

## 2021/12/13 陳嘉政 r10922171 HW9

### 1. Roberts operator(Threshold: 30)

主要程式碼:

(1)函式輸入分別為:照 hw8 方法擴張一次的圖、原圖及閾值。先宣告一個 result 矩陣，將原圖複製到 result，初始化兩個 mask 係數矩陣，將擴張圖 row by row，col by col，從(1,1)開始到(rows-1, col-1)，每個點作為原點圈出 2x2 矩形，分別與兩個 mask 求值(matrixSum 函式)，求出的兩個值平方後相加，然後加總再開根號看有沒有 $\geq$ 閾值，若有，則 result 圖中點(i - 1, j - 1)視為邊(value = 0)，否則 value = 255。

```
Mat Roberts_operator(Mat padded, Mat orig, int threshold)
{
    Mat result;
    orig.copyTo(result);

    Mat mask[2];
    mask[0] = (Mat_<double>(2, 2) << //r1
        -1, 0,
        0, 1);
    mask[1] = (Mat_<double>(2, 2) << //r2
        0, -1,
        1, 0);

    for (int i = 1; i < padded.rows - 1; i++) {
        for (int j = 1; j < padded.cols - 1; j++) {
            Mat kernel = padded(cv::Rect(j, i, 2, 2));
            double value = 0;
            for (int n = 0; n < sizeof(mask) / sizeof(*mask); n++) {
                double temp = matrixSum(kernel, mask[n]);
                value += pow(temp, 2);
            }
            if (sqrt(value) >= threshold)
                result.at<uint8_t>(i - 1, j - 1) = 0;
            else
                result.at<uint8_t>(i - 1, j - 1) = 255;
        }
    }
    return result;
}
```

matrixSum 的作用是将圈出的矩形中每個點與 mask 對應的係數相乘再加總。

```
double matrixSum(Mat kernel, Mat mask)
{
    double total = 0;
    for (int i = 0; i < kernel.rows; i++) {
        for (int j = 0; j < kernel.cols; j++) {
            total += kernel.at<uint8_t>(i, j) * mask.at<double>(i, j);
        }
    }
    return total;
}
```

結果:

此閾值產生的結果比閾值為 12 產生的結果的邊還要細，可以推得閾值越高邊會越細



## 2. Prewitt operator(Threshold: 24)

主要程式碼:

除了點 $(i, j)$ 圈出的矩形原點為 $(j - 1, i - 1)$ ，大小為  $3 \times 3$ ，以及  $\text{mask}$  矩陣的大小及係數改變，其他做法都跟 1.相似。

```
Mat Prewitt_operator(Mat padded, Mat orig, int threshold)
{
    Mat result;
    orig.copyTo(result);

    Mat mask[2];
    mask[0] = (Mat_<double>(3, 3) << //p1
        -1, -1, -1,
        0, 0, 0,
        1, 1, 1);
    mask[1] = (Mat_<double>(3, 3) << //p2
        -1, 0, 1,
        -1, 0, 1,
        -1, 0, 1);

    for (int i = 1; i < padded.rows - 1; i++) {
        for (int j = 1; j < padded.cols - 1; j++) {
            Mat kernel = padded(cv::Rect(j - 1, i - 1, 3, 3));
            double value = 0;
            for (int n = 0; n < sizeof(mask) / sizeof(*mask); n++) {
                double temp = matrixSum(kernel, mask[n]);
                value += pow(temp, 2);
            }
            if (sqrt(value) >= threshold)
                result.at<uint8_t>(i - 1, j - 1) = 0;
            else
                result.at<uint8_t>(i - 1, j - 1) = 255;
        }
    }
    return result;
}
```

結果:



### 3. Sobel operator(Threshold: 38)

主要程式碼:

除了點 $(i, j)$ 圈出的矩形原點為 $(j - 1, i - 1)$ ，大小為  $3 \times 3$ ，以及 mask 矩陣的大小及係數改變，其他做法都跟 1.相似

```
Mat Sobel_operator(Mat padded, Mat orig, int threshold)
{
    Mat result;
    orig.CopyTo(result);

    Mat mask[2];
    mask[0] = (Mat_<double>(3, 3) << //s1
        -1, -2, -1,
        0, 0, 0,
        1, 2, 1);
    mask[1] = (Mat_<double>(3, 3) << //s2
        -1, 0, 1,
        -2, 0, 2,
        -1, 0, 1);

    for (int i = 1; i < padded.rows - 1; i++) {
        for (int j = 1; j < padded.cols - 1; j++) {
            Mat kernel = padded(cv::Rect(j - 1, i - 1, 3, 3));
            double value = 0;
            for (int n = 0; n < sizeof(mask) / sizeof(*mask); n++) {
                double temp = matrixSum(kernel, mask[n]);
                value += pow(temp, 2);
            }
            if (sqrt(value) >= threshold)
                result.at<uint8_t>(i - 1, j - 1) = 0;
            else
                result.at<uint8_t>(i - 1, j - 1) = 255;
        }
    }
    return result;
}
```

