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Lecture 5: Value Function Approximation

Emma Brunskill

CS234 Reinforcement Learning.

Winter 2019

The value function approximation structure for today closely follows much of David Silver's Lecture 6.

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VFA for Prediction

3 Control using Value Function Approximation

Class Structure

- Last time: Control (making decisions) without a model of how the world works
- This time: Value function approximation
- Next time: Deep reinforcement learning

Last time: Model-Free Control

- Last time: how to learn a good policy from experience
- So far, have been assuming we can represent the value function or state-action value function as a vector/ matrix
 - Tabular representation
- Many real world problems have enormous state and/or action spaces
- Tabular representation is insufficient

Recall: Reinforcement Learning Involves

- Optimization
- Delayed consequences
- Exploration
- Generalization

Today: Focus on Generalization

- Optimization
- Delayed consequences
- Exploration
- Generalization

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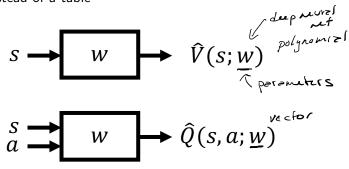
Introduction

VFA for Prediction

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Value Function Approximation (VFA)

 Represent a (state-action/state) value function with a parameterized function instead of a table



Motivation for VFA

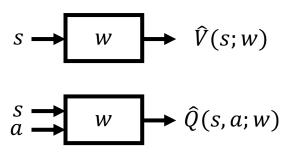
- Don't want to have to explicitly store or learn for every single state a
 - Dynamics or reward model
 - Value
 - State-action value
 - Policy
- Want more compact representation that generalizes across state or states and actions

Benefits of Generalization

- Reduce memory needed to store $(P,R)/V/Q/\pi$
- Reduce computation needed to compute $(P,R)/V/Q/\pi$
- Reduce experience needed to find a good $P, R/V/Q/\pi$

Value Function Approximation (VFA)

 Represent a (state-action/state) value function with a parameterized function instead of a table



• Which function approximator?

Function Approximators

- Many possible function approximators including
 - Linear combinations of features
 - Neural networks
 - · Decision trees highly interpretable
 - Nearest neighbors
 - Fourier/ wavelet bases
- In this class we will focus on function approximators that are differentiable (Why?)
- Two very popular classes of differentiable function approximators
 - Linear feature representations (Today)
 - Neural networks (Next lecture)

Review: Gradient Descent



- Consider a function J(w) that is a differentiable function of a parameter vector w
- ullet Goal is to find parameter $oldsymbol{w}$ that minimizes J
- The gradient of $J(\mathbf{w})$ is $\nabla_{\mathbf{w}} J(\omega) = \begin{bmatrix} \partial J(\omega) & \partial J(\omega) \\ \partial \omega_1 & \partial \omega_2 \end{bmatrix} \qquad \frac{\partial J(\omega)}{\partial \omega_N} = \begin{bmatrix} \partial J(\omega) & \partial J(\omega) \\ \partial \omega_N & \partial \omega_N \end{bmatrix}$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} \leftarrow \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} = \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} = \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} = \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} = \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} = \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} = \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of $J(\mathbf{w})$ is $\vec{\omega} = \vec{\omega} \alpha \quad \nabla_{\mathbf{w}} J(\omega)$ The gradient of

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Value Function Approximation for Policy Evaluation with an Oracle

$$\pi(s) \rightarrow \infty$$
rould be stockash
 $s \rightarrow p(\infty)$

- First assume we could query any state s and an oracle would return the true value for $V^{\pi}(s)$ $(s, \vee^{\pi}(s))$
- The objective was to find the best approximate representation of V^{π} given a particular parameterized function

Stochastic Gradient Descent

- Goal: Find the parameter vector w that minimizes the loss between a true value function $V^{\pi}(s)$ and its approximation $\hat{V}(s; \mathbf{w})$ as represented with a particular function class parameterized by \boldsymbol{w} .
- Generally use mean squared error and define the loss as $J(\mathbf{w}) = \mathbb{E}_{\pi}[(V^{\pi}(s) - \hat{V}(s; \mathbf{w}))^2]$
- Can use gradient descent to find a local minimum

$$\Delta \mathbf{w} = -\frac{1}{2} \alpha \nabla_{\mathbf{w}} J(\mathbf{w})$$

• Stochastic gradient descent (SGD) samples the gradient: Vw J(w) = En /2(UT(s) - V(G, W))] Vw V Δω= α (Uⁿ(s)- Ū(s,ω)) Vω((s) Expected SGD is the same as the full gradient update

