



RIYA Week 4 Presentation

Frequency Domain Analysis

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Tasks accomplished

- Performed calibration of the FFT code using a pure sinusoid function
- Attempted to improve the FFT results of the non-linear system

FFT Calibration

Acceleration signal = Sinusoid with frequency 250 Hz and RMS value 0.1g

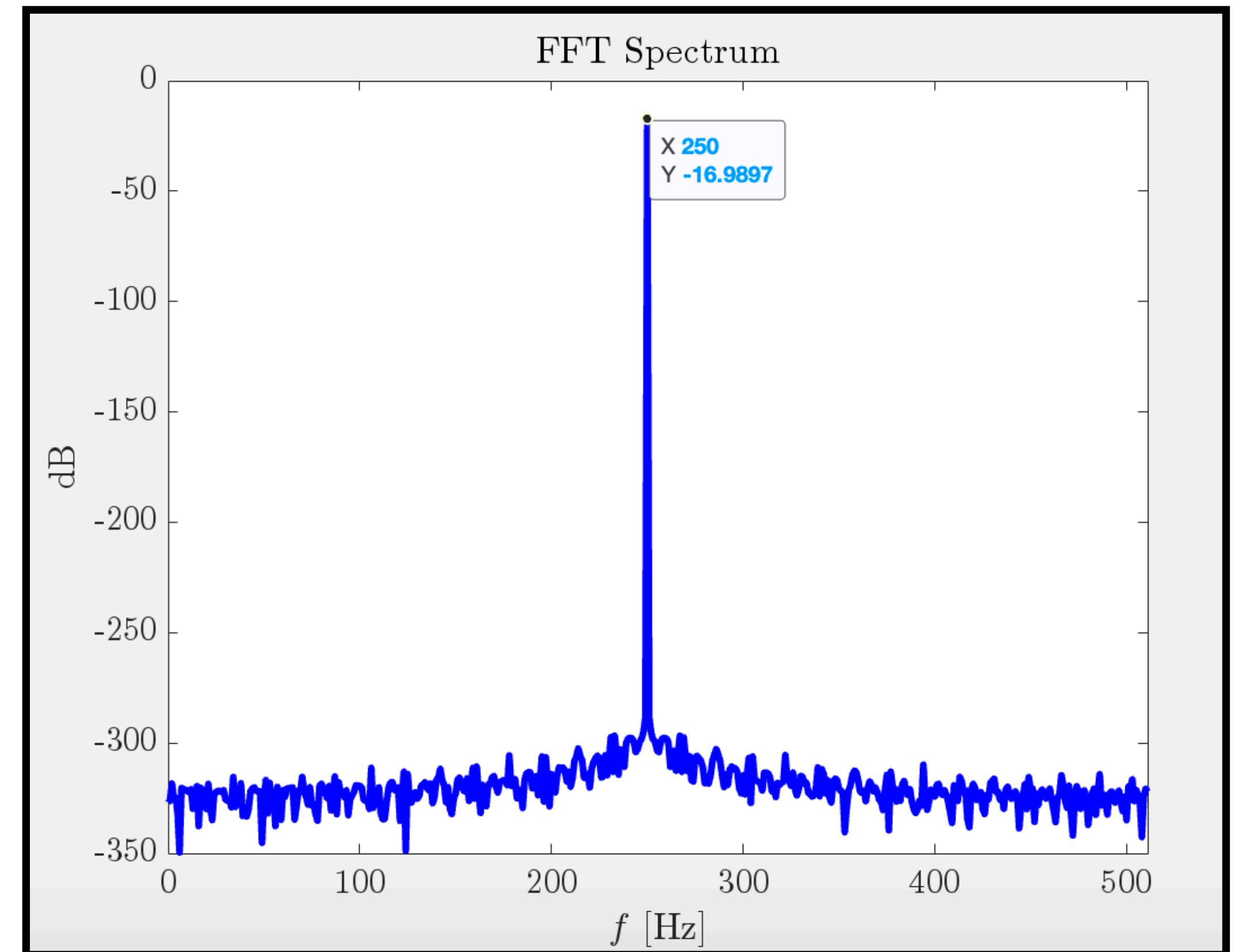
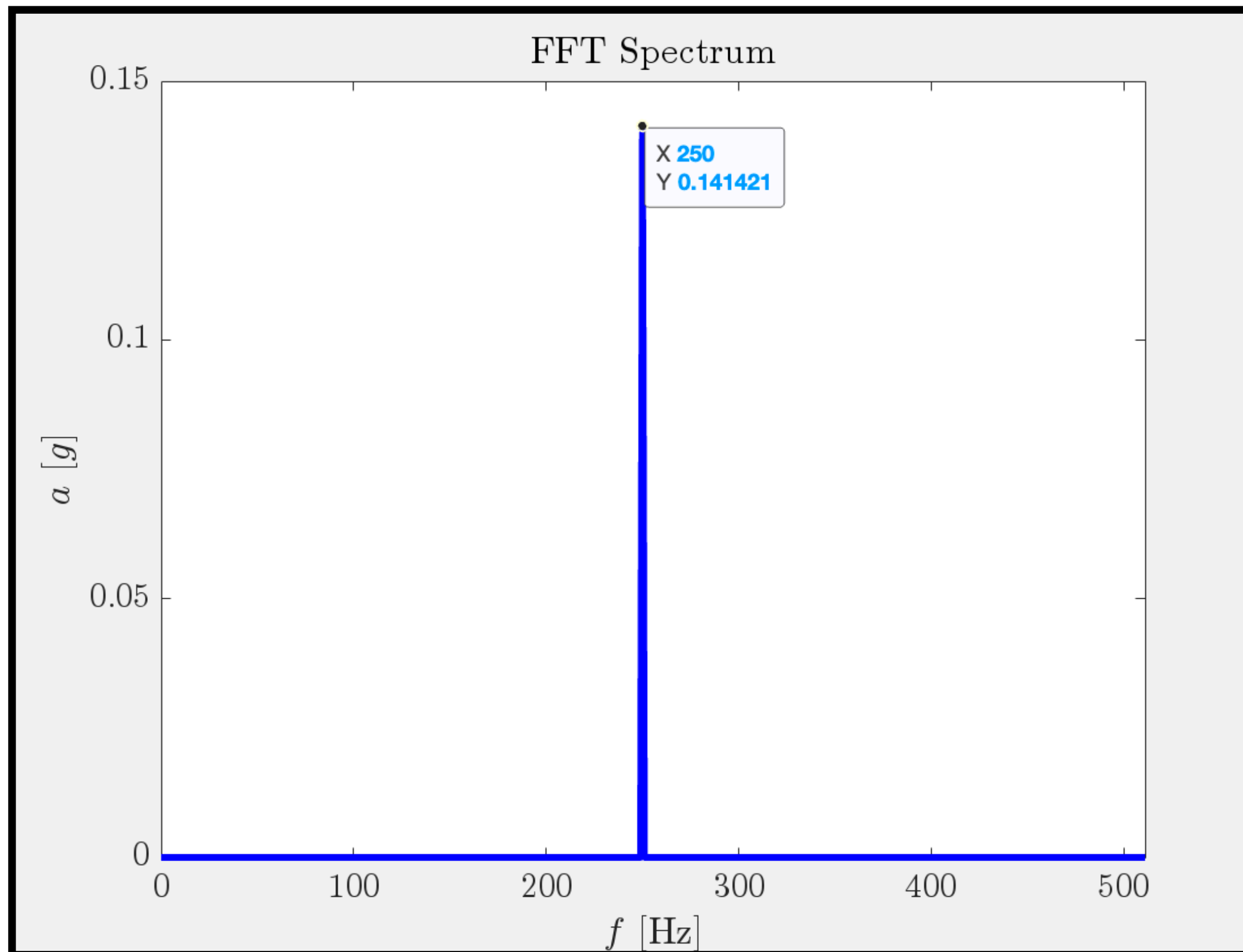
%% Case 3	
fs3 = 1024; % Sampling frequency	
duration3 = 30; % Duration of signal	
N3 = fs3 * duration3; % Number of samples	
t3 = 0:1/fs3:duration3-1/fs3; % Time vector	
f3 = 0.1*sqrt(2)*sin(250*2*pi*t3); % Vector representing 250 Hz sinusoidal signal with 0.1g RMS	

