

Energy conversion I

Lecture 5:

Topic 2: Transformers & its performance (S. Chapman, ch. 2)

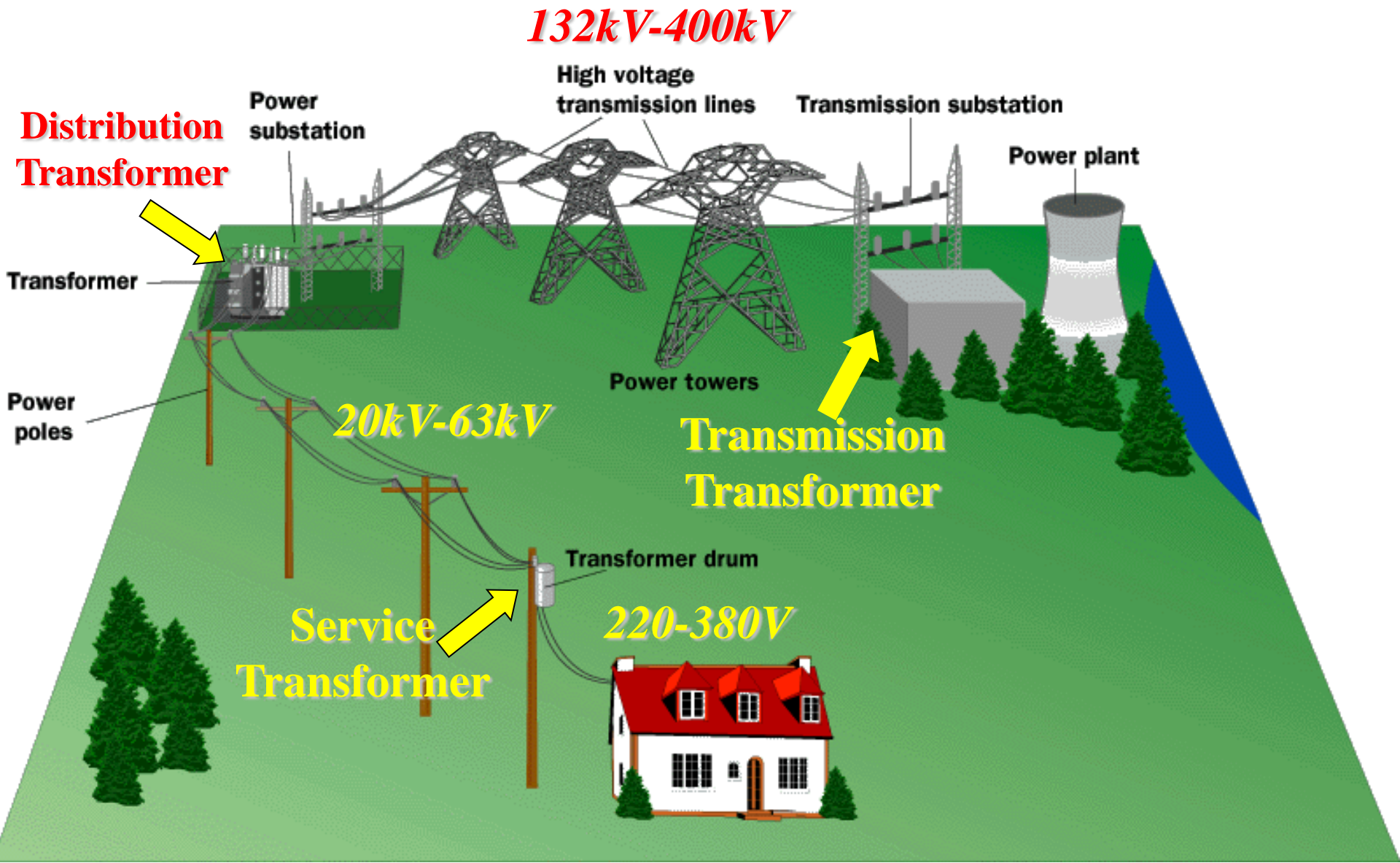
- **Introduction**
- **Types and Construction of Transformers.**
- **Ideal Transformer.**
- Theory of operation of real single-phase transformers.
- The Equivalent Circuit of a Transformer.
- The Per-Unit System of Measurement
- Transformer voltage regulation and efficiency
- Autotransformers
- Three phase transformers

Introduction

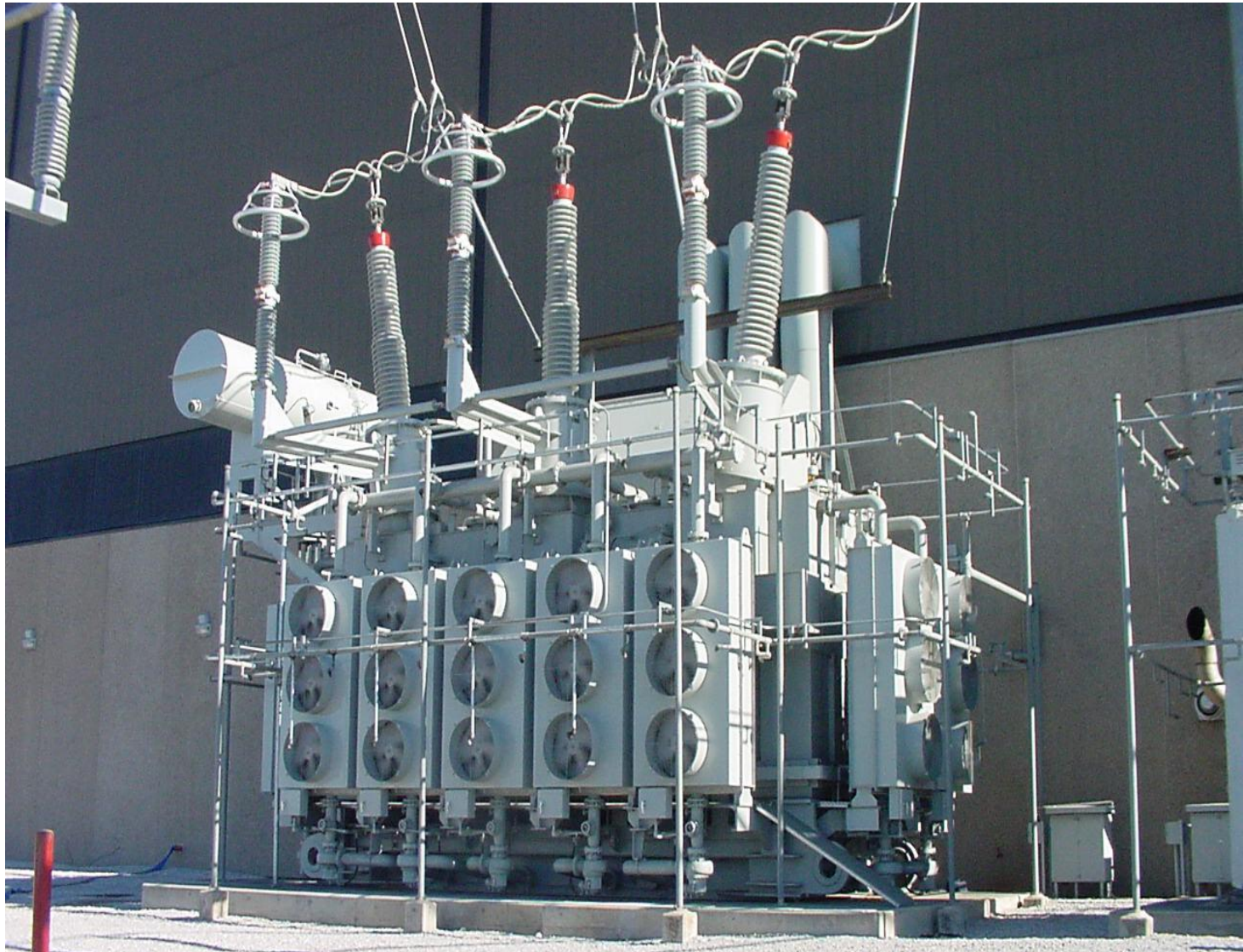
Transformer: a device to **change AC electric power at one voltage level to AC electric power at another voltage level** through the action of a magnetic field.

