

## COMP408 Assignment #2

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1. [6 points] Show that  $S = \{(2, -2, 5), (-3, 1, 1), (2, 7, -4)\}$  is independent in  $\mathbb{R}^3$ .
2. Answer the following questions related to the vectors  $b_1 = [1, 2, -1]^T$  and  $b_2 = [-1, 1, 3]^T$ :
  - a. [5 points] Show that  $\{b_1, b_2\}$  is a basis of  $S = \text{Span}\{b_1, b_2\}$ .
  - b. [3 points] Find the coordinate vector  $[x]_B$ , where  $x = [-1, 7, 7]^T$ .
  - c. [3 points] Find the vector  $y$ , where  $[y]_B = [5, -6]^T$ .
  - d. [2 points] What is the dimension of  $S$ ?
3. [9 points] Find a basis for each of the spaces  $\text{null}(A)$ ,  $\text{row}(A)$ , and  $\text{col}(A)$ , where
$$\mathbf{A} = \begin{bmatrix} 1 & 2 & 5 & 2 & 4 \\ -1 & -2 & -5 & -2 & -3 \\ 0 & 1 & 3 & -2 & 8 \\ 2 & 3 & 7 & 6 & 0 \end{bmatrix}.$$
4. [10 points] Use a least squares solution to find a parabola that best fits the data points  $(-2, 8)$ ,  $(0, 8)$ ,  $(2, 4)$ , and  $(2, 17)$ .