```
rm(list = ls())
sessionInfo()
## R version 4.2.1 (2022-06-23 ucrt)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 22000)
## Matrix products: default
##
## locale:
## [1] LC_COLLATE=English_United States.utf8
## [2] LC_CTYPE=English_United States.utf8
## [3] LC_MONETARY=English_United States.utf8
## [4] LC_NUMERIC=C
## [5] LC_TIME=English_United States.utf8
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                                datasets methods
                                                                     base
## loaded via a namespace (and not attached):
## [1] compiler_4.2.1 magrittr_2.0.3 fastmap_1.1.0 cli_3.3.0
## [5] tools_4.2.1
                        htmltools_0.5.3 rstudioapi_0.13 yaml_2.3.5
## [9] stringi_1.7.8 rmarkdown_2.15 knitr_1.39
                                                         stringr_1.4.0
## [13] xfun_0.32
                        digest_0.6.29
                                         rlang_1.0.4
                                                         evaluate_0.16
library(covdepGE)
library(loggle)
library(HeteroGGM)
library(mclust)
## Package 'mclust' version 5.4.10
## Type 'citation("mclust")' for citing this R package in publications.
library(ggplot2)
library(ggpubr)
library(kableExtra)
now <- format(Sys.time(), "%Y%m%d_%H%M%S")</pre>
# initialize storage for results, time, and progress tracking
set.seed(1)
n trials <- 1
results <- vector("list", n_trials + 1)
names(results) <- c(paste0("trial", 1:n_trials), "time")</pre>
results$time <- Sys.time()</pre>
pb <- txtProgressBar(0, n_trials, style = 3)</pre>
##
# define data dimensions
p <- 3
(n \leftarrow round(2 * 3 * p))
```

```
## [1] 18
(nj \leftarrow n \%/\% 3)
## [1] 6
# function for surpressing cat
quiet <- function(x) {
  sink(tempfile())
  on.exit(sink())
  invisible(force(x))
}
# get number of available workers
(num_workers <- parallel::detectCores() - 1)</pre>
## [1] 15
# function for evaluating estimated graphs compared to ground truth
eval_est <- function(est, true){</pre>
  # get true number of edges and non-edges
  num_edge <- sum(true, na.rm = T)</pre>
  num_non <- sum(true == 0, na.rm = T)</pre>
  # calculate sensitivity and specificity
  true_edge <- sum(est == true & true == 1, na.rm = T)</pre>
  true_non <- sum(est == true & true == 0, na.rm = T)</pre>
  sens <- true_edge / num_edge</pre>
  spec <- true_non / num_non</pre>
  list(sens = sens, spec = spec)
}
#```
#```\{r, eval = F\}
# perform trials
for (j in 1:n_trials){
  # generate the data and create storage for the models
  data <- generateData(p, nj, nj, nj)</pre>
  trial <- vector("list", 4)</pre>
  names(trial) <- c("data", "covdepGE", "loggle", "HeteroGGM")</pre>
  prec_arr_dim <- c(p, p, n)</pre>
  trial$data <- data
  # convert the true precision to an array and then to a graph; mask diagonal
  prec <- array(unlist(data$true_precision), prec_arr_dim)</pre>
  graph <- (prec != 0) * 1 + replicate(n, diag(rep(NA, p)) * 1)</pre>
```

fit each method, save details about results, time, etc.

