# Assignment #8: 图论: 概念、遍历,及 树算

Updated 1919 GMT+8 Apr 8, 2024

2024 spring, Complied by ==同学的姓名、院系==

#### 说明:

- 1)请把每个题目解题思路(可选),源码Python,或者C++(已经在Codeforces/Openjudge上AC),截图(包含Accepted),填写到下面作业模版中(推荐使用 typora <a href="https://typoraio.cn">https://typoraio.cn</a>,或者用word)。AC或者没有AC,都请标上每个题目大致花费时间。
- 2) 提交时候先提交pdf文件,再把md或者doc文件上传到右侧"作业评论"。Canvas需要有同学清晰头像、提交文件有pdf、"作业评论"区有上传的md或者doc附件。
- 3) 如果不能在截止前提交作业,请写明原因。

#### 编程环境

== (请改为同学的操作系统、编程环境等) ==

操作系统: macOS Ventura 13.4.1 (c)

Python编程环境: Spyder IDE 5.2.2, PyCharm 2023.1.4 (Professional Edition)

C/C++编程环境: Mac terminal vi (version 9.0.1424), g++/gcc (Apple clang version 14.0.3, clang-

1403.0.22.14.1)

# 1. 题目

## 19943: 图的拉普拉斯矩阵

matrices, <a href="http://cs101.openjudge.cn/practice/19943/">http://cs101.openjudge.cn/practice/19943/</a>

请定义Vertex类, Graph类, 然后实现

思路: 把两个类里的各种方法都用了一下

```
class Vertex:
    def __init__(self, key):
        self.id = key
        self.connectedTo = {}

    def addNeighbor(self, nbr, weight=0):
        self.connectedTo[nbr] = weight

    def getConnections(self):
```

```
return self.connectedTo.keys()
    def getId(self):
        return self.id
    def getWeight(self, nbr):
        return self.connectedTo[nbr]
class Graph:
    def __init__(self):
        self.vertList = {}
        self.numVertices = 0
    def addvertex(self, key):
        self.numVertices = self.numVertices + 1
        newVertex = Vertex(key)
        self.vertList[key] = newVertex
        return newVertex
    def getVertex(self, n):
        if n in self.vertList:
            return self.vertList[n]
        else:
            return None
    def addEdge(self, f, t, weight=0):
        if f not in self.vertList:
            nv = self.addvertex(f)
        if t not in self.vertList:
            nv = self.addVertex(t)
        self.vertList[f].addNeighbor(self.vertList[t], weight)
    def getVertices(self):
        return self.vertList.keys()
    def __iter__(self):
        return iter(self.vertList.values())
def constructLaplacianMatrix(n, edges):
    graph = Graph()
    for i in range(n):
        graph.addVertex(i)
    for edge in edges:
        a, b = edge
        graph.addEdge(a, b)
        graph.addEdge(b, a)
    laplacianMatrix = []
    for vertex in graph:
        row = [0] * n
        row[vertex.getId()] = len(vertex.getConnections())
        for neighbor in vertex.getConnections():
            row[neighbor.getId()] = -1
        laplacianMatrix.append(row)
```

```
return laplacianMatrix

n, m = map(int, input().split())
edges = []
for i in range(m):
    a, b = map(int, input().split())
    edges.append((a, b))
laplacianMatrix = constructLaplacianMatrix(n, edges)
for row in laplacianMatrix:
    print(' '.join(map(str, row)))
```

代码运行截图 == (至少包含有"Accepted") ==

状态: Accepted

```
源代码
 class Vertex:
     def __init__(self, key):
    self.id = key
         self.connectedTo = {}
     def addNeighbor(self, nbr, weight=0):
         self.connectedTo[nbr] = weight
     def getConnections(self):
         return self.connectedTo.keys()
     def getId(self):
         return self.id
     def getWeight(self, nbr):
         return self.connectedTo[nbr]
 class Graph:
     def __init__(self):
         self.vertList = {}
         self.numVertices = 0
```

#### 基本信息 #: 44668392 题目: 19943

提交人: 23n2300012140(zyt) 内存: 3752kB 时间: 25ms 语言: Python3

提交时间: 2024-04-15 21:43:09

### 18160: 最大连通域面积

matrix/dfs similar, <a href="http://cs101.openjudge.cn/practice/18160">http://cs101.openjudge.cn/practice/18160</a>

