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Advanced Policy Gradients

CS 285

Instructor: Sergey Levine

UC Berkeley



Recap: policy gradients

REINFORCE algorithm:



1. sample $\{\tau^i\}$ from $\pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)$ (run the policy)

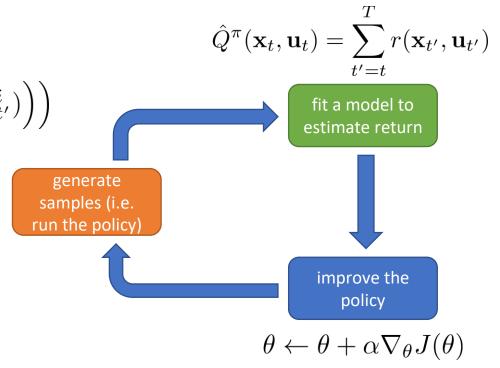
2.
$$\nabla_{\theta} J(\theta) \approx \sum_{i} \left(\sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{t}^{i} | \mathbf{s}_{t}^{i}) \left(\sum_{t'=t}^{T} r(\mathbf{s}_{t'}^{i}, \mathbf{a}_{t'}^{i}) \right) \right)$$

3.
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \hat{Q}_{i,t}^{\pi}$$

"reward to go"

can also use function approximation here



Why does policy gradient work?

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \hat{A}_{i,t}^{\pi}$$



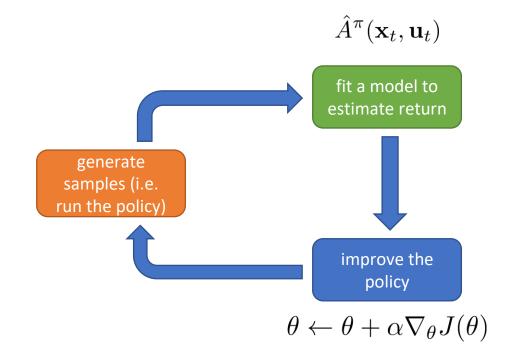
- 1. Estimate $\hat{A}^{\pi}(\mathbf{s}_t, \mathbf{a}_t)$ for current policy π
- 2. Use $\hat{A}^{\pi}(\mathbf{s}_t, \mathbf{a}_t)$ to get improved policy π'

look familiar?

policy iteration algorithm:



- 1. evaluate $A^{\pi}(\mathbf{s}, \mathbf{a})$
- 2. set $\pi \leftarrow \pi'$



Policy gradient as policy iteration

$$J(\theta) = E_{\tau \sim p_{\theta}(\tau)} \left| \sum_{t} \gamma^{t} r(\mathbf{s}_{t}, \mathbf{a}_{t}) \right|$$

$$J(\theta') - J(\theta) = J(\theta') - E_{\mathbf{s}_0 \sim p(\mathbf{s}_0)} [V^{\pi_{\theta}}(\mathbf{s}_0)]$$

$$= J(\theta') - E_{\tau \sim p_{\theta'}(\tau)} [V^{\pi_{\theta}}(\mathbf{s}_0)]$$

$$= J(\theta') - E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t V^{\pi_{\theta}}(\mathbf{s}_t) - \sum_{t=1}^{\infty} \gamma^t V^{\pi_{\theta}}(\mathbf{s}_t) \right]$$

$$= J(\theta') + E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t (\gamma V^{\pi_{\theta}}(\mathbf{s}_{t+1}) - V^{\pi_{\theta}}(\mathbf{s}_t)) \right]$$

$$= E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t r(\mathbf{s}_t, \mathbf{a}_t) \right] + E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t (\gamma V^{\pi_{\theta}}(\mathbf{s}_{t+1}) - V^{\pi_{\theta}}(\mathbf{s}_t)) \right]$$

$$= E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t (r(\mathbf{s}_t, \mathbf{a}_t) + \gamma V^{\pi_{\theta}}(\mathbf{s}_{t+1}) - V^{\pi_{\theta}}(\mathbf{s}_t)) \right]$$

$$= E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t A^{\pi_{\theta}}(\mathbf{s}_t, \mathbf{a}_t) \right]$$

Policy gradient as policy iteration

$$J(\theta') - J(\theta) = E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t} \gamma^t A^{\pi_{\theta}}(\mathbf{s}_t, \mathbf{a}_t) \right]$$
expectation under $\pi_{\theta'}$ advantage under π_{θ}

importance sampling

$$E_{x \sim p(x)}[f(x)] = \int p(x)f(x)dx$$

$$= \int \frac{q(x)}{q(x)}p(x)f(x)dx$$

$$= \int q(x)\frac{p(x)}{q(x)}f(x)dx$$

$$= E_{x \sim q(x)}\left[\frac{p(x)}{q(x)}f(x)\right]$$

$$E_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] = \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta'}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$

$$= \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta'}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$
is it OK to use $p_{\theta}(\mathbf{s}_{t})$ instead?