Transformer Applications:

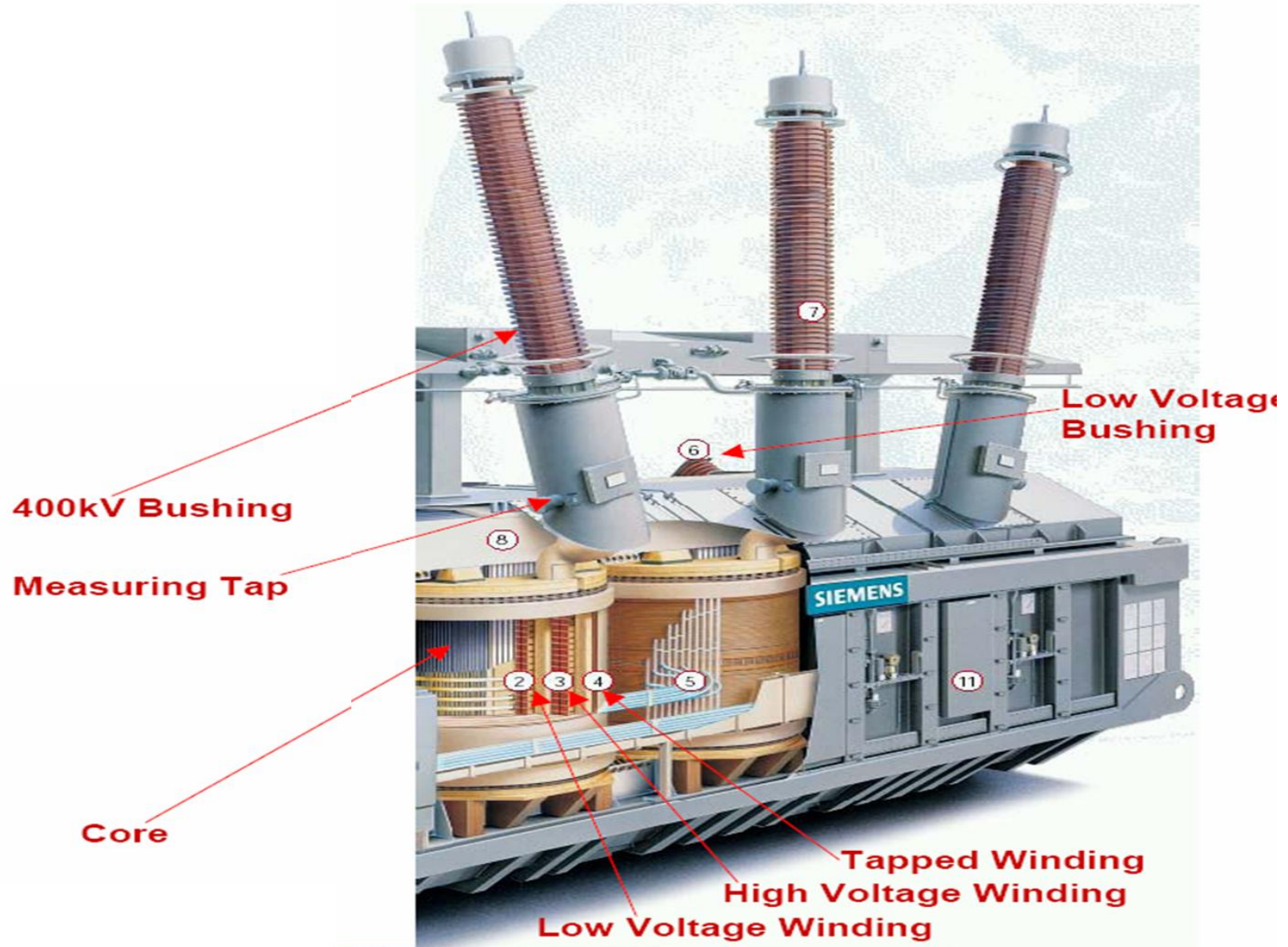
- **Increase voltage of generator's output**
 - Transmit high power at low current
 - Reduce cost of transmission system
- **Adjust voltage to a usable level**
- **Convert voltage or current to measurable levels**
- **Create electrical isolation**
- **Match load impedance**
- **Filters**