結果:



#### 4. Frei and Chen operator(Threshold: 30)

主要程式碼:

除了點 $(i, j)$ 圈出的矩形原點為 $(j - 1, i - 1)$ ，大小為  $3 \times 3$ ，以及  $\text{mask}$  矩陣的大小及係數改變，其他做法都跟 1.相似

```
Mat Frei_and_Chen_operator(Mat padded, Mat orig, int threshold)
{
    Mat result;
    orig.CopyTo(result);

    Mat mask[2];
    mask[0] = (Mat_<double>(3, 3) << // f1
        -1, -sqrt(2), -1,
        0, 0, 0,
        1, sqrt(2), 1);
    mask[1] = (Mat_<double>(3, 3) << // f2
        -1, 0, 1,
        -sqrt(2), 0, sqrt(2),
        -1, 0, 1);

    for (int i = 1; i < padded.rows - 1; i++) {
        for (int j = 1; j < padded.cols - 1; j++) {
            Mat kernel = padded(cv::Rect(j - 1, i - 1, 3, 3));
            double value = 0;
            for (int n = 0; n < sizeof(mask) / sizeof(*mask); n++) {
                double temp = matrixSum(kernel, mask[n]);
                value += pow(temp, 2);
            }
            if (sqrt(value) >= threshold)
                result.at<uint8_t>(i - 1, j - 1) = 0;
            else
                result.at<uint8_t>(i - 1, j - 1) = 255;
        }
    }

    return result;
}
```

結果:



## 5. Kirsch compass operator(Threshold: 135)

主要程式碼:

Mask 係數矩陣有 8 個，宣告長度為 8 的 value 陣列，分別將每個係數矩陣與擴張圖圈出的 3x3 矩形計算出的 matrixSum 存入 value 陣列。呼叫 findMax 函式將 array 由小到大排列並回傳最大值。若此值>=閾值，則 result 中此點 value = 0，否則 value = 255。

```
Mat Kirsch_compass_operator(Mat padded, Mat orig, int threshold)

{
    Mat result;
    orig.CopyTo(result);

    Mat mask[8];
    mask[0] = (Mat_<double>(3, 3) << //k0
        -3, -3, 5,
        -3, 0, 5,
        -3, -3, 5);
    mask[1] = (Mat_<double>(3, 3) << //k1
        -3, 5, 5,
        -3, 0, 5,
        -3, -3, -3);
    mask[2] = (Mat_<double>(3, 3) << //k2
        5, 5, 5,
        -3, 0, -3,
        -3, -3, -3);
    mask[3] = (Mat_<double>(3, 3) << //k3
        5, 5, -3,
        5, 0, -3,
        -3, -3, -3);
    mask[4] = (Mat_<double>(3, 3) << //k4
        5, -3, -3,
        5, 0, -3,
        5, -3, -3);
    mask[5] = (Mat_<double>(3, 3) << //k5
        -3, -3, -3,
        5, 0, -3,
        5, 5, -3);
```

```

mask[6] = (Mat_<double>(3, 3) << //k6
-3, -3, -3,
-3, 0, -3,
5, 5, 5);
mask[7] = (Mat_<double>(3, 3) << //k7
-3, -3, -3,
-3, 0, 5,
-3, 5, 5);

for (int i = 1; i < padded.rows - 1; i++) {
    for (int j = 1; j < padded.cols - 1; j++) {
        Mat kernel = padded(cv::Rect(j - 1, i - 1, 3, 3));
        double value[8] = { 0 };
        for (int n = 0; n < sizeof(mask) / sizeof(*mask); n++) {
            value[n] = matrixSum(kernel, mask[n]);
        }
        if (findMax(value, 8) >= threshold)
            result.at<uint8_t>(i - 1, j - 1) = 0;
        else
            result.at<uint8_t>(i - 1, j - 1) = 255;
    }
}
return result;

```

findMax 函式就是在做 bubble sort 並回傳最後一個元素(最大值)

```

double findMax(double array[], int arraysize)
{
    for (int i = arraysize - 2; i >= 0; i--) {
        for (int j = 0; j <= i; j++) {
            if (array[j] > array[j + 1]) {
                double temp = array[j];
                array[j] = array[j + 1];
                array[j + 1] = temp;
            }
        }
    }
    return array[arraysize - 1];
}

```

結果:



## 6. Robinson compass operator(Threshold: 43)

主要程式碼:

做法與 5.相同，差在 mask 矩陣係數改變

```

Mat Robinson_compass_operator(Mat padded, Mat orig, int threshold)
{
    Mat result;
    orig.copyTo(result);

    Mat mask[8];
    mask[0] = (Mat_<double>(3, 3) << //r0
        -1, 0, 1,
        -2, 0, 2,
        -1, 0, 1);
    mask[1] = (Mat_<double>(3, 3) << //r1
        0, 1, 2,
        -1, 0, 1,
        -2, -1, 0);
    mask[2] = (Mat_<double>(3, 3) << //r2
        1, 2, 1,
        0, 0, 0,
        -1, -2, -1);
    mask[3] = (Mat_<double>(3, 3) << //r3
        2, 1, 0,
        1, 0, -1,
        0, -1, -2);
    mask[4] = -mask[0]; //r4
    mask[5] = -mask[1]; //r5
    mask[6] = -mask[2]; //r6
    mask[7] = -mask[3]; //r7

    for (int i = 1; i < padded.rows - 1; i++) {
        for (int j = 1; j < padded.cols - 1; j++) {
            Mat kernel = padded(cv::Rect(j - 1, i - 1, 3, 3));
            double value[8] = { 0 };
            for (int n = 0; n < sizeof(mask) / sizeof(*mask); n++) {
                value[n] = matrixSum(kernel, mask[n]);
            }
            if (findMax(value, 8) >= threshold)
                result.at<uint8_t>(i - 1, j - 1) = 0;
            else
                result.at<uint8_t>(i - 1, j - 1) = 255;
        }
    }
    return result;
}

```

結果:



## 7. Nevatia Babu operator(Threshold: 12500)

主要程式碼:

將原圖擴張 2 次作為擴張圖，mask 矩陣有 6 個，大小為 5x5，宣告長度為 6 的 value 陣列。Row by row, col by col，從擴張圖中(2,2)開始到(rows - 2, cols - 2)，每個點(i, j)都以(j - 2, i - 2)為原點，圈出 5x5 大小的矩形，將矩形分別與每個 mask 算出 matrixSum，存入 value 陣列，之後呼叫 findMax，回傳 value 陣列最大值，將此值與閾值比較，若為 >=，原圖點(i - 2, j - 2) 設為 0，否則設為 255。

```

Mat Nevatia_Babu_operator(Mat padded, Mat orig, int threshold)
{
    Mat result;
    orig.copyTo(result);

    Mat mask[6];
    mask[0] = (Mat_<double>(5, 5) << //0度
        100, 100, 100, 100, 100,
        100, 100, 100, 100, 100,
        0, 0, 0, 0, 0,
        -100, -100, -100, -100, -100,
        -100, -100, -100, -100, -100);
    mask[1] = (Mat_<double>(5, 5) << //30度
        100, 100, 100, 100, 100,
        100, 100, 100, 78, -32,
        100, 92, 0, -92, -100,
        32, -78, -100, -100, -100,
        -100, -100, -100, -100, -100);
    mask[2] = (Mat_<double>(5, 5) << //60度
        100, 100, 100, 32, -100,
        100, 100, 92, -78, -100,
        100, 100, 0, -100, -100,
        100, 78, -92, -100, -100,
        100, -32, -100, -100, -100);
    mask[3] = (Mat_<double>(5, 5) << //90度
        -100, -100, 0, 100, 100,
        -100, -100, 0, 100, 100,
        -100, -100, 0, 100, 100,
        -100, -100, 0, 100, 100,
        -100, -100, 0, 100, 100);
    mask[4] = (Mat_<double>(5, 5) << //-60度
        -100, 32, 100, 100, 100,
        -100, -78, 92, 100, 100,
        -100, -100, 0, 100, 100,
        -100, -100, -92, 78, 100,
        -100, -100, -100, -32, 100);
    mask[5] = (Mat_<double>(5, 5) << //-30度
        100, 100, 100, 100, 100,
        -32, 78, 100, 100, 100,
        -100, -92, 0, 92, 100,
        -100, -100, -100, -78, 32,
        -100, -100, -100, -100, -100);

    for (int i = 2; i < padded.rows - 2; i++) {
        for (int j = 2; j < padded.cols - 2; j++) {
            Mat kernel = padded(cv::Rect(j - 2, i - 2, 5, 5));
            double value[6] = { 0 };
            for (int n = 0; n < sizeof(mask) / sizeof(*mask); n++) {
                value[n] = matrixSum(kernel, mask[n]);
            }
            if (findMax(value, 6) >= threshold)
                result.at<uint8_t>(i - 2, j - 2) = 0;
            else
                result.at<uint8_t>(i - 2, j - 2) = 255;
        }
    }

    return result;
}

```

結果:

