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The unstable Adams spectral sequence for S^3 .

Algebraic topology (Evanston, IL, 1988), 125–162, *Contemp. Math.*, 96, Amer. Math. Soc., Providence, RI, 1989.

Systematic calculations of the unstable homotopy groups of spheres using the *EHP* sequence were begun by Toda and have been continued through the calculation of the 30-stem in the work of Barratt, Mimura, Mori, and Oda. The authors of this paper make use of algebraic *EHP* sequences to calculate the E_2 terms of the unstable Adams spectral sequence for spheres, with the advantage that the main difficulty in the “geometric computation”, the computation of the map P , can be handled by the formula for the differential in the lambda algebra. The paper is concerned mainly with the computation of the higher differentials in the spectral sequence for S^3 , which is achieved by means of a stable map $\Omega^2 S^3 \langle 3 \rangle \rightarrow Q\Sigma\mathbf{RP}^2$. Other considerations (e.g. v_1 -periodicity) are sometimes used as well. The first 52 stems of $E_\infty^{*,*}(S^3)$ are given and in many cases the group extension is determined to obtain the actual homotopy group.

{For the collection containing this paper see [MR1022668](#)}

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