### **Energy conversion I**

#### Lecture 2:

Topic 1: Magnetic materials and Circuits (S. Chapman, ch. 1)

- Magnetic Field production and Mag. Circuits modeling
- Ferromagnetic Materials behavior
- Electrical Equivalent Cct. For magnetic Ccts
- Faraday's law
- Permanent Magnet Materials
- Force applied on a wire by ext. magnetic field
- Voltage induced in on moving conductor in magnetic field

EE Course No: 25741 Energy Conversion I Sharif University of Technology

#### **Magnetic Field**

**Magnetic Fields** is the fundamental Mechanism by which **energy converts** from one form to another in **Motors**, **Generators** & **Transformers**.

Basic Principles of energy conversion using magnetic fields:

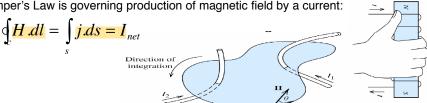
- 1- current carrying wire produces magnetic field.
- 2- time-varying magnetic field induces voltage.
- 3- current carrying wire in an external magnetic field experience a force.
- 4- voltage is induced in a wire moving in an external magnetic field.

2

### **Magnetic Field**

#### Ampere's law

Amper's Law is governing production of magnetic field by a current:



the line integral of the tangential component of the magnetic field intensity H around a closed contour C is equal to the total current passing through any surface S linking that contour.

- H : Magnetic field intensity produced by Inet
- dl: Differential element of the length of the closed path of integration
- J: Current density
- ds: Differential element of the area of integration

In SI I measured in amperes (A) and H in ampere-turns per meter At/m 3 Sharif University of EE Course No: 25741 Energy Conversion I Technology

### **Magnetic Field**

# **Example:**

#### **EXAMPLE**:

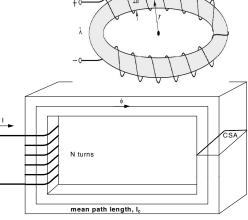
a rectangular ferromagnetic core with N turns of winding on one leg.

#### assumption:

- path of integration would be mean path of core lc.
- H and Ic are in the same direction.
- all magnetic field produced by current in winding confined to core boundary (flux Calculation)

EE Course No: 25741 Energy Conversion I

Sharif University of Technology



### **Magnetic Field**

#### **Magnetic Flux and Magnetic Flux Density**

Magnetic field flux also depends on core material.

 $B = \mu . H$ 

μ: magnetic permeability of material, Henrys per meter H/m (show how?)

B: magnetic flux density produced, Tesla (Webers per sq.meter) Wb/m²

 $\mu_0$ = free space permeability ( $\mu_0$ =  $4\pi \times 10^{-7}$ )

 $\mu = \mu_r \mu_0$  (µr relative permeability) Used to compare magnetizing ability

for steels used in modern machines 2000-6000

Magnetic materials are used in transformer or motor core to increase & concentrate magnetic flux (similar to the role of conductors in circuits)

EE Course No: 25741 Energy Conversion I Sharif University of Technology 5

### **Magnetic Field**

#### **Magnetic Flux and Magnetic Flux Density**

Much higher permeability of core w.r.t. air cause great majority of flux in core

Total flux passing an area A:

$$\varphi = \int_A B \cdot dA$$

dA: differential unit of area

If flux density vector perpendicular to plane of A & const.

Total flux in core of Example:

C core

Armature

flux tube

 $\phi$  = B A =  $\mu$  H A=  $\mu$  N i A / Ic

A: core cross sectional area

EE Course No: 25741 Energy Conversion I Sharif University of Technology

In example of magnetic field production, current in coil producing flux, is an analogous to voltage in electric circuit producing current.

Magnetic Equivalent Circuit defined as an analogous to Equivalent **Electric Circuit.** 

In Electric circuit voltage source V drives I through R (V=R.I),

#### while:

In Magnetic circuit Magneto-motive force (mmf) F = NI drives flux through reluctance of the core path.

EE Course No: 25741 Energy Conversion I

Sharif University of Technology

7

### **Magnetic Circuits Modeling**

mmf of magnetic circuit has also a polarity:

Positive end is associated to end from which flux exits if fingers of R.H. curl in direction of current in coil, thumb point in direction of positive mmf. A F=Ni Reluctance, R (mmf) **Electric System Magnetic System** V = IR $F = \varphi R$ R: Resistance R: Reluctance I : current φ: flux V: voltage(EMF) F:MMF **EMF: Electromotive Force MMF: Magnetomotive Force** EE Course No: 25741 Sharif University of Energy Conversion I

Technology

#### **Magnetic Reluctance:**

**Magnetic Reluctance:** the measure of material resistance to the flow of magnetic flux.

$$\phi = BA = \mu HA$$

$$- \mu Ni \quad A = F \mu A$$

$$= \mu \frac{Ni}{l_c} A = F \frac{\mu A}{l_c} = \frac{F}{R}$$

$$\therefore R = \frac{l_c}{\mu A}$$
 I<sub>c</sub>: length of the magnetic path A: cross section of magnetic flux path  $\mu$ : magnetic permeability

#### Reluctance very similar to resistance!

Equiv. reluctance of reluct.s in series (conducting the same flux):

$$Req = R1 + R2 + R3 + ...$$

For parallel reluctances (parallel path of fluxes):

EE Course No: 25741 Energy Conversion I Sharif University of Technology

### **Magnetic Circuits Modeling**

Employing equivalent cct. **Flux** in core is approximated (within 5 percent of real value at best)

Reasons of inaccuracy:

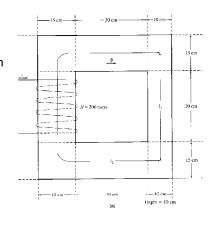
- 1- against the assumption of confining flux to core boundary, **small fraction** of flux circled through **air (leakage flux).**
- 2- assuming a **certain mean path** length and **cross section** in reluctance calculation (not exact specially at corners).
- 3- in ferromagnetic materials,  $\pmb{\mu}$  varies with existing flux in material (a nonlinear effect).
- 4- Air gaps in flux path of the core, causes **fringing effect** on magnetic field in air gap . Therefore effective cross sectional area of air gap is larger than cross sectional area of iron core:  $\mathbf{B_g} < \mathbf{B_c}$

Exact calculation using Maxwell's equations too difficult & not needed in many cases.

