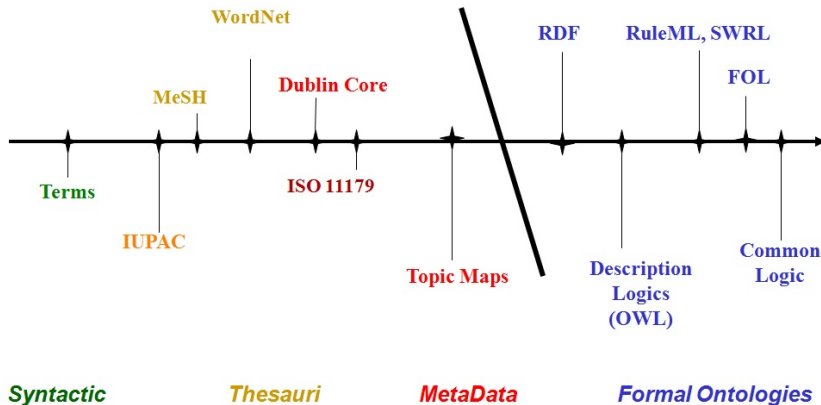


# What Is an Ontology

- An ontology defines objects – the types, properties, and interrelationships of entities that exist in a particular domain;
- Ontologies differ on the language used for the specification of meaning;
- A formal ontology includes a declaration of terminology together with a logical specification of the meaning (semantics) of the terms;

# Semantic Spectrum<sup>1</sup>



<sup>1</sup>Source: Handbook on Ontologies, Springer, 2009. Editors: Staab, Steffen, Studer, Rudi.

# Observations on Objects

- Objects are members of multiple categories (e.g. a doctor, a wife, a mother of two);
- Categories of objects can be more or less specific than others (e.g. a doctor, a professional, a surgeon);
- Categories of objects can have parts, sometimes in multiples (e.g. books have titles, tables have legs and a surface);
- The relation among the parts of an object can be critical in its being a member of a category (e.g. a stack of bricks vs. a pile of bricks)

# Noun Phrases: Objects in English

- Categories and properties of objects can be represented by atomic predicates
  - In some cases, these correspond to simple nouns in English such as Person or City;
  - In other cases, the predicates seem to be more like noun phrases such as MarriedPerson or CanadianCity or AnimalWithFourLegs.
- By definition, these predicates have an internal structure and connections to other predicates (e.g. A married person must be a person.)
- This lecture introduces a formal framework that allows us to have both atomic and non-atomic predicates: a description logic.

# Concepts, Roles, Constants: Objects in DL

In a description logic, there are sentences that will be true or false. It allows three sorts of expressions that act like nouns and noun phrases in English:

- *Concepts* are like category nouns (Dog, Teenager, GraduateStudent)
- *roles* are like relational nouns (:Age, :Parent, :AreaOfStudy)
- *constants* are like proper nouns (johnSmith, chair128)

# Symbols of DL

- Three types of non-logical symbols:
  - atomic concepts: (Dog, Teenager, GraduateStudent)
  - roles: (:Age, :Parent, :AreaOfStudy)
  - constants: (johnSmith, chair128)
- Four types of logical symbols:
  - punctuation: [, ], (, )
  - positive integers: 1, 2, 3, ...
  - concept-forming operators: ALL, EXISTS, FILLS, AND
  - connectives:  $\sqsubseteq$ ,  $\overset{\circ}{=}$ , and  $\rightarrow$

# Syntax of DL

- The set of concepts is the one satisfying:
  - Every atomic concept is a concept,
  - If  $r$  is a role and  $d$  is a concept, then  $[ALL\ r\ d]$  is a concept,
  - If  $r$  is a role and  $n$  is an integer, then  $[EXISTS\ n\ r]$  is a concept,
  - If  $r$  is a role and  $c$  is a constant, then  $[FILLS\ r\ c]$  is a concept,
  - If  $d_1, \dots, d_k$  are concepts, then so is  $[AND\ d_1, \dots, d_k]$ .
- Three types of sentences in DL:
  - If  $d$  and  $e$  are concepts, then  $(d \sqsubseteq e)$  is a sentence,
  - if  $d$  and  $e$  are concepts, then  $(d \doteq e)$  is a sentence,
  - If  $d$  is a concept and  $c$  is a constant, then  $(c \rightarrow d)$  is a sentence.

