

# **COMP 224 Database Management Systems**

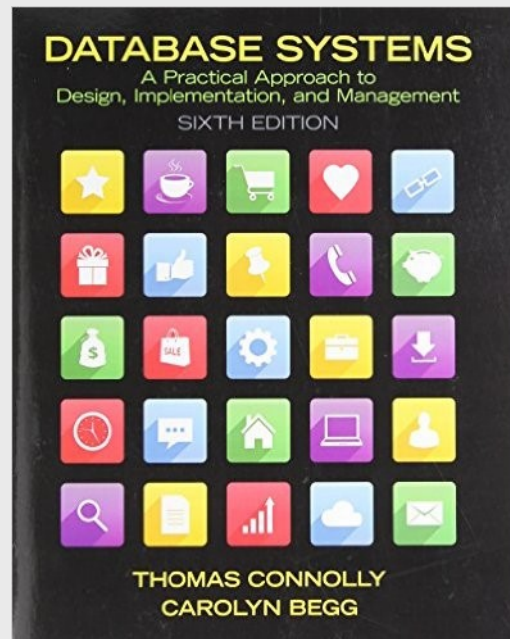
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# Text book

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Thomas Connolly, Carolyn Begg (2015). *DATABASE SYSTEMS: A Practical Approach to Design, Implementation and Management* (6th ed.). Addison Wesley.



# Assessment

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## Assignments

- One project 15%
- One writing assignment 15%
- In-class exercise 5%

One test (knowledge assessment) 15%

Final examination 50%

# COMP 224 Overview

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**The subject is aimed at introducing students to advanced topics in the design and management of database systems.**

- Relational algebra
- Query processing and optimization
- Data Definition Language – Oracle Project (15%)
- Transaction management – Test (15%)
- Distributed database systems– Assignment 2 (15%)
- Big data
- Database Security

# How “*Big Data*” will change your life....

“We swim in a sea of data ... and the sea level is rising rapidly.”

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Data-driven World in the future !

# Relational Algebra

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# Content

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- ❑ **Introduction of relational algebra ;**
- ❑ **Five fundamental operations in relational algebra:  
Selection, Projection, Cartesian product, Union, and Set  
Difference;**
- ❑ **Join, Intersection, and Division operations which can be  
expressed in terms of the five basic operations ;**
- ❑ **Relational algebra exercises.**

## **Objective:**

- ❖ **How to form queries in relational algebra**

# Introduction

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- ❑ Relational algebra is formal language associated with the relational model.
- ❑ Relational algebra is used as the basis for other, higher-level Data Manipulation Languages (DMLs) for relational databases.
- ❑ It illustrates the basic operations required of any DML.
- ❑ It can be used to tell the DBMS how to build a new relation from one or more relations in the database.



# Relational Algebra

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- ❑ Relational algebra operations work on one or more relations to define another relation without changing the original relations.
- ❑ Both operands and result are relations, so output from one operation can become input to another operation.
- ❑ Allows expressions to be nested, just as in arithmetic. This property is called closure.

# Relational Algebra

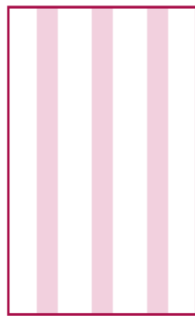
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- ❑ Five basic operations in relational algebra:
  - Selection
  - Projection
  - Cartesian product
  - Union
  - Set Difference
- ❑ These perform most of the data retrieval operations needed.
- ❑ Also have Join, Intersection, and Division operations, which can be expressed in terms of 5 basic operations.

