll use several different plots. First, we want our residuals to be normally distributed. We check this with a histogram and a QQ plot, as usual.

```
ggplot(wgt_wrist_aug, aes(x = .std.resid)) +
   geom_histogram(binwidth = 0.5, boundary = 0)
```

¹The real story is quite a bit more complicated than that, but there is little harm in thinking of these as if they were z-scores.



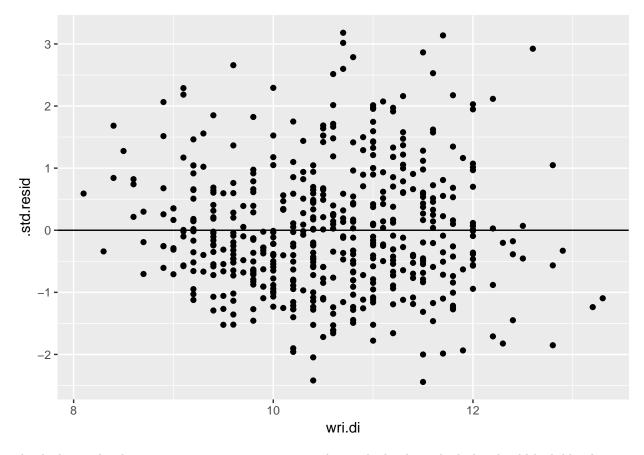
ggplot(wgt_wrist_aug, aes(sample = .std.resid)) +
 geom_qq()



We see that the shape is mostly normal. There's a little bit of skew in the histogram, but nothing alarming. We should also create a *residual plot*, which looks at the residuals above each value along the x-axis. (In

We should also create a residual plot, which looks at the residuals above each value along the x-axis. (In the command below, we also add a horizontal reference line so that it is clear which points have positive or negative residuals.)

```
ggplot(wgt_wrist_aug, aes(y = .std.resid, x = wri.di)) +
   geom_point() +
   geom_hline(yintercept = 0)
```

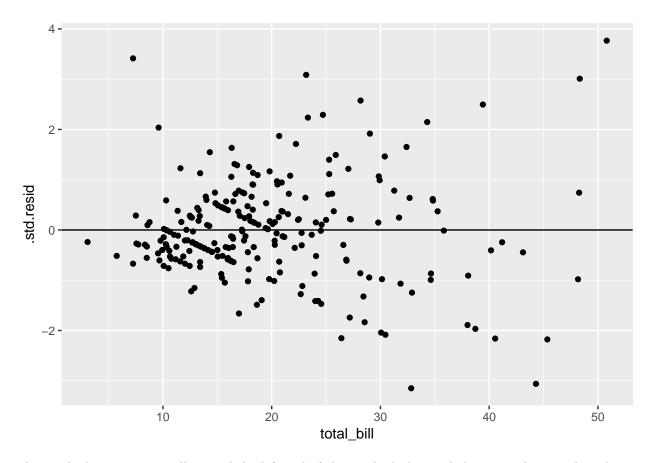


This looks good. There are no systematic patterns in the residuals. A residual plot should look like the most boring plot you've ever seen.

Residual patterns that are problematic often involve curved data (where the dots follow a curve around the horizontal reference line instead of spreading evenly around it) and *heteroscedasticity*, which is a fanning out pattern.

As an example of the latter, let's look at the residual plot for the tipping example from the correlation module.

```
tips <- reshape2::tips
tip_bill <- lm(tip ~ total_bill, data = tips)
tip_bill_aug <- augment(tip_bill)
ggplot(tip_bill_aug, aes(y = .std.resid, x = total_bill)) +
    geom_point() +
    geom_hline(yintercept = 0)</pre>
```



The residuals are quite small toward the left end of the residual plot, and then spread out and get larger toward the right end. This is a violation of the "patterns in the residuals" condition. It would be problematic to pursue a regression analysis of the tip data even though correlation was okay to report.

R^2

The correlation coefficient R is of limited utility. The number doesn't have any kind of intrinsic meaning; it can only be judged by how close it is to 0 or 1 (or -1) in conjunction with a scatterplot to give you a sense of the strength of the correlation. In particular, some people try to interpret R as some kind of percentage, but it's not.

On the other hand, R^2 can be interpreted as a percentage. It represents the percent of variation in the y variable that can be explained by variation in the x variable.