Transmission Transformer



Transmission Transformer



Distribution Transformer



Distribution Transformer



Dry Type Distribution Transformer

No Explosion

Inflammable

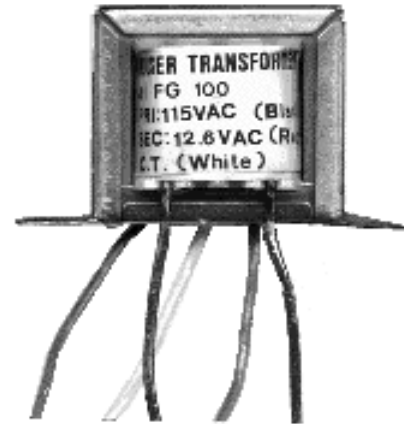
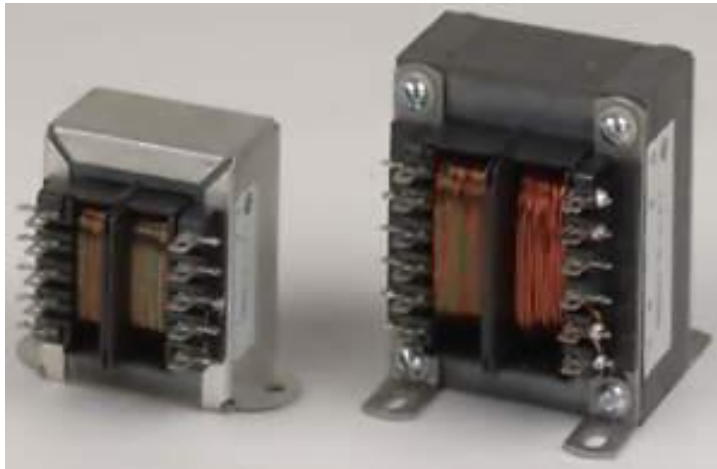
Environment friendly

Non-enclosed indoor

Cast Resin winding



Low Power Transformer



Old electronic apparatus power supply

Measurement Transformer

CT: Current transformer

Converts **High** (/low) currents to more usual currents **XX/5** or **XX/1**.

Usually **primary** is the **main** (hot) line. **Secondary** will be in series with current measuring terminals.

Isolation is required.



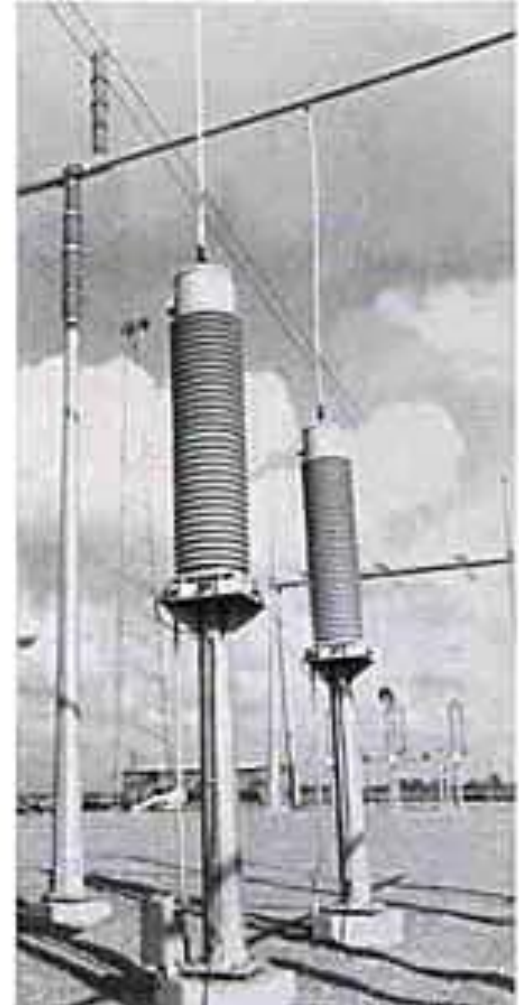
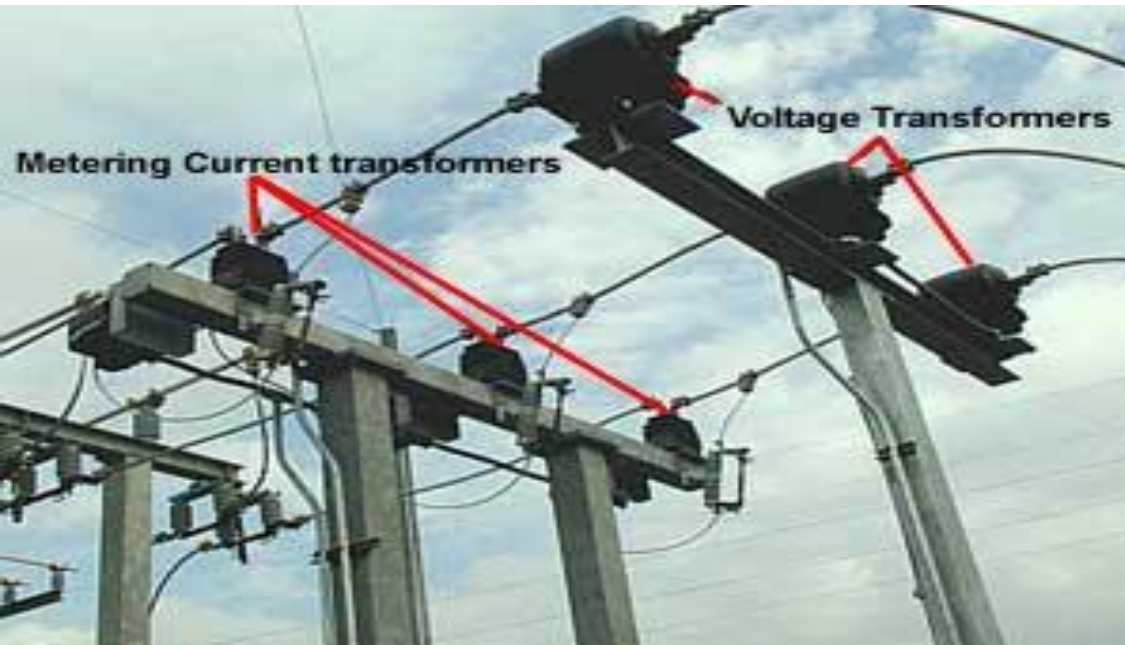
Measurement Transformer

PT: Potential transformer

Converts **High** (/low) voltages to
More **usual voltages XX/110**

Primary is **connected** to the **main**.
Secondary is **connected** to
voltage measuring terminals.

