

# The project of Computational Methods in Physics

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## 1 Principle of the magnetic bottle

### 1.1 Calculate the magnetic field

We can get the magnetic field which is generated by a coil(at the origin of the coordinate) by integrating

$$\begin{cases} B_{x0}(x, y, z) = \int_0^{2\pi} \frac{Rz\cos\phi}{(x^2+y^2+z^2+R^2-2xR\cos\phi-2yR\sin\phi)^{3/2}} d\phi \\ B_{y0}(x, y, z) = \int_0^{2\pi} \frac{Rz\sin\phi}{(x^2+y^2+z^2+R^2-2xR\cos\phi-2yR\sin\phi)^{3/2}} d\phi \\ B_{z0}(x, y, z) = \int_0^{2\pi} \frac{R(R-x\cos\phi-y\sin\phi)}{(x^2+y^2+z^2+R^2-2xR\cos\phi-2yR\sin\phi)^{3/2}} d\phi \end{cases} \quad (1)$$

Then we can get the magnetic field of a magnetic bottle (two coils) by a transformation

$$\begin{cases} B_x(x, y, z) = B_{x0}(x, y, z - d/2) + B_{x0}(x, y, z + d/2) \\ B_y(x, y, z) = B_{y0}(x, y, z - d/2) + B_{y0}(x, y, z + d/2) \\ B_z(x, y, z) = B_{z0}(x, y, z - d/2) + B_{z0}(x, y, z + d/2) \end{cases} \quad (2)$$

d in these equations means the distance between two coils.

### 1.2 Calculate the movement of the electron

According to the Newton equation and Lorentz force equation

$$\begin{cases} F = ma \\ F_{Lorentz} = qv \times x \end{cases} \quad (3)$$

Then we can get the equation,

$$qv \times x = ma \quad (4)$$

Then we need to solve the second order Ordinary Differential Equations, because we study this problem in 3D.

$$\begin{cases} x'' = -\frac{m}{q}(y'Bz(x, y, z) - z'B_y(x, y, z)) \\ y'' = -\frac{m}{q}(z'Bx(x, y, z) - x'Bz(x, y, z)) \\ z'' = -\frac{m}{q}(x'By(x, y, z) - y'Bx(x, y, z)) \end{cases} \quad (5)$$

We transfer the them into first order Ordinary Differential Equations,

$$\begin{cases} vx' = -sc(vy * Bz(x, y, z) - vz * By(x, y, z)) \\ vy' = -sc(vz * Bx(x, y, z) - vx * Bz(x, y, z)) \\ vz' = -sc(vx * By(x, y, z) - vy * Bx(x, y, z)) \\ x' = vx \\ y' = vy \\ z' = vz \end{cases} \quad (6)$$

Its initial values are

$$\begin{cases} vx(0) = 0 \\ vy(0) = 0.30e6 \\ vz(0) = 0.15e6 \\ x(0) = 0 \\ y(0) = 0 \\ z(0) = 0 \end{cases} \quad (7)$$

## 1.3 Solution

### 1.3.1 Equation to be solved

### 1.3.2 Numerical method used

### 1.3.3 Results

### 1.3.4 Discussions