Homework Assignment #2

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Part 1 Vectors:

1.) Consider again the data on populations, illiteracy rates, and murder rates for 10 states of the United States: population in thousands, percent illiteracy, and murders per 100,000 population. First create the following vectors:

```
illit <- c(2.1, 1.5, 1.8, 1.9, 1.1, 0.7, 1.1, 0.9, 1.3, 2.0)

murder <- c(15.1, 11.3, 7.8, 10.1, 10.3, 6.8, 3.1, 6.2, 10.7, 13.9)

pop <- c(3615, 365, 2212, 2110, 21198, 2541, 3100, 579, 8277, 4931)
```

a. Use rev() to print the elements of illit in reverse order.

```
rev(illit)
## [1] 2.0 1.3 0.9 1.1 0.7 1.1 1.9 1.8 1.5 2.1
```

b. Print the elements of illit that are greater than the median illiteracy rate. Use median() to get the median illiteracy rate.

```
median(illit)
## [1] 1.4
illit[illit[] > median(illit)]
## [1] 2.1 1.5 1.8 1.9 2.0
```

c. Print the elements of murder for which the illiteracy rate is greater than its median.

```
murder[illit[] > median(illit)]
## [1] 15.1 11.3 7.8 10.1 13.9
```

- 2.) Consider again the data on murder rates from the previous exercise.
- a. Write a command involving which() that determines the indices of the murder rates that are greater than 12.

```
which(murder[] > 12, TRUE)
## [1] 1 10
```

b. The following command does the same thing as which (murder > 12):

```
(1:10) [murder >12]
## [1] 1 10
```

Why do you think the parentheses are included in the expression? Experiment a little.

I think that the parentheses are included to show that [murder > 12] needs to be applied to all 10 values.

3.) Consider the data vector:

```
x \leftarrow c(-3, -2, 0, 0, 4, 5, 9, 0, -6, 7, -2, 8)
```

Write a command involving sum() and == that counts the number of elements of x that are equal to 0.

```
sum(x == 0)
## [1] 3
```

Part 2 Matrices and Arrays:

- 4.) Create the following matrix in three different ways:
- a. Using matrix()

```
X \leftarrow \text{matrix}(c(1:5), \text{nrow} = 5, \text{ncol} = 8)
print(X)
##
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## [1,]
          1 1 1 1 1
                                   1
                                        1
                                             1
## [2,]
          2
               2
                     2
                          2
                               2
                                    2
                                              2
                               3
## [3,]
          3
             3 3
                          3
                                    3
                                         3
                                              3
         4
                  4
                       4
               4
                               4
                                    4
                                              4
## [4,]
                                         4
                   5
                               5
                                    5
## [5,]
               5
```

b. Using rbind()

```
rbind(rep(1, times = 8),
     rep(2, times = 8),
     rep(3, times = 8),
     rep(4, times = 8),
     rep(5, times = 8))
##
       [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## [1,]
        1
            1
                    1
                        1
                             1
                                1
                                       1
                                            1
## [2,]
          2
               2
                    2
                         2
                              2
                                  2
                                       2
                                            2
## [3,]
          3
               3
                    3
                         3
                              3
                                  3
                                       3
                                            3
## [4,]
          4
               4
                    4
                         4
                              4
                                  4
                                       4
                                            4
## [5,]
        5
               5 5 5
                              5
                                  5
```

c. Using cbind()

```
cbind(1:5, 1:5, 1:5, 1:5, 1:5, 1:5, 1:5)
##
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## [1,]
           1
                1
                      1
                           1
                                1
                                      1
                                           1
                                                1
## [2,]
           2
                2
                      2
                           2
                                2
                                      2
                                           2
                                                2
                                3
                                      3
## [3,]
           3
                3
                      3
                           3
                                           3
                                                3
## [4,]
           4
                4
                      4
                           4
                                4
                                      4
                                           4
                                                4
## [5,]
           5
                 5
                      5
                           5
                                5
                                      5
                                                5
```

- 5.)
- a. Write a command that uses apply() to find the minimum value in each row of a matrix X.

```
apply(X, MARGIN = 1, min)
## [1] 1 2 3 4 5
```

b. Write a command that uses apply() to sort each column of a matrix X.

```
apply(X, MARGIN = 2, sort)
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
##
## [1,]
                               1
           1
                1
                     1
                          1
                                    1
## [2,]
           2
                2
                     2
                          2
                               2
                                     2
                                          2
                                               2
## [3,]
           3
                3
                     3
                          3
                               3
                                     3
                                          3
                                               3
## [4,]
           4
                4
                     4
                          4
                               4
                                     4
                                          4
                                               4
                5
                        5
                               5
                                     5
## [5,]
        5
                     5
                                               5
```