Here we introduce the last of the broom functions: glance. Whereas tidy reports summary statistics related to parameters of the model, and augment reports values associated to each data point separately, the glance function gathers up summaries for the entire model.

```
wgt_wrist_glance <- glance(wgt_wrist_lm)</pre>
wgt_wrist_glance
##
   r.squared adj.r.squared
                       sigma statistic
 1 0.5846215
             0.5837989 8.609838
                           710.7585
##
##
##
 logLik
                AIC
                       BIC deviance df.residual
    2 -1809.923 3625.846 3638.531 37435.3
                                      505
```

A more advanced statistics course might discuss the other model summaries present in the glance output. The R^2 value is stored in wgt_wrist_glance\$r.squared. Its value is 0.585. We will word it this way:

58.4621457% of the variability in weight can be explained by variability in wrist diameter.

Thus, R^2 is a measure of the fit of the model. High values of R^2 mean that the line predicts the data values closely, whereas lower values of R^2 mean that there is still a lot of variability left in the residuals (presumably due to other factors that are not measured here). What we're saying here is that there are lots of factors that account for variability in weight, and not all that can be explained by the variability in wrist diameter.

Inference for the regression slope

The sample gives us the regression equation

$$\hat{y} = b_0 + b_1 x.$$

The idea of inference is that this line is meant to be an estimate of a true regression line

$$\hat{y} = \beta_0 + \beta_1 x.$$

In other words, if we plotted weight against wrist diameters for everybody in the world, there is, in theory, some perfect regression line that goes through the middle of all those points. And that ideal intercept and slope are the true population parameters β_0 and β_1 . (β is the Greek letter "beta".)

We have already seen that the intercept is not particularly interesting, so we restrict attention to inference for the slope. As with correlation, the full inferential rubric for the regression slope is a little overkill. Nevertheless, the rubric forces us to be careful to identify our sample and population and state proper conclusions.

The sampling distribution for the slope parameter is somewhat complicated. There is a formula for the standard error of the sample slope estimates, and with that, one can compute t scores that are distributed as a t model with n-2 degrees of freedom. We won't get into any of the mathematical details here.

Also note that a typical regression analysis will start by checking conditions so that the regression line can be calculated and graphed. Therefore, we will work through the rubric under the assumption that the conditions have already been checked.

Exploratory data analysis

Use data documentation (help files, code books, Google, etc.), the View command, the str command, and other summary functions to understand the data.

