5. Abstract Data Type (ADT) Stack, Queue

- What is an abstract data type (ADT)?
- Stack as an ADT, its data structure, operations, and error conditions.
- Stack implementations and applications.
- Queue as an ADT, its data structure, operations, and error conditions.
- Queue implementations and applications.

stack and queue

Abstract Data Types (ADTs)

- An abstract data type (ADT) is an abstraction of a data structure.
- ADT refers to a way of packaging some intermediate-level data structures and their operations into a useful collection whose properties have been carefully studied.
- An ADT has a clean and simple interface.
- An ADT specifies:
 - Data stored
 - Operations on the data (clean, simple interface)
 - Error conditions associated with operations

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An ADT Example

- Example: ADT modeling a simple stock trading system
 - The data stored are buy/sell orders
 - The operations supported are
 - order buy(stock, shares, price)
 - order sell(stock, shares, price)
 - void cancel(order)
 - Error conditions:
 - Buy/sell a nonexistent stock
 - · Cancel a nonexistent order

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Stacks • spring-loaded plate dispenser

The Stack ADT

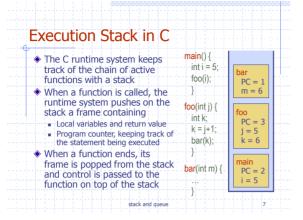
- ◆ The Stack ADT stores arbitrary elements
- Insertions and deletions follow the last-in first-out scheme
- Main stack operations:push(element): inserts
 - push(element): inserts an element
 - element pop(): removes and returns the last inserted element
- Auxiliary stack operations:
 - element top(): returns the last inserted element without removing it
 - integer size(): returns the number of elements stored
 - boolean isEmpty(): indicates whether no elements are stored

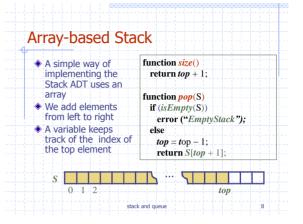
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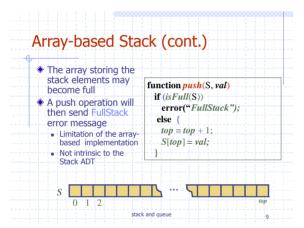
Applications of Stacks

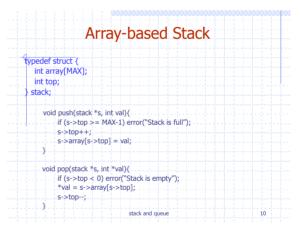
- Direct applications
 - Undo sequence in a text editor
 - Chain of function calls in any language runtime system
- Indirect applications
 - Auxiliary data structure for algorithms
 - Component of other data structures

stack and queue







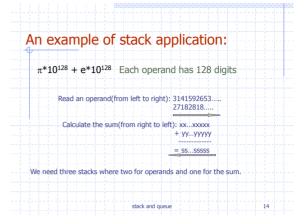


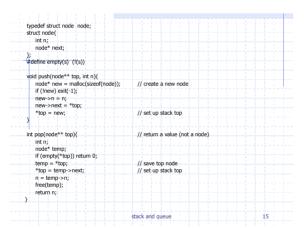
Performance and Limitations Performance Let n be the number of elements in the stack The space used is O(n) Each operation runs in time O(1) Limitations The maximum size of the stack must be defined a priori and cannot be changed Trying to push a new element into a full stack causes an implementation-specific error

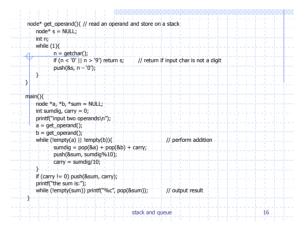
A stack is defined by how it is used, not by its underlying structure. We can implement a stack by different data structures. Inked lists arrays what else? The only requirement for a stack is the ability to store elements in order of insertion, so that we can get the LIFO behavior.