# The Meaning of DL Concepts

- Constants stand for individuals, concepts for sets of individuals, and roles for binary relations.
- The meaning of a complex concept is derived from the meaning of its parts the same way a noun phrases is:
  - $[EXISTS\ n\ r]$  describes those individuals that stand in relation  $r$  to at least  $n$  other individuals (e.g.,  $[EXISTS\ 1\ :Child]$  );
  - $[FILLS\ r\ c]$  describes those individuals that stand in the relation  $r$  to the individual denoted by  $c$  (e.g.,  $[FILLS\ :Cousin\ joe]$ );
  - $[ALL\ r\ d]$  describes those individuals that stand in relation  $r$  only to individuals that are described by  $d$  (e.g.,  $[ALL\ :Employee\ UnionMember]$ );
  - $[AND\ d_1\ \dots\ d_k]$  describes those individuals that are described by all of the  $d_i$  (e.g.,  $[AND\ Professor\ Canadian]$ ).



# The Meaning of DL Concepts: An Example

- a company with at least 7 directors, whose managers are all women with PhDs, and whose min salary is \$40/hr"
- *[AND Company*  
    *[EXISTS 7 :Director]*  
    *[ALL :Manager [AND Woman [FILLS :Degree PhD]]]*  
    *[FILLS :MinSalary \$40.00/hour]*  
    *]*

# A DL Knowledge Base

A DL knowledge base is a set of DL sentences serving mainly to

- give names to definitions (e.g., "A FatherOfDaughters is precisely a male with at least one child and all of whose children are female")

*FatherOfDaughters*  $\doteq$

$[AND\ Male\ [EXISTS\ 1\ :Child][ALL\ :Child\ Female]]$

- give names to partial definitions (e.g., "A dog is among other things a mammal that is a pet whose voice call includes barking"<sup>2</sup>)

*Dog*  $\sqsubseteq [AND\ Mammal\ Pet\ [FILLS\ :VoiceCall\ barking]]$

- assert properties of individuals (e.g., "Joe is a FatherOfDaughters and a Surgeon")

*joe*  $\rightarrow [AND\ FatherOfDaughters\ Surgeon]$

---

<sup>2</sup>This gives necessary but not sufficient conditions.

# Formal Semantics

- Interpretation  $\mathcal{I} = \langle D, I \rangle$ , where
  - for every constant  $c$ ,  $I[c] \in D$
  - for every atomic concept  $a$ ,  $I[a] \subseteq D$
  - for every role  $r$ ,  $I[r] \subseteq D \times D$

We then extend the interpretation to all concepts:

- $I[[ALL\ r\ d]] = \{x \in D \mid \text{for any } y, \text{ if } \langle x, y \rangle \in I[r] \text{ then } y \in I[d]\}$
- $I[[EXISTS\ n\ r]] = \{x \in D \mid \text{there are at least } n\ y \text{ such that } \langle x, y \rangle \in I[r]\}$
- $I[[FILLS\ r\ c]] = \{x \in D \mid \langle x, I[c] \rangle \in I[r]\}$
- $I[[AND\ d_1 \dots d_k]] = I[d_1] \cap \dots \cap I[d_k]$
- A sentence of DL will then be true or false as follows:
  - $\mathcal{I} \models (d \sqsubseteq e)$  iff  $I[d] \subseteq I[e]$
  - $\mathcal{I} \models (d \doteq e)$  iff  $I[d] = I[e]$
  - $\mathcal{I} \models (c \rightarrow e)$  iff  $I[c] \in I[e]$

# Entailment vs. Validity

- In some cases, an entailment will hold because the sentence in question is valid.
  - $[AND\ Doctor\ Female] \sqsubseteq Doctor$
  - $[FILLS :Child\ sue] \sqsubseteq [EXISTS\ 1 :Child]$
- But in most other cases, the entailment depends on the sentences in the KB.