DSP parameters (in seconds/ Hz appropriately)

DSP Parameters	
"Time resolution"	"0.00097656"
"Time record"	"29.999"
"Sampling frequency"	"1024"
"Frequency resolution"	"1"
"Number of points"	"1024"

Post-Calibration results

For the previous sinusoid acceleration signal, used for calibration



Post-Calibration results

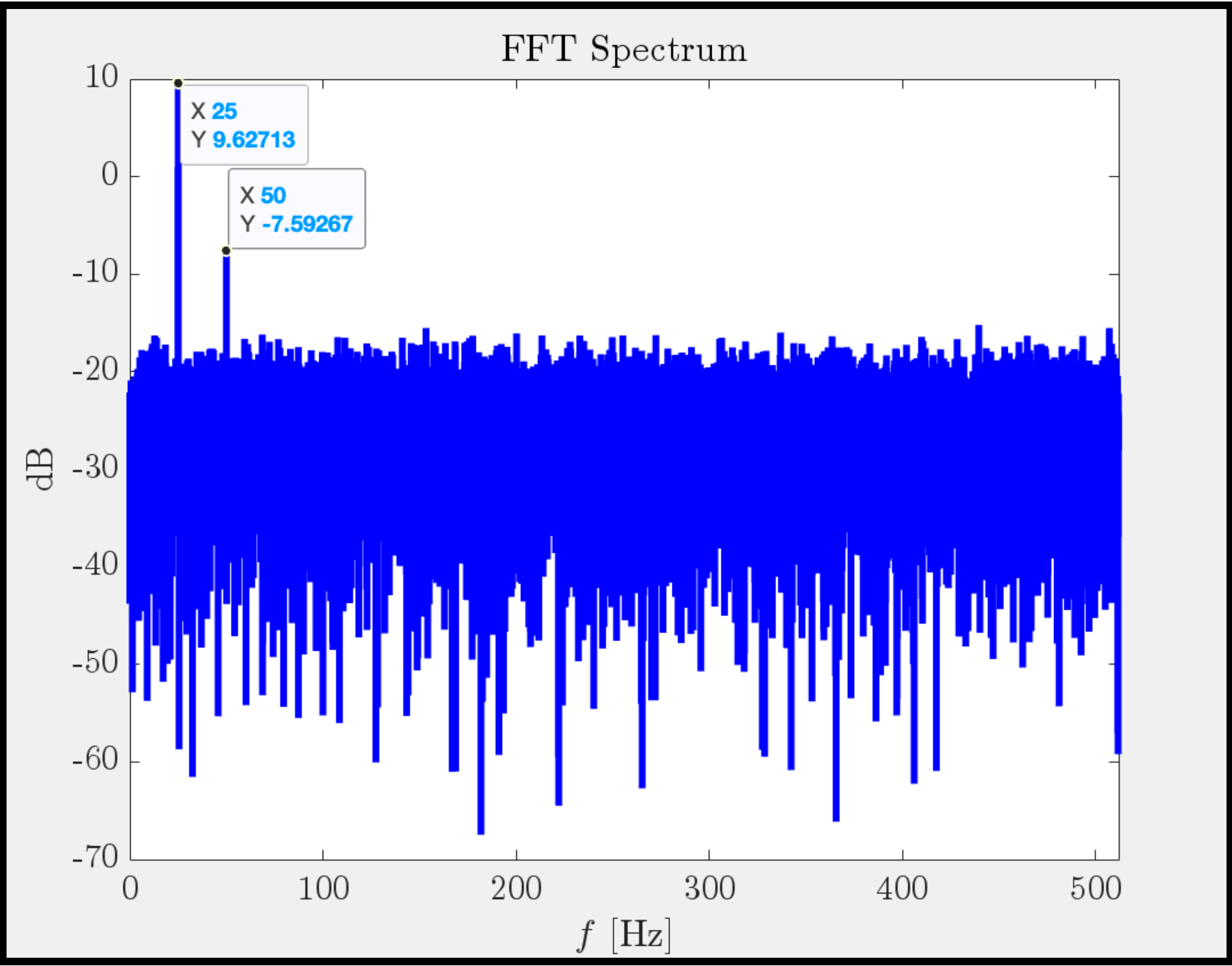
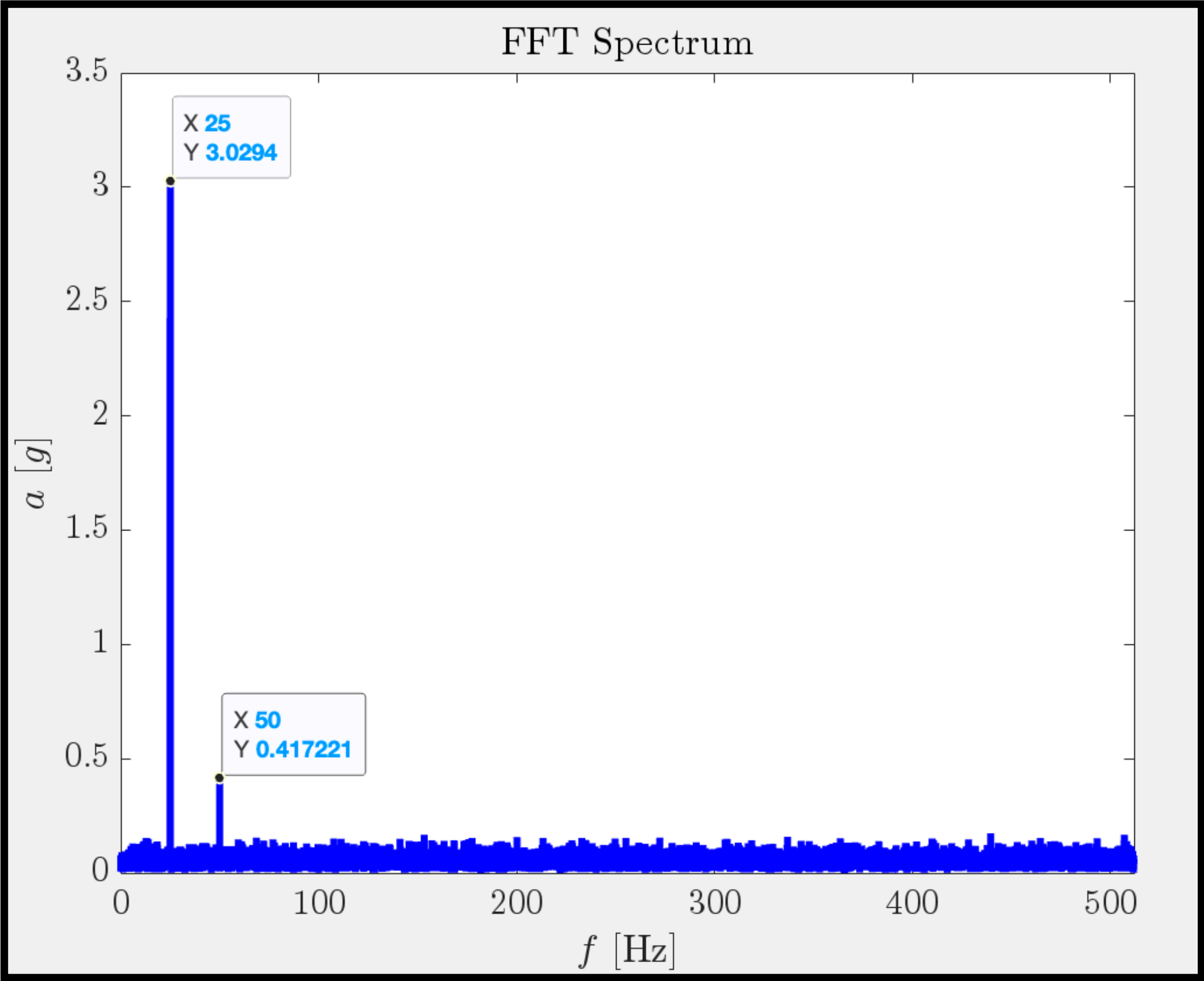
Example 2

```
fs2 = 1024;  
duration2 = 30;  
N2 = fs2 * duration2;  
t2 = 0:1/fs2:duration2-1/fs2;  
f2 = 3*sin(25*2*pi*t2) + 0.4*sin(50*2*pi*t2 - 49*pi/180) + 5*(randn(size(t2)));
```

