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# Lecture 14: Reinforcement Learning

### Administrative

#### Grades:

- Midterm grades released last night, see Piazza for more information and statistics
- A2 and milestone grades scheduled for later this week

### Administrative

### Projects:

- All teams must register their project, see Piazza for registration form
- Tiny ImageNet evaluation server is online

### Administrative

#### Survey:

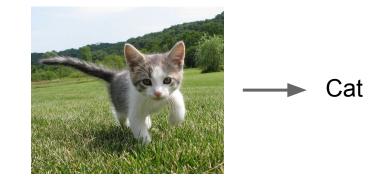
- Please fill out the course survey!
- Link on Piazza or <a href="https://goo.gl/forms/eQpVW7IPjqapsDkB2">https://goo.gl/forms/eQpVW7IPjqapsDkB2</a>

## So far... Supervised Learning

Data: (x, y) x is data, y is label

**Goal**: Learn a *function* to map x -> y

**Examples**: Classification, regression, object detection, semantic segmentation, image captioning, etc.



Classification

## So far... Unsupervised Learning

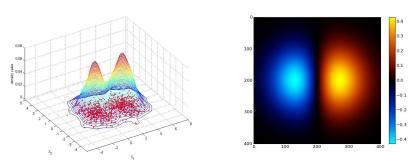
**Data**: x Just data, no labels!

**Goal**: Learn some underlying hidden *structure* of the data

**Examples**: Clustering, dimensionality reduction, feature learning, density estimation, etc.



1-d density estimation



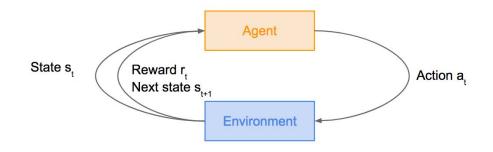
2-d density estimation

2-d density images <u>left</u> and <u>right</u> are <u>CC0 public domain</u>

## Today: Reinforcement Learning

Problems involving an **agent** interacting with an **environment**, which provides numeric **reward** signals

**Goal**: Learn how to take actions in order to maximize reward





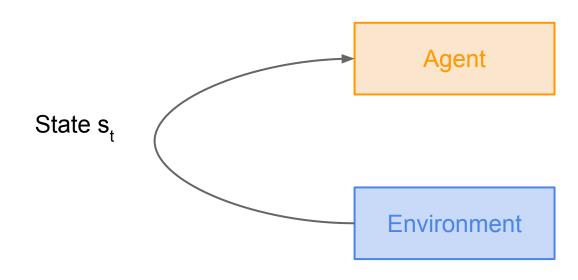
Atari games figure copyright Volodymyr Mnih et al., 2013. Reproduced with permission.

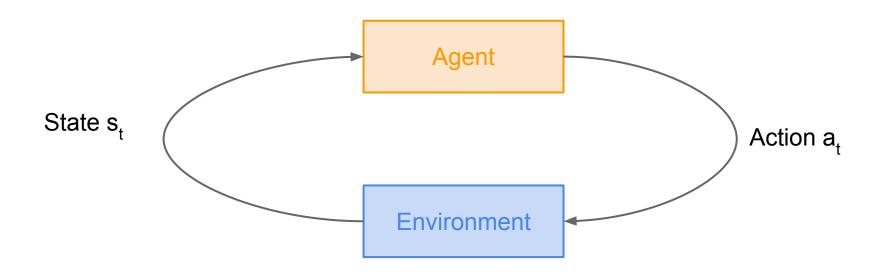
### Overview

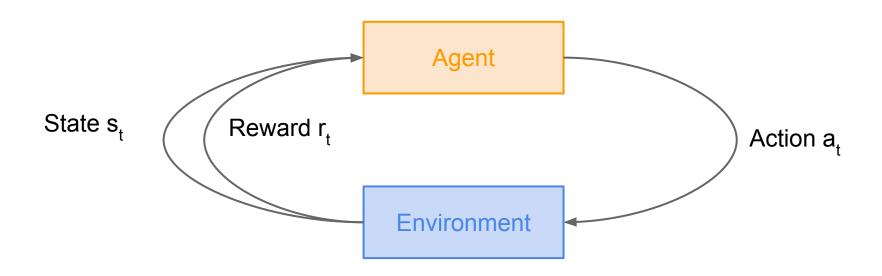
- What is Reinforcement Learning?
- Markov Decision Processes
- Q-Learning
- Policy Gradients