Model Free VFA Policy Evaluation

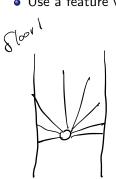
- \bullet Don't actually have access to an oracle to tell true $V^\pi(s)$ for any state s
- Now consider how to do model-free value function approximation for prediction / evaluation / policy evaluation without a model

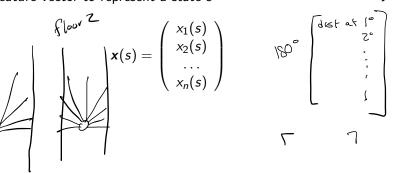
Model Free VFA Prediction / Policy Evaluation

- Recall model-free policy evaluation (Lecture 3)
 - Following a fixed policy π (or had access to prior data)
 - Goal is to estimate V^{π} and/or Q^{π}
- Maintained a look up table to store estimates V^{π} and/or Q^{π}
- Updated these estimates after each episode (Monte Carlo methods) or after each step (TD methods)
- Now: in value function approximation, change the estimate update step to include fitting the function approximator

Feature Vectors

• Use a feature vector to represent a state s







Linear Value Function Approximation for Prediction With An Oracle

 Represent a value function (or state-action value function) for a particular policy with a weighted linear combination of features

$$\hat{V}(s; \mathbf{w}) = \sum_{j=1}^{n} x_j(s) w_j = \mathbf{x}(s)^T \mathbf{w}$$

Objective function is

is
$$\int_{\mathcal{S}} \int_{\mathcal{T}} \int_{\mathcal{T}$$

Recall weight update is

$$\Delta \mathbf{w} = -\frac{1}{2} \alpha \nabla_{\mathbf{w}} J(\mathbf{w})$$

 $\Delta \mathbf{w} = -\frac{1}{2} \alpha \nabla_{\mathbf{w}} J(\mathbf{w})$ • Update is: $\Delta \omega = -\frac{1}{2} \alpha \left(2 \left(V^{\pi}(s) - \hat{V}(s; \omega) \right) \chi(s) \right)$

Update = step-size × prediction error × feature value

Monte Carlo Value Function Approximation

- Return G_t is an unbiased but noisy sample of the true expected return $V^{\pi}(s_t)$
- Therefore can reduce MC VFA to doing supervised learning on a set of (state, return) pairs: $\langle s_1, G_1 \rangle, \langle s_2, G_2 \rangle, \ldots, \langle s_T, G_T \rangle$ estimate of Substitute G_t for the true $V^{\pi}(s_t)$ when fit function approximator
- Concretely when using linear VFA for policy evaluation

$$\Delta \mathbf{w} = \alpha (G_t - \hat{V}(s_t; \mathbf{w})) \nabla_{\mathbf{w}} \hat{V}(s_t; \mathbf{w})$$

$$= \alpha (G_t - \hat{V}(s_t; \mathbf{w})) \mathbf{x}(s_t)$$

$$= \alpha (G_t - \mathbf{x}(s_t)^T \mathbf{w}) \mathbf{x}(s_t)$$

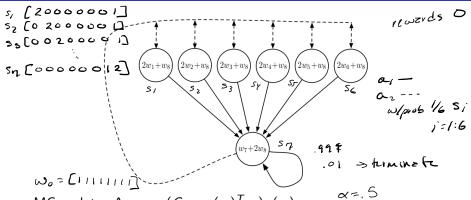
• Note: G_t may be a very noisy estimate of true return

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MC Linear Value Function Approximation for Policy Evaluation

```
1: Initialize \mathbf{w} = \mathbf{0}, k = 1
 2: loop
        Sample k-th episode (s_{k,1}, a_{k,1}, r_{k,1}, s_{k,2}, \dots, s_{k,L_k}) given \pi
 3:
        for t = 1, \ldots, L_k do
 4:
           if First visit to (s) in episode k then could also do every visit
 5:
              G_t(s) = \sum_{i=t}^{L_k} r_{k,i} \gamma^{j-t}
 6:
              Update weights: \omega = \omega - \alpha \left(G_{t}(s) - \hat{V}(s, \omega)\right) X(s)
 7:
           end if
 8.
        end for
 9.
       k = k + 1
10:
11: end loop
```

