

1. For each of the following encryption schemes, state whether the scheme is perfectly secret. Justify your answer in each case.

a. The message space is  $M = \{0, \dots, 4\}$ . Algorithm Gen chooses a uniform key from the key space  $\{0, \dots, 5\}$ .  $Enc_k(m)$  returns  $[k+m \bmod 5]$ , and  $Dec_k(c)$  returns  $[c-k \bmod 5]$ .

Not perfectly secret. When found  $c=0$ , it is more likely to be  $m=0$ , and  $c=1$  is more likely to be  $m=1$ , and  $c=2$  is more likely to be  $m=2$

M	K	C
0	0	0
0	1	1
0	2	2
0	3	3
0	4	4
0	5	0
1	0	1
1	1	2
1	2	3
1	3	4
1	4	0
1	5	1
2	0	2
2	1	3
2	2	4
2	3	0
2	4	1
2	5	2

b. The message space is  $M = \{m \in \{0,1\}^* \mid \text{the last bit of } m \text{ is } 0\}$ . Gen chooses a uniform key from  $\{0,1\}^*-1$ .  $Enc_k(m)$  returns cipher-text  $m \oplus (k \parallel 0)$ , and  $Dec_k(c)$  returns  $c \oplus (k \parallel 0)$ .

As  $k$  is from  $\{0, 1\}^{l-1}$  and  $||$  is logical OR operator, which means  $0 || 1$  is 1,  $0 || 0$  is 0, so there is nothing effect on the  $k$ . Therefore,  $Enc_k(m)$  is actually  $m \oplus k$  and  $Dec_k(c)$  is  $c \oplus k$ , which is the binary cipher.

The binary cipher is perfectly secret, so this is perfectly secret.

## 2. Present two methods to generate pseudo-random numbers using hardware.

Yarrow algorithm

Clock drift