

Recursion Problem

1. *M Apples are placed in N Plates.*

We want M apples to be placed in N plates. It allows empty plates. How many choices to distribute apples to plates? And it allows repeatable combinations. For example, M=4, N=3, (1, 1, 2), (1, 2, 1) and (2, 1, 1) are repeatable combinations, they are regarded as three choices.

```
int fun(int m, int n){
    if(m <= 0)
        return 1;
    if(n <= 0)
        return 0;
    int num=0;
    for(int i=0; i<=m; ++i){
        num += fun(m-i, n-1);
    }
    return num;
}
```

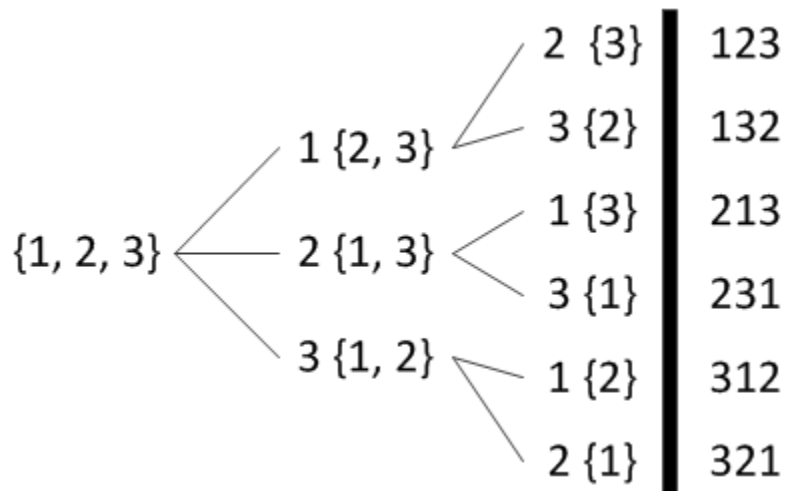
2. *4 0~9 Numbers form 24 points with +-*/**

We want 4 decimal numbers which ranges from 0~9 to form 24 point with operations +-*/*/. For example, 4 numbers: 7, 3, 2, 4. Then $(7+3)*2+4=24$.

The issue can be divided into two parts:

- 1) Four numbers in various orders, totally $4*3*2*1 = 24$ choices.
- 2) For each order, justify whether it can form 24 or not.

For 1),



```

SET_COMB[MAX][4];
Set_cnt=0;
Permute(set, start, end){
    If (start==end){
        Malloc(MEMORY_SIZE);
        Memcpy(SET_COMB[set_cnt], set, 4 * sizeof(int)); // save the final result
        Set_cnt++;
    }
    For (i=start;i<end;i++){
        Swap(set, start, i); // exchange set[start] and set[i]
        Permute(set, start+1, end);
        Swap(set, start, i); // recover the set
    }
}

```

比如说，有{1, 2, 3, 4}, 先固定 1，然后用 1, 2, 3, 4 去替换 1，得到 4 个并行的集合

{1, x, x, x},

{2, 1, x, x},

{3, x, 1, x},

{4, x, x, 1}

然后分别对单个集合做第二层的处理，第一个元素不用管了，因为数值不同，所以后面不会产生重复的组合。

{1, x, x, x} = {1, 2, 3, 4} => {2, 3, 4}, 固定 2，用后面的元素替换(包括自己)，得到以下集合

{2, x, x},

{3, 2, x},

{4, x, 2}

接着又可以延申到第三层。。。

For 2)

```

int func(int result, int* nums, int len){
    int i;
    int success;
}

```

```

int temp_result;

if ((len == 1) && (result == nums[0]))
{
    return 1;
}

if(len == 1){
    return 0;
}

success = 0;
for (i=0;i<4;i++){
    switch (i){
        case 0: temp_result = result - nums[len-1]; break;
        case 1: temp_result = result + nums[len-1]; break;
        case 2: temp_result = result * nums[len-1]; break;
        case 3:
            if ((result%nums[len-1])==0){
                temp_result = result / nums[len-1];
            }else{
                return success;
            }
            break;
    }

    success += func(temp_result, nums, len-1);
}

return success;
}

```