For example,

$$[AND\ Surgeon\ Female] \sqsubseteq Doctor$$

is not valid.

But it is entailed by a KB that contains

- 1  $Surgeon \doteq [AND\ Specialist\ [FILLS :Specialty\ surgery]]$
- 2  $Specialist \sqsubseteq Doctor$

# Entailment and Reasoning

- Entailment in DL:
  - A set of DL sentences  $S$  entails a sentence  $\alpha$  (which we write  $S \models \alpha$ ) iff for every  $\mathcal{I}$ , if  $\mathcal{I} \models S$  then  $\mathcal{I} \models \alpha$
  - A sentence is valid iff it is entailed by the empty set.
- Given a KB consisting of DL sentences, there are two basic sorts of reasoning we consider:
  - determining if  $KB \models (c \rightarrow e)$ : whether a named individual **satisfies** a certain description
  - determining if  $KB \models (d \sqsubseteq e)$ : whether one description is **subsumed** by another
  - the other case,  $KB \models (d \doteq e)$  reduces to  $KB \models (e \sqsubseteq d)$  and  $KB \models (d \sqsubseteq e)$

# Computing Subsumption

- We begin with computing subsumption, that is, determining whether or not  $KB \models (d \sqsubseteq e)$ .
- Some simplifications to the KB:
  - we can remove the  $(c \rightarrow d)$  assertions from the KB
  - we can replace  $(d \sqsubseteq e)$  in KB by  $(d \overset{\circ}{=} [AND\ e\ a])$ , where  $a$  is a new atomic concept
  - we assume that in the KB for each  $(d \overset{\circ}{=} e)$ , the  $d$  is atomic and appears only once on the LHS
  - we assume that the definitions in the KB are acyclic vs. cyclic  $(d \overset{\circ}{=} [AND\ e\ f]), (e \overset{\circ}{=} [AND\ d\ g])$
- Under these assumptions, it is sufficient to do the following:
  - normalization: using the definitions in the KB, put  $d$  and  $e$  into a special normal form,  $d'$  and  $e'$
  - structure matching: determine if each part of  $e'$  is matched by a part of  $d'$

# Normalization

Repeatedly apply the following operations to the two concepts:

- expand a definition: replace an atomic concept by its KB definition
- flatten an AND concept:  
 $[AND \dots [AND \textit{d e f}] \dots] \Rightarrow [AND \dots \textit{d e f} \dots]$
- combine the ALL operations with the same role:  
 $[AND \dots [ALL \textit{r d}] \dots [ALL \textit{r e}] \dots] \Rightarrow$   
 $[AND \dots [ALL \textit{r} [AND \textit{d e}]] \dots]$
- combine the EXISTS operations with the same role:  
 $[AND \dots [EXISTS \textit{n}_1 \textit{r}] \dots [EXISTS \textit{n}_2 \textit{r}] \dots] \Rightarrow$   
 $[AND \dots [EXISTS \textit{n} \textit{r}] \dots] \text{ (where } \textit{n} = \text{Max}(\textit{n}_1, \textit{n}_2)\text{)}$

# Normalization Example

[AND Person  
  [ALL :Friend Doctor]  
  [EXISTS 1:Accountant]  
  [ALL :Accountant [EXISTS 1 :Degree]]  
  [ALL :Friend Rich]  
  [ALL :Accountant [AND Lawyer [EXISTS 2 :Degree]]]]]



[AND Person  
  [EXISTS 1 :Accountant]  
  [ALL :Friend [AND Rich Doctor]]  
  [ALL :Accountant [AND Lawyer [EXISTS 1 :Degree] [EXISTS 2 :Degree]]]]]



[AND Person  
  [EXISTS 1 :Accountant]  
  [ALL :Friend [AND Rich Doctor]]  
  [ALL :Accountant [AND Lawyer [EXISTS 2 :Degree]]]]]



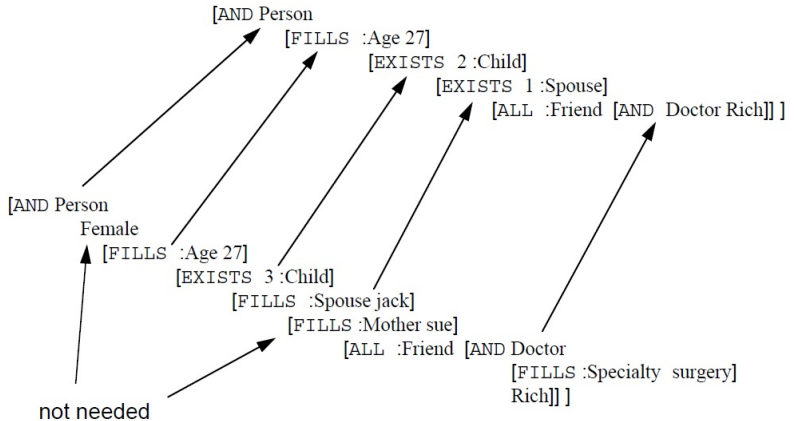
# Structure matching

Once we have replaced atomic concepts by their definitions, we no longer need to use the KB. To see if a normalized concept  $[AND\ e_1 \dots e_m]$  subsumes a normalized concept  $[AND\ d_1 \dots d_n]$ , we do the following – for each component  $e_j$ , check that there is a matching component  $d_i$ :

- if  $e_j$  is atomic or  $[FILLS\ r\ c]$ , then  $d_i$  must be identical to it;
- if  $e_j = [EXISTS\ 1\ r]$ , then  $d_i$  must be  $[EXISTS\ n\ r]$  or  $[FILLS\ r\ c]$ ;
- if  $e_j = [EXISTS\ n\ r]$  where  $n > 1$ , then  $d_i$  must be of the form  $[EXISTS\ m\ r]$  where  $m \geq n$ ;
- if  $e_j = [ALL\ r\ e']$ , then  $d_i$  must be  $[ALL\ r\ d']$ , where recursively  $e'$  subsumes  $d'$ .

In other words, for every part of the more general concept, there must be a corresponding part in the more specific one. It can be shown that this procedure is sound and complete: it returns YES iff  $KB \models (d \sqsubseteq e)$ .

# Structure Matching Example



# Computing Satisfaction

- To determine if  $KB \models (c \rightarrow e)$ , we use the following procedure:
  - find the most specific concept  $d$  such that  $KB \models (c \rightarrow d)$
  - determine whether or not  $KB \models (d \sqsubseteq e)$ , as before.
- To a first approximation, the  $d$  we need is the AND of every  $d_i$  such that  $(c \rightarrow d_i) \in KB$ . However, this can miss some inferences.
- for example: Suppose the KB contains  $(joe \rightarrow Person)$   
 $(canCorp \rightarrow$   
 $[AND Company[ALL:Manager Canadian][FILLS:Manager joe]])$   
then the  $KB \models (joe \rightarrow Canadian)$ .
- To find the  $d$ , a more complex procedure is used that propagates constraints from one individual (canCorp) to another (joe).

# Some Applications of DL

- DL have been and can be used in a number of applications:
  - To develop directly meta-data, not only representing taxonomies and inheritance of properties of objects, but also reasoning over them;
  - To formalize the semantics of the tags of those syntax-based markup languages and tools such as XML;
  - To create interface for relational database (through providing a higher level view of the data based on objects);
  - To detect contradiction in a system.