Fast Isotropic Median Filtering—Supplemental Material

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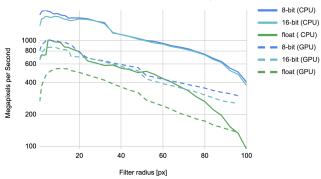


Fig. 1. Our method's performance curves for various platforms and data types, superimposed.

1 RUNTIME CHARACTERISTICS

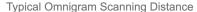
As shown in Fig. 1, our method's throughput with respect to filter radius does not follow a simple characteristic curve like O(1) or O(r). Instead, at first it becomes faster as the radius increases, then displays a nearly flat runtime between radius 8 and radius ~32 (particularly for integer types on CPU), then tapers off roughly linearly for large radii, dipping more sharply toward radius 100. As the algorithm is nominally O(r), it displays unexpectedly strong performance in the intermediate range of filter sizes from roughly radius 8 to 60. This unusual performance curve deserves more explanation.

On CPU, the flat part of the curve is partly attributable to the ability of wide SIMD architectures to absorb much of the early filter size increase "for free". For instance, our inner loop scans the omnigram in 64-element sections; SIMD parallelization and pipelining make this nearly as fast as processing a much smaller number of elements. We also find that the minimum practical output tile size is 32x32; smaller tile sizes make it difficult to saturate the

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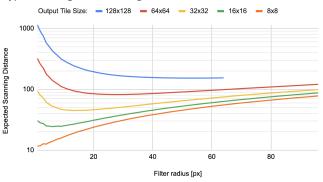


Fig. 2. Average omnigram scanning distance, by filter radius and output tile size, for the 8-megapixel photo from the paper's leading figure. The sharp increase for small radii, combined with reduced vectorizability of smaller tiles, limits our method's performance in the small-kernel range.

concurrency of the SIMD architecture, such as AVX2 which has a native width of 32 8-bit elements.

A second important factor is omnigram scanning distance. The pivots-and-counts technique relies on the heuristic that adjacent median-filtered values are usually similar. We find that for a given output tile size, this heuristic also performs best for an intermediate range of filter sizes. Fig. 2 illustrates the relationship between output tile size, filter radius, and average scanning distance.

For very large kernels, we reach a "cliff" at an input tile size of 256x256, where exceeding that limit would require doubling the omnigram size to 32 bits per element. For this reason, our current implementation constrains the input tile size to 256x256. This leads to an $O((128-r)^{-2})$ performance curve for large radii (where the bottleneck becomes the ordinal transform), and this explains the dip in performance as the filter radius approaches 100. But this dip is not fundamental to the algorithm; in principle, switching to a 32-bit omnigram would yield an O(r) performance curve as the radius scales to 100 and beyond.

On GPU, the primary considerations are fast memory capacity and thread occupancy. For our algorithm, the 32-threads-per-warp CUDA architecture works most naturally when the output tile size is a multiple of 32. For a 64x64 output tile size, we reach the 16-bit omnigram limit at radius 96. It would be possible to implement up to radius 112 by using a 32x32 output tile size, but performance would drop substantially for that minimal increase in filter radius. However, as GPU L1 cache sizes increase in the future (already some datacenter GPU's have ~256k of fast memory per SM), we expect larger kernels to become more viable by switching to a 32-bit omnigram.

2 ALGORITHMS (PSEUDOCODE)

For the benefit of those who would like to implement our algorithm on their own, we provide a pseudocode outline of our CPU and GPU methods. Note that for a more complete reference, our working code can be found at https://github.com/google/fast-isotropic-median-filter.

2.1 CPU Algorithm

```
Algorithm 1. CPU Implementation (pseudocode)
 1: for all columns of cardinal output tiles O_c do
 2: for all tiles in column do
      generate data structures: I_c \mapsto \{I, \Omega_I, C_I\}
                                                          ▶ Eq. 5
      if top tile in column then
       solve m(0,0), storing aligned pivot p and count c
 5:
       shear/transpose top rows of input pixels
 6:
       for all output pixel columns col in top row do
 7:
         slide window right, updating c[col]
 8:
         solve m(col, 0) by scanning \Omega_I from p[col]
 9:
         select nearby 64-element-aligned p[col] and c[col]
10:
11:
         write to output: O_c(col, 0) = C_I[m(col, 0)]
12:
       end for
13:
       Incorporate forwarded solutions from previous tile
14:
15:
       for all pixels (x, 0) in first row do
         Obtain median from ordinal image.
16:
         []If I is quantized, scan \Omega_I to refine exact median.]
17:
   m(x, 0) = I(\text{last\_offset}[x] + (x + \text{rad}, \text{rad}))
18:
       end for
      end if
19:
      for all subsequent rows in output tile do
20:
       for all leading/trailing pixel offsets (dx, dy) do
21:
         for all output columns do
                                                         ▶ Fig. 8
22:
          c[col] += Compare(I[col + dx, row + dy], p[col])
23:
         end for
24:
       end for
25:
       for all output columns do
26:
         scan \Omega_I from p[col] to find exact m(col, row)
27:
         select nearby 64-element-aligned p[col] and c[col]
28:
         write to output: O_c(col, row) = C_I[m(col, row)]
29:
30:
       end for
       Forwards last-row solutions to next tile
31:
32:
       if last row in tile then
33:
         for all pixels (x, y) in last row do
          Store offset of m(x, y) from window center
34:
          last\_offset[x] = \Omega_I[m(x, y)] - (x + rad, y + rad)
35:
         end for
36:
       end if
37:
      end for
38:
    end for
39:
40: end for
```