DSP Parameters

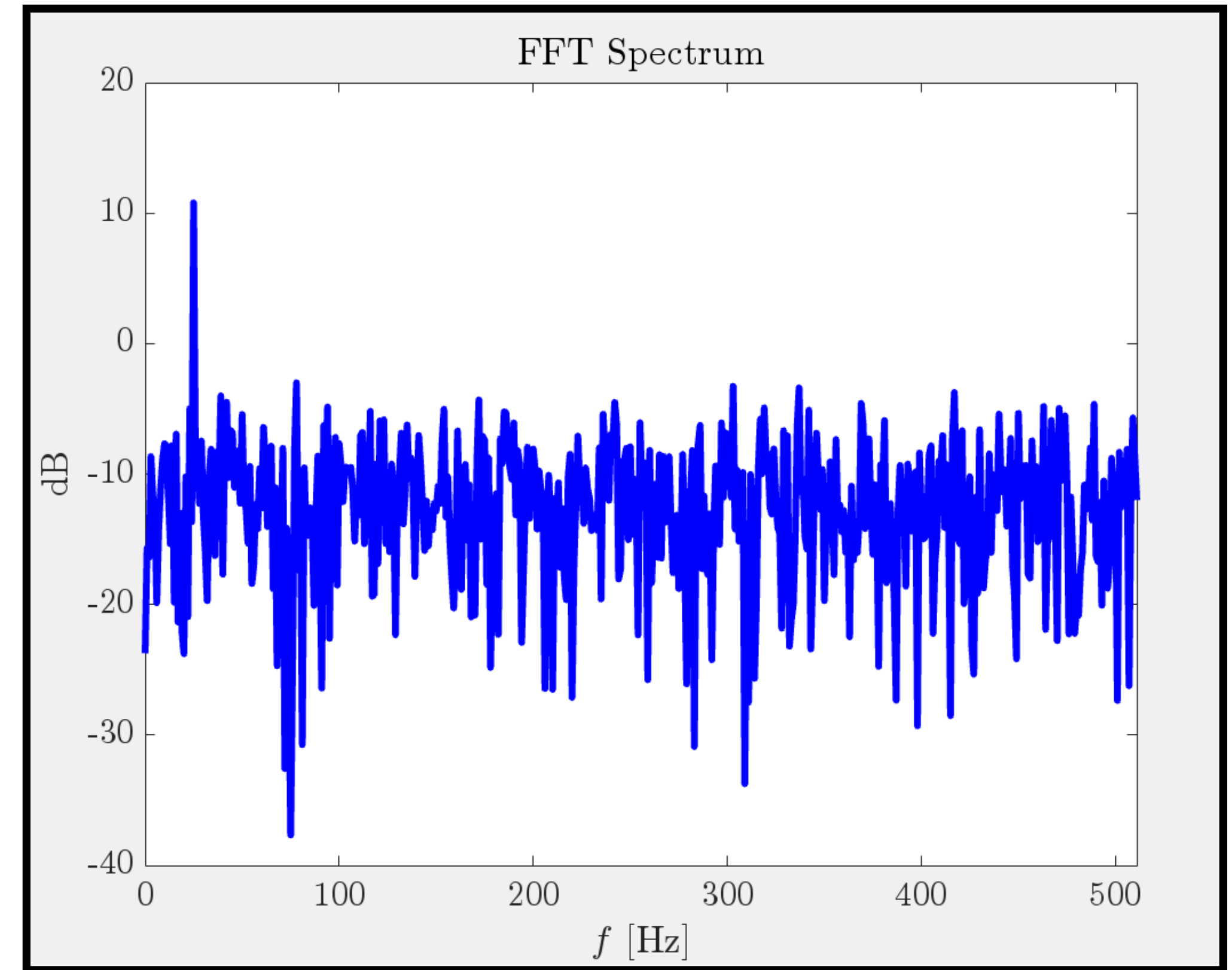
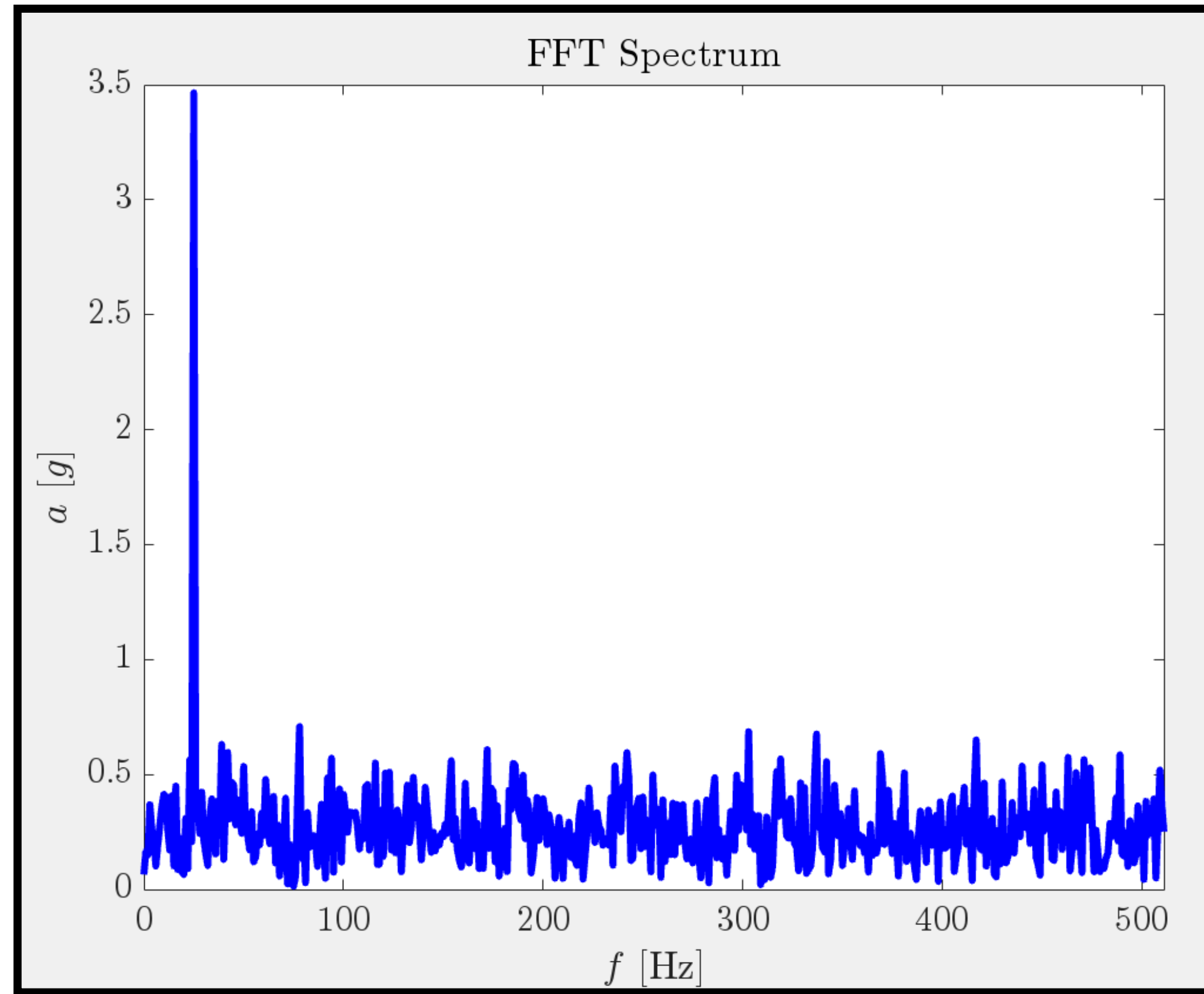
"Time resolution"	"0.00097656"
"Time record"	"29.999"
"Sampling frequency"	"1024"
"Frequency resolution"	"0.033333"
"Number of points"	"30720"