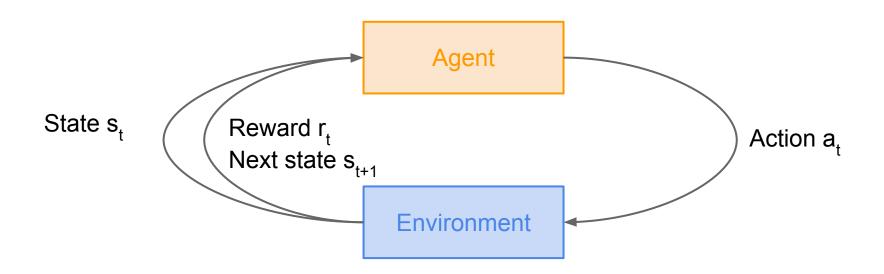
Agent

**Environment** 

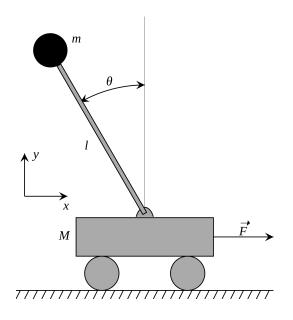








### Cart-Pole Problem



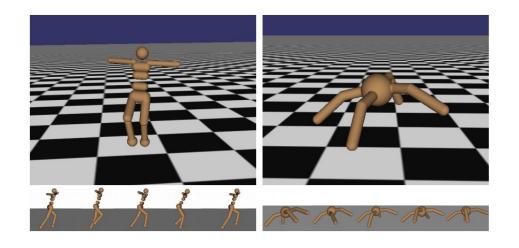
**Objective**: Balance a pole on top of a movable cart

**State:** angle, angular speed, position, horizontal velocity

**Action:** horizontal force applied on the cart

**Reward:** 1 at each time step if the pole is upright

### Robot Locomotion



**Objective**: Make the robot move forward

**State:** Angle and position of the joints

**Action:** Torques applied on joints

**Reward:** 1 at each time step upright +

forward movement

### Atari Games



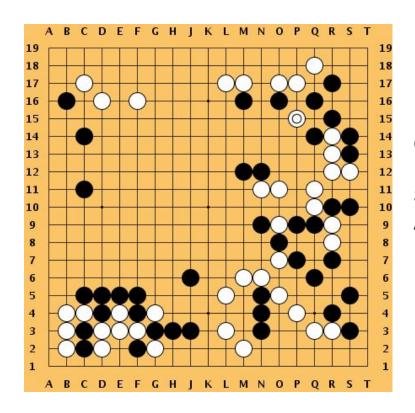
**Objective**: Complete the game with the highest score

**State:** Raw pixel inputs of the game state

**Action:** Game controls e.g. Left, Right, Up, Down

**Reward:** Score increase/decrease at each time step

### Go



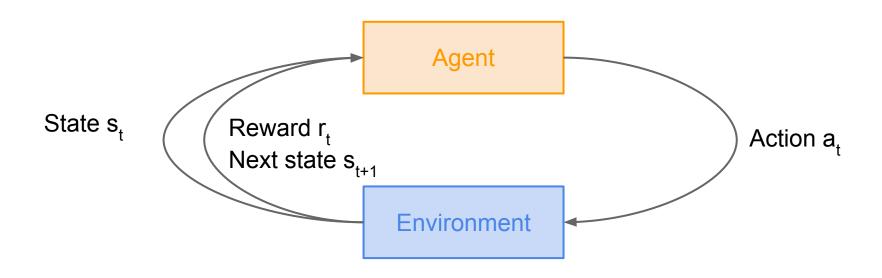
**Objective**: Win the game!

**State:** Position of all pieces

Action: Where to put the next piece down

**Reward:** 1 if win at the end of the game, 0 otherwise

### How can we mathematically formalize the RL problem?



### Markov Decision Process

- Mathematical formulation of the RL problem
- Markov property: Current state completely characterises the state of the world

```
Defined by: (\mathcal{S},\mathcal{A},\mathcal{R},\mathbb{P},\gamma)
```

 ${\cal S}\,$  : set of possible states

 $\mathcal{A}$ : set of possible actions

R: distribution of reward given (state, action) pair

P: transition probability i.e. distribution over next state given (state, action) pair

 $\gamma$ : discount factor

### Markov Decision Process

- At time step t=0, environment samples initial state  $s_0 \sim p(s_0)$
- Then, for t=0 until done:
  - Agent selects action a,
  - Environment samples reward r<sub>t</sub> ~ R( . | s<sub>t</sub>, a<sub>t</sub>)
  - Environment samples next state  $s_{t+1} \sim P(\cdot, |s_t, a_t)$
  - Agent receives reward r, and next state s,+1

- A policy  $\pi$  is a function from S to A that specifies what action to take in each state
- **Objective**: find policy  $\mathbf{\pi}^*$  that maximizes cumulative discounted reward:  $\sum \gamma^t r_t$

### A simple MDP: Grid World

```
actions = {

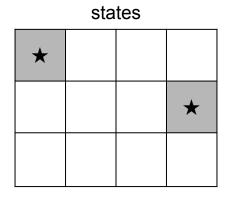
1. right →

2. left →

3. up  

4. down  

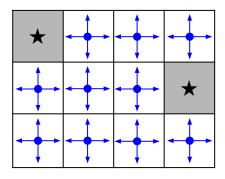
}
```



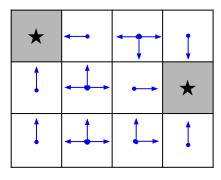
Set a negative "reward" for each transition (e.g. r = -1)

**Objective:** reach one of terminal states (greyed out) in least number of actions

## A simple MDP: Grid World



**Random Policy** 



**Optimal Policy** 

### The optimal policy $\pi^*$

We want to find optimal policy  $\pi^*$  that maximizes the sum of rewards.

