

ME321 10-02-2017

Independent and dependant properties:

- Two properties are independent if one can be varied without varying the other

State postulate:

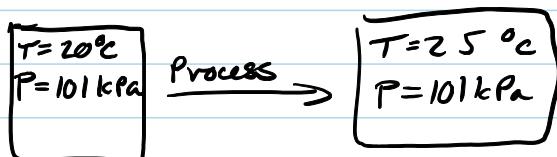
The state of a simple compressible system is completely specified by two independent intensive properties.

- State: Conditions at a system characterized by the values of its properties.

An equation of state relates a system of state properties.

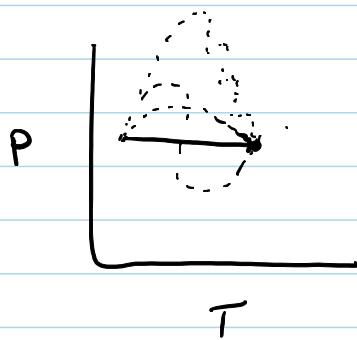
$$P = \rho RT$$

What is the state of the air in this room?



In this example the process may be heat addition.

The series of states through which a process passes is the process path.

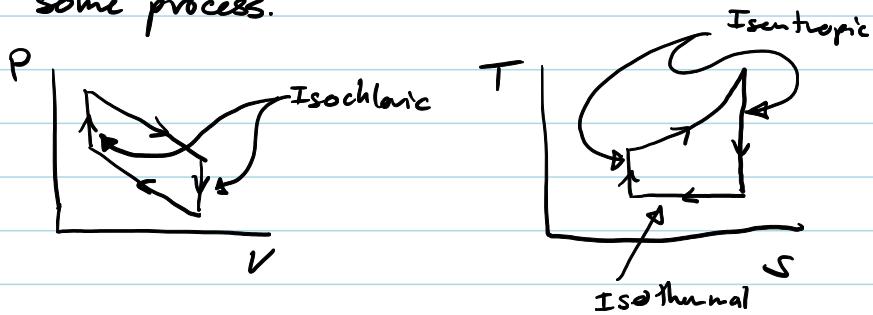


Types of processes.

ISO \rightarrow constant

isothermal	const. T
isobaric	const. P
isochoric	const. V
isentropic	const. entropy
isenthalpic	const. enthalpy

Cycles - Initial and final states are the same after some process.



Pure Substances

A homogeneous substance with invariant chemical composition which may exist in multiple phases.

Phases of pure substances

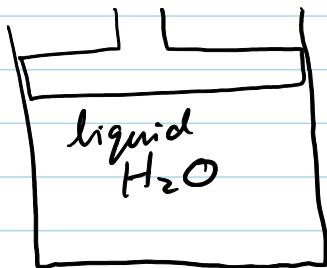
Solid: close-packed molecules oscillating about a fixed position.

Liquid: not a fixed position

Gas: large separation

State 1:

State 1

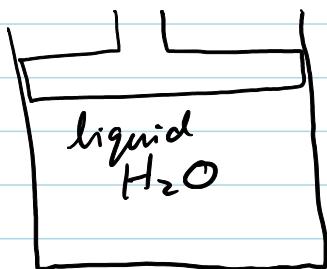


$$\begin{aligned} P &= 1 \text{ atm} \\ T &= 20^\circ\text{C} \\ V &= V_1 \end{aligned}$$

compressed liquid

Add Q until T reaches 100°C

State 2

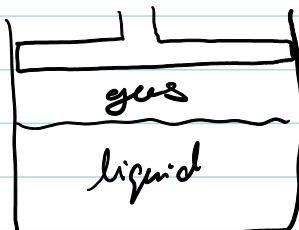


$$\begin{aligned} P &= 1 \text{ atm} \\ T &= 100^\circ\text{C} \\ V &= V_2 > V_1 \end{aligned}$$

saturated liquid
"about to vaporize"

Add $Q \rightarrow$ phase change

State 3



$$\begin{aligned} P &= 1 \text{ atm} \\ T &= 100^\circ\text{C} \\ V &= V_3 > V_2 \end{aligned}$$

saturated liquid
saturated vapor

Temp const. for pressure $P \rightarrow (T, P)$ const
 $\rightarrow (T_{\text{const.}}, P_{\text{const.}})$