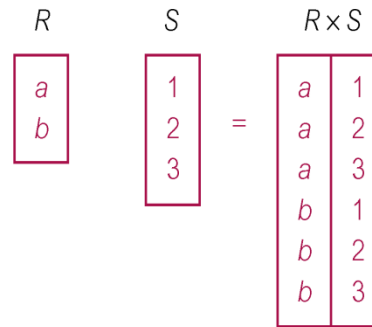
# Relational Algebra Operations



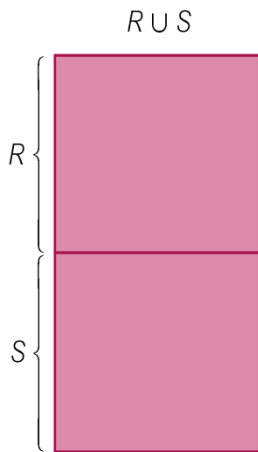
(a) Selection



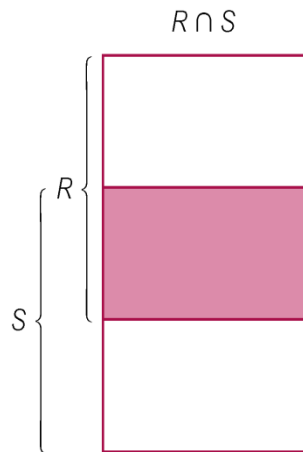
(b) Projection



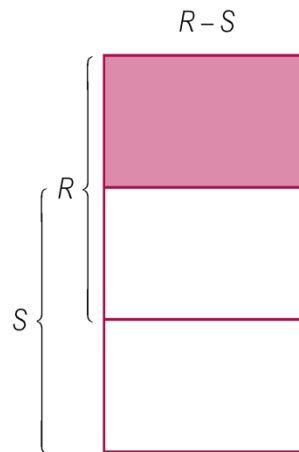
(c) Cartesian product



(d) Union



(e) Intersection



(f) Set difference

**Selection and Projection** are unary operations.

The other operations are binary operations.

# Selection (or Restriction) $\sigma$

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□  $\sigma_{\text{predicate}}(\mathbf{R})$  [*Greek letter called sigma*]

- Works on a single relation  $\mathbf{R}$  and defines a relation that contains only those tuples (rows) of  $\mathbf{R}$  that satisfy the specified condition (*predicate*).

Example of selection:

$\sigma_{\text{branch-name}=\text{'Macau'}}(\text{account})$

# Selection

---

A



The restriction of relation A on the condition:

`A WHERE condition`  
is a relation with the same heading as A and with a body consisting of the set of all tuples t of A such that the condition is true for t.

## Selection Condition (predicate)

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may have Boolean conditions **AND** ( $\wedge$ ) , **OR** ( $\vee$ ) , and **NOT** ( $\sim$ )

- has clauses of the form:

»  $\langle \text{attribute name} \rangle \langle \text{comparison op} \rangle \langle \text{constant value} \rangle$

*or*

»  $\langle \text{attribute name} \rangle \langle \text{comparison op} \rangle \langle \text{attribute name} \rangle$

$\sigma_{(Dno=4 \text{ AND } Salary>2500) \text{ OR } (Dno=5 \text{ AND } Salary>30000)}(\text{EMPLOYEE})$

Relational model is set-based (no duplicate tuples),  
Relation R has no duplicates, therefore selection cannot produce duplicates.

# Selection

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Do not confuse this with SQL's SELECT statement!

## Correspondence

- Relational algebra

$$\sigma_{\langle \textit{selection condition} \rangle}(R)$$

- SQL

SELECT \*

FROM R

WHERE <selection condition>

## Example - Selection (or Restriction) $\sigma$

List all staff information with a salary greater than £10,000.

$\sigma_{\text{salary} > 10000}$  (Staff)

| staffNo | fName | lName | position   | sex | DOB        | salary | branchNo |
|---------|-------|-------|------------|-----|------------|--------|----------|
| SL21    | John  | White | Manager    | M   | 1-Oct-45   | 30000  | B005     |
| SG37    | Ann   | Beech | Assistant  | F   | 10-Nov-60  | 12000  | B003     |
| SG14    | David | Ford  | Supervisor | M   | 24- Mar-58 | 18000  | B003     |
| SG5     | Susan | Brand | Manager    | F   | 3-Jun-40   | 24000  | B003     |



## Example - Selection (or Restriction)

---

- Relation  $r$

| $A$      | $B$      | $C$ | $D$ |
|----------|----------|-----|-----|
| $\alpha$ | $\alpha$ | 1   | 7   |
| $\alpha$ | $\beta$  | 5   | 7   |
| $\beta$  | $\beta$  | 12  | 3   |
| $\beta$  | $\beta$  | 23  | 10  |

- $\sigma_{A=B \wedge D > 5}(r)$

| $A$      | $B$      | $C$ | $D$ |
|----------|----------|-----|-----|
| $\alpha$ | $\alpha$ | 1   | 7   |
| $\beta$  | $\beta$  | 23  | 10  |