How do we handle the randomness (initial state, transition probability...)?

### The optimal policy $\pi^*$

We want to find optimal policy  $\pi^*$  that maximizes the sum of rewards.

How do we handle the randomness (initial state, transition probability...)? Maximize the **expected sum of rewards!** 

Formally: 
$$\pi^* = \arg\max_{\pi} \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | \pi\right]$$
 with  $s_0 \sim p(s_0), a_t \sim \pi(\cdot|s_t), s_{t+1} \sim p(\cdot|s_t, a_t)$ 

#### Definitions: Value function and Q-value function

Following a policy produces sample trajectories (or paths)  $s_0$ ,  $a_0$ ,  $r_0$ ,  $s_1$ ,  $a_1$ ,  $r_1$ , ...

#### Definitions: Value function and Q-value function

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#### How good is a state?

The **value function** at state s, is the expected cumulative reward from following the policy from state s:

$$V^{\pi}(s) = \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | s_0 = s, \pi
ight]$$

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#### How good is a state-action pair?

The **Q-value function** at state s and action a, is the expected cumulative reward from taking action a in state s and then following the policy:

$$Q^\pi(s,a) = \mathbb{E}\left[\sum_{t\geq 0} \gamma^t r_t | s_0 = s, a_0 = a, \pi
ight]$$

### Bellman equation

The optimal Q-value function Q\* is the maximum expected cumulative reward achievable from a given (state, action) pair:

$$Q^*(s,a) = \max_{\pi} \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | s_0 = s, a_0 = a, \pi
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Q\* satisfies the following **Bellman equation**:

$$Q^*(s, a) = \mathbb{E}_{s' \sim \mathcal{E}} \left[ r + \gamma \max_{a'} Q^*(s', a') | s, a \right]$$

**Intuition:** if the optimal state-action values for the next time-step  $Q^*(s',a')$  are known, then the optimal strategy is to take the action that maximizes the expected value of  $r + \gamma Q^*(s',a')$ 

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**Intuition:** if the optimal state-action values for the next time-step Q\*(s',a') are known, then the optimal strategy is to take the action that maximizes the expected value of  $r + \gamma Q^*(s',a')$ 

The optimal policy  $\pi^*$  corresponds to taking the best action in any state as specified by Q\*

Value iteration algorithm: Use Bellman equation as an iterative update

$$Q_{i+1}(s, a) = \mathbb{E}\left[r + \gamma \max_{a'} Q_i(s', a') | s, a\right]$$

Q<sub>i</sub> will converge to Q\* as i -> infinity

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Not scalable. Must compute Q(s,a) for every state-action pair. If state is e.g. current game state pixels, computationally infeasible to compute for entire state space!

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Not scalable. Must compute Q(s,a) for every state-action pair. If state is e.g. current game state pixels, computationally infeasible to compute for entire state space!

Solution: use a function approximator to estimate Q(s,a). E.g. a neural network!

## Solving for the optimal policy: Q-learning

Q-learning: Use a function approximator to estimate the action-value function

$$Q(s, a; \theta) \approx Q^*(s, a)$$

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If the function approximator is a deep neural network => deep q-learning!

Q-learning: Use a function approximator to estimate the action-value function

$$Q(s,a;\theta) pprox Q^*(s,a)$$
 function parameters (weights)

If the function approximator is a deep neural network => deep q-learning!

Remember: want to find a Q-function that satisfies the Bellman Equation:

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#### **Forward Pass**

Loss function: 
$$L_i(\theta_i) = \mathbb{E}_{s,a \sim \rho(\cdot)} \left[ (y_i - Q(s,a;\theta_i))^2 \right]$$

where 
$$y_i = \mathbb{E}_{s' \sim \mathcal{E}}\left[r + \gamma \max_{a'} Q(s', a'; \theta_{i-1}) | s, a\right]$$

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#### **Backward Pass**

Gradient update (with respect to Q-function parameters  $\theta$ ):

$$\nabla_{\theta_i} L_i(\theta_i) = \mathbb{E}_{s, a \sim \rho(\cdot); s' \sim \mathcal{E}} \left[ r + \gamma \max_{a'} Q(s', a'; \theta_{i-1}) - Q(s, a; \theta_i)) \nabla_{\theta_i} Q(s, a; \theta_i) \right]$$

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## Case Study: Playing Atari Games



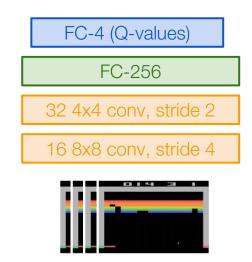
**Objective**: Complete the game with the highest score

