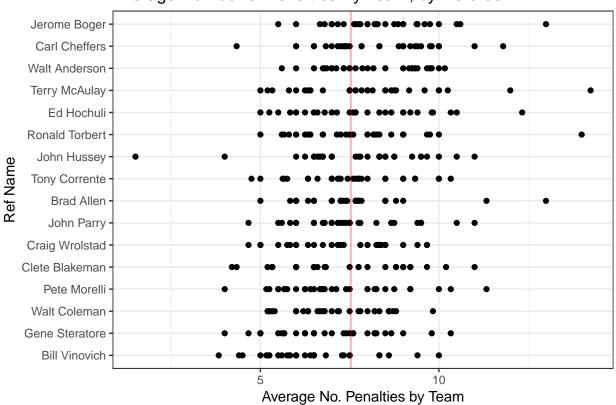
## Penalties\_byTeam\_byReferee

```
#NOW WE LOOK BY REFEREE BY TEAM
penRef<-refData %>%
  group_by(Referee,PenaltyTeam) %>%
  summarize(n=n())
#penRef
penaltiesPerGame<-refData %>%
  group_by(GameDate,PenaltyTeam) %>%
  summarize(n=n())
colnames(penRef)<-c("Referee", "PenaltyTeam", "NPenalties")</pre>
#So we have the number of penalties by ref...now we just need the number of games each ref did for each
#The best way that we can do this is through using two DPYLR statements, one to get unique games by tea
#to summarize by ref by team
refDataTemp<-refData
NoGamesRef<- refDataTemp %>%
  filter(!is.na(PenaltyTeam)) %>%
  group_by(Referee,PenaltyTeam,GameDate) %>%
  summarize(Unique_Elements = n_distinct(GameDate))
NoGamesRef <- NoGamesRef%>%
  group_by(Referee,PenaltyTeam) %>%
  summarize(n=n())
colnames(NoGamesRef)<-c("Referee", "PenaltyTeam", "NGames")</pre>
penRef<-merge(x=penRef,y=NoGamesRef)</pre>
penRef$PenPerGame <- penRef$NPenalties/penRef$NGames</pre>
temP<-penRef%>%
  group_by(PenaltyTeam)%>%
  dplyr::summarize(Median = median(PenPerGame))
#temP
penRef<-merge(x=penRef,y=temP)</pre>
penRef<-penRef[complete.cases(penRef),]</pre>
ggplot(penRef, aes(x=reorder(Referee,PenPerGame),y=PenPerGame))+geom_point()+coord_flip()+ggtitle("Aver
```

## Average Number of Penalties By Team, by Referee

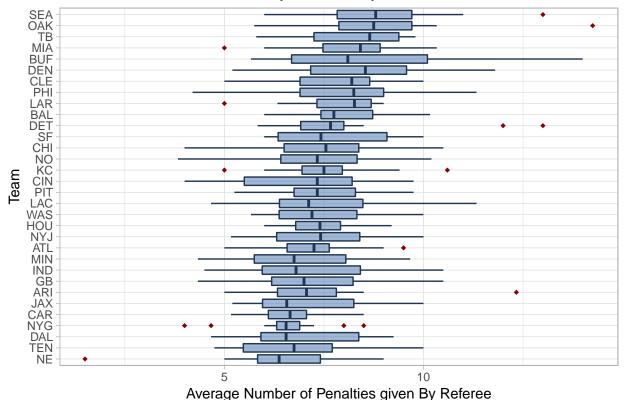


The above is data prep.

```
fill <- "#4271AE"
line <- "#1F3552"
```

boxPlotTeam<-ggplot(penRef, aes(x=reorder(PenaltyTeam,Median),y=PenPerGame))+geom\_boxplot(fill=fill,col boxPlotTeam