# What is the equivalent relational algebra expression?

---

## Employee

| ID | Name | S | Dept | JobType    |
|----|------|---|------|------------|
| 12 | Chen | F | CS   | Faculty    |
| 13 | Wang | M | MATH | Secretary  |
| 14 | Lin  | F | CS   | Technician |
| 15 | Liu  | M | ECE  | Faculty    |

```
SELECT *  
FROM Employee  
WHERE JobType = 'Faculty';
```

# Projection Operation

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❑  $\Pi_{col1, \dots, coln}(R)$  [*Greek letter called pi*]

where *col1*, *col2* are attribute names and *R* is a relation name.

➤ **Works on a single relation *R* and defines a relation that contains a vertical subset of *R*, extracting the values of specified attributes and **eliminating duplicates**.**

❑ The projection operator produces the output table by

- eliminating all attributes not specified, and
- eliminating any duplicated tuples

R

|  |  |  |  |  |
|--|--|--|--|--|
|  |  |  |  |  |
|  |  |  |  |  |

## Example - Projection

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- ❑ Produce a list of salaries for all staff, showing only staffNo, fName, lName, and salary details.

$\Pi_{\text{staffNo, fName, lName, salary}}(\text{Staff})$

| staffNo | fName | lName | salary |
|---------|-------|-------|--------|
| SL21    | John  | White | 30000  |
| SG37    | Ann   | Beech | 12000  |
| SG14    | David | Ford  | 18000  |
| SA9     | Mary  | Howe  | 9000   |
| SG5     | Susan | Brand | 24000  |
| SL41    | Julie | Lee   | 9000   |

# Example - Projection

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## Airports

| airport_name | country_name |
|--------------|--------------|
| Naples       | Italy        |
| London/Gk    | England      |
| London/Hw    | England      |
| Pisa         | Italy        |
| Venice/MP    | Italy        |
| Manchester   | England      |
| Kai Tak      | Hong Kong    |
| Changi       | Singapore    |

## $\Pi_{\text{country\_name}}(\text{Airports})$

| country_name |
|--------------|
| Italy        |
| England      |
| Hong Kong    |
| Singapore    |

# Projection

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## Correspondence

- Relational algebra

$$\pi_{\langle \text{attribute list} \rangle}(R)$$

- SQL

```
SELECT DISTINCT <attribute list>  
FROM R
```

- Note the need for DISTINCT in SQL

# What is the equivalent relational algebra expression?

---

## Employee

| ID | Name | S | Dept | JobType    |
|----|------|---|------|------------|
| 12 | Chen | F | CS   | Faculty    |
| 13 | Wang | M | MATH | Secretary  |
| 14 | Lin  | F | CS   | Technician |
| 15 | Liu  | M | ECE  | Faculty    |

```
SELECT  DISTINCT Name, S, Dept
FROM    Employee;
```

# Union Operation

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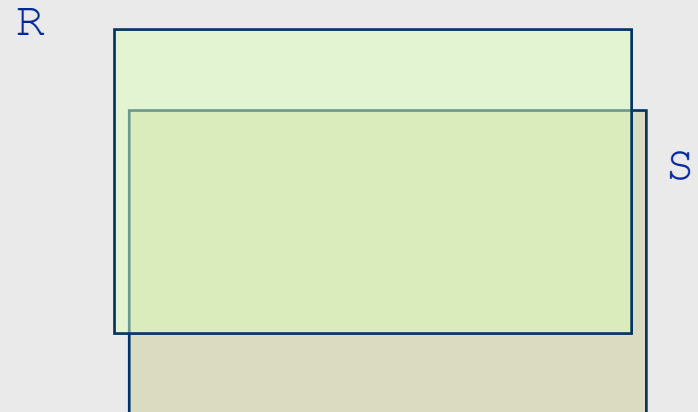
## □ $R \cup S$

➤ Union of two relations  $R$  and  $S$  defines a relation that contains all the tuples of  $R$ , or  $S$ , or both  $R$  and  $S$ , **duplicate tuples being eliminated**.

➤  $R$  and  $S$  must be **union-compatible**.