Ignoring distribution mismatch?

$$\sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta'}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right] \approx \sum_{t} E_{\mathbf{s}_{t}} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$
why do we want this to be true?

why do we want this to be true?

$$J(\theta') - J(\theta) \approx \bar{A}(\theta') \implies \theta' \leftarrow \arg\max_{\theta'} \bar{A}(\theta)$$

2. Use $\hat{A}^{\pi}(\mathbf{s}_t, \mathbf{a}_t)$ to get improved policy π'

is it true? and when?

Claim: $p_{\theta}(\mathbf{s}_t)$ is close to $p_{\theta'}(\mathbf{s}_t)$ when π_{θ} is close to $\pi_{\theta'}$

Bounding the Distribution Change

Ignoring distribution mismatch?

$$\sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta'}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right] \approx \sum_{t} E_{\mathbf{s}_{t}} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$
why do we want this to be true?

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$$J(\theta') - J(\theta) \approx \bar{A}(\theta') \implies \theta' \leftarrow \arg \max_{\theta'} \bar{A}(\theta)$$

2. Use $\hat{A}^{\pi}(\mathbf{s}_t, \mathbf{a}_t)$ to get improved policy π'

is it true? and when?

Claim: $p_{\theta}(\mathbf{s}_t)$ is close to $p_{\theta'}(\mathbf{s}_t)$ when π_{θ} is close to $\pi_{\theta'}$

Bounding the distribution change

Claim: $p_{\theta}(\mathbf{s}_t)$ is close to $p_{\theta'}(\mathbf{s}_t)$ when π_{θ} is close to $\pi_{\theta'}$

Simple case: assume π_{θ} is a deterministic policy $\mathbf{a}_t = \pi_{\theta}(\mathbf{s}_t)$

 $\pi_{\theta'}$ is close to π_{θ} if $\pi_{\theta'}(\mathbf{a}_t \neq \pi_{\theta}(\mathbf{s}_t)|\mathbf{s}_t) \leq \epsilon$

$$p_{\theta'}(\mathbf{s}_t) = (1 - \epsilon)^t p_{\theta}(\mathbf{s}_t) + (1 - (1 - \epsilon)^t)) p_{\text{mistake}}(\mathbf{s}_t)$$

seem familiar?

probability we made no mistakes some other distribution

$$|p_{\theta'}(\mathbf{s}_t) - p_{\theta}(\mathbf{s}_t)| = (1 - (1 - \epsilon)^t)|p_{\text{mistake}}(\mathbf{s}_t) - p_{\theta}(\mathbf{s}_t)| \le 2(1 - (1 - \epsilon)^t)$$
useful identity: $(1 - \epsilon)^t \ge 1 - \epsilon t$ for $\epsilon \in [0, 1]$ $\le 2\epsilon t$

not a great bound, but a bound!

Bounding the distribution change

Claim: $p_{\theta}(\mathbf{s}_t)$ is close to $p_{\theta'}(\mathbf{s}_t)$ when π_{θ} is close to $\pi_{\theta'}$

General case: assume π_{θ} is an arbitrary distribution

 $\pi_{\theta'}$ is close to π_{θ} if $|\pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t) - \pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)| \leq \epsilon$ for all \mathbf{s}_t

Useful lemma: if $|p_X(x)-p_Y(x)| = \epsilon$, exists p(x,y) such that $p(x) = p_X(x)$ and $p(y) = p_Y(y)$ and $p(x=y) = 1 - \epsilon$ $\Rightarrow p_X(x)$ "agrees" with $p_Y(y)$ with probability ϵ $\Rightarrow \pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t)$ takes a different action than $\pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)$ with probability at most ϵ

$$|p_{\theta'}(\mathbf{s}_t) - p_{\theta}(\mathbf{s}_t)| = (1 - (1 - \epsilon)^t)|p_{\text{mistake}}(\mathbf{s}_t) - p_{\theta}(\mathbf{s}_t)| \le 2(1 - (1 - \epsilon)^t)$$

$$\le 2\epsilon t$$

Proof based on: Schulman, Levine, Moritz, Jordan, Abbeel. "Trust Region Policy Optimization."