[You should type ?bdims at the Console to read the help file and use View to look at the spreadsheet view of the data.]

```
str(bdims)
```

```
507 obs. of 25 variables:
  'data.frame':
   $ bia.di: num
                   42.9 43.7 40.1 44.3 42.5 43.3 43.5 44.4 43.5 42 ...
                  26 28.5 28.2 29.9 29.9 27 30 29.8 26.5 28 ...
   $ bii.di: num
   $ bit.di: num
                  31.5 33.5 33.3 34 34 31.5 34 33.2 32.1 34 ...
                  17.7 16.9 20.9 18.4 21.5 19.6 21.9 21.8 15.5 22.5 ...
   $ che.de: num
   $ che.di: num
                  28 30.8 31.7 28.2 29.4 31.3 31.7 28.8 27.5 28 ...
   $ elb.di: num 13.1 14 13.9 13.9 15.2 14 16.1 15.1 14.1 15.6 ...
##
                  10.4 11.8 10.9 11.2 11.6 11.5 12.5 11.9 11.2 12 ...
   $ wri.di: num
   $ kne.di: num 18.8 20.6 19.7 20.9 20.7 18.8 20.8 21 18.9 21.1 ...
```

```
$ ank.di: num 14.1 15.1 14.1 15 14.9 13.9 15.6 14.6 13.2 15 ...
   $ sho.gi: num 106 110 115 104 108 ...
##
## $ che.gi: num 89.5 97 97.5 97 97.5 ...
## $ wai.gi: num
                  71.5 79 83.2 77.8 80 82.5 82 76.8 68.5 77.5 ...
   $ nav.gi: num 74.5 86.5 82.9 78.8 82.5 80.1 84 80.5 69 81.5 ...
##
   $ hip.gi: num 93.5 94.8 95 94 98.5 95.3 101 98 89.5 99.8 ...
   $ thi.gi: num 51.5 51.5 57.3 53 55.4 57.5 60.9 56 50 59.8 ...
##
   $ bic.gi: num
                  32.5 34.4 33.4 31 32 33 42.4 34.1 33 36.5 ...
##
   $ for.gi: num
                  26 28 28.8 26.2 28.4 28 32.3 28 26 29.2 ...
##
   $ kne.gi: num 34.5 36.5 37 37 37.7 36.6 40.1 39.2 35.5 38.3 ...
   $ cal.gi: num 36.5 37.5 37.3 34.8 38.6 36.1 40.3 36.7 35 38.6 ...
##
                  23.5 24.5 21.9 23 24.4 23.5 23.6 22.5 22 22.2 ...
   $ ank.gi: num
   $ wri.gi: num 16.5 17 16.9 16.6 18 16.9 18.8 18 16.5 16.9 ...
## $ age
           : int 21 23 28 23 22 21 26 27 23 21 ...
   $ wgt
                  65.6 71.8 80.7 72.6 78.8 74.8 86.4 78.4 62 81.6 ...
            : num
   $ hgt
            : num
                  174 175 194 186 187 ...
## $ sex
            : int 1 1 1 1 1 1 1 1 1 1 ...
head(bdims)
    bia.di bii.di bit.di che.de che.di elb.di wri.di kne.di ank.di sho.gi
## 1
      42.9
              26.0
                     31.5
                            17.7
                                   28.0
                                          13.1
                                                 10.4
                                                        18.8
                                                               14.1 106.2
                                                 11.8
## 2
       43.7
              28.5
                     33.5
                            16.9
                                   30.8
                                          14.0
                                                        20.6
                                                               15.1 110.5
## 3
      40.1
              28.2
                     33.3
                            20.9
                                   31.7
                                          13.9
                                                 10.9
                                                        19.7
                                                               14.1 115.1
## 4
      44.3
              29.9
                     34.0
                            18.4
                                   28.2
                                          13.9
                                                 11.2
                                                        20.9
                                                               15.0 104.5
## 5
      42.5
              29.9
                     34.0
                            21.5
                                   29.4
                                          15.2
                                                 11.6
                                                        20.7
                                                               14.9 107.5
              27.0
                                   31.3
                                          14.0
## 6
      43.3
                     31.5
                            19.6
                                                 11.5
                                                        18.8
                                                               13.9 119.8
##
     che.gi wai.gi nav.gi hip.gi thi.gi bic.gi for.gi kne.gi cal.gi ank.gi
## 1
      89.5
             71.5
                     74.5
                            93.5
                                   51.5
                                          32.5
                                                 26.0
                                                        34.5
                                                               36.5
                                                                      23.5
## 2
      97.0
              79.0
                     86.5
                            94.8
                                   51.5
                                          34.4
                                                 28.0
                                                        36.5
                                                               37.5
                                                                      24.5
## 3
      97.5
              83.2
                     82.9
                            95.0
                                   57.3
                                          33.4
                                                 28.8
                                                        37.0
                                                               37.3
                                                                      21.9
## 4
      97.0
              77.8
                     78.8
                            94.0
                                   53.0
                                          31.0
                                                 26.2
                                                        37.0
                                                               34.8
                                                                      23.0
## 5
      97.5
              80.0
                     82.5
                            98.5
                                   55.4
                                          32.0
                                                 28.4
                                                        37.7
                                                               38.6
                                                                      24.4
                                                 28.0
      99.9
              82.5
                                          33.0
## 6
                     80.1
                            95.3
                                   57.5
                                                        36.6
                                                               36.1
                                                                      23.5
##
    wri.gi age wgt hgt sex
      16.5 21 65.6 174.0
## 1
                             1
      17.0 23 71.8 175.3
## 2
                             1
      16.9 28 80.7 193.5
## 3
                             1
## 4
      16.6 23 72.6 186.5
                             1
## 5
      18.0 22 78.8 187.2
                             1
      16.9 21 74.8 181.5
We can also look at each numerical variable of interest with favstats:
favstats(bdims$wgt)
##
          Q1 median
                       QЗ
                            max
                                                    n missing
                                    mean
                                               sd
     42 58.4
              68.2 78.85 116.4 69.14753 13.34576 507
favstats(bdims$wri.di)
## min Q1 median
                     Q3 max
                                mean
                                           sd
                                                n missing
## 8.1 9.8 10.5 11.2 13.3 10.5426 0.944361 507
```