□ If  $R$  and  $S$  have  $I$  and  $J$  tuples, respectively, union is obtained by concatenating them into one relation with a **maximum of  $(I + J)$  tuples**.

Two relations are **union-compatible** if they have the *same set of attributes* which are defined *on the same domains*.





# Example - Union

Produce a list of all staff that work **in either of** two departments (*each department has a separate database*), showing only their staffNo, and date of birth.

$$\Pi_{\text{staffNo, dob}}(\text{Staff\_DepA}) \cup \Pi_{\text{staffNo, dob}}(\text{Staff\_DepB})$$

Staff\_DepA

| staffNo | dob      |
|---------|----------|
| SL10    | 14-02-64 |
| SA51    | 21-11-82 |
| DS40    | 01-01-40 |

Staff\_DepB

| staffNo | dob      |
|---------|----------|
| CC15    | 11-03-66 |
| SA51    | 21-11-82 |



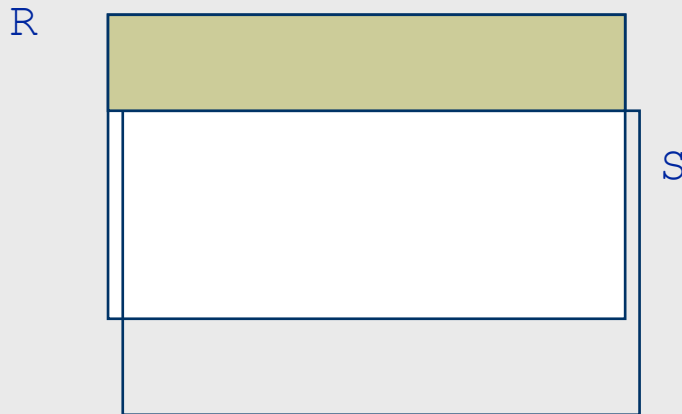
| staffNo | dob      |
|---------|----------|
| SL10    | 14-02-64 |
| SA51    | 21-11-82 |
| DS40    | 01-01-40 |
| CC15    | 11-03-66 |

# Set Difference

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## □ $R - S$

- Defines a relation consisting of the tuples that are **in** relation **R**, **but not in S**.
- **R** and **S** must be **union-compatible**.



# Example - Difference

Produce a list of all staff that **only work in department A** (*each department has a separate database*), showing only their staffNo, and date of birth.

$\Pi_{\text{staffNo, dob}}(\text{Staff\_DepA}) - \Pi_{\text{staffNo, dob}}(\text{Staff\_DepB})$

Staff\_DepA

| staffNo | dob      |
|---------|----------|
| SL10    | 14-02-64 |
| SA51    | 21-11-82 |
| DS40    | 01-01-40 |

Staff\_DepB

| staffNo | dob      |
|---------|----------|
| CC15    | 11-03-66 |
| SA51    | 21-11-82 |

—



| staffNo | dob      |
|---------|----------|
| SL10    | 14-02-64 |
| DS40    | 01-01-40 |

# Intersection

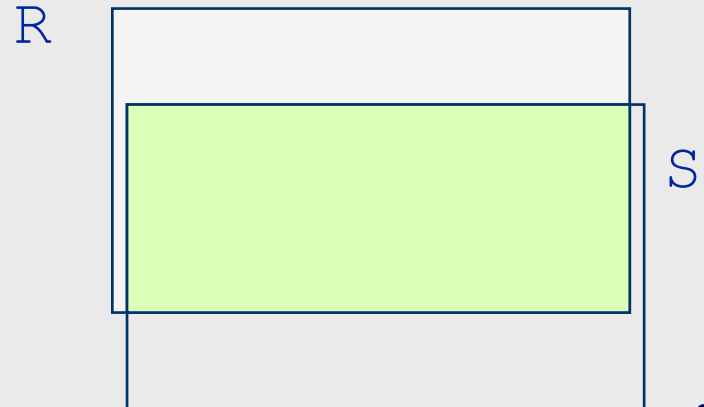
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## □ $R \cap S$

- Defines a relation consisting of the set of all tuples that are **in both R and S**.
- R and S must be **union-compatible**.

## □ Expressed using basic operations:

$$R \cap S = R - (R - S)$$



# Example - Intersection

Produce a list of staff that work in **both** department A and department B, showing only their staffNo, and date of birth.