## Number of Penalties Given by Referee By Team



#interactiveBoxTeam<-ggplotly(boxPlotTeam)
#interactiveBoxTeam</pre>

In the chart above, we are looking at the distribution of the average number of penalties per Referee. IE, for each team there will be 16 data points as we are looking at 16 referees. Each of the referees will have an average penalties per game for each time, which is what we are charting above. Note that in the absolute majority of cases, referee's call a similar number of penalties; however there are a few cases where referees call many more or many less penalties against a team. Note that some teams have a huge variance of penalties called against, such as Buffalo while others, such as the New York Giants, have a very small variance in the average number of penalties called. Regardless, what we are truly interested in within this chart are the outliers. Having referees make calls that are expected is not something that we are looking for, and as such a closer look at the outliers is below.

```
is_outlier <- function(x) {
  return(x < quantile(x, 0.25) - 1.5 * IQR(x) | x > quantile(x, 0.75) + 1.5 * IQR(x))
}

#penRef %>%
# group_by(PenaltyTeam) %>%
# mutate(outlier = ifelse(is_outlier(PenPerGame), Referee,NA)) %>%
# ggplot(., aes(x = factor(PenaltyTeam), y = PenPerGame)) +
# geom_boxplot() +
# geom_text(aes(label = outlier), na.rm = TRUE, hjust = -0.3)

#Buffalo (BUF), Oakland (OAK), Detroit (DET), NYG seem like interesting ones
#SEA,KC, ATL,ARI,NE
```

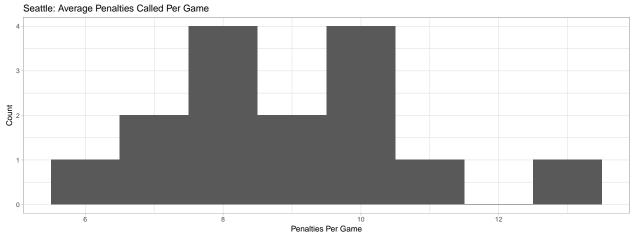
```
BUFPenRef<-penRef[penRef[,1]=='BUF',]</pre>
OAKPenRef<-penRef[penRef[,1]=='OAK',]</pre>
NYGPenRef<-penRef[penRef[,1]=='NYG',]</pre>
DETPenRef<-penRef[penRef[,1]=='DET',]</pre>
NEPenRef<-penRef[penRef[,1]=='NE',]</pre>
KCPenRef<-penRef[penRef[,1]=='KC',]</pre>
ATLPenRef<-penRef[penRef[,1]=='ATL',]
ARIPenRef<-penRef[penRef[,1]=='ARI',]
SEAPenRef<-penRef[penRef[,1]=='SEA',]</pre>
SEAPenRef
##
       PenaltyTeam
                            Referee NPenalties NGames PenPerGame Median
## 452
                SEA
                       Walt Coleman
                                              36
                                                      5
                                                           7.200000
                                                                        8.9
                SEA Gene Steratore
## 453
                                              68
                                                      8
                                                           8.500000
                                                                        8.9
                                             58
## 454
                SEA Walt Anderson
                                                      6
                                                          9.666667
                                                                        8.9
## 455
                SEA Bill Vinovich
                                              30
                                                      5
                                                           6.000000
                                                                        8.9
## 456
                SEA Carl Cheffers
                                              47
                                                          7.833333
                                                                        8.9
## 457
                SEA
                         Brad Allen
                                              44
                                                      5
                                                          8.800000
                                                                        8.9
## 458
                SEA Ronald Torbert
                                              39
                                                      4
                                                           9.750000
                                                                        8.9
                                                      4
## 459
                SEA
                       John Hussey
                                              37
                                                           9.250000
                                                                        8.9
## 460
                SEA
                       Jerome Boger
                                                         13.000000
                                                                        8.9
                                              13
                                                          7.250000
## 461
                SEA
                         John Parry
                                              29
                                                      4
                                                                        8.9
## 462
                SEA Terry McAulay
                                              48
                                                      5
                                                           9.600000
                                                                        8.9
## 463
                SEA Tony Corrente
                                              47
                                                      6
                                                                        8.9
                                                          7.833333
                SEA Clete Blakeman
                                              22
                                                         11.000000
                                                                        8.9
## 464
                       Pete Morelli
## 465
                SEA
                                              32
                                                          8.000000
                                                                        8.9
                         Ed Hochuli
## 466
                SEA
                                              59
                                                           9.833333
                                                                        8.9
subsetTeams <- rbind(KCPenRef,OAKPenRef)</pre>
subsetTeams <- rbind(subsetTeams, NYGPenRef)</pre>
subsetTeams <- rbind(subsetTeams,DETPenRef)</pre>
subsetTeams <- rbind(subsetTeams,NEPenRef)</pre>
subsetTeams <- rbind(subsetTeams,ARIPenRef)</pre>
subsetTeams <- rbind(subsetTeams,SEAPenRef)</pre>
subsetTeams <- rbind(subsetTeams,ATLPenRef)</pre>
subsetTeams
##
                            Referee NPenalties NGames PenPerGame
       PenaltyTeam
                                                                      Median
## 251
                     Walt Anderson
                                             45
                                                          7.500000 7.500000
                     Carl Cheffers
## 252
                                              29
                                                          7.250000 7.500000
                 KC
## 253
                 KC
                         John Parry
                                              30
                                                      4
                                                          7.500000 7.500000
## 254
                 KC Bill Vinovich
                                             43
                                                      5
                                                          8.600000 7.500000
## 255
                 KC Craig Wrolstad
                                             47
                                                          9.400000 7.500000
                 KC Ronald Torbert
## 256
                                              45
                                                      6
                                                          7.500000 7.500000
## 257
                 KC Gene Steratore
                                              27
                                                          9.000000 7.500000
## 258
                 KC
                      Pete Morelli
                                              47
                                                          6.714286 7.500000
```