**State:** Raw pixel inputs of the game state

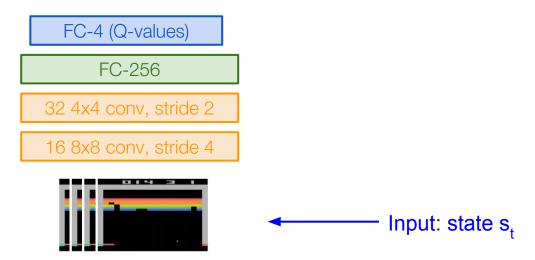
Action: Game controls e.g. Left, Right, Up, Down

Reward: Score increase/decrease at each time step

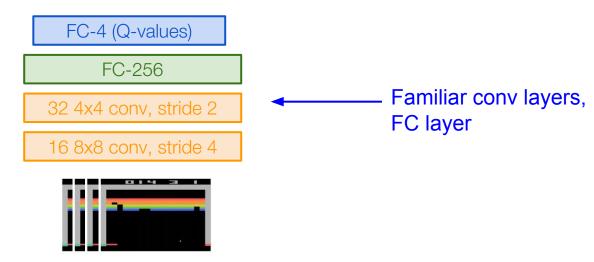
Q(s,a; heta) : neural network with weights heta



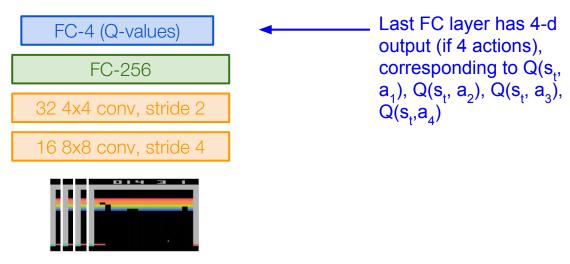
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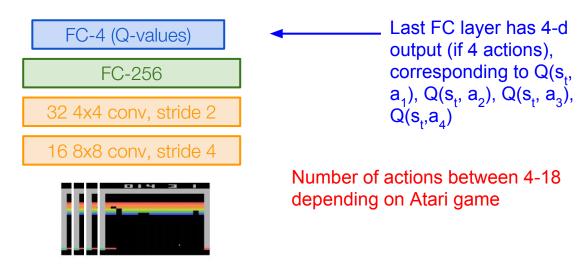
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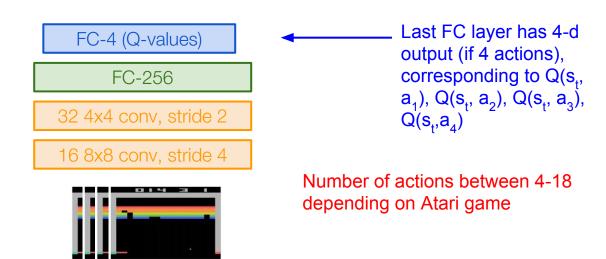


Q(s,a; heta) : neural network with weights heta



Q(s,a; heta) : neural network with weights heta

A single feedforward pass to compute Q-values for all actions from the current state => efficient!



## Training the Q-network: Loss function (from before)

Remember: want to find a Q-function that satisfies the Bellman Equation:

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## Training the Q-network: Experience Replay

Learning from batches of consecutive samples is problematic:

- Samples are correlated => inefficient learning
- Current Q-network parameters determines next training samples (e.g. if maximizing action is to move left, training samples will be dominated by samples from left-hand size) => can lead to bad feedback loops

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#### Address these problems using experience replay

- Continually update a **replay memory** table of transitions (s<sub>t</sub>, a<sub>t</sub>, r<sub>t</sub>, s<sub>t+1</sub>) as game (experience) episodes are played
- Train Q-network on random minibatches of transitions from the replay memory, instead of consecutive samples

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  Each transition can also cont

Each transition can also contribute to multiple weight updates => greater data efficiency

```
Algorithm 1 Deep Q-learning with Experience Replay
   Initialize replay memory \mathcal{D} to capacity N
   Initialize action-value function Q with random weights
   for episode = 1, M do
       Initialise sequence s_1 = \{x_1\} and preprocessed sequenced \phi_1 = \phi(s_1)
       for t = 1, T do
            With probability \epsilon select a random action a_t
            otherwise select a_t = \max_a Q^*(\phi(s_t), a; \theta)
            Execute action a_t in emulator and observe reward r_t and image x_{t+1}
            Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
            Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
            Sample random minibatch of transitions (\phi_i, a_i, r_i, \phi_{i+1}) from \mathcal{D}
            Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
            Perform a gradient descent step on (y_i - Q(\phi_i, a_i; \theta))^2 according to equation 3
       end for
   end for
```