Baird (1995)-Like Example with MC Policy Evaluation¹



- MC update: $\Delta \mathbf{w} = \alpha (G_t \mathbf{x}(s_t)^T \mathbf{w}) \mathbf{x}(s_t)$
- Small prob s_7 goes to terminal state, $\mathbf{x}(s_7)^T = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 1 & 2 \end{bmatrix}$ $s_1 a_1 O s_7 a_1 O s_7 a_1 O s_1 a_1 O s_2 a_1 O s_2 a_1 O s_2 a_2 O s_2 O s_$

 $\Delta \omega = 0.5 \ (0.5) \times = -0.3 \ (0.5) \times = 0.5$

Convergence Guarantees for Linear Value Function Approximation for Policy Evaluation: Preliminaries

- The Markov Chain defined by a MDP with a particular policy will eventually converge to a probability distribution over states d(s)
- d(s) is called the stationary distribution over states of π
- $\sum_s d(s) = 1$
- d(s) satisfies the following balance equation:

$$d(s') = \sum_{s} \sum_{a} \pi(a|s) p(s'/s, a) d(s)$$

Convergence Guarantees for Linear Value Function Approximation for Policy Evaluation²

• Define the mean squared error of a linear value function approximation for a particular policy π relative to the true value as

$$MSVE(\mathbf{w}) = \sum_{s \in S} d(s)(V^{\pi}(s) - \hat{V}^{\pi}(s; \mathbf{w}))^{2}$$

- where
 - d(s): stationary distribution of π in the true decision process
 - $\hat{V}^{\pi}(s; \mathbf{w}) = \mathbf{x}(s)^{T}\mathbf{w}$, a linear value function approximation

Convergence Guarantees for Linear Value Function Approximation for Policy Evaluation¹

ullet Define the mean squared error of a linear value function approximation for a particular policy π relative to the true value as

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- where
 - d(s): stationary distribution of π in the true decision process
 - $\hat{V}^{\pi}(s; \mathbf{w}) = \mathbf{x}(s)^{T}\mathbf{w}$, a linear value function approximation
- Monte Carlo policy evaluation with VFA converges to the weights *w_{MC}* which has the minimum mean squared error possible:

$$MSVE(\mathbf{w}_{MC}) = \min_{\mathbf{w}} \sum_{s \in S} d(s) (V^{\pi}(s) - \hat{V}^{\pi}(s; \mathbf{w}))^{2}$$

¹Tsitsiklis and Van Roy. An Analysis of Temporal-Difference Learning with Function Approximation. 1997.https://web.stanford.edu/ bvr/pubs/td.pdf

Batch Monte Carlo Value Function Approximation

- ullet May have a set of episodes from a policy π
- Can analytically solve for the best linear approximation that minimizes mean squared error on this data set
- Let $G(s_i)$ be an unbiased sample of the true expected return $V^{\pi}(s_i)$

arg min
$$\sum_{i=1}^{N} (G(s_i) - \mathbf{x}(s_i)^T \mathbf{w})^2$$

Take the derivative and set to 0

$$\boldsymbol{w} = (X^T X)^{-1} X^T \boldsymbol{G}$$

- where G is a vector of all N returns, and X is a matrix of the features of each of the N states $x(s_i)$
- Note: not making any Markov assumptions



Recall: Temporal Difference Learning w/ Lookup Table

- ullet Uses bootstrapping and sampling to approximate V^π
- Updates $V^{\pi}(s)$ after each transition (s, a, r, s'):

$$V^{\pi}(s) = V^{\pi}(s) + \alpha(\underbrace{r + \gamma V^{\pi}(s')}_{Semplin} - V^{\pi}(s))$$

- ullet Target is $r+\gamma V^\pi(s')$, a biased estimate of the true value $V^\pi(s)$
- Represent value for each state with a separate table entry

Temporal Difference (TD(0)) Learning with Value Function Approximation

- ullet Uses bootstrapping and sampling to approximate true V^π
- Updates estimate $V^{\pi}(s)$ after each transition (s, a, r, s'):

$$V^{\pi}(s) = V^{\pi}(s) + \alpha(r + \gamma V^{\pi}(s') - V^{\pi}(s))$$

- Target is $r + \gamma V^{\pi}(s')$, a biased estimate of of the true value $V^{\pi}(s)$
- In value function approximation, target is $r + \gamma \hat{V}^{\pi}(s'; \mathbf{w})$, a biased and approximated estimate of of the true value $V^{\pi}(s)$
- 3 forms of approximation:

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Temporal Difference (TD(0)) Learning with Value Function Approximation

- In value function approximation, target is $r + \gamma \hat{V}^{\pi}(s'; \mathbf{w})$, a biased and approximated estimate of the true value $V^{\pi}(s)$
- Can reduce doing TD(0) learning with value function approximation to supervised learning on a set of data pairs:
 - $\langle s_1, r_1 + \gamma \hat{V}^{\pi}(s_2; \boldsymbol{w}) \rangle, \langle s_2, r_2 + \gamma \hat{V}(s_3; \boldsymbol{w}) \rangle, \dots$
- Find weights to minimize mean squared error

$$J(\mathbf{w}) = \mathbb{E}_{\pi}[(r_j + \gamma \hat{V}^{\pi}(s_{j+1}, \mathbf{w}) - \hat{V}(s_j; \mathbf{w}))^2]$$

Temporal Difference (TD(0)) Learning with Value Function Approximation

- In value function approximation, target is $r + \gamma \hat{V}^{\pi}(s'; \mathbf{w})$, a biased and approximated estimate of the true value $V^{\pi}(s)$
- Supervised learning on a different set of data pairs: $\langle s_1, r_1 + \gamma \hat{V}^{\pi}(s_2; \mathbf{w}) \rangle, \langle s_2, r_2 + \gamma \hat{V}(s_3; \mathbf{w}) \rangle, \dots$
- In linear TD(0) $\Delta \mathbf{w} = \alpha (\mathbf{r} + \gamma \hat{V}^{\pi}(s'; \mathbf{w}) \hat{V}^{\pi}(s; \mathbf{w})) \nabla_{\mathbf{w}} \hat{V}^{\pi}(s; \mathbf{w})$ $= \alpha (\mathbf{r} + \gamma \hat{V}^{\pi}(s'; \mathbf{w}) \hat{V}^{\pi}(s; \mathbf{w})) \mathbf{x}(s)$ $= \alpha (\mathbf{r} + \gamma \mathbf{x}(s')^{T} \mathbf{w} \mathbf{x}(s)^{T} \mathbf{w}) \mathbf{x}(s)$ $= \alpha (\mathbf{r} + \gamma \mathbf{x}(s')^{T} \mathbf{w} \mathbf{x}(s)^{T} \mathbf{w}) \mathbf{x}(s)$

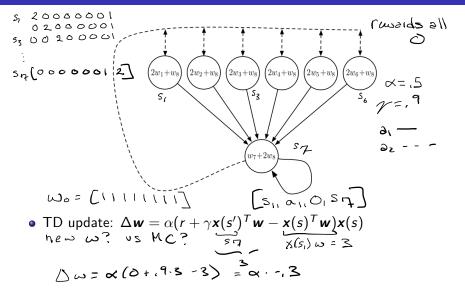
TD(0) Linear Value Function Approximation for Policy Evaluation

- 1: Initialize $\mathbf{w} = \mathbf{0}, k = 1$
- 2: **loop**
- 3: Sample tuple (s_k, a_k, r_k, s_{k+1}) given π
- 4: Update weights:

$$\mathbf{w} = \mathbf{w} + \alpha (\mathbf{r} + \gamma \mathbf{x} (\mathbf{s}')^T \mathbf{w} - \mathbf{x} (\mathbf{s})^T \mathbf{w}) \mathbf{x} (\mathbf{s})$$

- 5: k = k + 1
- 6: end loop

Baird Example with TD(0) On Policy Evaluation ¹



¹Figure from Sutton and Barto 2018

Convergence Guarantees for Linear Value Function Approximation for Policy Evaluation

• Define the mean squared error of a linear value function approximation for a particular policy π relative to the true value as

$$MSVE(\mathbf{w}) = \sum_{s \in S} d(s) (V^{\pi}(s) - \hat{V}^{\pi}(s; \mathbf{w}))^{2}$$

- where
 - d(s): stationary distribution of π in the true decision process
 - $\hat{V}^{\pi}(s; \mathbf{w}) = \mathbf{x}(s)^T \mathbf{w}$, a linear value function approximation
- TD(0) policy evaluation with VFA converges to weights \mathbf{w}_{TD} which is within a constant factor of the minimum mean squared error possible:

$$MSVE(\mathbf{w}_{TD}) \leq \frac{1}{1-\gamma} \min_{\mathbf{w}} \sum_{s \in S} d(s) (V^{\pi}(s) - \hat{V}^{\pi}(s; \mathbf{w}))^2$$