$(\Pi_{\text{staffNo}, \text{dob}}(\text{Staff\_DepA})) \cap (\Pi_{\text{staffNo}, \text{dob}}(\text{Staff\_DepB}))$

Staff\_DepA

| staffNo | dob      |
|---------|----------|
| SL10    | 14-02-64 |
| SA51    | 21-11-82 |
| DS40    | 01-01-40 |

Staff\_DepB

| staffNo | dob      |
|---------|----------|
| CC15    | 11-03-66 |
| SA51    | 21-11-82 |



| staffNo | dob      |
|---------|----------|
| SA51    | 21-11-82 |

# Example of Union/Intersection/Difference

| A  |       |        |        | B  |       |        |        |
|----|-------|--------|--------|----|-------|--------|--------|
| S# | SNAME | STATUS | CITY   | S# | SNAME | STATUS | CITY   |
| S1 | Smith | 20     | London | S1 | Smith | 20     | London |
| S4 | Clark | 20     | London | S2 | Jones | 10     | Paris  |

| a. Union<br>(A UNION B) |       |        |        |
|-------------------------|-------|--------|--------|
| S#                      | SNAME | STATUS | CITY   |
| S1                      | Smith | 20     | London |
| S4                      | Clark | 20     | London |
| S2                      | Jones | 10     | Paris  |

| b. Intersection<br>(A INTERSECT B) |       |        |        |
|------------------------------------|-------|--------|--------|
| S#                                 | SNAME | STATUS | CITY   |
| S1                                 | Smith | 20     | London |

| c. Difference<br>(A MINUS B) |       |        |        |
|------------------------------|-------|--------|--------|
| S#                           | SNAME | STATUS | CITY   |
| S4                           | Clark | 20     | London |

| d. Difference<br>(B MINUS A) |       |        |       |
|------------------------------|-------|--------|-------|
| S#                           | SNAME | STATUS | CITY  |
| S2                           | Jones | 10     | Paris |

# Cartesian product

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## □ R X S

➤ Defines a relation that is the concatenation of **every tuple** of relation R with **every tuple** of relation S.

□ The Cartesian product operation multiplies two relations to define another relation consisting of **all possible pairs** of tuples from the two relation.

|    |   |    |   |    |    |
|----|---|----|---|----|----|
| a1 | X | b1 | = | a1 | b1 |
| a2 |   | b2 |   | a1 | b2 |
|    |   |    |   | a2 | b1 |
|    |   |    |   | a2 | b2 |

# More about product operation

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- ❑ If one relation has  $I$  tuples, and  $N$  attributes; the other has  $J$  tuples and  $M$  attributes
  - The **Cartesian product** relation will contain  $(I * J)$  tuples with  $(N + M)$  attributes.
  - If the two relations have attributes with the same name, the attribute names are prefixed with the relation name to maintain the uniqueness of attributes name within a relation.
- ❑ The result is often large and **space-costly** but produces no more information than there was in the input.



# Example - Cartesian product

---

Relations  $r, s$ :

| $A$ | $B$ |
|-----|-----|
|-----|-----|

|          |   |
|----------|---|
| $\alpha$ | 1 |
| $\beta$  | 2 |

$r$

| $C$ | $D$ | $E$ |
|-----|-----|-----|
|-----|-----|-----|

|          |    |     |
|----------|----|-----|
| $\alpha$ | 10 | $a$ |
| $\beta$  | 10 | $a$ |
| $\beta$  | 20 | $b$ |
| $\gamma$ | 10 | $b$ |

$s$

$r \times s$ :

| $A$ | $B$ | $C$ | $D$ | $E$ |
|-----|-----|-----|-----|-----|
|-----|-----|-----|-----|-----|

|          |   |          |    |     |
|----------|---|----------|----|-----|
| $\alpha$ | 1 | $\alpha$ | 10 | $a$ |
| $\alpha$ | 1 | $\beta$  | 10 | $a$ |
| $\alpha$ | 1 | $\beta$  | 20 | $b$ |
| $\alpha$ | 1 | $\gamma$ | 10 | $b$ |
| $\beta$  | 2 | $\alpha$ | 10 | $a$ |
| $\beta$  | 2 | $\beta$  | 10 | $a$ |
| $\beta$  | 2 | $\beta$  | 20 | $b$ |
| $\beta$  | 2 | $\gamma$ | 10 | $b$ |

# Example - Cartesian product

Combine details of staff (S) and the departments (D).