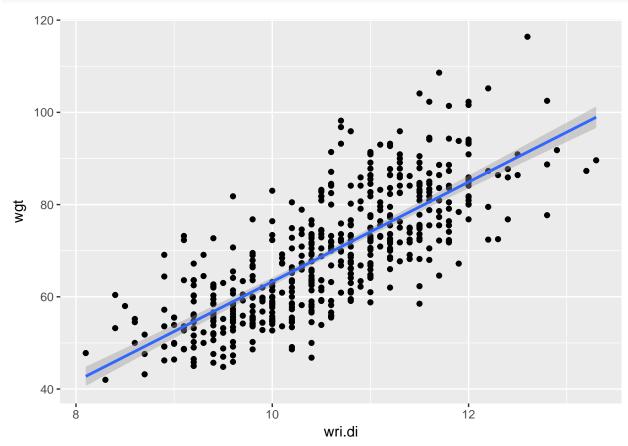
Prepare the data for analysis. [Not always necessary.]

The two variables of interest, wgt and wri.di, are already coded as numerical variables.

Make tables or plots to explore the data visually.

Here is the scatterplot with the regression line added:

```
ggplot(bdims, aes(y = wgt, x = wri.di)) +
    geom_point() +
    geom_smooth(method = "lm")
```



Commentary: It would be inappropriate to show this regression line on the graph before the conditions have been checked. However, most regression analyses start by checking the conditions and writing down the equation of the regression line before doing inference on the slope parameter.

Hypotheses

Identify the sample (or samples) and a reasonable population (or populations) of interest.

The sample consists of 507 physically active individuals (a mix of females and males). The population is all physically active individuals.

Express the null and alternative hypotheses as contextually meaningful full sentences.

 H_0 : There is no relationship between weight and wrist diameter.

 H_A : There is a relationship between weight and wrist diameter.

Express the null and alternative hypotheses in symbols (when possible).

```
H_0: \beta_1 = 0H_A: \beta_1 \neq 0
```

Commentary: We are performing a two-sided test here. One could perform a one-sided test if the question of interest was about a positive or a negative slope specifically. Unless otherwise specified, though, the default is to run a two-sided test.

Model

Identify the sampling distribution model.

We use a t model with 505 degrees of freedom.

Check the relevant conditions to ensure that model assumptions are met.

The conditions have already been checked.

Mechanics

Compute and report the test statistic.

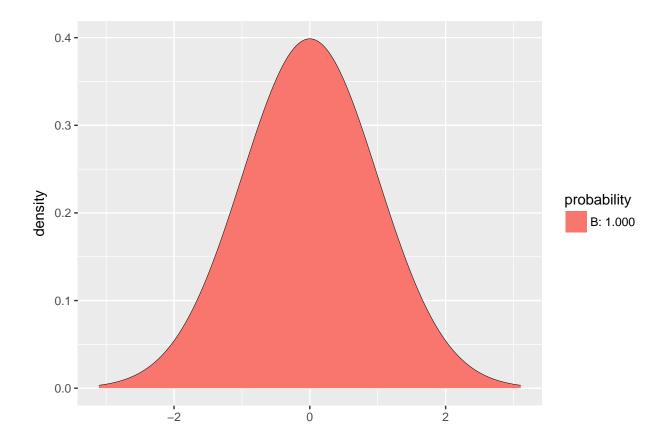
```
t <- wgt_wrist_tidy$statistic[2]
t</pre>
```

```
## [1] 26.66005
```

The sample slope estimate has a t score of 26.6600546.

Commentary: wgt_wrist_tidy\$statistic has t scores for both the intercept and the slope. Be sure to grab the 2nd entry to get the slope test statistic.

Plot the null distribution.



Commentary: The correct degrees of freedom are stored in wgt_wrist_glance\$df.residual, not wgt_wrist_glance\$df as you might expect.

Calculate and report the P-value.

wgt_wrist_tidy\$p.value[2]

Commentary: Not only are there two P-values in wgt_wrist_tidy\$p.value (one for the intercept and one for the slope), but there's one in wgt_wrist_glance too. The one in the glance output, though, is the same as the P-value for the slope, so either wgt_wrist_tidy\$p.value[2] or wgt_wrist_glance\$p.value will give the right answer.

Conclusion

P < 0.001

State the statistical conclusion.

We reject the null hypothesis.

State (but do not overstate) a contextually meaningful conclusion.

There is sufficient evidence that there is a relationship between weight and wrist diameter.