Post-Calibration results

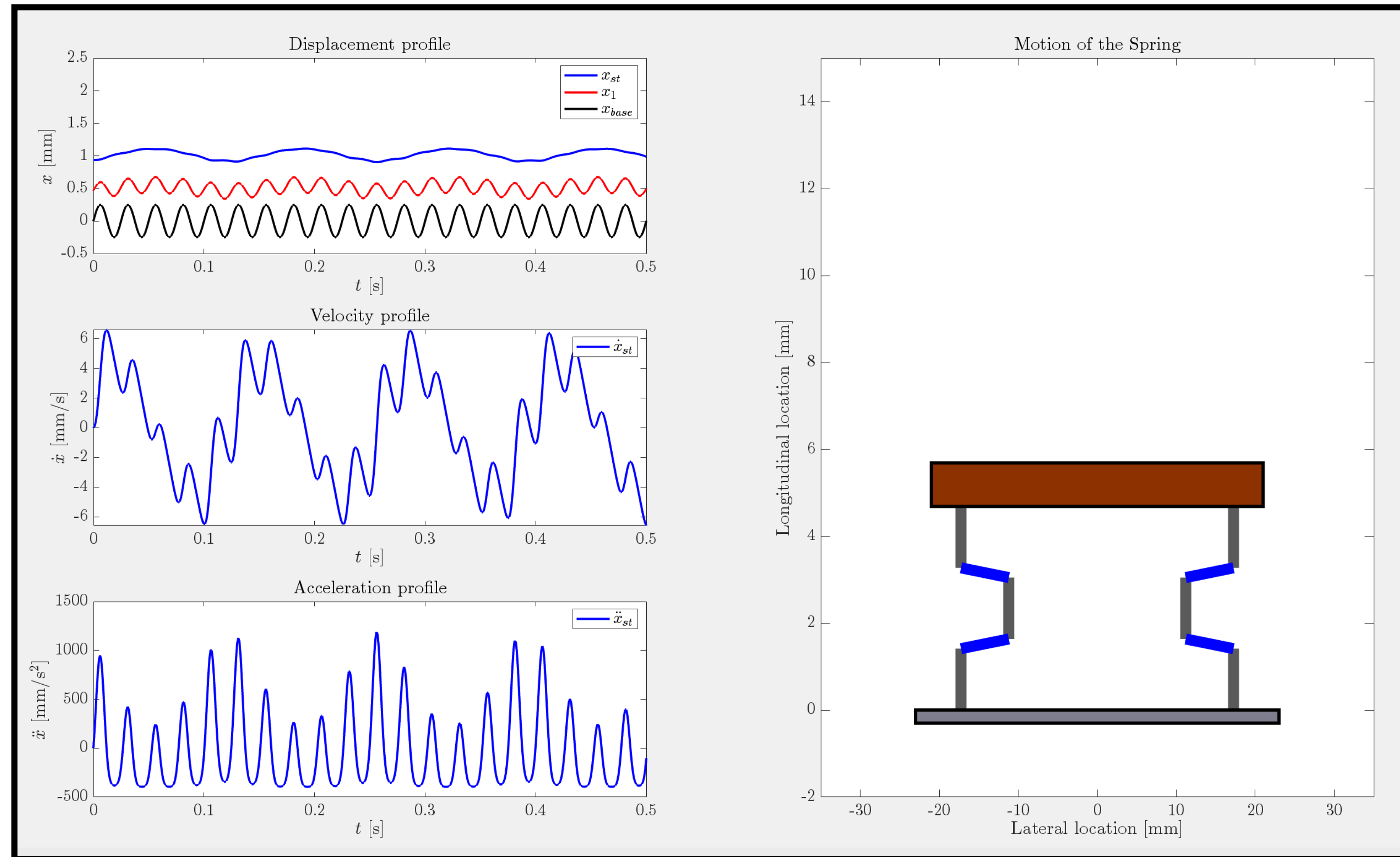


Post-Calibration results

When **NFFT = 1024**, where is the other peak ??