Bounding the objective value

 $\pi_{\theta'}$ is close to π_{θ} if $|\pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t) - \pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)| \leq \epsilon$ for all \mathbf{s}_t

$$|p_{\theta'}(\mathbf{s}_t) - p_{\theta}(\mathbf{s}_t)| \le 2\epsilon t$$

$$E_{p_{\theta'}(\mathbf{s}_t)}[f(\mathbf{s}_t)] = \sum_{\mathbf{s}_t} p_{\theta'}(\mathbf{s}_t) f(\mathbf{s}_t) \ge \sum_{\mathbf{s}_t} p_{\theta}(\mathbf{s}_t) f(\mathbf{s}_t) - |p_{\theta}(\mathbf{s}_t) - p_{\theta'}(\mathbf{s}_t)| \max_{\mathbf{s}_t} f(\mathbf{s}_t)$$

$$\ge E_{p_{\theta}(\mathbf{s}_t)}[f(\mathbf{s}_t)] - 2\epsilon t \max_{\mathbf{s}_t} f(\mathbf{s}_t)$$

$$\sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta'}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right] \geq O(Tr_{\text{max}}) \text{ or } O\left(\frac{r_{\text{max}}}{1 - \gamma}\right)$$

$$\sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right] - \sum_{t} 2\epsilon t C$$
maximizing this maximizes a bound on the thing we want!

maximizing this maximizes a bound on the thing we want!

Where are we at so far?

$$\theta' \leftarrow \arg\max_{\theta'} \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$
such that $|\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) - \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})| \leq \epsilon$

for small enough ϵ , this is guaranteed to improve $J(\theta') - J(\theta)$

Policy Gradients with Constraints

A more convenient bound

Claim: $p_{\theta}(\mathbf{s}_t)$ is close to $p_{\theta'}(\mathbf{s}_t)$ when π_{θ} is close to $\pi_{\theta'}$

 $\pi_{\theta'}$ is close to π_{θ} if $|\pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t) - \pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)| \leq \epsilon$ for all \mathbf{s}_t

$$|p_{\theta'}(\mathbf{s}_t) - p_{\theta}(\mathbf{s}_t)| \le 2\epsilon t$$

a more convenient bound: $|\pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t) - \pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)| \leq \sqrt{\frac{1}{2}D_{\mathrm{KL}}(\pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t)|\pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t))}$

 $\Rightarrow D_{\mathrm{KL}}(\pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t)||\pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t))$ bounds state marginal difference

$$D_{\text{KL}}(p_1(x)||p_2(x)) = E_{x \sim p_1(x)} \left[\log \frac{p_1(x)}{p_2(x)} \right]$$

KL divergence has some very convenient properties that make it much easier to approximate!

How do we optimize the objective?

$$\theta' \leftarrow \arg\max_{\theta'} \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$
such that $D_{\mathrm{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$

for small enough ϵ , this is guaranteed to improve $J(\theta') - J(\theta)$

How do we enforce the constraint?

$$\theta' \leftarrow \arg\max_{\theta'} \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$
such that $D_{\mathrm{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$

$$\mathcal{L}(\theta', \lambda) = \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right] - \lambda (D_{\mathrm{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) - \epsilon)$$

- 1. Maximize $\mathcal{L}(\theta', \lambda)$ with respect to θ' \leftarrow can do this incompletely (for a few grad steps)
- 2. $\lambda \leftarrow \lambda + \alpha(D_{\mathrm{KL}}(\pi_{\theta'}(\mathbf{a}_t|\mathbf{s}_t)||\pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)) \epsilon)$

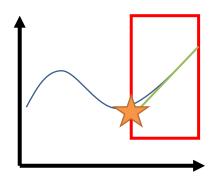
Intuition: raise λ if constraint violated too much, else lower it an instance of dual gradient descent (more on this later!)