Isolation is required.



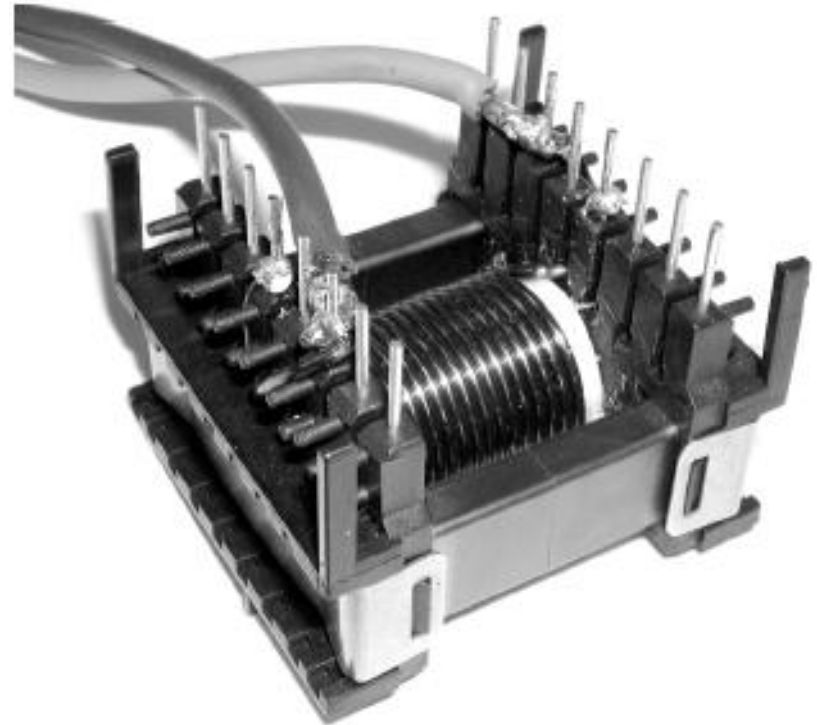
High Frequency (Pulse) Transformer

To be used in Electronic,
Communication and Power
Electronic Switching Circuits.