FFT analysis for Disc spring stack



Height/Thickness ratio

$$\frac{h_1}{\tau} = \frac{h_2}{\tau} = \sqrt{2}$$

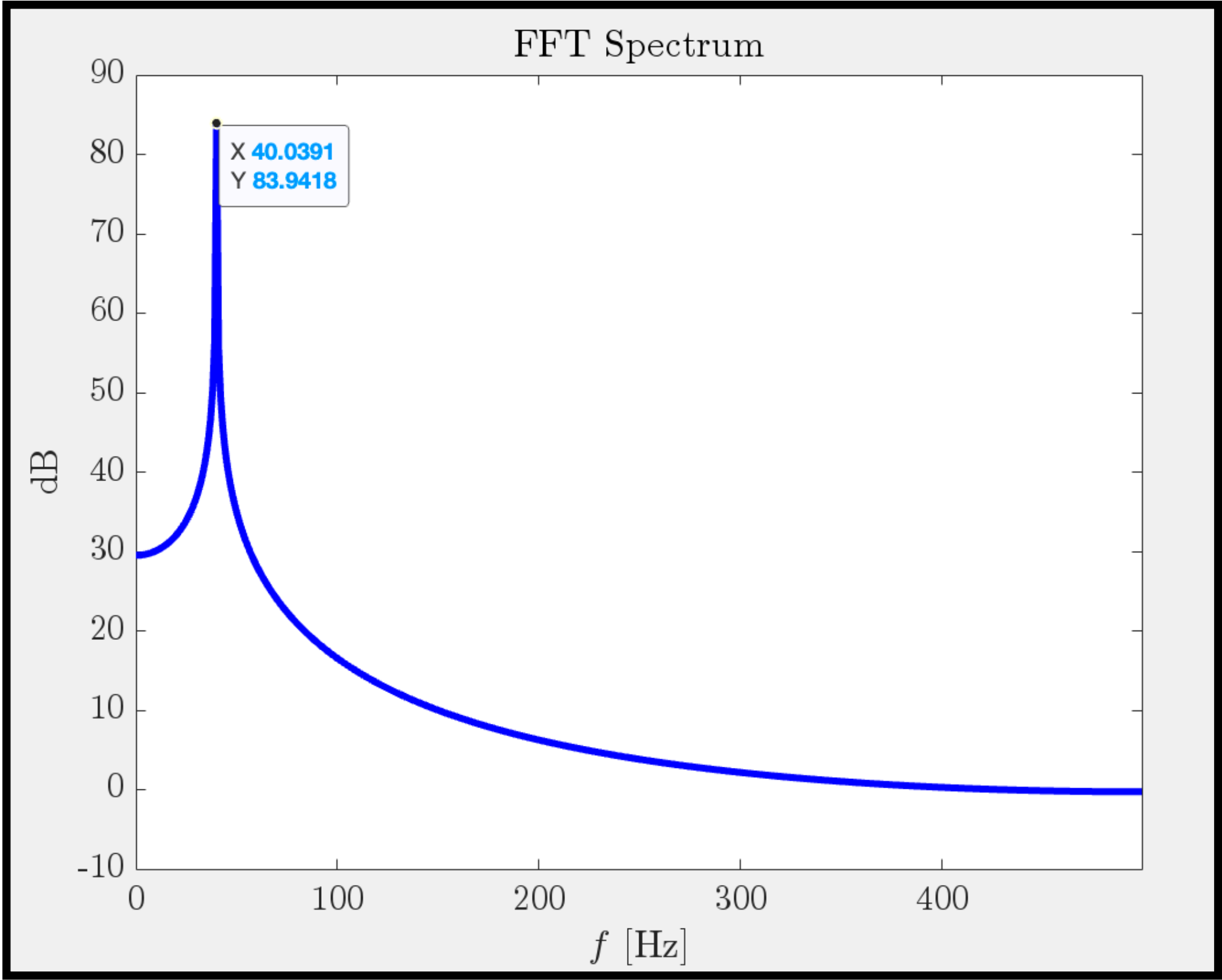
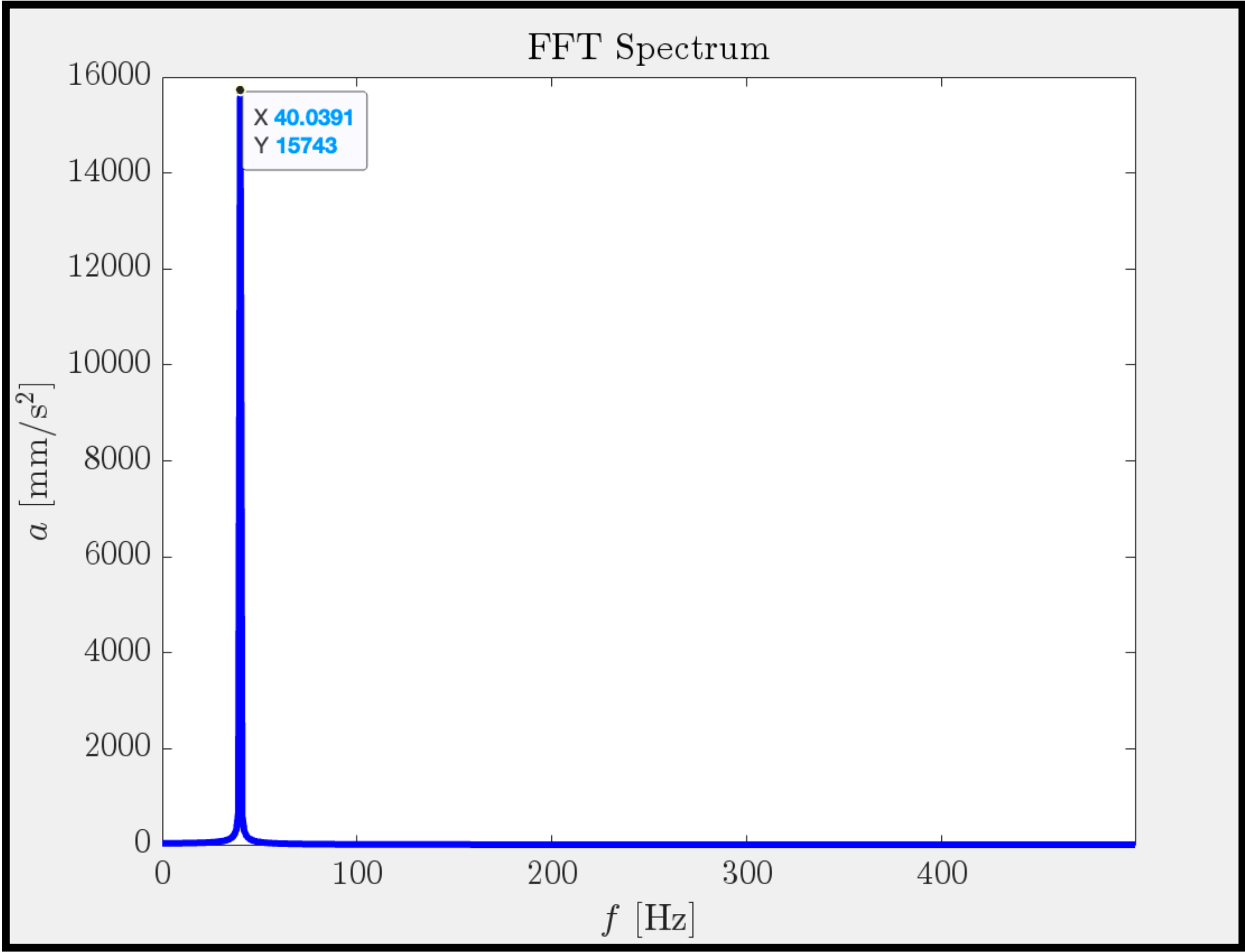
Base displacement

