CS 6001 Homework 3

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1 Problem 1

$$(9x^2 + 3x + 5)/(7x + 3)$$

$$(9x^2 + 3x + 5)/(7x + 3) = 6x + 1, R 2$$

2 Problem 2

2.1 Addition

$$(x^5 + x^3 + x^2 + x + 1) + (x^2 + x + 1)$$

= $x^5 + x^3$

2.2 Subtraction

$$(x^5 + x^3 + x^2 + x + 1) - (x^2 + x + 1)$$

= $x^5 + x^3$

2.3 Multiplication

$$(x^5 + x^3 + x^2 + x + 1) * (x^2 + x + 1)$$

$$x^{5} + x^{3} + x^{2} + x + 1 * x^{2} = x^{7} + x^{5} + x^{4} + x^{3} + x^{2}$$

$$x^{5} + x^{3} + x^{2} + x + 1 * x^{2} = x^{6} + x^{4} + x^{3} + x^{2} + x$$

$$x^{5} + x^{3} + x^{2} + x + 1 * 1 = x^{5} + x^{3} + x^{2} + x + 1$$

2.4 Division

$$(x^5 + x^3 + x^2 + x + 1) / (x^2 + x + 1)$$

$$= x^3 + x^2 + x + 1, R x$$

3 Problem 3

MI of 010 with IP $x^3 + x + 1 = x^2 + 1$

MI of 010 with IP $x^3 + x^2 + 1 = x^2 + x$

4 Problem 4

Solved using program for Problem 6 With IP $x^3 + x + 1$

$$(x^{2} + x + 1) + (x^{2} + 1) = x$$

$$(x^{2} + x + 1) - (x^{2} + 1) = x$$

$$(x^{2} + x + 1) * (x^{2} + 1) = x^{2} + x$$

$$(x^{2} + x + 1)/(x^{2} + 1) = (x^{2} + x + 1) * (x^{2} + 1)^{-1} \mod (x^{3} + x + 1)$$

$$= (x^{2} + x + 1) * x \mod (x^{3} + x + 1)$$

$$= (x^{3} + x^{2} + x) \mod (x^{3} + x + 1)$$

$$= x^{2} + 1$$

With IP $x^3 + x^2 + 1$

$$(x^{2} + x + 1) + (x^{2} + 1) = x$$

$$(x^{2} + x + 1) - (x^{2} + 1) = x$$

$$(x^{2} + x + 1) * (x^{2} + 1) = 1$$

$$(x^{2} + x + 1)/(x^{2} + 1) = \text{new calculations}$$

5 Problem 5

Solved with our program for Problem 6.

5.1 Binary Representations

$$f(x) = 0xad = 1010 \ 1101$$

 $g(x) = 0x0d = 0000 \ 1101$

5.2 Multiplicative Inverses

MI of
$$0xad = 0xe7 = x^7 + x^6 + x^5 + x^2 + x + 1$$

MI of $0x0d = 0xe1 = x^7 + x^6 + x^5 + 1$

6 Problem 6

See emailed code.