Natural Gradient

How (else) do we optimize the objective?

$$\frac{\bar{A}(\theta')}{\theta' \leftarrow \arg\max_{\theta'} \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]}$$
such that $D_{\mathrm{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$

for small enough ϵ , this is guaranteed to improve $J(\theta') - J(\theta)$



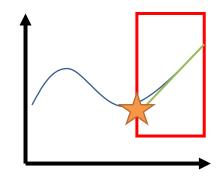
$$\theta' \leftarrow \arg \max_{\theta'} \nabla_{\theta} \bar{A}(\theta)^{T} (\theta' - \theta)$$

such that $D_{\text{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$

Use first order Taylor approximation for objective (a.k.a., linearization)

How do we optimize the objective?

$$\theta' \leftarrow \arg \max_{\theta'} \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$
such that $D_{\text{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$



$$\theta' \leftarrow \arg \max_{\theta'} \nabla_{\theta} \bar{A}(\theta)^{T} (\theta' - \theta)$$

such that $D_{\text{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$

$$\nabla_{\theta'} \bar{A}(\theta') = \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} \nabla_{\theta'} \log \pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$

(see policy gradient lecture for derivation)

$$\nabla_{\theta} \bar{A}(\theta) = \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\frac{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})}{\pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \gamma^{t} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t}) A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right]$$

$$\nabla_{\theta} \bar{A}(\theta) = \sum_{t} E_{\mathbf{s}_{t} \sim p_{\theta}(\mathbf{s}_{t})} \left[E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})} \left[\gamma^{t} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t}) A^{\pi_{\theta}}(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \right] = \nabla_{\theta} J(\theta)$$

exactly the normal policy gradient!

Can we just use the gradient then?

$$\theta' \leftarrow \arg \max_{\theta'} \nabla_{\theta} J(\theta)^{T} (\theta' - \theta)$$

such that $D_{\text{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$

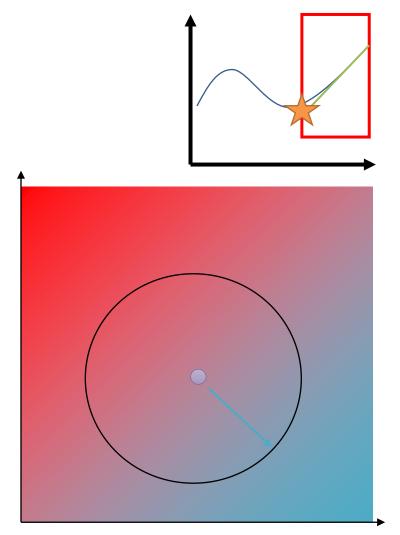
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$
 $\pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t)$

some parameters change probabilities a lot more than others!

Claim: gradient ascent does this:

$$\theta' \leftarrow \arg \max_{\theta'} \nabla_{\theta} J(\theta)^{T} (\theta' - \theta)$$
such that $\|\theta - \theta'\|^{2} \le \epsilon$

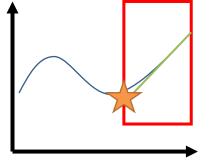
$$\theta' = \theta + \sqrt{\frac{\epsilon}{\|\nabla_{\theta} J(\theta)\|^{2}}} \nabla_{\theta} J(\theta)$$



Can we just use the gradient then?

$$\theta' \leftarrow \arg \max_{\theta'} \nabla_{\theta} J(\theta)^{T} (\theta' - \theta)$$

such that $D_{\text{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$



not the same!

$$\theta' \leftarrow \arg\max_{\theta'} \nabla_{\theta} J(\theta)^T (\theta' - \theta)$$

such that
$$\|\theta - \theta'\|^2 \le \epsilon$$

second order Taylor expansion

$$D_{\mathrm{KL}}(\pi_{\theta'} \| \pi_{\theta}) \approx \frac{1}{2} (\theta' - \theta)^T \mathbf{F} (\theta' - \theta) \qquad \mathbf{F} = E_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta} (\mathbf{a} | \mathbf{s}) \nabla_{\theta} \log \pi_{\theta} (\mathbf{a} | \mathbf{s})^T]$$

$$\mathbf{F} = E_{\pi_{\theta}} [\nabla_{\theta} \log \pi_{\theta}(\mathbf{a}|\mathbf{s}) \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}|\mathbf{s})^{T}]$$
can estimate with samples

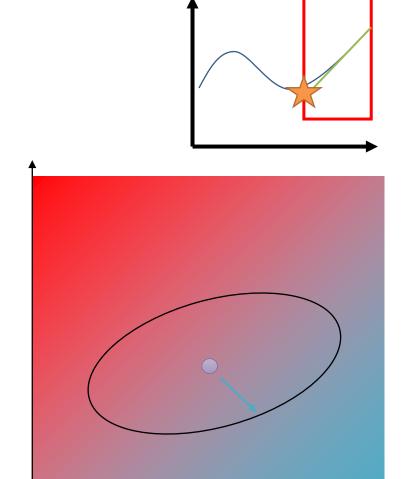
Can we just use the gradient then?