EE Course No: 25741 Energy Conversion I Sharif University of Technology

### Example 1:

A ferromagnetic core shown below. Its three sides has uniform width, while fourth side is somewhat thinner. depth of core (into page): 10 cm Others shown , 200 turn coil on left leg,  $\mu_r$ = 2500, Passing 1 A, **flux**?



#### Solution:

Core can be divided into 2 regions:

- (1) thinner side with a mean path length of 45 cm, & a cross-sectional area of 10x10  $\,\mathrm{cm^2}$
- (2) other three sides with a mean path of 130 cm (5+30+7.5+7.5+30+7.5+7.5+30+5) & a cross sectional area of 15x10 cm

EE Course No: 25741 Energy Conversion I Sharif University of Technology 11

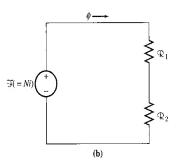
### **Magnetic Circuits Modeling**

Reluctance of region 1:  $\mathbf{R_1}$ R<sub>1</sub> = 0.45/[2500x4 $\pi$ x10<sup>-7</sup>x0.01] =14300 Atr/ Wb

Reluctamce of region 2:  $\mathbf{R_2}$ R<sub>2</sub>=1.3/[ 2500x4 $\pi$ x10<sup>-7</sup>x0.015]=27600 Atr/ Wb

Neglecting flux leakage : Flux is the same in both regions:  $\mathbf{R_1}$  in series with  $\mathbf{R_2}$ 

flux in core:  $\phi$ =F/ (R<sub>1</sub>+R<sub>2</sub>) = 200x1 / (14300+27600) = 0.0048 Wb



EE Course No: 25741 Energy Conversion I Sharif University of Technology

N = 400

#### Example 2:

Ferromagnetic core of figure below: mean path length 40cm, Gap 0.05 cm A:12 cm<sup>2</sup>, N:400 t.s,  $\mu_r$ = 4000 fringing increase A in air gap by 5%

- a) total R?
- b) I required for B=0.5T

#### Solution:

a) Rc=lc / ( $\mu$  Ac) = 0.4 /(4000x4 $\pi$ x10<sup>-7</sup>x0.0012) = 66300 At/ Wb

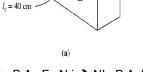
Effective air gap area: 12 x 1.05 =12.6 cm<sup>2</sup> Ra=la/[ $\mu_0$ Aa ]=0.0005/( $4\pi x 10^{-7} x 0.00126$ )

=316000 A.t/Wb

 $R_{eq}$ =66300+316000=382300 At./Wb

b) F = $\phi$  R ,  $\phi$ =B.A , F= N i  $\Rightarrow$  NI =B.A .R I =BAR/N=0.5x0.00126x383200/400=0.602 A

EE Course No: 25741 Energy Conversion I Sharif University of Technology



13

0.05 cm

 $A = 12 \text{ cm}^2$ 

## **Magnetic Circuits Modeling**

#### Example 3:

A simplified rotor stator of dc motor as shown, mean path of stator 50 cm, A=12 cm², mean length of rotor 5 cm, air gaps 0.05 cm, Air gap area (including fringing) 14 cm², Iron  $\mu$ r=2000, N=200

If I=1A, Ba=?

#### Solution:

Three different parts: stator (Rs), rotor (Rr) and air gap (Ra) in two parts with the same flux (series resiatnces)

Rs=ls/( $\mu_r \mu_0$  As)=0.5/ (2000x4 $\pi$ x10<sup>-7</sup>x0.0012)

=166000 At/ Wb

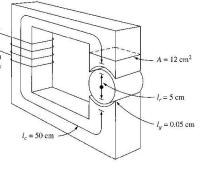
 $Rr = Ir/(\mu_r \ \mu_0 \ Ar) = 0.05/(2000x4\pi x 10^{-7} x 0.0012)$ 

=16600 At/ Wb

Ra =  $Ia/(\mu r \mu 0 Aa) = 0.0005/(4\pi x 10^{-7} x 0.0014)$ 

=284000 At/ Wb

EE Course No: 25741 Energy Conversion I Sharif University of Technology



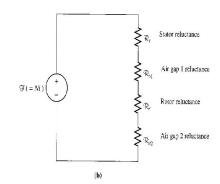
Equivalent magnetic circuit as shown:

 $R_{eq}$ =Rs+ $R_{a1}$ + $R_r$ + $R_{a2}$  = 166000+284000+16600+ 284000=751000 A.tr / Wb

Net mmf applied:

 $F = NI = 200 \times 1.0 = 200 \text{ A.tr}$   $\Phi = F / R = 200 / 751000$ =0.00266 Wb

 $B = \phi / A = 0.000266 / 0.0014 = 0.19 T$ 



EE Course No: 25741 Energy Conversion I Sharif University of Technology

This do a constant		Win2PDE available o		
The unregistere	was created with \ ed version of Win2	PDF is for evaluation	t http://www.daneprairie.com or non-commercial use only	
The unregistere	was created with \ ed version of Win2	PDF is for evaluation	or non-commercial use only.	
The unregistered	was created with \end{array}	PDF is for evaluation	or non-commercial use only.	