6.) state.x77 is a dataset that is supplied with R and stored in the form of a matrix. It contains information about the population, income, and other factors for each US state. You can see its values by typing its name, just as you would with datasets that you create yourself:

```
#state.x77
```

a. Write a command involving square brackets [] that prints the first 5 rows of state.x77.

```
state.x77[1:5,]
##
              Population Income Illiteracy Life Exp Murder HS Grad Frost
                                            69.05
                                                                41.3
## Alabama
                    3615
                           3624
                                        2.1
                                                       15.1
                                                                        20
## Alaska
                     365
                           6315
                                        1.5
                                               69.31
                                                       11.3
                                                                66.7
                                                                       152
                    2212
                           4530
                                        1.8
                                               70.55
                                                       7.8
                                                                58.1
## Arizona
                                                                        15
## Arkansas
                    2110
                           3378
                                        1.9
                                               70.66
                                                       10.1
                                                                39.9
                                                                        65
## California
                   21198
                           5114
                                        1.1
                                               71.71
                                                       10.3
                                                                62.6
                                                                        20
##
                Area
## Alabama
               50708
## Alaska
              566432
## Arizona
              113417
## Arkansas
               51945
## California 156361
```

b. Write a command that determines how many rows state.x77 has.

```
nrow(state.x77)
## [1] 50
```

c. Write a command involving square brackets [] that extracts from state.x77 the rows corresponding to states whose graduation rates are below 50

```
state.x77[state.x77[1:50, 6] < 50,]
##
               Population Income Illiteracy Life Exp Murder HS Grad Frost
## Alabama
                                          69.05
                     3615
                           3624
                                2.1
                                                  15.1
                                                          41.3
## Arkansas
                     2110
                           3378
                                     1.9
                                            70.66
                                                   10.1
                                                          39.9
                                                                 65
## Georgia
                    4931
                           4091
                                     2.0
                                           68.54
                                                  13.9
                                                          40.6
                                                                 60
                    3387 3712
                                                          38.5
## Kentucky
                                     1.6 70.10 10.6
                                                                 95
                    3806 3545
                                     2.8 68.76 13.2
                                                         42.2
## Louisiana
                                                               12
## Mississippi
                   2341 3098
                                     2.4 68.09
                                                  12.5
                                                         41.0
                                                               50
## Missouri
                    4767 4254
                                    0.8 70.69
                                                  9.3
                                                         48.8
                                                                108
                 5441
                           3875
                                    1.8
                                          69.21
                                                          38.5
## North Carolina
                                                  11.1
                                                                80
## Rhode Island
                    931
                           4558
                                     1.3
                                           71.90
                                                   2.4
                                                         46.4
                                                                127
                   2816
## South Carolina
                           3635
                                     2.3
                                           67.96
                                                   11.6
                                                          37.8
                                                                 65
## Tennessee
                    4173
                           3821
                                    1.7
                                           70.11
                                                  11.0
                                                         41.8
                                                                 70
                                                         47.4
                   12237
                                                                 35
## Texas
                           4188
                                    2.2 70.90 12.2
## Virginia
                    4981
                           4701
                                    1.4 70.08 9.5
                                                         47.8
                                                                 85
## West Virginia
                     1799
                                    1.4 69.48
                                                          41.6
                           3617
                                                  6.7
                                                               100
##
                Area
                50708
## Alabama
## Arkansas
                51945
## Georgia
                58073
## Kentucky
                39650
## Louisiana
                44930
## Mississippi
                47296
## Missouri
                68995
## North Carolina 48798
## Rhode Island
                1049
## South Carolina 30225
## Tennessee
               41328
               262134
## Texas
## Virginia
               39780
## West Virginia
                24070
```

d. Find the mean life expectancy for states whose high school graduation rates are below 50

```
mean(state.x77[state.x77[1:50,6] < 50, 4])
## [1] 69.68071
```

e. Find the mean and standard deviation of each column.

```
mean(state.x77[,1])
## [1] 4246.42
```

```
sd(state.x77[,1])
## [1] 4464.491
mean(state.x77[,2])
## [1] 4435.8
sd(state.x77[,2])
## [1] 614.4699
mean(state.x77[,3])
## [1] 1.17
sd(state.x77[,3])
## [1] 0.6095331
mean(state.x77[,4])
## [1] 70.8786
sd(state.x77[,4])
## [1] 1.342394
mean(state.x77[,5])
## [1] 7.378
sd(state.x77[,5])
## [1] 3.69154
mean(state.x77[,6])
## [1] 53.108
sd(state.x77[,6])
## [1] 8.076998
mean(state.x77[,7])
## [1] 104.46
sd(state.x77[,7])
## [1] 51.98085
mean(state.x77[,8])
## [1] 70735.88
sd(state.x77[,8])
## [1] 85327.3
```