Identify the possibility of either a Type I or Type II error and state what making such an error means in the context of the hypotheses.

If we've made a Type I error, then there might not be any relationship between weight and wrist diameter, but our sample showed a relationship.

Confidence interval

Check the relevant conditions to ensure that model assumptions are met.

All the conditions have already been checked.

Calculate the confidence interval.

```
wgt_wrist_tidy$conf.low[2]
## [1] 10.00916
wgt_wrist_tidy$conf.high[2]
```

[1] 11.60174

Commentary: Because we used the conf.int = TRUE argument to tidy earlier, we can grab the confidence interval for the slope. But the intercept also has a confidence interval, so be sure to tack on [2] to grab the second entries of wgt_wrist_tidy\$conf.low and wgt_wrist_tidy\$conf.high, the ones that correspond to the slope parameter.

State (but do not overstate) a contextually meaningful interpretation.

We are 95% confident that the true slope of the relationship between weight and wrist diameter is captured in the interval (10.0091554, 11.6017377).

Your turn

The Rubber data set contains data on the testing of tires. (Since it was a British study, they tested "tyres".)

Explore the relationship between the loss of tire material in an abrasion test (measured in grams per hour) and the hardness of the tire (measured in something called Shore units—Google it if you want to know more). We will consider the loss of tire material to be response and hardness to be explanatory.

Please perform the steps below, following the code examples from earlier in the module.

• Run the lm command and then use tidy, augment, and glance respectively on the output. (It's technically incorrect to run regression before checking conditions, but we need the output of lm in order to check those conditions.)

ANSWER		

Add code here to generate regression output

• Check conditions for regression.

	ANSWER
# Add code here to check conditions for	regression
Please write up your answer here.	
• If the conditions are met, plot the regress	sion line on top of a scatterplot of the data. ANSWER
# Add code here to plot the regression	line
Write the regression equation mathematic using contextually meaningful variable na	cally (enclosing your answer in double dollar signs as above), ames. ANSWER
Please write up your answer here.	
• Interpret the coefficients: interpret the s comment on the appropriateness of that it	
Please write up your answer here.	
• Report and interpret \mathbb{R}^2 .	ANSWER
Please write up your answer here.	
• Run the full rubric for inference on the sl	ope parameter.
Exploratory data analysis	
Use data documentation (help files, cod command, and other summary functions	e books, Google, etc.), the View command, the str to understand the data.
	ANSWER

# Add code here to understand the data.	
Prepare the data for analysis. [Not alway	vs necessary.]
	ANSWER
# Add code here to prepare the data for	analysis.
Make tables or plots to explore the data	visually.
	ANSWER
# Add code here to make tables or plots.	
Hypotheses	
Identify the sample (or samples) and a re	easonable population (or populations) of interest.
	ANSWER
Please write up your answer here.	
Express the null and alternative hypothe	ses as contextually meaningful full sentences.
	ANSWER
H_0 : Null hypothesis goes here. H_A : Alternative hypothesis goes here.	
H_A : Alternative hypothesis goes here.	
Express the null and alternative hypothes	ses in symbols (when possible).
	ANSWER

Model
Identify the sampling distribution model.
ANSWER
Please write up your answer here.
Check the relevant conditions to ensure that model assumptions are met.
ANSWER
Please write up your answer here. (Some conditions may require R code as well.)
Mechanics
Compute and report the test statistic.
ANSWER
Add code here to compute the test statistic.
Please write up your answer here.
Plot the null distribution.
ANSWER
Add code here to plot the null distribution.

Calculate and report the P-value.	- ANSWER
# Add code here to calculate the P-val	21.0
Please write up your answer here.	
Constant and	
Conclusion	
State the statistical conclusion.	
	ANSWER
Please write up your answer here.	
State (but do not overstate) a contextua	ally meaningful conclusion.
	ANSWER
Please write up your answer here.	
Identify the possibility of either a Type	e I or Type II error and state what making such an
error means in the context of the hypot	
	ANSWER
Please write up your answer here.	
Confidence interval	
	that model assumptions are mot
Check the relevant conditions to ensure	
	ANSWER
Please write up your answer here. (Some cond	ditions may require R code as well.)

Calculate the confidence interval.					
ANSWER					
# Add code here to calculate the confidence interval.					
State (but do not overstate) a contextually meaningful interpretation.					
ANSWER					
Please write up your answer here.					