$$\theta' \leftarrow \arg \max_{\theta'} \nabla_{\theta} J(\theta)^{T} (\theta' - \theta)$$

such that $D_{\text{KL}}(\pi_{\theta'}(\mathbf{a}_{t}|\mathbf{s}_{t}) || \pi_{\theta}(\mathbf{a}_{t}|\mathbf{s}_{t})) \leq \epsilon$

$$D_{\mathrm{KL}}(\pi_{\theta'} || \pi_{\theta}) \approx \frac{1}{2} (\theta' - \theta)^T \mathbf{F} (\theta' - \theta)$$

$$\theta' = \theta + \alpha \mathbf{F}^{-1} \nabla_{\theta} J(\theta)$$
 natural gradient
$$\frac{2\epsilon}{}$$



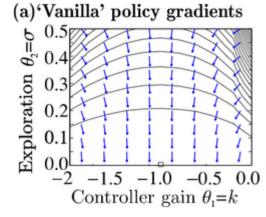
Is this even a problem in practice?



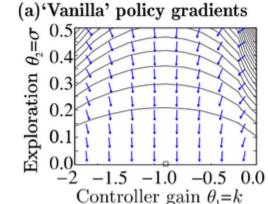
$$r(\mathbf{s}_t, \mathbf{a}_t) = -\mathbf{s}_t^2 - \mathbf{a}_t^2$$

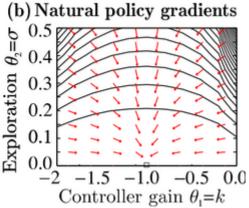
$$\log \pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t) = -\frac{1}{2\sigma^2}(k\mathbf{s}_t - \mathbf{a}_t)^2 + \text{const} \qquad \theta = (k, \sigma)$$

$$\theta = (k, \sigma)$$



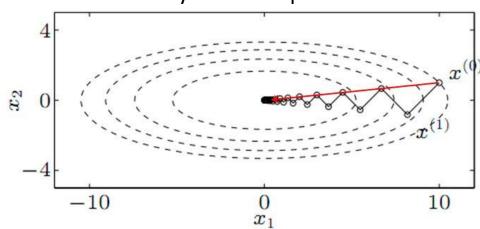
(image from Peters & Schaal 2008)





(figure from Peters & Schaal 2008)

Essentially the same problem as this:



Practical methods and notes

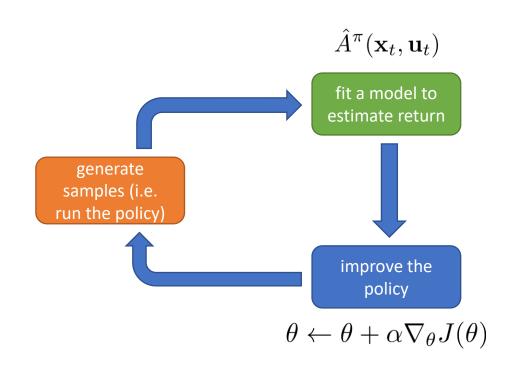
Natural policy gradient

- $\theta' = \theta + \alpha \mathbf{F}^{-1} \nabla_{\theta} J(\theta)$
- Generally a good choice to stabilize policy gradient training
- See this paper for details:
 - Peters, Schaal. Reinforcement learning of motor skills with policy gradients.
- Practical implementation: requires efficient Fisher-vector products, a bit non-trivial to do without computing the full matrix
 - See: Schulman et al. Trust region policy optimization
- Trust region policy optimization
- Just use the IS objective directly
 - Use regularization to stay close to old policy
 - See: Proximal policy optimization

$$\alpha = \sqrt{\frac{2\epsilon}{\nabla_{\theta} J(\theta)^T \mathbf{F} \nabla_{\theta} J(\theta)}}$$

Review

- Policy gradient = policy iteration
- Optimize advantage under new policy state distribution
- Using old policy state distribution optimizes a bound, if the policies are close enough
- Results in *constrained* optimization problem
- First order approximation to objective = gradient ascent
- Regular gradient ascent has the wrong constraint, use natural gradient
- Practical algorithms
 - Natural policy gradient
 - Trust region policy optimization



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