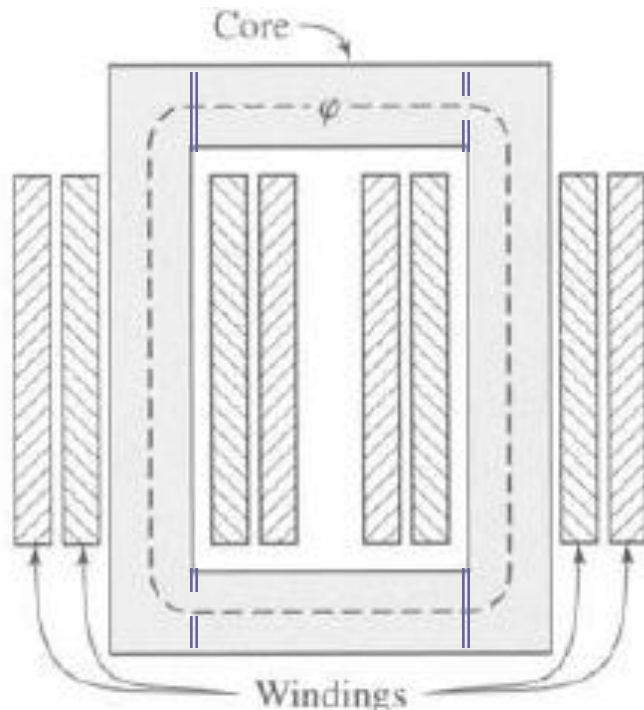
Air, Ferrite or Iron powder cores

Some kHz up to MHz

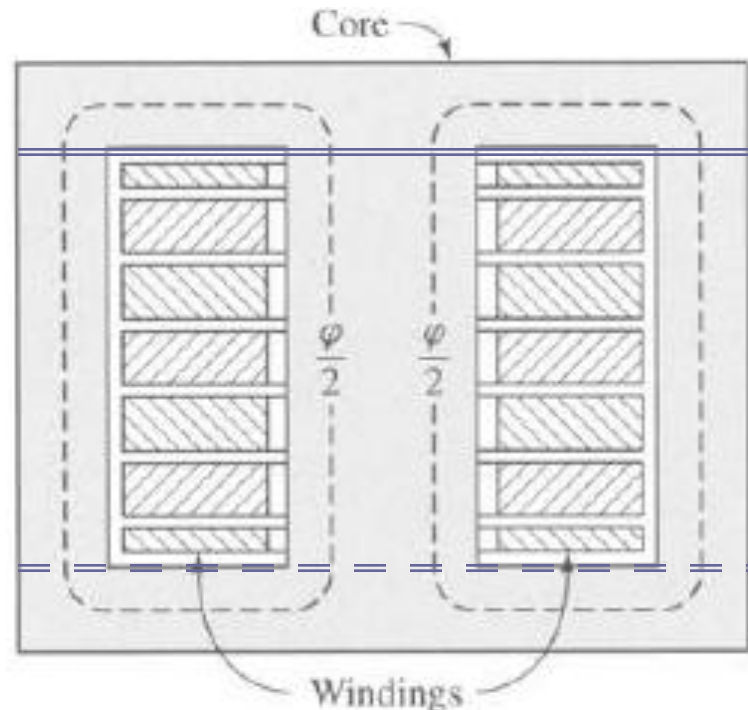
Some mW up to some kW



Types of Iron Core Transformers

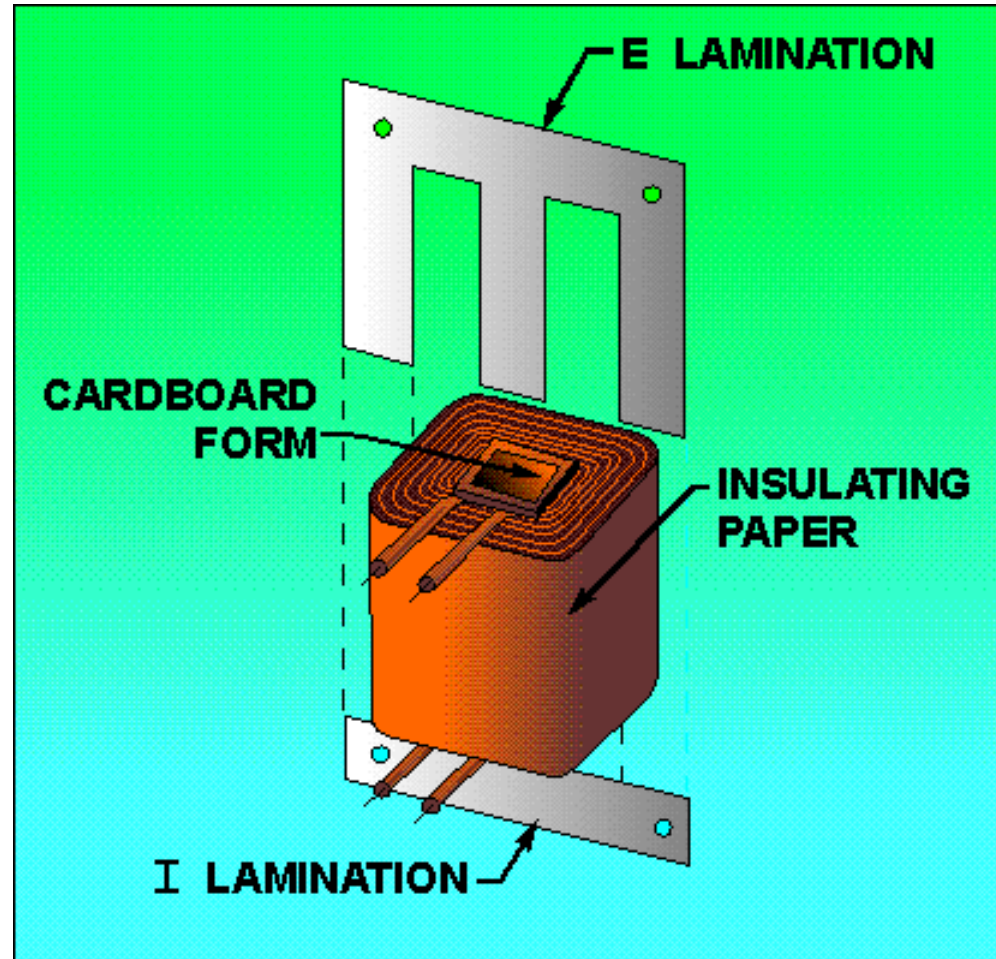
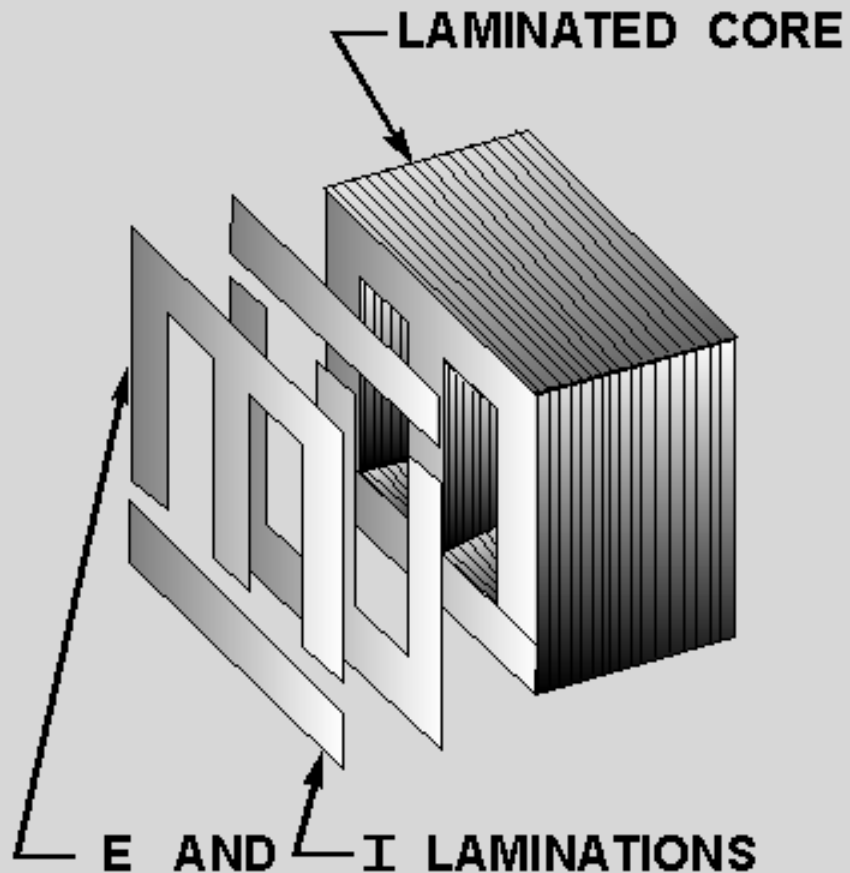


