| Continuity and Asymptotes for common functions |  |                                      |  |
|--|--|--------------------------------------|--|
| Function                                       | Continuous on  | Vertical Asymp-                      | Horizontal Asymp-                            |
|  |  | totes                                | totes  |
| $f(x) = \frac{1}{x^n}$ for $n$ a pos-          | $\mathbb{R}\setminus\{0\}$                               | x = 0                                | y = 0  |
| itive integer                                  |  |                                      |  |
| $f(x) = \sqrt[n]{x}$                           | $\mathbb{R}$ if $n$ is odd, $\mathbb{R}_{\geq 0}$ if $n$ | None                                 | None   |
|  | is even  |                                      |  |
| $f(x) = a_n x^n + \dots +$                     | $\mathbb{R}$   | None                                 | None   |
| $a_1x + a_0$                                   |  |                                      |  |
| $f(x) = \frac{P(x)}{Q(x)}$ , where             | All real numbers ex-                                     | It depends!                          | It depends!                                  |
| P(x), $Q(x)$ are poly-                         | cept those $x \in \mathbb{R}$ for                        |                                      |  |
| nomials  | which $Q(x) = 0$   |                                      |  |
| $f(x) = a^x \text{ for } a > 0$                | $\mathbb{R}$   | None                                 | y = 0  |
| and $a \neq 1$                                 |  |                                      |  |
| $f(x) = \ln(x)$                                | $\mathbb{R}_+ = (0, +\infty)$                            | x = 0                                | None   |
| $f(x) = \sin(x)$                               | $\mathbb{R}$   | None                                 | None   |
| $f(x) = \tan(x)$                               | All real numbers but                                     | $x = \frac{k\pi}{2}$ , where k is an | None   |
|  | $\frac{k\pi}{2}$ , where k is an odd                     | odd integer.                         |  |
|  | integer. (This is where                                  |                                      |  |
|  | $\cos(x) = 0.$   |                                      |  |
| $f(x) = \arcsin(x)$                            | [-1,1]   | None                                 | None   |
| $f(x) = \arccos(x)$                            | [-1,1]   | None                                 | None   |
| $f(x) = \arctan(x)$                            | $\mathbb{R}$   | None                                 | $y = \frac{\pi}{2}$ and $y = -\frac{\pi}{2}$ |