2.2 GPU Algorithm

end for

```
Algorithm 2. GPU Implementation (pseudocode)
for all output tiles O_c do
 pack input pixels + coords (Fig. 10) into key-value arrays
end for
Using e.g. cub::SegmentedDeviceRadixSort():
key-value sort arrays to construct \Omega_I and C_I
for all output tiles O_c do
 for all seed pixel windows W_{s_{x,y}} in parallel do
  Construct coarse seed-window histogram H_{s_{xy}}
  for all indices k in \Omega_I do
   if \Omega_I[k] \in W_{s_{xy}} then H_{s_{xy}}[k >> 6] ++
  Note: the approximate median defines the pivot p[s_{xy}].
  scan H_{s_{xy}} to find approximate median for W_{s_{xy}}
  refine to exact median m(s_{xy}) by scanning \Omega_I
  write to output: O_c(s_{xy}) = C_I[m(s_{xy})]
 end for
 Construct ordinal image into shared memory
 for all indices k in \Omega_I do
  I[\Omega_I[k]] = k \gg 6
 end for
 Slide horizontally from seed windows to solve seed rows
 for all seed windows W(s_{xy}) in parallel do
  for all remaining columns until seed row is solved do
   for all leading/trailing pixel offsets (dx, dy) do
     c[xy] += Compare(I[col + dx, row + dy], p[xy])
    end for
    scan \Omega_I from p[xy] to find exact median m(xy)
    set p[xy] to a quantized value near m(xy)
   write to output: O_c(xy) = C_I[m(xy)]
  end for
 end for
 Slide vertically from seed rows to solve rest of tile
 for all seed row windows W_{xy} in parallel do
  for all remaining rows until tile is solved do
   for all leading/trailing pixel offsets (dx, dy) do
     c[xy] += Compare(I[col + dx, row + dy], p[xy])
    end for
   scan \Omega_I from p[xy] to find exact median
   write to output: O_c(xy) = C_I[m(xy)]
  end for
 end for
```

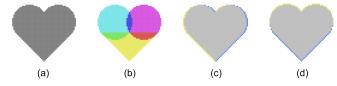


Fig. 3. (a) A heart shape can be represented by (b) two intersecting circles and a triangle. During the window-sliding phase, leading and trailing pixels are shown for (c) horizontal and (d) vertical sliding.

3 ARBITRARY CONVEX KERNEL SHAPES

While we anticipate that circular-kernel filtering will be the primary use case for our algorithm, it can be modified to handle a variety of convex (or mostly-convex) kernel shapes. Simple shapes such as polygons (including squares) can be achieved by correspondingly modifying the analytical test in the paper's Eq. 3, remaining fully vectorizable on CPU. For instance, a heart shape (Fig. 3) could be modeled as the union of two intersecting circles $\{C_1, C_2\}$ and a triangle T. In this specific case, Eq. 3 would be replaced with:

$$H_{\heartsuit}[v] = \begin{cases} 1 & \text{if } (\Omega_I[v] \in C_1) \lor (\Omega_I[v] \in C_2) \lor (\Omega_I[v] \in T) \\ 0 & \text{otherwise} \end{cases}$$
 (1)

and the sliding-window phase would use leading and trailing offsets as shown in Fig. 3.

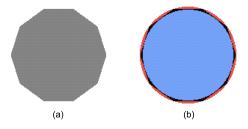


Fig. 4. (a) A decagon could be implemented with a more complex analytical formula, or with a "trimap" approach (b). Points inside the blue circle would be included, points outside the red circle excluded, and intermediate points solved by bitmap lookup.

More complex shapes could be achieved by implementing the paper's Eq. 2 with a bitmap lookup, which would remain efficient on GPU, but might sacrifice pure vectorizability on CPU, even if most queries could still be solved analytically by testing against e.g. a bounding circle. Shapes of intermediate complexity could be implemented with a "trimap" approach (Fig. 4): testing all omnigram elements against inscribed and circumscribed shapes, and reserving bitmap lookups only for the infrequent "midliers".

MacBook Pro - M1 Max CPU - 8 threads - 8 fast cores

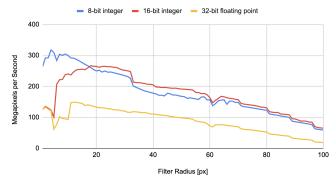


Fig. 5. Our method's performance on arm64 CPU.

4 ADDITIONAL ARCHITECTURES

In addition to x86 64 and CUDA, we have implemented an optimized version of our algorithm for the arm64 architecture, which runs on both desktop and mobile devices. As shown in Fig. 5, performance on an M1 MacBook Pro CPU is very strong; on a per-core basis it consistently outperforms the AMD 5995WX Threadripper by about 20 to 60 percent.

For our particular algorithm, one specific advantage we find on both x86 64 and CUDA architectures is the presence of a "find-nthset-bit" hardware instruction, as "pdep" on x86 and "__fns()" on CUDA. The presence of an x86 instruction to rotate just the low bits of an integer register is also helpful for our custom radix sort.

On NVIDIA GPU's, we find that our method's performance scales almost exactly linearly with CUDA cores; e.g. on RTX 5080 hardware (with 3.5x the core count) we've measured that the per-core throughput is ~99% that of the RTX 4060. For other GPU architectures such as AMD, we find that the limiting factor is the scarcity of pre-existing libraries for e.g. parallel key-value-sorting or merging. As more such foundational libraries become available, we expect that algorithms like ours will become that much easier to develop and distribute across a wider variety of platforms.