

Homework 1 - Jackson Wakefield - jswakefi

1.1) FIRST SETS

a) Initialization pass

- i) $\text{FIRST}(b) = \{b\}$
- ii) $\text{FIRST}(c) = \{c\}$
- iii) $\text{FIRST}(d) = \{d\}$
- iv) $\text{FIRST}(\&) = \{\&\}$
- v) $\text{FIRST}(!) = \{!\}$
- vi) $\text{FIRST}(\epsilon) = \{\epsilon\}$
- vii) $\text{FIRST}(S) = \{\}$
- viii) $\text{FIRST}(A) = \{\}$
- ix) $\text{FIRST}(B) = \{\}$
- x) $\text{FIRST}(C) = \{\}$
- xi) $\text{FIRST}(D) = \{\}$

b) First Pass

- i) $\text{FIRST}(b) = \{b\}$
- ii) $\text{FIRST}(c) = \{c\}$
- iii) $\text{FIRST}(d) = \{d\}$
- iv) $\text{FIRST}(\&) = \{\&\}$
- v) $\text{FIRST}(!) = \{!\}$
- vi) $\text{FIRST}(\epsilon) = \{\epsilon\}$
- vii) $\text{FIRST}(S) = \{\}$
- viii) $\text{FIRST}(A) = \{\}$
- ix) $\text{FIRST}(B) = \{b, \epsilon\}$
- x) $\text{FIRST}(C) = \{\epsilon\}$
- xi) $\text{FIRST}(D) = \{d, \epsilon\}$

c) Second Pass

- i) $\text{FIRST}(b) = \{b\}$
- ii) $\text{FIRST}(c) = \{c\}$
- iii) $\text{FIRST}(d) = \{d\}$
- iv) $\text{FIRST}(\&) = \{\&\}$
- v) $\text{FIRST}(!) = \{!\}$
- vi) $\text{FIRST}(\epsilon) = \{\epsilon\}$
- vii) $\text{FIRST}(S) = \{\}$
- viii) $\text{FIRST}(A) = \{d, \epsilon\}$
- ix) $\text{FIRST}(B) = \{b, \epsilon, d, c\}$
- x) $\text{FIRST}(C) = \{\epsilon, d, c\}$
- xi) $\text{FIRST}(D) = \{d, \epsilon\}$

d) Final Results

- i) $\text{FIRST}(b) = \{b\}$
 - ii) $\text{FIRST}(c) = \{c\}$
 - iii) $\text{FIRST}(d) = \{d\}$
 - iv) $\text{FIRST}(\&) = \{\&\}$
 - v) $\text{FIRST}(!) = \{!\}$
 - vi) $\text{FIRST}(\epsilon) = \{\epsilon\}$
 - vii) $\text{FIRST}(S) = \{d, b, c, \epsilon, \&\}$
 - viii) $\text{FIRST}(A) = \{d, \epsilon, b, c, \&\}$
 - ix) $\text{FIRST}(B) = \{b, \epsilon, d, c, \&\}$
 - x) $\text{FIRST}(C) = \{\epsilon, d, c, b, \&\}$
 - xi) $\text{FIRST}(D) = \{d, \epsilon\}$
-

1.2) FOLLOW SETS

e) Initialization Pass/One Pass

- i) $\text{FOLLOW}(S) = \{\$ \}$
- ii) $\text{FOLLOW}(A) = \{b, d, c, \&\}$
- iii) $\text{FOLLOW}(B) = \{b, d, c, \&, !\}$
- iv) $\text{FOLLOW}(C) = \{d\}$
- v) $\text{FOLLOW}(D) = \{\}$

f) First Pass

- i) $\text{FOLLOW}(S) = \{\$ \}$
- ii) $\text{FOLLOW}(A) = \{b, d, c, \&, \$ \}$
- iii) $\text{FOLLOW}(B) = \{b, d, c, \&, !, \$ \}$
- iv) $\text{FOLLOW}(C) = \{d, \$, b, c, \&, !\}$
- v) $\text{FOLLOW}(D) = \{\$, b, d, c, \&\}$

g) Second Pass

- i) $\text{FOLLOW}(S) = \{\$ \}$
- ii) $\text{FOLLOW}(A) = \{b, d, c, \&, \$ \}$
- iii) $\text{FOLLOW}(B) = \{b, d, c, \&, !, \$ \}$
- iv) $\text{FOLLOW}(C) = \{d, \$, b, c, \&, !\}$
- v) $\text{FOLLOW}(D) = \{\$, b, d, c, \&\}$

h) Final Results

- i) $\text{FOLLOW}(S) = \{\$ \}$
- ii) $\text{FOLLOW}(A) = \{b, d, c, \&, \$ \}$
- iii) $\text{FOLLOW}(B) = \{b, d, c, \&, !, \$ \}$
- iv) $\text{FOLLOW}(C) = \{d, \$, b, c, \&, !\}$
- v) $\text{FOLLOW}(D) = \{\$, b, d, c, \&\}$

2) Predictive Parser - Unsatisfied Cases

a) FIRST/FOLLOW (terminals and epsilon not shown)

