CS 6001 Homework 3

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1 Problem 1

$(9x^2 + 3x + 5)/(7x + 3)$

$$\begin{array}{rrrrr} & & 6\text{x} & +\ 1 & \text{R } 2 \\ \cline{3-5} 7\text{x+3} &) & 9x^2 & +\ 3\text{x} & +\ 5 \\ & - & 9x^2 & +\ 7\text{x} & \\ \cline{3-5} & & & 7\text{x} & +\ 5 \\ & & - & 7\text{x} & +\ 3 \\ \cline{4-5} & & & & 2 \end{array}$$

$(9x^2 + 3x + 5)/(7x + 3) = 6x + 1,\ R\ 2$

2 Problem 2

2.1 Addition

$(x^5 + x^3 + x^2 + x + 1)\ +\ (x^2 + x + 1)$
$= x^5 + x^3$

2.2 Subtraction

$(x^5 + x^3 + x^2 + x + 1)\ -\ (x^2 + x + 1)$
$= x^5 + x^3$

2.3 Multiplication

$(x^5 + x^3 + x^2 + x + 1)\ *\ (x^2 + x + 1)$

$$x^5 + x^3 + x^2 + x + 1 * x^2 = x^7 + x^5 + x^4 + x^3 + x^2$$
$$x^5 + x^3 + x^2 + x + 1 * x^2 = x^6 + x^4 + x^3 + x^2 + x$$
$$x^5 + x^3 + x^2 + x + 1 * 1 = x^5 + x^3 + x^2 + x + 1$$

$$
\begin{array}{ccccccccc}
x^7 & & + x^5 & + x^4 & + x^3 & + x^2 & & & \\
 & + x^6 & & + x^4 & + x^3 & + x^2 & + x & & \\
 & & + x^5 & & + x^3 & + x^2 & + x & + 1 &
\end{array}
$$

$= x^7 + x^6 + x^3 + x^2 + 1$

2.4 Division

$(x^5 + x^3 + x^2 + x + 1)\ /\ (x^2 + x + 1)$

$$
\begin{array}{rcccccccc}
 & & x^3 & + x^2 & + \mathrm{x} & + 1 & & \mathrm{R\ x} \\
\cline{3-8}
x^2 + \mathrm{x} + 1 &) & x^5 & & + x^3 & + x^2 & + \mathrm{x} & + 1 \\
 & - & x^5 & + x^4 & + x^3 & & & \\
\cline{3-8}
 & & & x^4 & & + x^2 & + \mathrm{x} & + 1 \\
 & & - & x^4 & + x^3 & + x^2 & & \\
\cline{3-8}
 & & & & x^3 & & + \mathrm{x} & + 1 \\
 & & & - & x^3 & + x^2 & + \mathrm{x} & \\
\cline{3-8}
 & & & & & x^2 & & + 1 \\
 & & & & - & x^2 & + \mathrm{x} & + 1 \\
\cline{3-8}
 & & & & & & \mathrm{x} &
\end{array}
$$

$= x^3 + x^2 + x + 1,\ R\ x$

3 Problem 3

MI of 010 with IP $x^3 + x + 1 = x^2 + 1$
MI of 010 with IP $x^3 + x^2 + 1 = x^2 + x$

4 Problem 4

With IP $x^3 + x + 1$

$$
\begin{aligned}
(x^2 + x + 1) + (x^2 + 1) &= x \\
(x^2 + x + 1) - (x^2 + 1) &= x \\
(x^2 + x + 1) * (x^2 + 1) &= x^2 + x \\
(x^2 + x + 1)/(x^2 + 1) &= ?
\end{aligned}
$$

With IP $x^3 + x^2 + 1$

$$
\begin{aligned}
(x^2 + x + 1) + (x^2 + 1) &= x \\
(x^2 + x + 1) - (x^2 + 1) &= x \\
(x^2 + x + 1) * (x^2 + 1) &= 1 \\
(x^2 + x + 1)/(x^2 + 1) &= ?
\end{aligned}
$$

5 Problem 5

Solved with our program for Problem 6.

5.1 Binary Representations

$f(x) = 0xad = 1010\ 1101$
$g(x) = 0x0d = 0000\ 1101$

5.2 Multiplicative Inverses

MI of 0xad = 0xe7 = $x^7 + x^6 + x^5 + x^2 + x + 1$
MI of 0x0d = 0xe1 = $x^7 + x^6 + x^5 + 1$

6 Problem 6

See emailed code.