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                                                                                                    Initialize replay memory, Q-network
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   Initialize replay memory \mathcal{D} to capacity N
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                                                                                          ——— Play M episodes (full games)
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   end for
```

#### Algorithm 1 Deep Q-learning with Experience Replay Initialize replay memory $\mathcal{D}$ to capacity NInitialize action-value function Q with random weights for episode = 1, M do Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$ Initialize state for t = 1, T do (starting game With probability $\epsilon$ select a random action $a_t$ screen pixels) at the otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$ beginning of each Execute action $a_t$ in emulator and observe reward $r_t$ and image $x_{t+1}$ episode Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$ Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in $\mathcal{D}$ Sample random minibatch of transitions $(\phi_i, a_i, r_i, \phi_{i+1})$ from $\mathcal{D}$ Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$ Perform a gradient descent step on $(y_i - Q(\phi_i, a_i; \theta))^2$ according to equation 3 end for end for

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Algorithm 1 Deep Q-learning with Experience Replay
   Initialize replay memory \mathcal{D} to capacity N
   Initialize action-value function Q with random weights
   for episode = 1, M do
       Initialise sequence s_1 = \{x_1\} and preprocessed sequenced \phi_1 = \phi(s_1)
       for t = 1, T do
                                                                                                                           For each timestep t
            With probability \epsilon select a random action a_t
                                                                                                                           of the game
            otherwise select a_t = \max_a Q^*(\phi(s_t), a; \theta)
            Execute action a_t in emulator and observe reward r_t and image x_{t+1}
            Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
            Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
            Sample random minibatch of transitions (\phi_i, a_i, r_i, \phi_{i+1}) from \mathcal{D}
           Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
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       for t = 1, T do
            With probability \epsilon select a random action a_t
                                                                                                                     With small probability,
            otherwise select a_t = \max_a Q^*(\phi(s_t), a; \theta)
                                                                                                                     select a random
            Execute action a_t in emulator and observe reward r_t and image x_{t+1}
                                                                                                                     action (explore),
            Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
                                                                                                                     otherwise select
            Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
                                                                                                                     greedy action from
            Sample random minibatch of transitions (\phi_i, a_i, r_i, \phi_{i+1}) from \mathcal{D}
                                                                                                                     current policy
           Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
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            Execute action a_t in emulator and observe reward r_t and image x_{t+1}
            Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
                                                                                                                           Take the action (a,),
                                                                                                                           and observe the
            Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
            Sample random minibatch of transitions (\phi_i, a_i, r_i, \phi_{i+1}) from \mathcal{D}
                                                                                                                           reward r, and next
           Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
                                                                                                                           state s<sub>++1</sub>
            Perform a gradient descent step on (y_i - Q(\phi_i, a_i; \theta))^2 according to equation 3
       end for
   end for
```