```
# covdepGE
out_covdepGE <- tryCatch(suppressWarnings(covdepGE(</pre>
  data$X, data$Z, parallel = T, num_workers = num_workers)),
  error = function(e) list(error = e))
if (names(out_covdepGE)[[1]] == "error"){
  out covdepGE <- out covdepGE$error</pre>
}else{
  out covdepGE$time <- as.numeric(out covdepGE$model details$elapsed, units = "secs")
  out covdepGE$str <- array(unlist(out covdepGE$graphs$graphs), dim = prec arr dim)
  out_covdepGE[c("sens", "spec")] <- eval_est(out_covdepGE$str, graph)[c("sens", "spec")]</pre>
trial$covdepGE <- out_covdepGE</pre>
rm(list = "out_covdepGE")
gc()
# loggle
start <- Sys.time()</pre>
out_loggle <- tryCatch(quiet(loggle.cv(t(data$X), num.thread = num_workers)),</pre>
                         error = function(e) list(error = e))
if (names(out_loggle)[[1]] == "error"){
  out_loggle <- out_loggle$error</pre>
}else{
  out loggle <- out loggle$cv.select.result
  out_loggle$time <- as.numeric(Sys.time() - start, units = "secs")</pre>
  out_loggle$str <- array(unlist(lapply(lapply(</pre>
    out_loggle$adj.mat.opt, `-`, diag(p)), as.matrix)), dim = prec_arr_dim)
  out_loggle[c("sens", "spec")] <- eval_est(out_loggle$str, graph)[c("sens", "spec")]</pre>
trial$loggle <- out_loggle</pre>
rm(list = "out_loggle")
gc()
# HeteroGGM
clust <- Mclust(data$Z, verbose = F)</pre>
lambda <- genelambda.obo(lambda2_min = 0.15)</pre>
start <- Sys.time()</pre>
out hetGGM <- tryCatch(GGMPF(lambda, data$X + clust$classification * 10, clust$G),</pre>
                         error = function(e) list(error = e))
if (names(out_hetGGM)[[1]] == "error"){
  out hetGGM <- out hetGGM$error</pre>
}else{
  out_hetGGM$time <- as.numeric(Sys.time() - start, units = "secs")</pre>
  out_hetGGM$str <- (out_hetGGM$Theta_hat.list[[out_hetGGM$Opt_num]] != 0) * 1</pre>
  out_hetGGM$str <- out_hetGGM$str - replicate(dim(out_hetGGM$str)[3], diag(p))</pre>
  out_hetGGM$str <- out_hetGGM$str[ , , out_hetGGM$member.list[[out_hetGGM$Opt_num]]]</pre>
  out_hetGGM[c("sens", "spec")] <- eval_est(out_hetGGM$str, graph)[c("sens", "spec")]</pre>
trial$HeteroGGM <- out_hetGGM</pre>
rm(list = "out_hetGGM")
gc()
# for hp tuning lambda grid
# het_gr <- vector("list", n)</pre>
```

```
# for (l in 1:n){
  \# het_gr[[l]] \leftarrow out_hetGGM\$str[,, l]
  # }
  # # find the unique graphs
  # unique_graphs <- unique(het_gr)</pre>
  # # create a list where the j-th element is the j-th unique graph and the
  # # indices of the observations corresponding to this graph
  # unique_sum <- vector("list", length(unique_graphs))</pre>
  # names(unique_sum) <- paste0("graph", 1:length(unique_graphs))</pre>
  # # iterate over each of the unique graphs
  # for (j in 1:length(unique_graphs)){
  #
     # fix the unique graph
  #
      graphj <- unique_graphs[[j]]</pre>
  #
     # find indices of the observations corresponding to this graph
     graph_inds <- which(sapply(het_gr, identical, graphj))</pre>
  #
  #
     # split up the contiquous subsequences of these indices
     cont_inds <- split(sort(graph_inds), cumsum(c(1, diff(sort(graph_inds)))</pre>
