1 covdepGE: Covariate Dependent Graph Estimation

1.1 Installation

Run the following in R:

devtools::install_github("JacobHelwig/covdepGE")

1.2 Overview

Suppose $X \in \mathbb{R}^{n \times p}$ is a data matrix of independent observations $X = (\boldsymbol{x}_1, ..., \boldsymbol{x}_p)$, where, for $j \in 1, ..., p$:

$$\boldsymbol{x}_{i} \sim \mathcal{N}\left(\mu_{i}, \Sigma_{i,i}\right), \boldsymbol{x}_{i} \in \mathbb{R}^{n}$$
 $\boldsymbol{X} \sim \mathcal{N}\left(\mu, \Sigma\right)$ (1)

Let Z be an $n \times p'$ matrix of extraneous covariates. The conditional dependence structure of $x_1, ..., x_p$ can be modeled as an undirected graph \mathcal{G} such that:

$$\mathcal{G}_{i,j} = \begin{cases} 1 & \iff \operatorname{Cov}(\boldsymbol{x_i}, \boldsymbol{x_j}) \neq 0 \\ 0 & \text{otherwise} \end{cases}$$
 (2)

That is, there is an edge between the x_i and x_j nodes if, and only if, these variables are dependent on each other given all other variables.

Further suppose that the conditional dependence structure of X is not homogeneous across the individuals, and is instead a continuous function of the extraneous covariates Z1. Then, this methodology aims to estimate a graph for each of the individuals, possibly unique to the individual, such that similar estimates are made for those who are similar to one another in terms of the extraneous covariates.

For an example application, see 1, wherein the sample was composed of healthy and cancerous individuals, $x_1, ..., x_8$ were protein expression levels of 8 genes, and Z was the copy number variation of a gene z associated with cancer, $z \notin \{x_1, ..., x_8\}$.

1.3 Functionality

The main function, covdepGE::covdepGE(X, Z), estimates the posterior distribution of the graphical structure \mathcal{G}_l for each of the n individuals using a variational mean-field approximation. The function will output $n \ p \times p$ symmetric matrices \mathcal{A}_l , where $\mathcal{A}_{i,j}^{(l)}$ is the posterior inclusion probability of an edge between the node representing the i-th variable and the node representing the j-th variable.

1.4 To-do

- Complete documentation
- Add compatibility checks
- ggplot2 wrappers for graph visualization
- Implement KDE to obtain individual specific bandwidths; add KDE argument (boolean). Then, the argument tau is only used when KDE = F
- Allow for user specification of a norm ("1", "2", or "inf"), symmetrization method ("mean", "min", or "max") and hyperparameter sigmasq
- Change default pi_est to a scalar
- Implement automatic sigmabeta_sq grid generation via arguments varmax, varmin, n_sigma
- Add warnings for when the optimal sigmabeta_sq OR pi_est is chosen at either of the grid end points; a warning argument for when users would like to toggle off the warnings. Should only be enabled when either sigmabeta_sq or pi_est is longer than 2.
- Change return type of alpha_matrices from a list of p $n \times p$ matrices to a list of n $p \times p$ matrices
- Create a vignette demonstrating usage on a simple simulated dataset.
- Parallelization of the "main loop" over the predictors in covdepGE_main.R). This is complicated by the C++ code, however, two potential solutions are:
 - StackOverflow suggestion
 - RcppParallel

This is a finishing touch and likely will not be implemented in the package by the end of the semester.

References

[1] (1) Dasgupta, Sutanoy, et al. "An approximate Bayesian approach to covariate dependent graphical modeling." 2021