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            otherwise select a_t = \max_a Q^*(\phi(s_t), a; \theta)
            Execute action a_t in emulator and observe reward r_t and image x_{t+1}
            Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
                                                                                                                           Store transition in
            Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
                                                                                                                           replay memory
            Sample random minibatch of transitions (\phi_i, a_i, r_i, \phi_{i+1}) from \mathcal{D}
           Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
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                                                                                                                  Experience Replay:
            Sample random minibatch of transitions (\phi_i, a_i, r_i, \phi_{i+1}) from \mathcal{D}
                                                                                                                  Sample a random
           Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
                                                                                                                  minibatch of transitions
                                                                                                                  from replay memory
           Perform a gradient descent step on (y_i - Q(\phi_i, a_i; \theta))^2 according to equation 3
                                                                                                                  and perform a gradient
       end for
                                                                                                                  descent step
  end for
```



https://www.youtube.com/watch?v=V1eYniJ0Rnk

Video by Károly Zsolnai-Fehér. Reproduced with permission.

What is a problem with Q-learning?
The Q-function can be very complicated!

Example: a robot grasping an object has a very high-dimensional state => hard to learn exact value of every (state, action) pair

What is a problem with Q-learning? The Q-function can be very complicated!

Example: a robot grasping an object has a very high-dimensional state => hard to learn exact value of every (state, action) pair

But the policy can be much simpler: just close your hand Can we learn a policy directly, e.g. finding the best policy from a collection of policies?

Formally, let's define a class of parametrized policies:  $\Pi = \{\pi_{\theta}, \theta \in \mathbb{R}^m\}$ 

For each policy, define its value:

$$J( heta) = \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | \pi_ heta
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How can we do this?

Gradient ascent on policy parameters!

Mathematically, we can write:

$$J(\theta) = \mathbb{E}_{\tau \sim p(\tau;\theta)} [r(\tau)]$$
$$= \int_{\tau} r(\tau) p(\tau;\theta) d\tau$$

Where  $r(\tau)$  is the reward of a trajectory  $\tau=(s_0,a_0,r_0,s_1,\ldots)$ 

Expected reward: 
$$J( heta) = \mathbb{E}_{ au \sim p( au; heta)}\left[r( au)
ight] \ = \int_{ au} r( au) p( au; heta) \mathrm{d} au$$

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Now let's differentiate this: 
$$\nabla_{\theta}J(\theta)=\int_{ au}r( au)\nabla_{\theta}p( au; heta)\mathrm{d} au$$

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However, we can use a nice trick: 
$$\nabla_{\theta} p(\tau; \theta) = p(\tau; \theta) \frac{\nabla_{\theta} p(\tau; \theta)}{p(\tau; \theta)} = p(\tau; \theta) \nabla_{\theta} \log p(\tau; \theta)$$

Expected reward: 
$$J(\theta) = \mathbb{E}_{\tau \sim p(\tau;\theta)}\left[r(\tau)\right]$$
 
$$= \int_{-}^{} r(\tau)p(\tau;\theta)\mathrm{d}\tau$$

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However, we can use a nice trick:  $\nabla_{\theta} p(\tau;\theta) = p(\tau;\theta) \frac{\nabla_{\theta} p(\tau;\theta)}{p(\tau;\theta)} = p(\tau;\theta) \nabla_{\theta} \log p(\tau;\theta)$  If we inject this back:

$$\nabla_{\theta} J(\theta) = \int_{\tau} (r(\tau) \nabla_{\theta} \log p(\tau; \theta)) p(\tau; \theta) d\tau$$
$$= \mathbb{E}_{\tau \sim p(\tau; \theta)} [r(\tau) \nabla_{\theta} \log p(\tau; \theta)]$$

Can estimate with Monte Carlo sampling

Can we compute those quantities without knowing the transition probabilities?

We have: 
$$p(\tau; \theta) = \prod_{t \geq 0} p(s_{t+1}|s_t, a_t) \pi_{\theta}(a_t|s_t)$$

Can we compute those quantities without knowing the transition probabilities?

We have: 
$$p( au; heta) = \prod p(s_{t+1}|s_t,a_t)\pi_{ heta}(a_t|s_t)$$

Thus: 
$$\log p(\tau;\theta) = \sum_{t\geq 0}^{\overline{t}\geq 0} \log p(s_{t+1}|s_t,a_t) + \log \pi_{\theta}(a_t|s_t)$$

Can we compute those quantities without knowing the transition probabilities?

We have: 
$$p(\tau; \theta) = \prod_{t \in \mathcal{A}} p(s_{t+1}|s_t, a_t) \pi_{\theta}(a_t|s_t)$$

Thus: 