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Check Your Understanding

 Monte Carlo policy evaluation with VFA converges to the weights *w_{MC}* which has the minimum mean squared error possible:

$$MSVE(\mathbf{w}_{MC}) = \min_{\mathbf{w}} \sum_{s \in S} d(s) (\underbrace{V^{\pi}(s) - \hat{V}^{\pi}(s; \mathbf{w})}^{2})^{2}$$

• TD(0) policy evaluation with VFA converges to weights **w**_{TD} which is within a constant factor of the minimum mean squared error possible:

$$MSVE(\boldsymbol{w}_{TD}) \leq \frac{1}{1-\gamma} \min_{\boldsymbol{w}} \sum_{s \in S} d(s) (V^{\pi}(s) - \hat{V}^{\pi}(s; \boldsymbol{w}))^{2}$$

If the VFA is a tabular representation (one feature for each state),
 what is the MSVE for MC and TD?

Convergence Rates for Linear Value Function Approximation for Policy Evaluation

- Does TD or MC converge faster to a fixed point?
- Not (to my knowledge) definitively understood
- Practically TD learning often converges faster to its fixed value function approximation point

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Control using Value Function Approximation

- Use value function approximation to represent state-action values $\hat{Q}^{\pi}(s,a;\mathbf{w}) \approx Q^{\pi}$
- Interleave
 - Approximate policy evaluation using value function approximation
 - ullet Perform ϵ -greedy policy improvement
- Can be unstable. Generally involves intersection of the following:
 - Function approximation
- Sampling

- Bootstrapping
- Off-policy learning

Action-Value Function Approximation with an Oracle

- $\hat{Q}^{\pi}(s,a;oldsymbol{w})pprox Q^{\pi}$
- Minimize the mean-squared error between the true action-value function $Q^{\pi}(s, a)$ and the approximate action-value function:

$$J(\boldsymbol{w}) = \mathbb{E}_{\pi}[(Q^{\pi}(s,a) - \hat{Q}^{\pi}(s,a;\boldsymbol{w}))^2]$$

Use stochastic gradient descent to find a local minimum

$$-\frac{1}{2}\nabla_{\mathbf{W}}J(\mathbf{w}) = \mathbb{E}\left[\left(Q^{\pi}(s,a) - \hat{Q}^{\pi}(s,a;\mathbf{w})\right)\nabla_{\mathbf{w}}\hat{Q}^{\pi}(s,a;\mathbf{w})\right]$$
$$\Delta(\mathbf{w}) = -\frac{1}{2}\alpha\nabla_{\mathbf{w}}J(\mathbf{w})$$

• Stochastic gradient descent (SGD) samples the gradient

Linear State Action Value Function Approximation with an Oracle

• Use features to represent both the state and action

$$m{x}(s,a) = \left(egin{array}{c} x_1(s,a) \ x_2(s,a) \ \dots \ x_n(s,a) \end{array}
ight)$$

 Represent state-action value function with a weighted linear combination of features

$$\hat{Q}(s, a; \mathbf{w}) = \mathbf{x}(s, a)^T \mathbf{w} = \sum_{j=1}^n x_j(s, a) w_j$$

• Stochastic gradient descent update:

$$abla_{oldsymbol{w}}J(oldsymbol{w})=
abla_{oldsymbol{w}}\mathbb{E}_{\pi}[(Q^{\pi}(s,a)-\hat{Q}^{\pi}(s,a;oldsymbol{w}))^{2}]$$

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Incremental Model-Free Control Approaches

- Similar to policy evaluation, true state-action value function for a state is unknown and so substitute a target value
- In Monte Carlo methods, use a return G_t as a substitute target (s_t, a_t)

$$\Delta \mathbf{w} = \alpha (G_t - \hat{Q}(s_t, a_t; \mathbf{w})) \nabla_{\mathbf{w}} \hat{Q}(s_t, a_t; \mathbf{w})$$

• For SARSA instead use a TD target $r + \gamma \hat{Q}(s', a'; \mathbf{w})$ which leverages the current function approximation value

$$\Delta \mathbf{w} = \alpha(\mathbf{r} + \gamma \hat{\mathbf{Q}}(\mathbf{s}', \mathbf{a}'; \mathbf{w}) - \hat{\mathbf{Q}}(\mathbf{s}, \mathbf{a}; \mathbf{w})) \nabla_{\mathbf{w}} \hat{\mathbf{Q}}(\mathbf{s}, \mathbf{a}; \mathbf{w})$$