- i) $\text{FIRST}(S) = \{c, a\}$
- ii) $\text{FIRST}(A) = \{d, a\}$
- iii) $\text{FIRST}(B) = \{a, \text{epsilon}\}$
- iv) $\text{FIRST}(C) = \{d, a, \text{epsilon}\}$
- v) $\text{FIRST}(D) = \{d, \text{epsilon}\}$
- vi) $\text{FOLLOW}(S) = \{\$, b, E\}$
- vii) $\text{FOLLOW}(A) = \{\}$
- viii) $\text{FOLLOW}(B) = \{c, a\}$
- ix) $\text{FOLLOW}(C) = \{c, a\}$
- x) $\text{FOLLOW}(D) = \{c, a\}$

b) RDP PARSING RULES

- i) A
 - (1) Condition 1 not met, $\text{FIRST}(CS)$ is not disjoint to $\text{FIRST}(CSE)$
(they are equal in fact, as $\text{FIRST}(S)$ does not include epsilon)
- ii) C
 - (1) Condition 1 not met, $\text{FIRST}(DB)$ is not disjoint to $\text{FIRST}(B)$, they both include "a", as $\text{FIRST}(D)$ includes epsilon
 - (2) Condition 2 not met, $\text{FIRST}(C)$ is not disjoint to $\text{FOLLOW}(C)$, both include "a"
- iii) B
 - (1) Condition 2 not met, $\text{FIRST}(B)$ is not disjoint to $\text{FOLLOW}(B)$, both include "a"

3) Predictive Parser - Satisfied Cases and Parse Function

a) FIRST/FOLLOW (terminals and epsilon not shown)

- i) $\text{FIRST}(S) = \{s, f, e, d, k\}$
- ii) $\text{FIRST}(A) = \{f, e, d, \text{epsilon}\}$
- iii) $\text{FIRST}(B) = \{b, g\}$
- iv) $\text{FIRST}(C) = \{c, e, \text{epsilon}\}$
- v) $\text{FIRST}(D) = \{d, \text{epsilon}\}$
- vi) $\text{FIRST}(E) = \{e, \text{epsilon}\}$
- vii) $\text{FOLLOW}(S) = \{\$, t\}$
- viii) $\text{FOLLOW}(A) = \{k, g\}$
- ix) $\text{FOLLOW}(B) = \{c, e, \$, t\}$
- x) $\text{FOLLOW}(C) = \{\$, t\}$
- xi) $\text{FOLLOW}(D) = \{k, g\}$
- xii) $\text{FOLLOW}(E) = \{d, k, g, \$, t\}$

b) RDP PARSING RULES

i) S

- (1) Condition 1 met, FIRST(sSt) is disjoint to FIRST(AkBC)
- (2) Condition 2 does not apply

ii) A

- (1) Condition 1 met, FIRST(fAg) is disjoint to FIRST(ED)
- (2) Condition 2 met, FIRST(A) is disjoint to FOLLOW(A)

iii) B

- (1) Condition 1 met, FIRST(bB) is disjoint to FIRST(g)
- (2) Condition 2 does not apply

iv) C

- (1) Condition 1 met, FIRST(c) is disjoint to FIRST(E)
- (2) Condition 2 met, FIRST(C) is disjoint to FOLLOW(C)

v) D

- (1) Condition 1 met, FIRST(dD) is disjoint to FIRST(epsilon)
- (2) Condition 2 met, FIRST(D) is disjoint to FOLLOW(D)

vi) E

- (1) Condition 1 met, FIRST(eE) is disjoint to FIRST(epsilon)
- (2) Condition 2 met, FIRST(E) is disjoint to FOLLOW(E)

c) parse_input()

```
{  
    parse_S();  
    expect EOF;  
}
```

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```
d) parse_S()
{
    t = lexer.peek(1);
    if(t.token_type == s_type){
        expect(s_type);
        parse_S();
        expect(t_type);
    } else if(t.token_type == f_type | e_type | d_type | k_type){
        parse_A();
        expect(k);
        parse_B();
        parse_C();
    } else {
        syntax_error();
    }
}
```

```
e) parse_A()
{
    t = lexer.peek(1);
    if(t.token_type == f_type){
        expect(f_type);
        parse_A();
        expect(g_type);
    } else if(t.token_type == e_type | d_type){
        parse_E();
        parse_D();
    } else if(t.token_type == g_type){
        return;
    } else {
        syntax_error();
    }
}
```

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- f) Full execution trace: input = s s f g k g t t
- i) `parse_input();`
 - ii) `parse_S();`
 - iii) `expect(s_type);`
 - iv) `parse_S();`
 - v) `expect(s_type);`
 - vi) `parse_S();`
 - vii) `parse_A();`
 - viii) `expect(f_type);`
 - ix) `parse_A();`
 - x) `expect(g_type);`
 - xi) `expect(k_type);`
 - xii) `parse_B();`
 - xiii) `expect(g_type);`
 - xiv) `parse_C();`
 - xv) `parse_E();`
 - xvi) `expect(t_type);`
 - xvii) `expect(t_type);`

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4) Usefulness

a) S

i) S is useless

- (1) The first rule involves G, which cannot generate a string of terminals
- (2) The second rule involves F, which cannot generate a string of terminals

b) A

i) A is useless

- (1) Since S cannot derive a string of terminals, there is not hope for A to be included in a string of terminals derived from S

c) B

i) B is useless

- (1) Since S cannot derive a string of terminals, there is not hope for B to be included in a string of terminals derived from S

d) C

i) C is useless

- (1) Since S cannot derive a string of terminals, there is not hope for C to be included in a string of terminals derived from S

e) D

i) D is useless

- (1) Since S cannot derive a string of terminals, there is not hope for D to be included in a string of terminals derived from S

f) E

i) E is useless

- (1) Since S cannot derive a string of terminals, there is not hope for E to be included in a string of terminals derived from S

g) F

i) F is useless

- (1) The first rule is recursive,
- (2) The second rule involves G, which cannot generate a string of characters

h) G

i) G is useless

- (1) The first rule is recursive,
- (2) The second rule involves F, which cannot generate a string of terminals (F→G is recursive by each second rule)