@ $T = 100^\circ\text{C}$ for a saturated mixture,
you can find table A-4:

$$\begin{aligned} V_f &= 0.001043 \frac{\text{m}^3}{\text{kg}} \quad (\text{liquid}) \\ V_g &= 1.6720 \frac{\text{m}^3}{\text{kg}} \end{aligned}$$

$$\text{Note: } \rho = \frac{1}{V}$$

State 4



Add just enough Q until only vapor remains

$$\begin{aligned} P &= 1 \text{ atm} \\ T &= 100^\circ\text{C} \\ V &= V_4 > V_3 \end{aligned}$$

saturated vapor



Add more Q

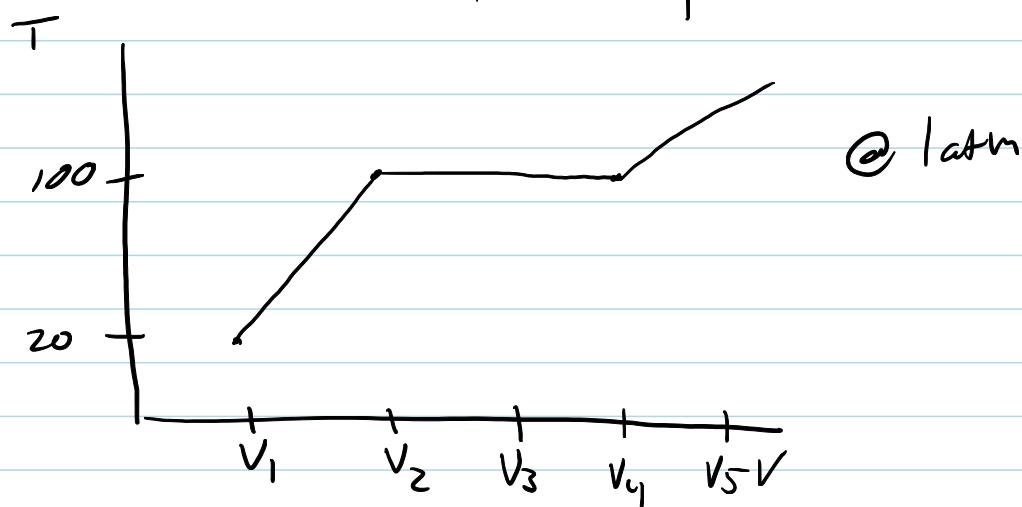
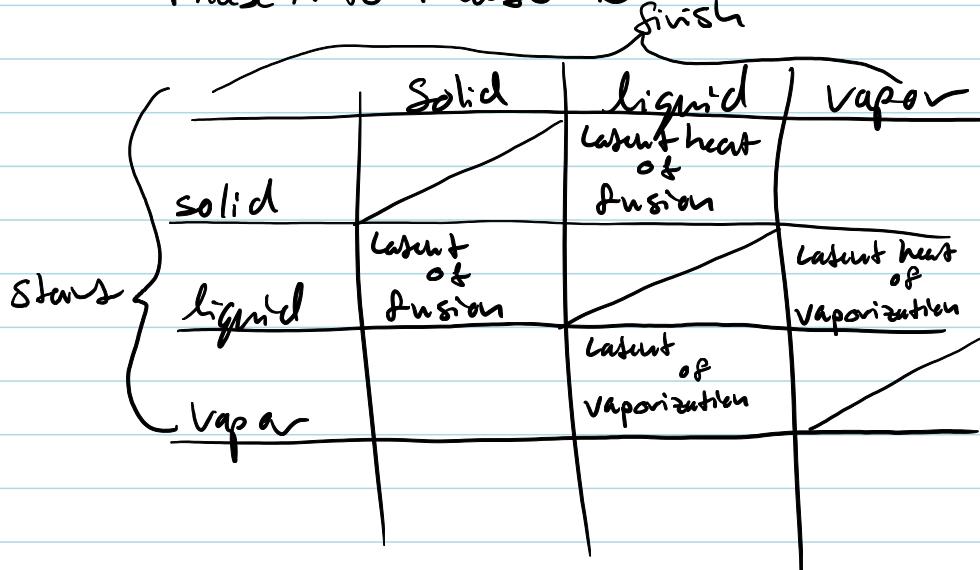
$Q \rightarrow T$

$$\begin{aligned} P &= 1 \text{ atm} \\ T &> 100^\circ\text{C} \\ V_5 &> V_4 \end{aligned}$$