$$x_{base}(t) = 0.25 \sin(80\pi t)$$

5-6 cycles of input displacement for one cycle of output !

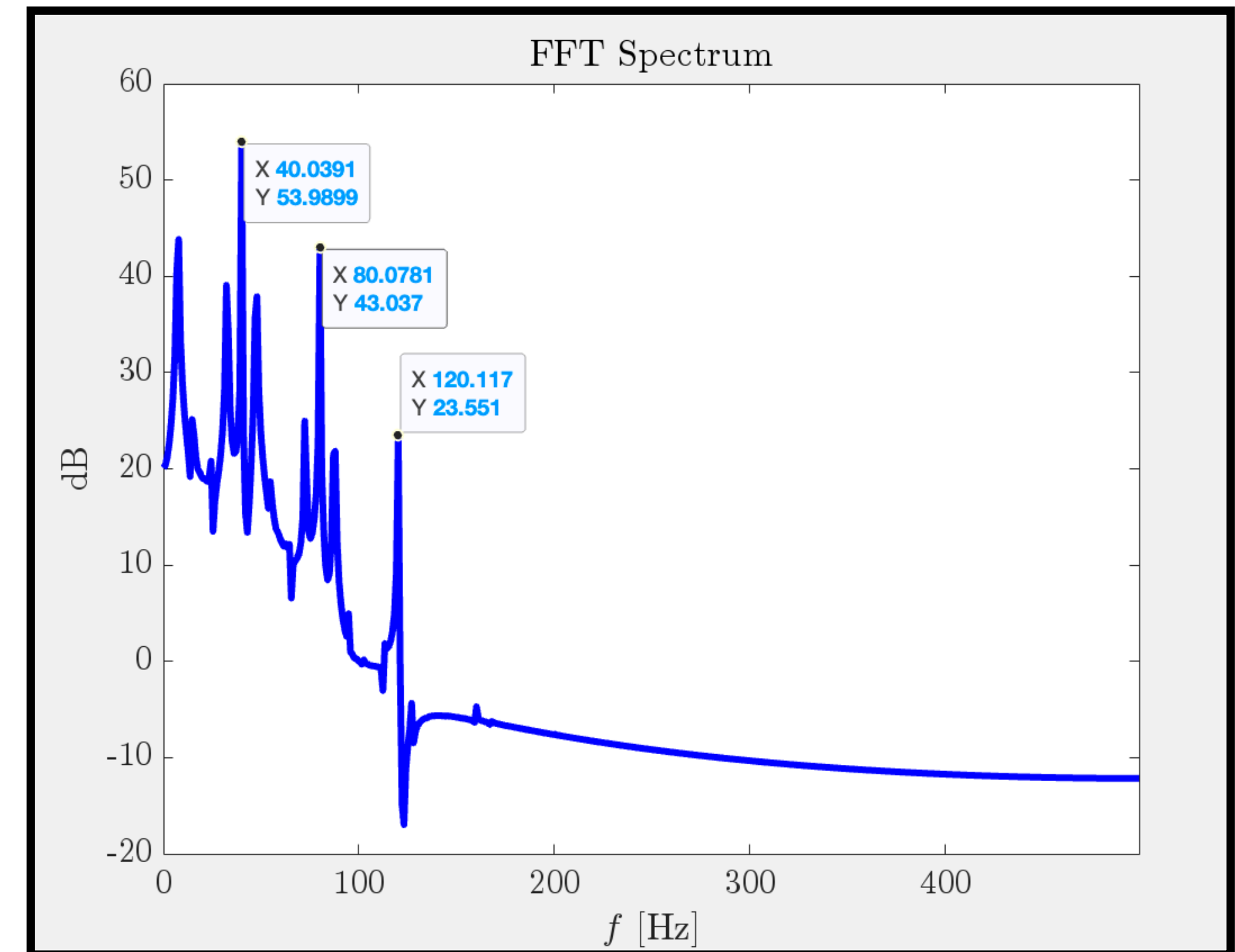
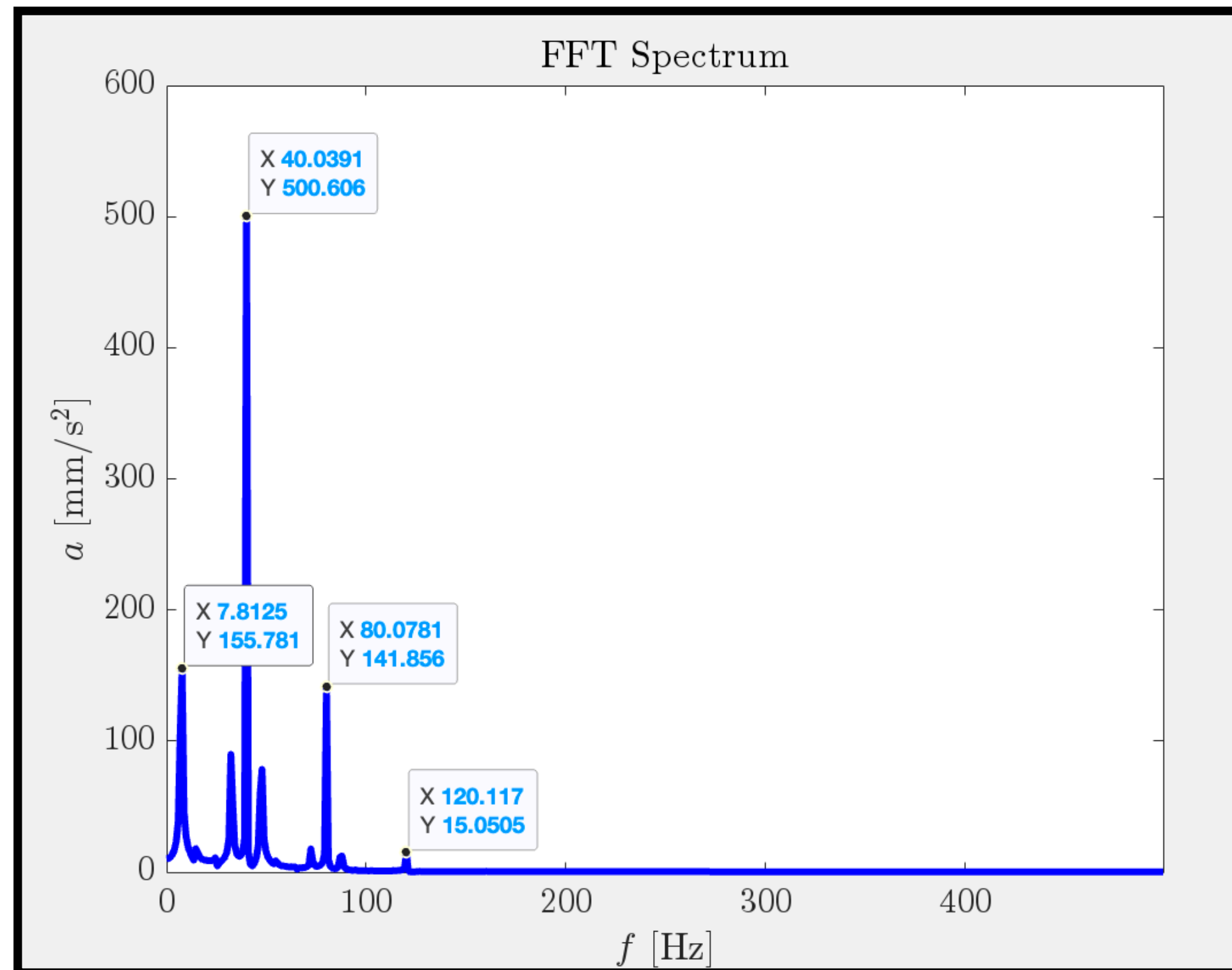
FFT analysis for Disc spring stack

FFT spectrum for input signal



FFT analysis for Disc spring stack

FFT spectrum for output signal



Spectral leakage even after windowing ! Need to investigate further

Future work

- Continue working on the “spectral leakage” problem
- Study the Dynamics of the linearized system in time and frequency domains
- Study for more combinations of h/τ ratios, especially cases with multiple solutions and are not numerically “nice”.
- Study effects of damping and hysteresis due to snap-through events and other non-linearities