                                                       != 1)))
  #
  #
  #
     # create a character summary for each of the contiguous sequences
     inds_sum <- sapply(cont_inds, function(idx_seq) ifelse(length(</pre>
  #
  #
       idx\_seq) > 3, paste0(min(idx\_seq), ", ..., ", max(idx\_seq)),
  #
       pasteO(idx_seq, collapse = ",")))
  #
  #
    # combine the summary
     inds_sum <- pasteO(inds_sum, collapse = ",")</pre>
  #
  #
  # # add the graph, indices, and summary to the unique graphs summary list
      unique_sum[[j]] <- list(graph = graphj, indices = graph_inds,</pre>
                               ind_sum = inds_sum)
  # }
  # for (graphj in unique_sum){
  # print(matViz(graphj$graph) + ggtitle(graphj$ind_sum))
  # out_hetGGM$Opt_lambda
  # lambda
  # save the trial and update the progress bar
  trial$elapsed <- sum(unlist(sapply(trial, `[[`, "time")))</pre>
  results$time <- c(results$time, Sys.time())</pre>
  results[[j]] <- trial
  setTxtProgressBar(pb, j)
  save(results, file = paste0("results_", now, ".Rda"))
}
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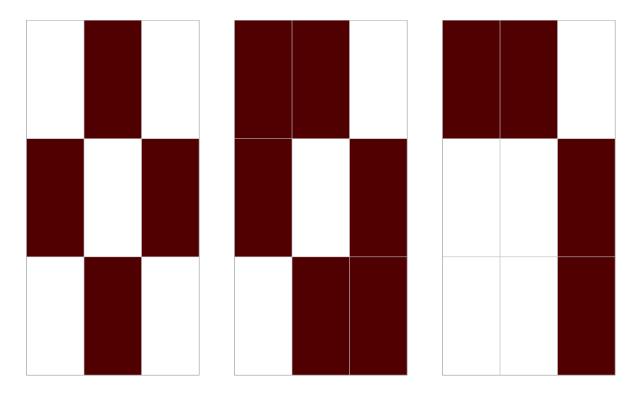
```
## Warning in log(d): NaNs produced
##
                                                                                               |==========
# save the results
save(results, file = paste0("results_", now, ".Rda"))
## Analysis
#load("simulation_study/results.Rda")
#load("/home/jacob.a.helwiq/covdepGE/simulation_study/results_20220817_150045.Rda")
# extract each of the models
results <- results[setdiff(names(results), "time")]</pre>
covdepGE_models <- lapply(results, `[[`, "covdepGE")</pre>
loggle_models <- lapply(results, `[[`, "loggle")</pre>
hetGGM_models <- lapply(results, `[[`, "HeteroGGM")</pre>
# extract the sensitivties, specificities, and time
covdepGE_sens <- sapply(covdepGE_models, `[[`, "sens")
covdepGE_spec <- sapply(covdepGE_models, `[[`, "spec")</pre>
covdepGE_times <- sapply(covdepGE_models, `[[`, "time")</pre>
loggle_sens <- sapply(loggle_models, `[[`, "sens")</pre>
loggle_spec <- sapply(loggle_models, `[[`, "spec")
loggle_times <- sapply(loggle_models, `[[`, "time")</pre>
hetGGM_sens <- sapply(hetGGM_models, `[[`, "sens")</pre>
```

```
hetGGM_spec <- sapply(hetGGM_models, `[[`, "spec")</pre>
hetGGM_times <- sapply(hetGGM_models, `[[`, "time")</pre>
# sensitivity analysis
summary(covdepGE_sens)
     Min. 1st Qu. Median
                          Mean 3rd Qu.
## 0.3333 0.3333 0.3333 0.3333 0.3333
summary(loggle_sens)
     Min. 1st Qu. Median
                            Mean 3rd Qu.
##
## 0.7381 0.7381 0.7381 0.7381 0.7381 0.7381
summary(hetGGM_sens)
         Length Class Mode
## trial1 0
               -none- NULL
summary(covdepGE_sens - loggle_sens)
     Min. 1st Qu. Median
                            Mean 3rd Qu.
## -0.4048 -0.4048 -0.4048 -0.4048 -0.4048
summary(covdepGE_sens - hetGGM_sens)
## Error in covdepGE_sens - hetGGM_sens: non-numeric argument to binary operator
# specificity analysis
summary(covdepGE_spec)
##
     Min. 1st Qu. Median
                            Mean 3rd Qu.
                                           Max.