思路: 用上学期提高班的做法处理

```
a = [[-1,-1],[-1,0],[-1,1],[0,-1],[0,1],[1,-1],[1,0],[1,1]]

b = 0

def lianjie(x,y):
    global b
    if juzhen[x][y] == ".":
        return

else:
        b += 1
        juzhen[x][y] = '.'
```

基本信息

代码运行截图 == (至少包含有"Accepted") ==

状态: Accepted

```
#: 44678547
                                                                                  题目: 18160
a = [[-1,-1],[-1,0],[-1,1],[0,-1],[0,1],[1,-1],[1,0],[1,1]]
                                                                                 提交人: 23n2300012140(zyt)
                                                                                  内存: 3740kB
def lianjie(x,y):
                                                                                  时间: 99ms
   global b
                                                                                  语言: Python3
    if juzhen[x][y] == ".":
                                                                               提交时间: 2024-04-16 21:45:24
       b += 1
        juzhen[x][y] = '.'
        for i in range(8):
           lianjie(x+a[i][0],y+a[i][1])
cishu = int(input())
for _ in range(cishu):
   hang, lie = map(int,input().split())
juzhen = [["." for _ in range(lie+2)] for _ in range(hang+2)]
    for w in range(1, hang+1):
       juzhen[w][1:-1] = input()
    daan = 0
    for s in range(1,hang+1):
        for t in range(1,lie+1):
            if juzhen[s][t] == 'W':
```

## sy383: 最大权值连通块

https://sunnywhy.com/sfbj/10/3/383

思路:比较平和的dfs

```
class Vertex:
```

```
def __init__(self,key,weight):
        self.key=key
        self.weight=weight
        self.nbrs=[]
    def addnbr(self,nbr):
        self.nbrs.append(nbr)
class Graph:
    def __init__(self):
       self.vertexs={}
    def addvertex(self,key,weight):
        cur=Vertex(key,weight)
        self.vertexs[key]=cur
        return cur
    def addedge(self,k1,k2):
        self.vertexs[k1].nbrs.append(self.vertexs[k2])
        self.vertexs[k2].nbrs.append(self.vertexs[k1])
def dfs(vertex):
    ans=vertex.weight
    check[vertex.key]=False
    for k in vertex.nbrs:
        if check[k.key]:
            ans+=dfs(k)
            check[k.key]=False
    return ans
n,m=map(int,input().split())
check=[True]*n
weights=list(map(int,input().split()))
p=Graph()
for i in range(n):
    p.addvertex(i,weights[i])
for j in range(m):
    k1,k2=map(int,input().split())
    p.addedge(k1,k2)
ans=0
for vertex in p.vertexs.values():
    if check[vertex.key]:
        ans=max(ans,dfs(vertex))
print(ans)
```



### 03441: 4 Values whose Sum is 0

data structure/binary search, http://cs101.openjudge.cn/practice/03441

思路: 纯用列表就会超时,看到答案的字典加列表感受到巧妙

```
n = int(input())
a = [0]*(n+1)
b = [0]*(n+1)
c = [0]*(n+1)

d = [0]*(n+1)

for i in range(n):
    a[i],b[i],c[i],d[i] = map(int, input().split())

dict1 = {}
for i in range(n):
    for j in range(n):
        if not a[i]+b[j] in dict1:
              dict1[a[i] + b[j]] = 0
              dict1[a[i] + b[j]] += 1

ans = 0
```

```
for i in range(n):
    for j in range(n):
        if -(c[i]+d[j]) in dict1:
            ans += dict1[-(c[i]+d[j])]

print(ans)
```

代码运行截图 == (AC代码截图,至少包含有"Accepted") ==

状态: Accepted

```
源代码
                                                                                           #: 44679173
                                                                                         题目: 03441
 n = int(input())
                                                                                      提交人: 23n2300012140(zyt)
 a = [0]*(n+1)

b = [0]*(n+1)
                                                                                        内存: 171728kB
 c = [0] * (n+1)
                                                                                        时间: 5612ms
 d = [0] * (n+1)
                                                                                        语言: Python3
                                                                                     提交时间: 2024-04-16 22:30:21
 for i in range(n):
     a[i],b[i],c[i],d[i] = map(int, input().split())
 dict1 = {}
 for i in range(n):
     for j in range(n):
         if not a[i]+b[j] in dict1:
    dict1[a[i] + b[j]] = 0
dict1[a[i] + b[j]] += 1
 ans = 0
 for i in range(n):
     for j in range(n):
        if -(c[i]+d[j]) in dict1:
              ans += dict1[-(c[i]+d[j])]
 print(ans)
```