$\Pi_{\text{staffNo, job, dept}}(\text{S}) \times \Pi_{\text{dept, name}}(\text{D})$

S

| staffNo | job      | dept |
|---------|----------|------|
| SL10    | Salesman | 10   |
| SA51    | Manager  | 20   |
| DS40    | Clerk    | 20   |

D

| dept | name      |
|------|-----------|
| 10   | Stratford |
| 20   | Barking   |

X

5 attributes, 2 dept



| staffNo | job      | S.dept | D.dept | name      |
|---------|----------|--------|--------|-----------|
| SL10    | Salesman | 10     | 10     | Stratford |
| SA51    | Manager  | 20     | 10     | Stratford |
| DS40    | Clerk    | 20     | 10     | Stratford |
| SL10    | Salesman | 10     | 20     | Barking   |
| SA51    | Manager  | 20     | 20     | Barking   |
| DS40    | Clerk    | 20     | 20     | Barking   |

# Relation Algebra Operations

# Join Operations

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- ❑ Join is a derivative of Cartesian product.
- ❑ Equivalent to performing a Selection, using join predicate as selection formula, over Cartesian product of the two operand relations.
- ❑ One of the most difficult operations to implement efficiently in an RDBMS and one reason why RDBMSs have intrinsic performance problems.

# Join Operations

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- ❑ **Various forms of join operation**
  - **Theta join**
  - **Equijoin (a particular type of Theta join)**
  - **Natural join**
  - **Outer join**
  - **Semijoin**

## Theta join ( $\theta$ -join) $\bowtie_{\langle \text{join condition} \rangle}$

---

$R \bowtie_{\langle \text{join condition} \rangle} S$

- Defines a relation that contains tuples satisfying the predicate F from the Cartesian product of R and S.
- The predicate F is of the form  $R.a_i \theta S.b_i$  where  $\theta$  may be one of the comparison operators ( $<, \leq, >, \geq, =, \neq$ ).
- Can rewrite Theta join using basic Selection and Cartesian product operations.

$$R \bowtie_F S = \sigma_F(R \times S)$$

- Degree of a Theta join is sum of degrees of the operand relations R and S. If predicate F contains only equality ( $=$ ), the term *Equijoin* is used.

# Theta join ( $\theta$ -join)

Produce a list of staff and the departments they work in.

$(\Pi_{\text{staffNo, job, dept}}(\text{Staff})) \bowtie_{\text{Staff.dept} = \text{Dept.dept}} (\Pi_{\text{dept, name}}(\text{Dept}))$

Staff

| staffNo | job      | dept |
|---------|----------|------|
| SL10    | Salesman | 10   |
| SA51    | Manager  | 20   |
| DS40    | Clerk    | 20   |

Dept

| dept | name      |
|------|-----------|
| 10   | Stratford |
| 20   | Barking   |



| staffNo | job      | S.dept | D.dept | name      |
|---------|----------|--------|--------|-----------|
| SL10    | Salesman | 10     | 10     | Stratford |
| SA51    | Manager  | 20     | 20     | Barking   |
| DS40    | Clerk    | 20     | 20     | Barking   |

Because the predicate operator is an '=' this is known as an *Equijoin*

# Natural join

## □ $R \bowtie S$

- An Equijoin of the two relations R and S **over all common attributes** x. One occurrence of each common attribute **is eliminated** from the result.

Produce a list of staff and the departments they work in.