Core type (L Sheets)
Concentric coils

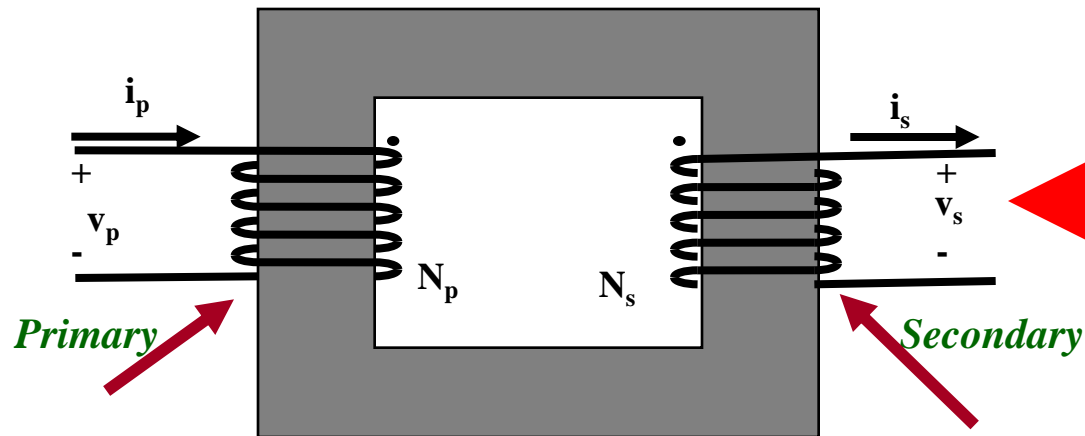
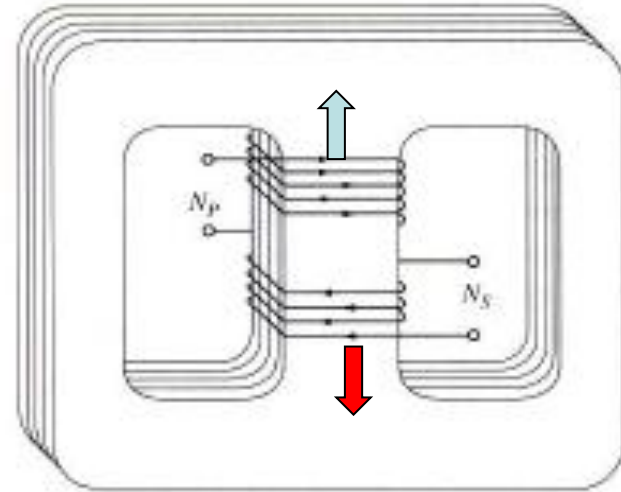
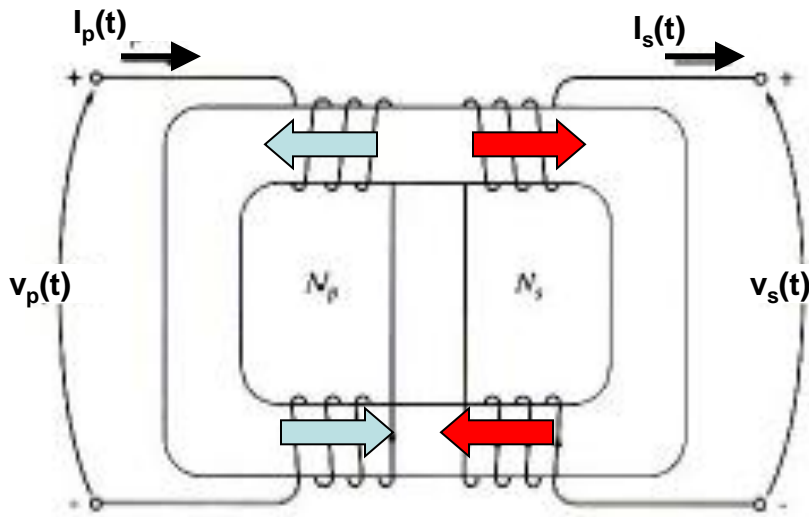


Shell type (EI Sheets)
Concentric/ pancake coils

Transformer's Iron Laminated Core



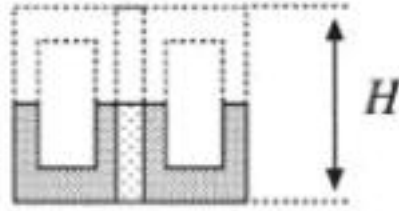
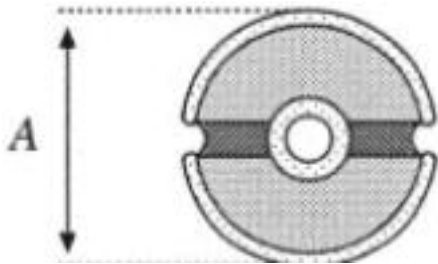
Transformer's Winding schematics



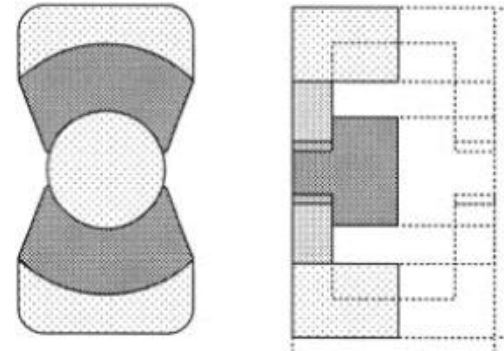
Schematic that will be used to show a transformer

Types of Ferrite Core Transformers

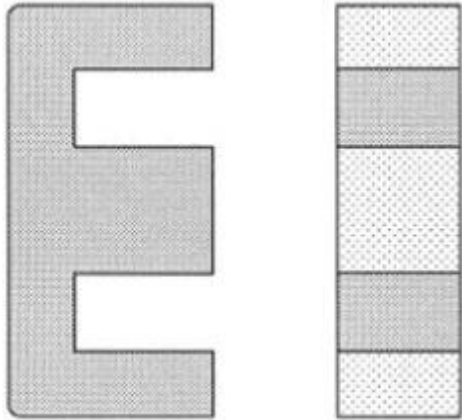
Pot core



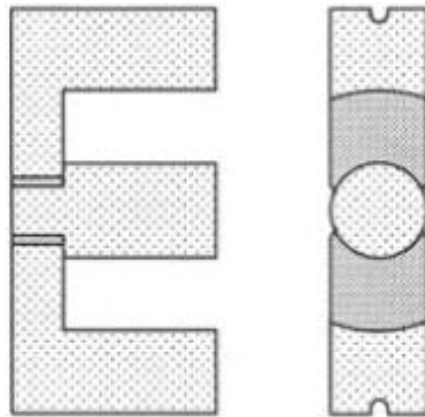
PQ core



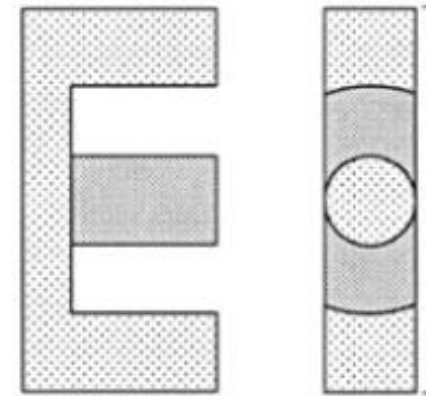
EE core



EC core



ETD core



Ideal Transformer

A **lossless** device with an input (**primary**) **winding** and an output (**secondary**) winding (at least).

