

$\text{fmap-}\Rightarrow : \forall \{P \ Q \ sd \ sd'\} \rightarrow (P \Rightarrow_s Q) \ sd \rightarrow sd \leq_s sd' \rightarrow (P \Rightarrow_s Q) \ sd'$   
 $\text{fmap-}\Rightarrow P \Rightarrow Q \ sd \leq_s sd' \ sd' \leq_s sd'' \ p = P \Rightarrow Q (\leq_s\text{-trans } sd \leq_s sd' \ sd' \leq_s sd'') \ p$

$\text{fmap-ty} : \forall \{A \ sd \ sd'\} \rightarrow \llbracket A \rrbracket_{\text{ty}} \ sd \rightarrow sd \leq_s sd' \rightarrow \llbracket A \rrbracket_{\text{ty}} \ sd'$

$\text{fmap-ty} \ \{\text{comm}\} = \text{fmap-}\Rightarrow \ \{\text{Compl}\} \ \{\text{Compl}\}$

$\text{fmap-ty} \ \{\text{intexp}\} = \text{fmap-}\Rightarrow \ \{\text{Intcompl}\} \ \{\text{Compl}\}$

$\text{fmap-ty} \ \{\text{intacc}\} = \text{fmap-}\Rightarrow \ \{\text{Compl}\} \ \{\text{Intcompl}\}$

$\text{fmap-ty} \ \{\text{intvar}\} \ ( \ exp \ , \ acc \ ) \ sd \leq_s sd' =$

$( \ \text{fmap-ty} \ \{\text{intexp}\} \ exp \ sd \leq_s sd' \ , \ \text{fmap-ty} \ \{\text{intacc}\} \ acc \ sd \leq_s sd' \ )$

$\text{fmap-ty} \ \{A \Rightarrow B\} = \text{fmap-}\Rightarrow \ \{\llbracket A \rrbracket_{\text{ty}}\} \ \{\llbracket B \rrbracket_{\text{ty}}\}$

$\text{fmap-ctx} : \forall \{\Gamma \ sd \ sd'\} \rightarrow \llbracket \Gamma \rrbracket_{\text{ctx}} \ sd \rightarrow sd \leq_s sd' \rightarrow \llbracket \Gamma \rrbracket_{\text{ctx}} \ sd'$

$\text{fmap-ctx} \ \{ \cdot \} \ \text{unit} \ \_ = \text{unit}$

$\text{fmap-ctx} \ \{\Gamma \ , \ A\} \ (\gamma \ , \ a) \ p = \text{fmap-ctx} \ \gamma \ p \ , \ \text{fmap-ty} \ \{A\} \ a \ p$