$(\Pi_{\text{staffNo, job, dept}}(\text{Staff})) \bowtie (\Pi_{\text{dept, name}}(\text{Dept}))$

Staff

| staffNo | job      | dept |
|---------|----------|------|
| SL10    | Salesman | 10   |
| SA51    | Manager  | 20   |
| DS40    | Clerk    | 20   |

Dept

| dept | name      |
|------|-----------|
| 10   | Stratford |
| 20   | Barking   |



| staffNo | job      | dept | name      |
|---------|----------|------|-----------|
| SL10    | Salesman | 10   | Stratford |
| SA51    | Manager  | 20   | Barking   |
| DS40    | Clerk    | 20   | Barking   |



# Example- Natural Join

Airports

| airport_name | country_name |
|--------------|--------------|
| Naples       | Italy        |
| London/Gk    | England      |
| London/Hw    | England      |
| Pisa         | Italy        |
| Venice/MP    | Italy        |
| Manchester   | England      |
| Kai Tak      | Hong Kong    |
| Changi       | Singapore    |

Stop

| flight_number | airport_name | stop_number |
|---------------|--------------|-------------|
| BA383         | Kai Tak      | 1           |
| BA019         | Changi       | 2           |

Stops (natural) JOIN Airports

| flight_number | airport_name | stop_number | country_name |
|---------------|--------------|-------------|--------------|
| BA383         | Kai Tak      | 1           | Hong Kong    |
| BA019         | Changi       | 2           | Singapore    |

# Example- Natural Join

Relations r, s:

| <i>A</i> | <i>B</i> | <i>C</i> | <i>D</i> |
|----------|----------|----------|----------|
| <i>m</i> | <i>1</i> | <i>s</i> | <i>a</i> |
| <i>n</i> | <i>2</i> | <i>t</i> | <i>a</i> |
| <i>o</i> | <i>4</i> | <i>t</i> | <i>b</i> |
| <i>p</i> | <i>1</i> | <i>u</i> | <i>a</i> |
| <i>q</i> | <i>2</i> | <i>v</i> | <i>b</i> |

*r*

| <i>B</i> | <i>D</i> | <i>E</i> |
|----------|----------|----------|
| <i>1</i> | <i>a</i> | <i>f</i> |
| <i>3</i> | <i>a</i> | <i>f</i> |
| <i>1</i> | <i>a</i> | <i>g</i> |
| <i>2</i> | <i>b</i> | <i>h</i> |
| <i>3</i> | <i>b</i> | <i>h</i> |

*s*

$r \bowtie s$

| <i>A</i> | <i>B</i> | <i>C</i> | <i>D</i> | <i>E</i> |
|----------|----------|----------|----------|----------|
| <i>m</i> | <i>1</i> | <i>s</i> | <i>a</i> | <i>f</i> |
| <i>m</i> | <i>1</i> | <i>s</i> | <i>a</i> | <i>g</i> |
| <i>p</i> | <i>1</i> | <i>u</i> | <i>a</i> | <i>f</i> |
| <i>p</i> | <i>1</i> | <i>u</i> | <i>a</i> | <i>g</i> |
| <i>q</i> | <i>2</i> | <i>v</i> | <i>b</i> | <i>h</i> |

Only tuples that have  $r.B=s.B$  and  $r.D=s.D$  can stay in the results relation.

# Outer join

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- ❑ To display rows in the result that do not have matching values in the join column, use **Outer join**.
- ❑  $R \bowtie S$ 
  - (Left) outer join is join in which tuples from R that do not have matching values in common columns of S are also included in result relation.

# Outer Join

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- ❑ An extension of the join operation that avoids loss of information by other types of join.
- ❑ Computes the join and then adds tuples from one relation that does not match tuples in the other relation to the result of the join.
- ❑ Uses *null* values:
  - *null* signifies that the value is unknown or does not exist
  - All comparisons involving *null* are (roughly speaking) **false** by definition.

# Example - Left Outer join

Produce a list of **all** departments and associated staff that work in them.

$(\Pi_{\text{dept, name}}(\text{Dept})) \bowtie (\Pi_{\text{staffNo, job, dept}}(\text{Staff}))$

Dept

| dept | name      |
|------|-----------|
| 10   | Stratford |
| 20   | Barking   |
| 30   | Watford   |

Staff

| staffNo | job      | dept |
|---------|----------|------|
| SL10    | Salesman | 10   |
| SA51    | Manager  | 20   |
| DS40    | Clerk    | 20   |



| dept | name      | staffNo | job      |
|------|-----------|---------|----------|
| 10   | Stratford | SL10    | Salesman |
| 20   | Barking   | SA51    | Manager  |
| 20   | Barking   | DS40    | Clerk    |
| 30   | Watford   | null    | null     |