super-heated vapor

State 5

Phase A to Phase B



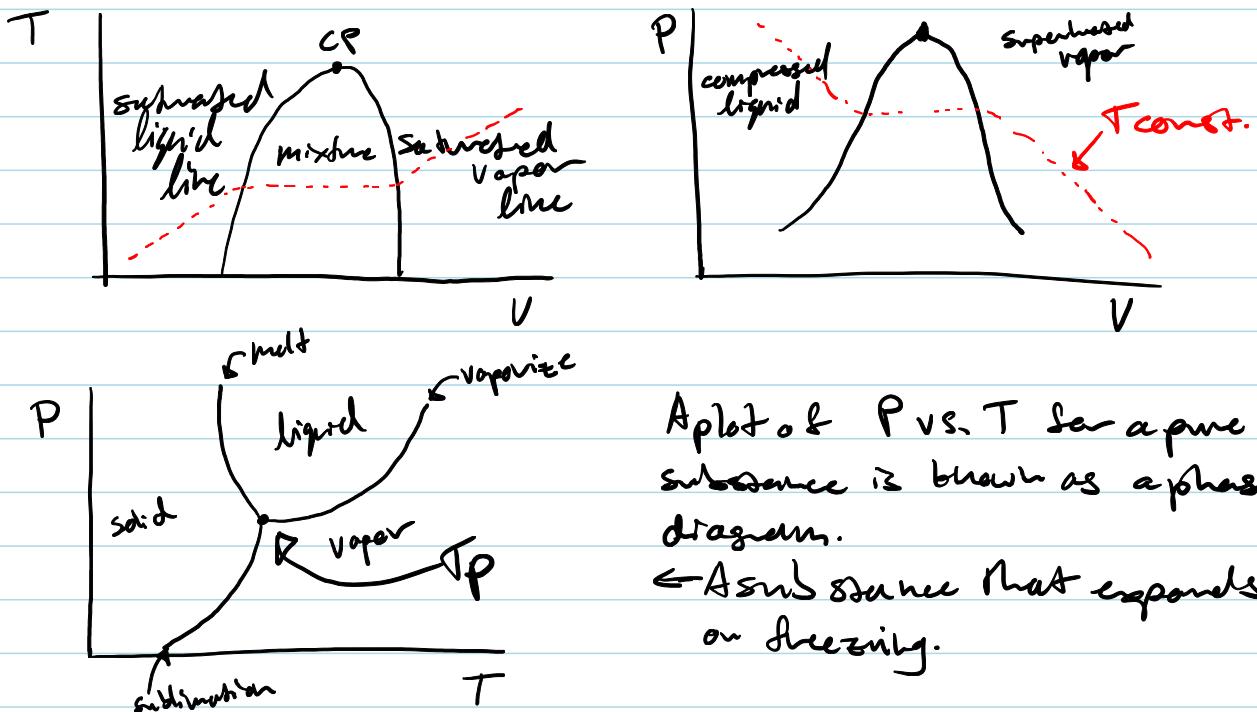
Critical Point - the point under sufficient pressure at which the energy associated with a phase change approaches zero. This pressure is called Critical

The dome defined by the end points of the saturation line is called the saturation dome.

For water, the critical point is defined by

$$P_{\text{crit}} = 22.06 \text{ MPa}, T_{\text{crit}} = 373.15^\circ\text{C}, \text{ and}$$

$$V_{\text{crit}} = 0.003106 \text{ m}^3/\text{kg}$$

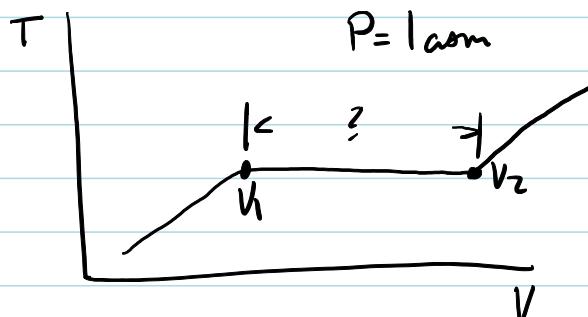


A plot of P vs. T for a pure substance is known as a phase diagram.

← A substance that expands on freezing.

Opposites

solidification → reverse sublimation or melting → freezing
vaporization → condensation



We can find out how much of each phase we have by interpolating volumes!

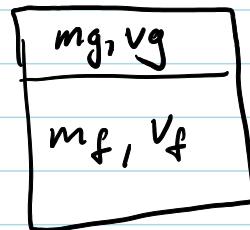
Quantity $X = \frac{\text{mass saturated vapor}}{\text{total mass}} = \frac{mg}{mg + mf}$

$\xrightarrow{\text{saturation liquid}} 0 \leq X \leq 1 \xleftarrow{\text{saturation vapor}}$

Consider the saturated mixture.

$$H = H_f + H_g$$

$$m = m_f + m_g$$



$$H_f = m_f V_f \quad H_g = m_g V_g$$

$$m V = m_f V_f + m_g V_g$$

$$H = \frac{m_f V_f + m_g V_g}{m}$$

$$H = \frac{m_f}{m} V_f + \frac{m_g}{m} V_g$$

$$x = \frac{m_g}{m_f + m_g} = \frac{m_g}{m}$$

$$\frac{m_f}{m} = \frac{(m_g + m_f) - m_g}{m} = 1 - x$$

$$V = (1 - x) V_f + x V_g$$

It follows that if we have a saturated mixture with quality x : the properties of the mixture are given by:

$$\text{prop mix} = (1 - x) \left(\begin{smallmatrix} \text{prop sat} \\ \text{liquid} \end{smallmatrix} \right) + (x) \left(\begin{smallmatrix} \text{prop sat} \\ \text{vapor} \end{smallmatrix} \right)$$