	259	KC	Ed Hochuli	5	1	5.000000 7.500000
##	261	KC	Jerome Boger	53	5	10.600000 7.500000
##	262	KC	Walt Coleman	34	5	6.800000 7.500000
##	263	KC	Brad Allen	31	4	7.750000 7.500000
##	264	KC	Tony Corrente	56	8	7.000000 7.500000
##	265	KC	John Hussey	14	2	7.000000 7.500000
##	266	KC	Terry McAulay	23	3	7.666667 7.500000
##	267	KC	Clete Blakeman	18	3	6.000000 7.500000
##	403	OAK	Craig Wrolstad	23	4	5.750000 8.825000
##	404	OAK	Terry McAulay	57	4	14.250000 8.825000
##	405	OAK	Jerome Boger	39	4	9.750000 8.825000
##	406	OAK	Brad Allen	31	4	7.750000 8.825000
##	407	OAK	Gene Steratore	31	3	10.333333 8.825000
##	408	OAK	Walt Anderson	47	5	9.400000 8.825000
##	409	OAK	Pete Morelli	41	5	8.200000 8.825000
##	410	OAK	Ronald Torbert	29	3	9.666667 8.825000
##	412	OAK	Ed Hochuli	50	6	8.333333 8.825000
##	413	OAK	Tony Corrente	48	6	8.000000 8.825000
##	414	OAK	John Hussey	20	3	6.666667 8.825000
##	415	OAK	John Parry	35	4	8.750000 8.825000
##	416	OAK	Bill Vinovich	30	4	7.500000 8.825000
##	417	OAK	Clete Blakeman	63	7	9.000000 8.825000
##	418	OAK	Carl Cheffers	39	4	9.750000 8.825000
##	369	NYG	Craig Wrolstad	28	6	4.666667 6.600000
##	370	NYG	Brad Allen	29	4	7.250000 6.600000
##	372	NYG	Jerome Boger	34	5	6.800000 6.600000
##	373	NYG	Tony Corrente	33	5	6.600000 6.600000
##	374	NYG	Ed Hochuli	26	4	6.500000 6.600000
##	375	NYG	Carl Cheffers	43	6	7.166667 6.600000
##	376	NYG	Ronald Torbert	27	4	6.750000 6.600000
##	377	NYG	John Parry	36	6	6.000000 6.600000
##	378	NYG	Walt Coleman	19	3	6.333333 6.600000
##	379	NYG	Bill Vinovich	39	6	6.500000 6.600000
##	380	NYG	Pete Morelli	25	4	6.250000 6.600000
##	381	NYG	Terry McAulay	27	4	6.750000 6.600000
##	382	NYG	Walt Anderson	24	3	8.000000 6.600000
##	383	NYG	Gene Steratore	16	4	4.000000 6.600000
##	384	NYG	Clete Blakeman	26	4	6.500000 6.600000
##	385	NYG	John Hussey	34	4	8.500000 6.600000
##	168	DET	Craig Wrolstad	16	2	8.000000 7.708333
##	169	DET	Walt Coleman	40	5	8.000000 7.708333
##	170	DET	John Parry	31	4	7.750000 7.708333
	171	DET	Bill Vinovich	35	6	5.833333 7.708333
	172	DET	Brad Allen	26	2	13.000000 7.708333
##	173	DET	Gene Steratore	32	4	8.000000 7.708333
	174	DET	Terry McAulay	12	1	12.000000 7.708333
##	175	DET	Walt Anderson	34	4	8.500000 7.708333
##	176	DET	Jerome Boger	46	6	7.666667 7.708333
	177	DET	Pete Morelli	45	6	7.500000 7.708333
	179	DET	Ed Hochuli	28	4	7.000000 7.708333
	180		Clete Blakeman	36	6	6.000000 7.708333
##	181	DET	Carl Cheffers	41	6	6.833333 7.708333
##	182	DET	Tony Corrente	43	6	7.166667 7.708333
##	183	DET	John Hussey	36	6	6.000000 7.708333