# Example

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## ❑ Relation *loan*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> |
|--------------------|--------------------|---------------|
| L-170              | Downtown           | 3000          |
| L-230              | Redwood            | 4000          |
| L-260              | Perryridge         | 1700          |

## ❑ Relation *borrower*

| <i>customer-name</i> | <i>loan-number</i> |
|----------------------|--------------------|
| Jones                | L-170              |
| Smith                | L-230              |
| Hayes                | L-155              |

# Example

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## ❑ Natural Join

*loan* ⋈ *Borrower*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> | <i>customer-name</i> |
|--------------------|--------------------|---------------|----------------------|
| L-170              | Downtown           | 3000          | Jones                |
| L-230              | Redwood            | 4000          | Smith                |

## ❑ Left Outer Join

*loan* ⋈<sub>L</sub> *borrower*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> | <i>customer-name</i> |
|--------------------|--------------------|---------------|----------------------|
| L-170              | Downtown           | 3000          | Jones                |
| L-230              | Redwood            | 4000          | Smith                |
| L-260              | Perryridge         | 1700          | <i>null</i>          |

# Semijoin

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$R \bowtie_F S$

- Defines a relation that contains the tuples of R that participate in the join of R with S.

**Can rewrite Semijoin using Projection and Join:**

$$R \bowtie_F S = \Pi_A(R \Join_F S)$$

- A is the set of all attributes for R



# Example - Semijoin

***Employee***

| Name    | EmpId | DeptName   |
|---------|-------|------------|
| Harry   | 3415  | Finance    |
| Sally   | 2241  | Sales      |
| George  | 3401  | Finance    |
| Harriet | 2202  | Production |

***Dept***

| DeptName   | Manager |
|------------|---------|
| Sales      | Bob     |
| Sales      | Thomas  |
| Production | Katie   |
| Production | Mark    |

**Employee**  $\bowtie$  *Employee.DeptName = Dept.DeptName* **Dept**

| Name    | EmpId | DeptName   |
|---------|-------|------------|
| Sally   | 2241  | Sales      |
| Harriet | 2202  | Production |

# Division Operation

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## □ $R \div S$

- Relation R has attribute set A; relation S has attribute set B; and  $B \subseteq A$ . Let  $C = A - B$ .
- Defines a relation over the attributes C that consists of set of tuples from R that match combination of *every* tuple in S.
- Suited to queries that include the phrase “for all”.
- Let  $r$  and  $s$  be relations on schemas R and S respectively where

$$\gg R = (A_1, \dots, A_m, B_1, \dots, B_n)$$

$$\gg S = (B_1, \dots, B_n)$$

The result of  $r \div s$  is a relation on schema

$$R - S = (A_1, \dots, A_m)$$

# Example - Division

Show all staff that use **all** the company's programming languages.

Staff\_Prog  $\div$  Prog

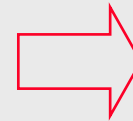
Staff\_Prog

| staffNo | language |
|---------|----------|
| SL10    | COBOL    |
| SA51    | BASIC    |
| SA51    | COBOL    |
| SE14    | BASIC    |
| SE18    | BASIC    |

$\div$

Prog

| language |
|----------|
| COBOL    |
| BASIC    |



| staffNo |
|---------|
| SA51    |

# Summary

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The fundamental intent of the algebra is to allow the writing of the relational expressions.

Selection  $\sigma_{\text{predicate}}(\mathbf{R})$

Projection  $\Pi_{\text{col1}, \dots, \text{coln}}(\mathbf{R})$

Union  $\mathbf{R} \cup \mathbf{S}$

Set difference  $\mathbf{R} - \mathbf{S}$

Intersection  $\mathbf{R} \cap \mathbf{S}$

Cartesian product  $\mathbf{R} \times \mathbf{S}$

# Summary

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Theta join  $\mathbf{R} \bowtie_{\mathbf{F}} \mathbf{S}$

Equijoin  $\mathbf{R} \bowtie_{\mathbf{F}} \mathbf{S}$

Natural join  $\mathbf{R} \bowtie \mathbf{S}$

(Left) Outer join  $\mathbf{R} \bar{\bowtie} \mathbf{S}$

Semijoin  $\mathbf{R} \Join_{\mathbf{F}} \mathbf{S}$

Division  $\mathbf{R} \div \mathbf{S}$