$$\log p(\tau; \theta) = \sum_{t>0}^{t\geq 0} \log p(s_{t+1}|s_t, a_t) + \log \pi_{\theta}(a_t|s_t)$$

And when differentiating: 
$$\nabla_{\theta} \log p(\tau; \theta) = \sum_{t \geq 0} \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

Doesn't depend on transition probabilities!

$$\nabla_{\theta} J(\theta) = \int_{\tau} (r(\tau) \nabla_{\theta} \log p(\tau; \theta)) p(\tau; \theta) d\tau$$
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Doesn't depend on transition probabilities!

Therefore when sampling a trajectory  $\tau$ , we can estimate  $J(\theta)$  with

$$\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

## Intuition

Gradient estimator:  $\nabla_{\theta} J(\theta) pprox \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$ 

#### Interpretation:

- If  $r(\tau)$  is high, push up the probabilities of the actions seen
- If  $r(\tau)$  is low, push down the probabilities of the actions seen

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#### Interpretation:

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Might seem simplistic to say that if a trajectory is good then all its actions were good. But in expectation, it averages out!

However, this also suffers from high variance because credit assignment is really hard. Can we help the estimator?

## Variance reduction

Gradient estimator:  $\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$ 

## Variance reduction

Gradient estimator: 
$$\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

**First idea:** Push up probabilities of an action seen, only by the cumulative future reward from that state

$$abla_{ heta} J( heta) pprox \sum_{t \geq 0} \left( \sum_{t' \geq t} r_{t'} \right) 
abla_{ heta} \log \pi_{ heta}(a_t | s_t)$$

## Variance reduction

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**Second idea:** Use discount factor  $\gamma$  to ignore delayed effects

$$\nabla_{\theta} J(\theta) pprox \sum_{t \geq 0} \left( \sum_{t' \geq t} \gamma^{t'-t} r_{t'} \right) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

## Variance reduction: Baseline

**Problem:** The raw value of a trajectory isn't necessarily meaningful. For example, if rewards are all positive, you keep pushing up probabilities of actions.

What is important then? Whether a reward is better or worse than what you expect to get

**Idea:** Introduce a baseline function dependent on the state. Concretely, estimator is now:

$$\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} \left( \sum_{t' \geq t} \gamma^{t'-t} r_{t'} - b(s_t) \right) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

$$abla_{\theta} J(\theta) pprox \sum_{t \geq 0} \left( \sum_{t' \geq t} \gamma^{t'-t} r_{t'} - b(s_t) \right) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

A simple baseline: constant moving average of rewards experienced so far from all trajectories

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A simple baseline: constant moving average of rewards experienced so far from all trajectories

Variance reduction techniques seen so far are typically used in "Vanilla REINFORCE"

A better baseline: Want to push up the probability of an action from a state, if this action was better than the **expected value of what we should get from that state**.

Q: What does this remind you of?

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A: Q-function and value function!

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Q: What does this remind you of?

A: Q-function and value function!

Intuitively, we are happy with an action  $a_t$  in a state  $s_t$  if  $Q^{\pi}(s_t, a_t) - V^{\pi}(s_t)$  is large. On the contrary, we are unhappy with an action if it's small.

A better baseline: Want to push up the probability of an action from a state, if this action was better than the **expected value of what we should get from that state**.

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Intuitively, we are happy with an action  $\mathbf{a}_t$  in a state  $\mathbf{s}_t$  if  $Q^{\pi}(s_t, a_t) - V^{\pi}(s_t)$  is large. On the contrary, we are unhappy with an action if it's small.

Using this, we get the estimator:  $\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} (Q^{\pi_{\theta}}(s_t, a_t) - V^{\pi_{\theta}}(s_t)) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$ 

## Actor-Critic Algorithm

**Problem:** we don't know Q and V. Can we learn them?

**Yes,** using Q-learning! We can combine Policy Gradients and Q-learning by training both an **actor** (the policy) and a **critic** (the Q-function).

- The actor decides which action to take, and the critic tells the actor how good its action was and how it should adjust
- Also alleviates the task of the critic as it only has to learn the values of (state, action) pairs generated by the policy
- Can also incorporate Q-learning tricks e.g. experience replay
- **Remark:** we can define by the **advantage function** how much an action was better than expected  $A^{\pi}(s, s) = O^{\pi}(s, s)$

## Actor-Critic Algorithm