##	336	NE	Craig Wrolstad	24	4	6.000000 6.5000	
##	337	NE	Pete Morelli	57	8	7.125000 6.5000	00
##	338	NE	Bill Vinovich	25	4	6.250000 6.5000	00
##	339	NE	Brad Allen	25	5	5.000000 6.5000	00
##	340	NE	John Parry	26	4	6.500000 6.5000	00
##	341	NE	Tony Corrente	67	9	7.444444 6.5000	00
##	342	NE	Walt Coleman	26	5	5.200000 6.5000	00
##	343	NE	Clete Blakeman	16	3	5.333333 6.5000	00
##	344	NE	Walt Anderson	30	4	7.500000 6.5000	00
##	345	NE	Ed Hochuli	34	5	6.800000 6.5000	00
##	346	NE	Jerome Boger	36	4	9.000000 6.5000	00
##	347	NE	Gene Steratore	37	5	7.400000 6.5000	00
##	349	NE	Terry McAulay	12	2	6.000000 6.5000	00
##	350	NE	Carl Cheffers	24	4	6.000000 6.5000	00
##	351	NE	Ronald Torbert	26	3	8.666667 6.5000	00
##	352	NE	John Hussey	3	2	1.500000 6.5000	00
##	1	ARI	Bill Vinovich	15	3	5.000000 7.0000	00
##	2	ARI	Walt Anderson	57	8	7.125000 7.0000	
##	3	ARI	Brad Allen	31	4	7.750000 7.0000	
##	4	ARI	John Parry	27	4	6.750000 7.0000	
##	5	ARI	Ronald Torbert	28	5	5.600000 7.0000	00
##	6	ARI	Pete Morelli	24	3	8.000000 7.0000	
	7	ARI	Tony Corrente	23	4	5.750000 7.0000	
	8		Craig Wrolstad	35	6	5.833333 7.0000	
##	9	ARI	Terry McAulay	34	4	8.500000 7.0000	
##	10		Gene Steratore	35	5	7.000000 7.0000	
##	12	ARI	John Hussey	14	2	7.000000 7.0000	
##	13	ARI	Ed Hochuli	37	3	12.333333 7.0000	
##	14	ARI	Jerome Boger	43	6	7.166667 7.0000	
##	15		Clete Blakeman	40	5	8.000000 7.0000	
##	16	ARI	Walt Coleman	45	6	7.500000 7.0000	
##	17	ARI	Carl Cheffers	26	4	6.500000 7.0000	
	452	SEA	Walt Coleman	36	5	7.200000 8.9000	
	453		Gene Steratore	68	8	8.500000 8.9000	
	454	SEA	Walt Anderson	58	6	9.666667 8.9000	
	455	SEA	Bill Vinovich	30	5	6.000000 8.9000	
	456	SEA	Carl Cheffers	47	6	7.833333 8.9000	
	457	SEA	Brad Allen	44	5	8.800000 8.9000	
	458		Ronald Torbert	39	4	9.750000 8.9000	
	459	SEA	John Hussey	37	4	9.250000 8.9000	
	460	SEA	Jerome Boger	13	1	13.000000 8.9000	
	461	SEA	John Parry	29	4	7.250000 8.9000	
	462	SEA	Terry McAulay	48	5	9.600000 8.9000	
	463	SEA	Tony Corrente	47	6	7.833333 8.9000	
	464		Clete Blakeman	22	2	11.000000 8.9000	
	465	SEA	Pete Morelli	32	4	8.000000 8.9000	
	466	SEA	Ed Hochuli	59	6	9.833333 8.9000	
	18	ATL	Pete Morelli	32	5	6.400000 7.2678	
		ATL	Walt Anderson			6.857143 7.2678	
	19	ATL	Bill Vinovich	48 51	7	7.285714 7.2678	
##	20		Ronald Torbert	51	7		
	22		Tony Corrente	36 38	4	9.000000 7.2678	
		ATL	•	38	5	7.600000 7.2678	
	23	ATL	Terry McAulay	30	4	7.500000 7.2678	
##	25	AIL	Gene Steratore	20	4	5.000000 7.2678	01