1.) Write commands that:

a. Locate all rows of a matrix X that are all-zero. Hint: One way to do this is to write a function all.zero() that takes a vector argument x and checks whether all of its elements are equal to 0 or not, returning TRUE if they are and FALSE otherwise. The function all() may come in handy. Then use apply() to apply all.zero() to each row of the matrix.

```
set.seed(1)
X <- matrix(sample(0:1, size = 150, replace = TRUE), nrow = 30)</pre>
Χ
##
         [,1] [,2] [,3] [,4] [,5]
##
    [1,]
                 0
                       1
                            0
##
    [2,]
            0
                 1
                       0
    [3,]
                 0
                       0
                                 0
##
            1
                            1
    [4,]
                 0
                       0
                                 0
##
            1
                            1
##
    [5,]
            0
                 1
                       1
                            1
                                 1
##
    [6,]
            1
                 1
                       0
                            1
                                 0
##
    [7,]
                       0
            1
                 1
                            0
                                 1
                 0
##
   [8,]
            1
                      1
                            0
                                 0
##
   [9,]
                 1
                      0
                                 0
## [10,]
            0
                 0
                      1
                            1
                                 1
## [11,]
                 1
                      0
            0
                            1
                                 1
## [12,]
            0
                 1
                       1
                            0
                                 0
## [13,]
            1
                 1
                       0
                            0
                                 0
                 1
                       0
## [14,]
            0
                            1
                                 1
                       0
## [15,]
                 1
                            1
            1
                                 1
## [16,]
            0
                 1
                       1
                            0
                                 1
## [17,]
                 0
## [18,]
                 0
                       0
                            0
                                 1
            1
## [19,]
            0
                 1
                       1
                            1
                                 1
## [20,]
            1
                 1
                       1
                            1
                                 1
## [21,]
            1
                 0
                       0
                            1
                                 1
## [22,]
            0
                 1
                       1
                            1
                                 1
## [23,]
                 0
                      0
                            0
            1
                                 0
## [24,]
               0
                      0
            0
                            0
                                 0
## [25,]
               0
                            0
                      1
                                1
## [26,]
            0
                 0
                      0
                            0
                                 0
## [27,]
            0
                 0
                       1
                                 0
                            1
## [28,]
            0
                 1
                       0
                            0
                                 1
## [29,]
                 1
                       0
                            0
            1
                                 0
## [30,]
                 0
            0
                            1
                                 1
all.zero <- function(x) {
  return (all(x == 0))
apply(X, MARGIN = 1, all.zero)
    [1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
   [12] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [23] FALSE TRUE FALSE TRUE FALSE FALSE FALSE
```

b. Find the first all-zero row of a matrix X.

```
X[(apply(X, MARGIN = 1, all.zero)),]
## [,1] [,2] [,3] [,4] [,5]
## [1,] 0 0 0 0 0
## [2,] 0 0 0 0 0
```

c. Compute the mean of the rows in which nonzero elements appear.

```
mean(X[(!apply(X, MARGIN = 1, all.zero))])
## [1] 0.5285714
```

d. Compute the mean of the nonzero elements in each row.

```
split <- X[!apply(X, MARGIN = 1, all.zero),]</pre>
for (i in 1:28) {
 print(mean(split[i,]))
## [1] 0.4
## [1] 0.2
## [1] 0.4
## [1] 0.4
## [1] 0.8
## [1] 0.6
## [1] 0.6
## [1] 0.4
## [1] 0.6
## [1] 0.6
## [1] 0.6
## [1] 0.4
## [1] 0.4
## [1] 0.6
## [1] 0.8
## [1] 0.6
## [1] 0.6
## [1] 0.4
## [1] 0.8
## [1] 1
## [1] 0.6
## [1] 0.8
## [1] 0.2
## [1] 0.4
## [1] 0.4
## [1] 0.4
## [1] 0.4
## [1] 0.4
```

e. Locate all rows for which the sum of the elements is odd.

```
X[((apply(X, MARGIN = 1, sum)) %% 2) != 0,]
## [,1] [,2] [,3] [,4] [,5]
```

```
[1,]
         0
            1
                  0
                      0
                          0
##
##
   [2,]
         1
             1
                  0
                      1
                          0
##
   [3,]
             1
                  0
                      0
         1
                          1
##
  [4,]
             1
                  0
                      1
                          0
         1
##
  [5,]
        0 0
                 1
  [6,]
##
                  0
        0 1
                      1
                         1
##
  [7,]
        0 1
                  0
                      1
                         1
           1
        0
##
  [8,]
                  1
                      0
                          1
##
  [9,]
        1
             0
                  1
                      0
                          1
        1
            1
## [10,]
                  1
                      1
                          1
        1 0
                 0
## [11,]
                     1
                          1
## [12,]
       1 0
                  0
                      0
```

Part 3 Lists:

- 8.) The function lapply() is designed to execute a function, given as an argument FUN to lapply(), on each element of a list.
- a. Use list() to construct a list containing the following three vectors:

```
v1 <- c(23, 18, 34, 14, 19, 22, 67, 37)

v2 <- c(0.1, 0.0, 3.0, 2.4, 4.1, 1.5, 1.2, 2.2)

v3 <- c("h", "b", "d", "c", "a", "f", "e", "g")

mylist <- list(v1, v2, v3)
```

b. Now use lapply() and sort() to sort each component of the list.

```
lapply(mylist, sort)

## [[1]]
## [1] 14 18 19 22 23 34 37 67

##

## [[2]]
## [1] 0.0 0.1 1.2 1.5 2.2 2.4 3.0 4.1

##

## [[3]]
## [1] "a" "b" "c" "d" "e" "f" "g" "h"
```