```
Initialize policy parameters \theta, critic parameters \phi
For iteration=1, 2 ... do
          Sample m trajectories under the current policy
          \Delta\theta \leftarrow 0
          For i=1, ..., m do
                    For t=1, ..., T do
                             A_t = \sum_{t' \ge t} \gamma^{t'-t} r_t^i - V_\phi(s_t^i)
                              \Delta \theta \leftarrow \Delta \theta + A_t \nabla_{\theta} \log(a_t^i | s_t^i)
         \Delta \phi \leftarrow \sum_{i} \sum_{t} \nabla_{\phi} ||A_{t}^{i}||^{2}\theta \leftarrow \alpha \Delta \theta
          \phi \leftarrow \beta \Delta \phi
```

**End for** 

**Objective:** Image Classification

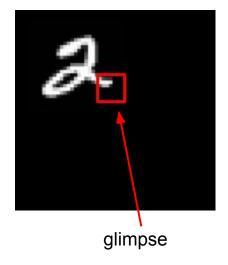
Take a sequence of "glimpses" selectively focusing on regions of the image, to predict class

- Inspiration from human perception and eye movements
- Saves computational resources => scalability
- Able to ignore clutter / irrelevant parts of image

State: Glimpses seen so far

**Action:** (x,y) coordinates (center of glimpse) of where to look next in image

Reward: 1 at the final timestep if image correctly classified, 0 otherwise



**Objective:** Image Classification

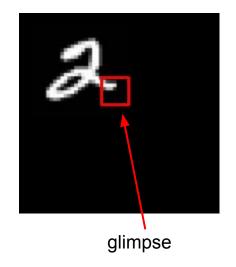
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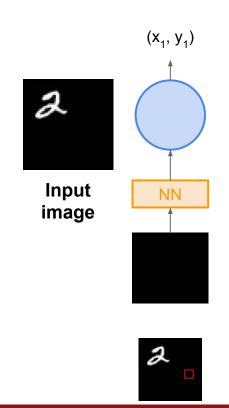
State: Glimpses seen so far

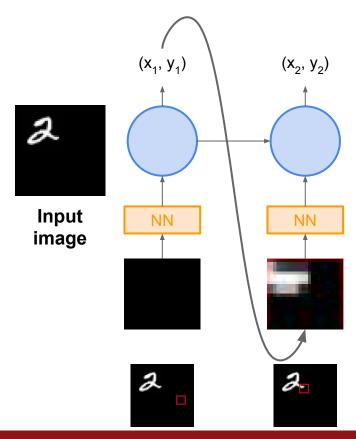
**Action:** (x,y) coordinates (center of glimpse) of where to look next in image

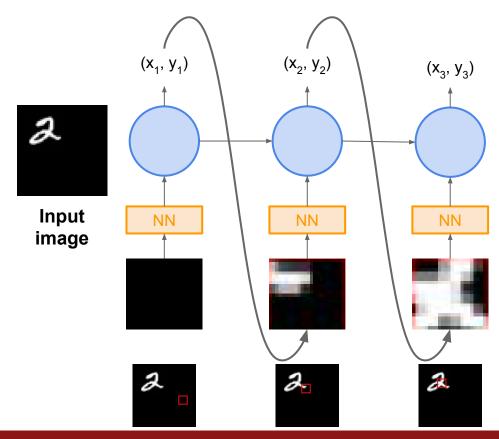
Reward: 1 at the final timestep if image correctly classified, 0 otherwise

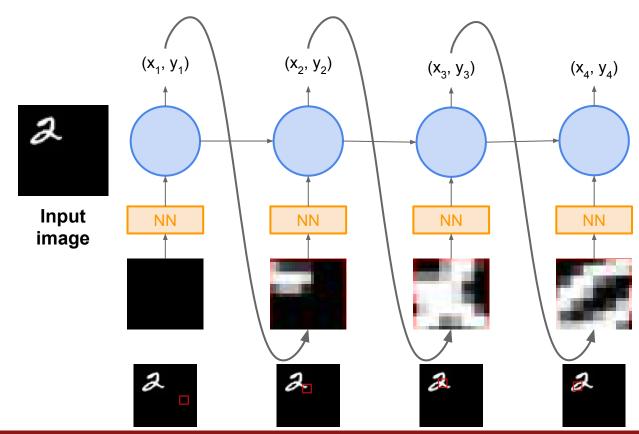


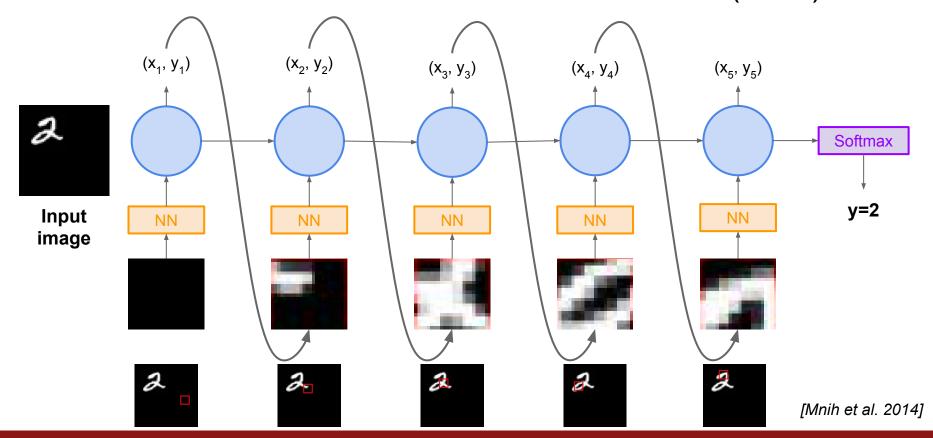
Glimpsing is a non-differentiable operation => learn policy for how to take glimpse actions using REINFORCE Given state of glimpses seen so far, use RNN to model the state and output next action

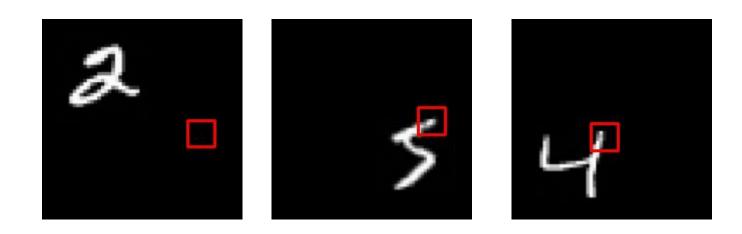












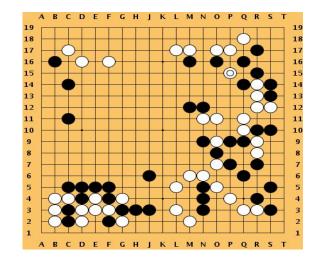
Has also been used in many other tasks including fine-grained image recognition, image captioning, and visual question-answering!

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# More policy gradients: AlphaGo

#### **Overview:**

- Mix of supervised learning and reinforcement learning
- Mix of old methods (Monte Carlo Tree Search) and recent ones (deep RL)



#### How to beat the Go world champion:

- Featurize the board (stone color, move legality, bias, ...)
- Initialize policy network with supervised training from professional go games, then continue training using policy gradient (play against itself from random previous iterations, +1 / -1 reward for winning / losing)
- Also learn value network (critic)
- Finally, combine combine policy and value networks in a Monte Carlo Tree
   Search algorithm to select actions by lookahead search

[Silver et al., Nature 2016]

This image is CC0 public domain

## Summary

- Policy gradients: very general but suffer from high variance so requires a lot of samples. Challenge: sample-efficiency
- **Q-learning**: does not always work but when it works, usually more sample-efficient. **Challenge**: exploration
- Guarantees:
  - **Policy Gradients**: Converges to a local minima of  $J(\theta)$ , often good enough!
  - **Q-learning**: Zero guarantees since you are approximating Bellman equation with a complicated function approximator

## **Next Time**

#### **Guest Lecture: Song Han**

- Energy-efficient deep learning
- Deep learning hardware
- Model compression
- Embedded systems
- And more...

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