### 04089: 电话号码

trie, http://cs101.openjudge.cn/practice/04089/

Trie 数据结构可能需要自学下。

思路: 学习了题解的方法

```
class TrieNode:
    def __init__(self):
        self.child={}

class Trie:
    def __init__(self):
        self.root = TrieNode()

    def insert(self, nums):
        curnode = self.root
        for x in nums:
```

```
if x not in curnode.child:
                curnode.child[x] = TrieNode()
            curnode=curnode.child[x]
    def search(self, num):
        curnode = self.root
        for x in num:
            if x not in curnode.child:
                return 0
            curnode = curnode.child[x]
        return 1
t = int(input())
p = []
for _ in range(t):
    n = int(input())
    nums = []
    for _ in range(n):
        nums.append(str(input()))
    nums.sort(reverse=True)
    s = 0
    trie = Trie()
    for num in nums:
        s += trie.search(num)
        trie.insert(num)
    if s > 0:
       print('NO')
    else:
        print('YES')
```

代码运行截图 == (AC代码截图,至少包含有"Accepted") ==

#### 状态: Accepted

```
源代码
 class TrieNode:
     def __init__(self):
    self.child={}
 class Trie:
     def __init__(self):
          self.root = TrieNode()
     def insert(self, nums):
         curnode = self.root
          for x in nums:
              if x not in curnode.child:
                 curnode.child[x] = TrieNode()
             curnode=curnode.child[x]
     def search(self, num):
         curnode = self.root
          for x in num:
             if x not in curnode.child:
                 return 0
              curnode = curnode.child[x]
```

基本信息 #: 44676670

> 题目: 04089 提交人: 23n2300012140(zyt)

内存: 24668kB 时间: 392ms 语言: Python3

提交时间: 2024-04-16 19:42:30

### 04082: 树的镜面映射

http://cs101.openjudge.cn/practice/04082/

思路:感觉还是很有难度的,一点一点看题解

```
from collections import deque
class TreeNode:
   def __init__(self, x):
        self.x = x
        self.children = []
def create_node():
    return TreeNode('')
def build_tree(tempList, index):
    node = create_node()
    node.x = tempList[index][0]
    if tempList[index][1] == '0':
        index += 1
        child, index = build_tree(tempList, index)
        node.children.append(child)
        index += 1
        child, index = build_tree(tempList, index)
        node.children.append(child)
    return node, index
def print_tree(p):
    Q = deque()
    s = deque()
    while p is not None:
       if p.x != '$':
            s.append(p)
        p = p.children[1] if len(p.children) > 1 else None
    while s:
       Q.append(s.pop())
    while Q:
        p = Q.popleft()
        print(p.x, end=' ')
        if p.children:
            p = p.children[0]
            while p is not None:
                if p.x != '$':
                    s.append(p)
                p = p.children[1] if len(p.children) > 1 else None
```

代码运行截图 == (AC代码截图,至少包含有"Accepted") ==

状态: Accepted

```
源代码
 from collections import deque
 class TreeNode:
     \begin{array}{ll} \textbf{def} \ \_\underline{\quad} \texttt{init}\underline{\quad} (\texttt{self, x}) : \\ \end{array}
         self.x = x
          self.children = []
 def create node():
     return TreeNode('')
 def build_tree(tempList, index):
     node = create_node()
     node.x = tempList[index][0]
     if tempList[index][1] == '0':
          index += 1
          child, index = build_tree(tempList, index)
          node.children.append(child)
          index += 1
          child, index = build_tree(tempList, index)
          node.children.append(child)
     return node, index
 def print_tree(p):
```

#### 基本信息

#: 44676785 题目: 04082 提交人: 23n2300012140(zyt) 内存: 3712kB 时间: 26ms 语言: Python3 提交时间: 2024-04-16 19:50:01

# 2. 学习总结和收获

==如果作业题目简单,有否额外练习题目,比如: OJ"2024spring每日选做"、CF、LeetCode、洛谷等网站题目。==

本周期中任务繁重,幸好在上学期学习了搜索和图的相关知识。