##
               1
                              1
summary(loggle_spec)
##
     Min. 1st Qu. Median
                            Mean 3rd Qu.
                                           Max.
## 0.6667 0.6667 0.6667 0.6667 0.6667
summary(hetGGM_spec)
         Length Class Mode
## trial1 0
            -none- NULL
summary(covdepGE_spec - loggle_spec)
     Min. 1st Qu. Median
                            Mean 3rd Qu.
## 0.3333 0.3333 0.3333 0.3333 0.3333
```

```
summary(covdepGE_spec - hetGGM_spec)
## Error in covdepGE_spec - hetGGM_spec: non-numeric argument to binary operator
# time analysis
summary(covdepGE_times)
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
##
     1.917
             1.917
                    1.917
                             1.917 1.917
                                              1.917
summary(loggle_times)
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
##
     80.23
            80.23
                    80.23
                             80.23
                                     80.23
                                              80.23
summary(hetGGM_times)
          Length Class Mode
## trial1 0
                 -none- NULL
# table of results
perf <- apply(cbind(covdepGE_sens, loggle_sens, hetGGM_sens,</pre>
                    covdepGE_spec, loggle_spec, hetGGM_spec,
                    covdepGE_times, loggle_times, hetGGM_times),
              2, function(x) paste0(round(mean(x), 3), " (", round(sd(x), 3), ")"))
## Warning in mean.default(x): argument is not numeric or logical: returning NA
## Error in var(if (is.vector(x) || is.factor(x)) x else as.double(x), na.rm = na.rm): is.atomic(x) is:
perf_df <- data.frame(t(matrix(perf, 3, 3)))</pre>
## Error in matrix(perf, 3, 3): object 'perf' not found
row.names(perf_df) <- c("Sensitivity", "Specificity", "Time(s)")</pre>
## Error in row.names(perf_df) <- c("Sensitivity", "Specificity", "Time(s)"): object 'perf_df' not foun
colnames(perf_df) <- c("covdepGE", "loggle", "HeteroGGM")</pre>
## Error in colnames(perf_df) <- c("covdepGE", "loggle", "HeteroGGM"): object 'perf_df' not found
kbl(perf_df, format = "latex", booktabs = T)
## Error in knitr::kable(x = x, format = format, digits = digits, row.names = row.names, : object 'perf
```

```
# visualize graphs
# pred_graphs <- plot(covdepGE_models[[12]])</pre>
true graphs <- unique(lapply(lapply(lapply(</pre>
 results$trial1$data$true_precision, `!=`, 0), `*`, 1), `-`, diag(p)))
graph_inds <- c(pasteO(c(1, nj), collapse = ",...,"),</pre>
                paste0(c(nj + 1, 2 * nj), collapse = ",...,"),
                paste0(c(2 * nj + 1, 3 * nj), collapse = ",...,"))
titles <- paste0("Graph ", 1:3, ", observations ", graph_inds)</pre>
true_graphs <- lapply(1:3, function(j)</pre>
  matViz(true_graphs[[j]]) +
    ggtitle(titles[[j]]) +
    geom_tile(color = "grey", size = 1e-10) +
    theme(axis.line = element_blank(),
          axis.text.x=element_blank(),
          axis.text.y = element_blank(),
          axis.ticks = element_blank(),
          axis.title.x = element_blank(),
          axis.title.y = element_blank(),
          legend.position = "none")
    )
# pred_graphs <- ggarrange(plotlist = pred_graphs, nrow = 1, legend = F)</pre>
true_graphs <- ggarrange(plotlist = true_graphs, nrow = 1, legend = F)</pre>
true_graphs
```

Graph 1, observations 1,...Graph 2, observations 7,...Graph 3, observations 13,...,



```
# ggsave("simulation_study/plots/preds.pdf", pred_graphs, height = 4, width = 11)
# ggsave("simulation_study/plots/true.pdf", true_graphs, height = 4, width = 11)
```