Windings are electrically **isolated**

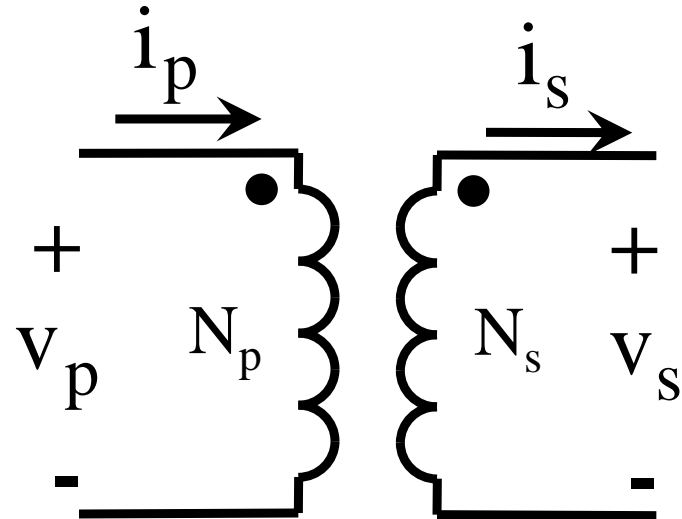
Relation between **input** and **output** voltages and currents are:

$$\frac{v_p(t)}{v_s(t)} = \frac{i_s(t)}{i_p(t)} = \frac{N_p}{N_s} = a \quad \text{attention to dotted terminals}$$

a : transformer **turn ratio**

Note: v_p and v_s are **in phase**
 i_p and i_s are **in phase**

$$v_p(t) \times i_p(t) = v_s(t) \times i_s(t) \quad \Rightarrow \quad P_{in}(t) = P_o(t)$$



Ideal Transformer

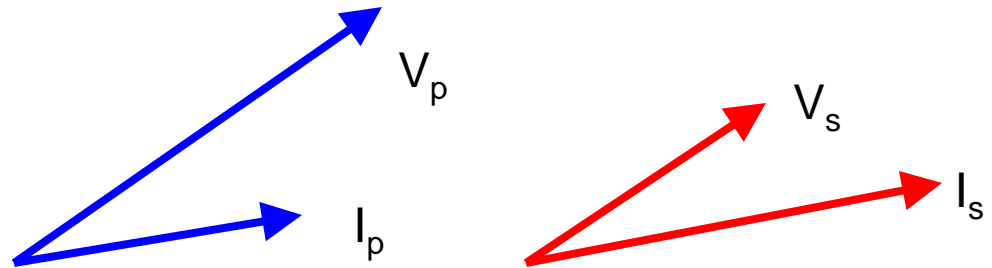
From time domain relations, phasor domain relations are:

$$\frac{V_p}{V_s} = \frac{I_s}{I_p} = \frac{N_p}{N_s} = a$$

$$S_{in} = V_p I_p^* = V_s I_s^* = S_{out}$$

$$P_{in} = P_{out}$$

$$Q_{in} = Q_{out}$$



Think about a CT with open circuit in the secondary!

Think about a PT with short circuit in the secondary!

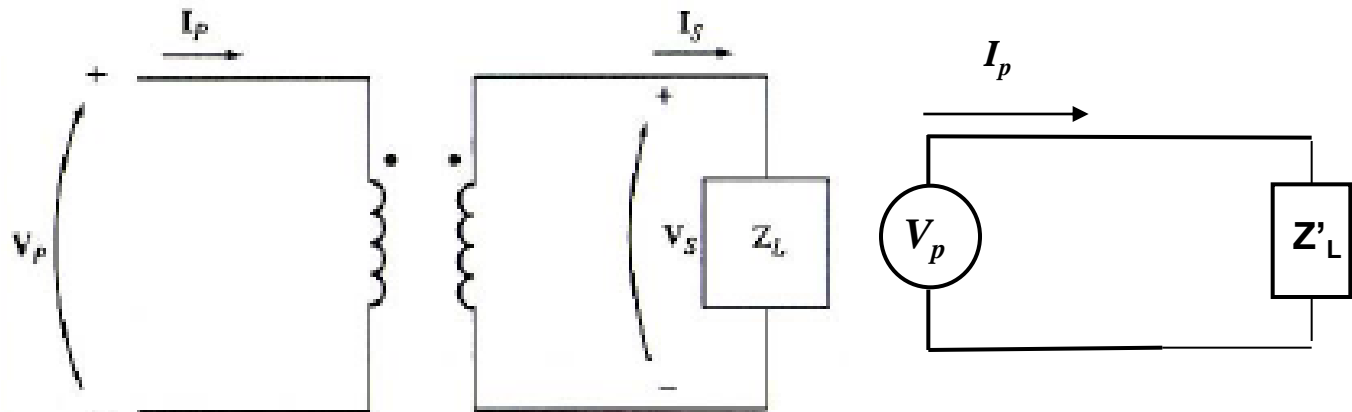
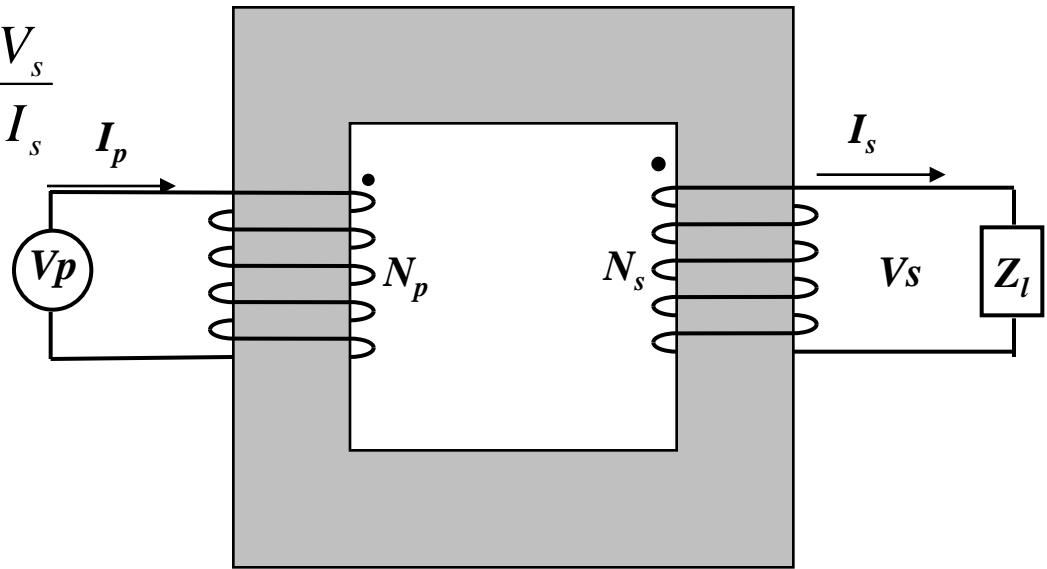
Impedance Transformation through an Ideal Transformer