Stack ---- behavior

List-based Stack: Linked-list can be used to implement stack data structure: add and remove node from the "top". Property: Last In First Out (LIFO). Operations: is_empty, push, pop







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Example: Computing Spans
 We show how to use a stack
   as an auxiliary data structure 5
   in an algorithm
• Given an an array X_i, the span \frac{4}{3}
   S[i] of X[i] is the maximum
   number of consecutive
   elements X[j] immediately
   preceding X[i] and such that
   X[j] \leq X[i]
                                       1 2 3 4
                                    0

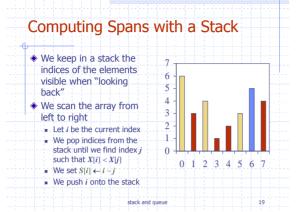
    Spans have applications to

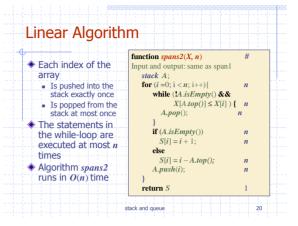
   financial analysis
                                         3
                                             4
                                                5
   . E.g., stock at 52-week high
                                             2
                                                 3
```

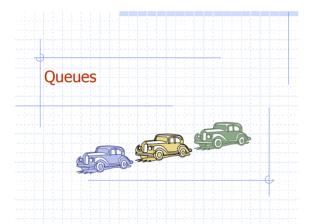
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Quadratic Algorithm

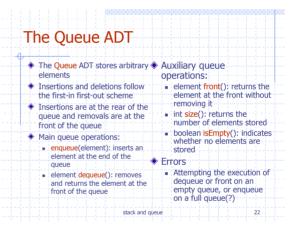
function spansI(X, n)
Input: X[n] integers
Output: array S[n] of spans of X
int s;
for (int i = 0; i < n; i++){
s = 1;
while (s \le i \&\& X[i-s] \le X[i]){
1 + 2 + ... + (n-1)
s = s + 1;
S[i] = s;
n
}
return S

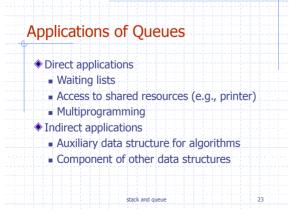
Algorithm spansI runs in O(n^2) time
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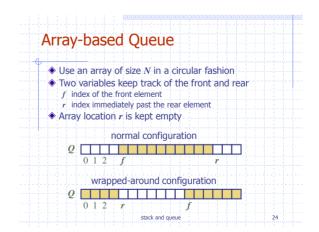


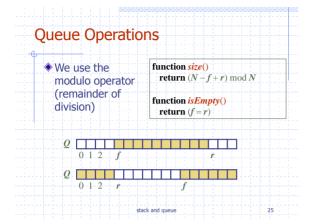


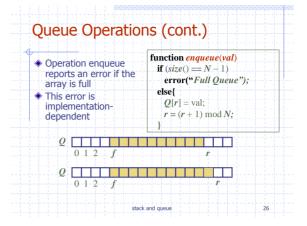


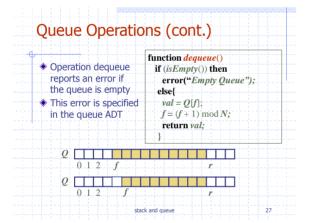


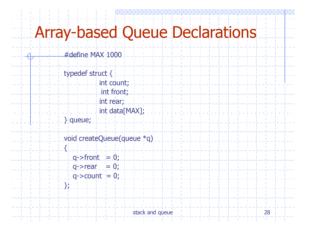












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Circular-Array-based: Enqueue

int queueFull(queue *q)
{
    return q->count >= MAX;
}

void enqueue(int x, queue *q)
{
    if (queueFull(q))
        error("QUEUE IS FULL");
    q->count++;
    q->data[q->rear] = x;
    /* Move to next open position */
    q->rear = (q->rear + 1) % MAX;
}
```

```
Circular-Array-based: Dequeue

void dequeue(int *x, queue *q)
{
    if (queueEmpty(q))
        error("QUEUE IS EMPTY");
    q->count--;
    *x = q->data[q->front]; /* data from front */
    /* Move to the next slot to dequeue */
    q->front = (q->front + 1) % MAX;
}

stack and queue 30
```