Incremental Model-Free Control Approaches

- Similar to policy evaluation, true state-action value function for a state is unknown and so substitute a target value
- In Monte Carlo methods, use a return G_t as a substitute target

$$\Delta \mathbf{w} = \alpha (G_t - \hat{Q}(s_t, a_t; \mathbf{w})) \nabla_{\mathbf{w}} \hat{Q}(s_t, a_t; \mathbf{w})$$

• For SARSA instead use a TD target $r + \gamma \hat{Q}(s', a'; \mathbf{w})$ which leverages the current function approximation value

$$\Delta \mathbf{w} = \alpha (\mathbf{r} + \gamma \hat{\mathbf{Q}}(\mathbf{s}', \mathbf{a}'; \mathbf{w}) - \hat{\mathbf{Q}}(\mathbf{s}, \mathbf{a}; \mathbf{w})) \nabla_{\mathbf{w}} \hat{\mathbf{Q}}(\mathbf{s}, \mathbf{a}; \mathbf{w})$$

• For Q-learning instead use a TD target $r + \gamma \max_{a'} \hat{Q}(s', a'; w)$ which leverages the max of the current function approximation value

$$\Delta \mathbf{w} = \alpha (r + \gamma \max_{\mathbf{a}'} \underbrace{\hat{Q}(\mathbf{s}', \mathbf{a}'; \mathbf{w})}_{\mathbf{X}(\mathbf{s}', \mathbf{a}')} - \hat{Q}(\mathbf{s}, \mathbf{a}; \mathbf{w})) \nabla_{\mathbf{w}} \hat{Q}(\mathbf{s}, \mathbf{a}; \mathbf{w})$$

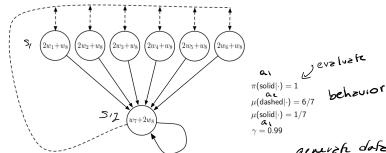
Convergence of TD Methods with VFA



- TD with value function approximation is not following the gradient of an objective function
- Informally, updates involve doing an (approximate) Bellman backup followed by best trying to fit underlying value function to a particular feature representation
- Bellman operators are contractions, but value function approximation fitting can be an expansion $|OV OV'|_{\infty} \leq |V V'|$

$$|OV - OV'|_{\infty} \leq |V - V'|$$
operator
 $p = |V - V'|$

Challenges of Off Policy Control: Baird Example 1

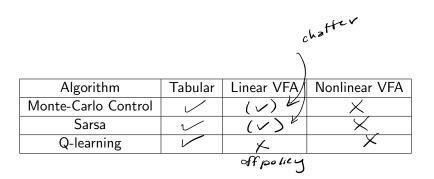


- Behavior policy and target policy are not identical
 Value can diverge $(s_1 \circ f_1 \circ f_2)$
- · Value can diverge (S, α, r, s')

 throw 2ωzy date if α≠π(s)

generate data under schauor pulicy

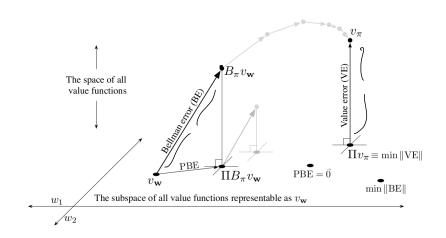
Convergence of Control Methods with VFA



Hot Topic: Off Policy Function Approximation Convergence

- Extensive work in better TD-style algorithms with value function approximation, some with convergence guarantees: see Chp 11 S& B
- Exciting recent work on batch RL that can converge with nonlinear VFA (Dai et al. ICML 2018): uses primal dual optimization
- An important issue is not just whether the algorithm converges, but what solution it converges too
- Critical choices: objective function and feature representation

Linear Value Function Approximation³



³Figure from Sutton and Barto 2018

What You Should Understand

- Be able to implement TD(0) and MC on policy evaluation with linear value function approximation
- Be able to define what TD(0) and MC on policy evaluation with linear VFA are converging to and when this solution has 0 error and non-zero error.
- Be able to implement Q-learning and SARSA and MC control algorithms
- List the 3 issues that can cause instability and describe the problems qualitiatively: function approximation, bootstrapping and off policy learning

Class Structure

- Last time: Control (making decisions) without a model of how the world works
- This time: Value function approximation
- Next time: Deep reinforcement learning

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