Load Impedance: $Z_l = \frac{V_l}{I_l} = \frac{V_s}{I_s}$

Load Impedance seen from primary winding:

$$Z'_L = \frac{V_p}{I_p} = \frac{aV_s}{I_s/a} = a^2 \frac{V_s}{I_s}$$

$$Z'_L = a^2 Z_L$$

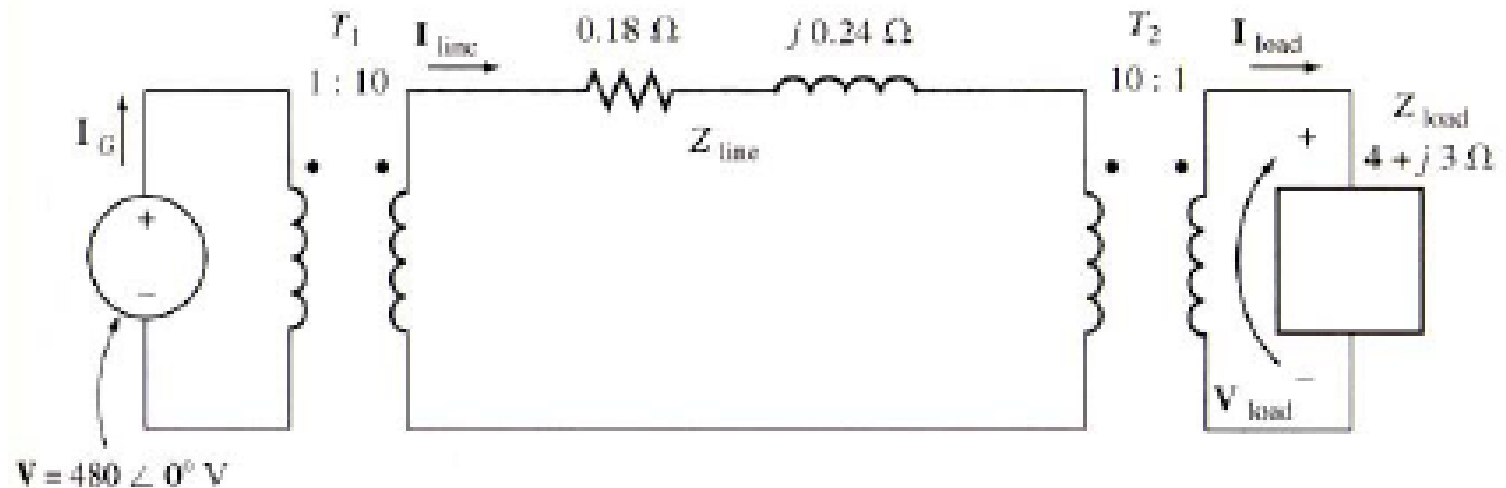


Impedance Transformation through an Ideal Transformer

Example: A generator rated at 480V, 60 Hz is connected to a transmission line with an impedance of $0.18 + j0.24 \Omega$ via a 1:10 step-up transformer. At the end of the transmission line a load of $4 + j3 \Omega$ is connected through a 10:1 transformer.

What will the load voltage be?

What will the transmission line losses be?



Transfer load impedance: $Z'_{\text{load}} = Z_{\text{load}} (10/1)^2 = 400 + j 300 \Omega$

The total Impedance at transmission line

$$Z_{\text{eq}} = Z'_{\text{load}} + Z_{\text{line}} = 400.18 + j300.24 \Omega$$

The total impedance seen from Generator

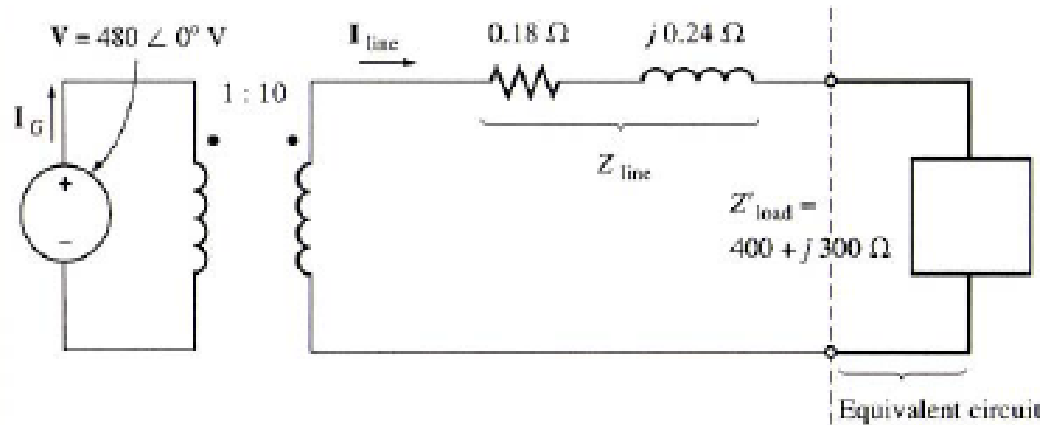
$$Z'_{\text{eq}} = Z_{\text{eq}} * (1/10)^2 = 4.0018 + j3.0024 \Omega$$

$$I_G = V_G / Z'_{\text{eq}} = 480 / (4.0018 + j3.0024) = 95.94 \angle -36.88^\circ$$

$$\text{Having } I_G : I_{\text{line}} = 1/10 * I_G = 9.594 \angle -36.88^\circ$$

$$\text{And } I_{\text{load}} = 10 * I_{\text{line}} = 95.94 \angle -36.88^\circ \text{ and } V_{\text{load}} = I_{\text{load}} * Z_{\text{load}} = 479.7 \angle -0.01^\circ \text{ V}$$

$$\text{For the transmission Power loss: } P_{\text{loss}} = I_{\text{line}}^2 * R_{\text{line}} = 9.594^2 * 0.18 = 16.7 \text{ W}$$



Compare with the case no transformer is used