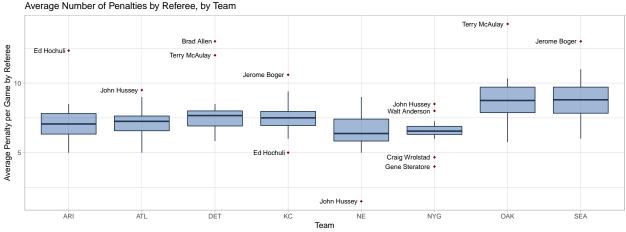
```
## 26
                ATL
                       John Hussey
                                             38
                                                          9.500000 7.267857
## 27
                ATL
                                             28
                                                      5
                                                          5.600000 7.267857
                         John Parry
                                                          6.750000 7.267857
## 28
                ATL Craig Wrolstad
                                             27
                                                      4
## 29
                        Ed Hochuli
                                             23
                                                      3
                                                          7.666667 7.267857
                ATL
## 30
                ATL
                        Brad Allen
                                             29
                                                      4
                                                          7.250000 7.267857
                                                      3
                                                          9.000000 7.267857
## 31
                ATL
                     Carl Cheffers
                                             27
                ATL Clete Blakeman
                                                      6
                                                          5.333333 7.267857
## 32
                                             32
                                                      4
## 33
                ATL
                      Walt Coleman
                                             27
                                                          6.750000 7.267857
```

ggplot(SEAPenRef,aes(x=PenPerGame))+geom\_histogram(binwidth =1)+theme\_light()+ylab('Count')+xlab('Penal')



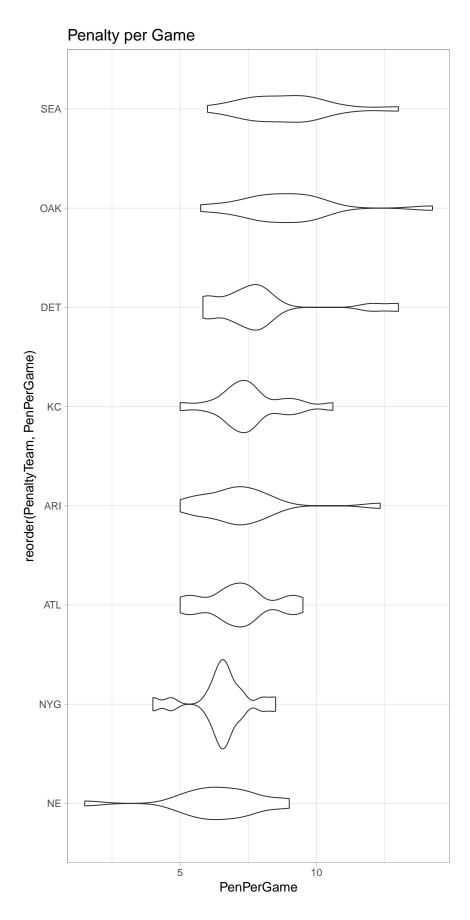
```
fill <- "#4271AE"
line <- "#1F3552"

subsetTeams %>%
  group_by(PenaltyTeam) %>%
  mutate(outlier = ifelse(is_outlier(PenPerGame), Referee,NA)) %>%
  ggplot(., aes(x = factor(PenaltyTeam), y = PenPerGame)) +
    geom_boxplot(fill=fill,colour=line,alpha = 0.5,outlier.colour = "red4", outlier.alpha=1,outlier.shar geom_text(aes(label = outlier), na.rm = TRUE,hjust = 1.1,size=3)+
    theme_light()+xlab('Team')+ylab('Average Penalty per Game by Referee')+ggtitle('Average Number of Penalty Penalty
```



To recap what this chart is showing, we essentially took the previous chart and removed the teams that did not have outliers. In this way, we are focusing on the points that we really care about. Note the recurring Referees. We see Terry McAulay's crew appears to call significantly more penalties against Detroit and Oakland than the other referees. Jerome Boger's crew also calls significantly more calls against Kansas City

and Seattle than other crews. Note the deviation in some of these cases. Perhaps more interestingly, we also see John Hussey's crew calls much fewer penalties against New England, while calling significantly more penalties against the New York Giants.



```
#ggplot(subsetTeams, aes(x = PenPerGame, y = reorder(PenaltyTeam, Median))) +geom_density_ridges(fill='b
Temp1<-penaltiesPerGame%>%
    group_by(PenaltyTeam)%>%
    dplyr::summarize(Median = median(n))

penaltiesPerGame<-merge(x=penaltiesPerGame, y=Temp1)
#penaltiesPerGame

ggplot(penaltiesPerGame, aes(x = n,y =reorder(PenaltyTeam,Median))) +geom_density_ridges(fill = 'blue', ggtitle("Penalty per Game") + theme_light()+xlim(0,25)

## Picking joint bandwidth of 1.04

## Warning: Removed 1 rows containing non-finite values (stat_density_ridges).</pre>
```

