ECE 311 Lab 3

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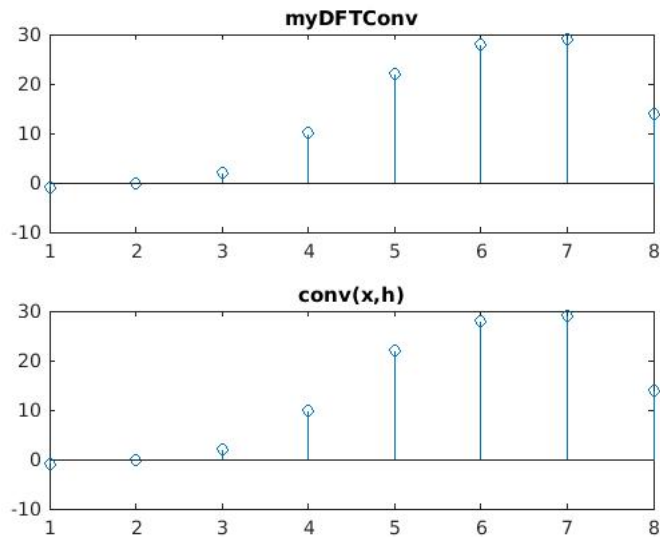
Report Item 1

```matlab
function [ y ] = myDFTConv( x, h )

%transfer over to frequency domain
l = size(x,2) + size(h,2) - 1;
x_w = fft(x,l);
h_w = fft(h,l);

%element multiplication to get y_w
y_w = x_w.*h_w;

%return to discrete domain
y = ifft(y_w);

%plot my result
figure;
subplot(211);
stem(y);
title('myDFTConv');

%plot key
subplot(212);
stem(conv(x,h));
title('conv(x,h)');

end
```

myDFTConv.m

Because of the use of fft and ifft, the time coplexity is also $O(Nlog(N))$.

Report Item 2

```matlab
function [ y_n ] = sys1( a,N )

%get delta function
x_n = zeros(1,N);
x_n(1) = 1;

%get shifted delta function
x_n_1 = zeros(1,N);
x_n_1(2) = 1;

y_n = zeros(1,N+1);

for i = 1:N,
    y_n(i+1) = a.*y_n(i) + 0.3.*x_n(i) -2.*x_n_1(i);
end
y_n = y_n(2:length(y_n)); % remove first element to get to N
figure;
stem(y_n);
title('a = 2, N = 64');
ylabel('y_n');
xlabel('N');
end
```
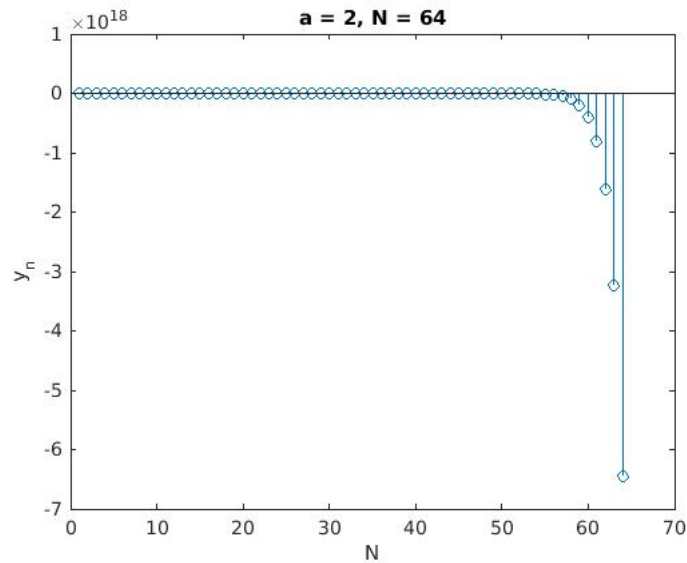
sys1.m

Notice that this function is in the order of a negative exponential, therefore, it is not stable $\lim_{N\to\infty} y_n = -\infty$. Because the system is LSI, we can also say that the sum of $|h[n]|$ over all integers N does not converge to a finite sum. The system is causal, however, by the finite difference equation, output only depends on past or current inputs.
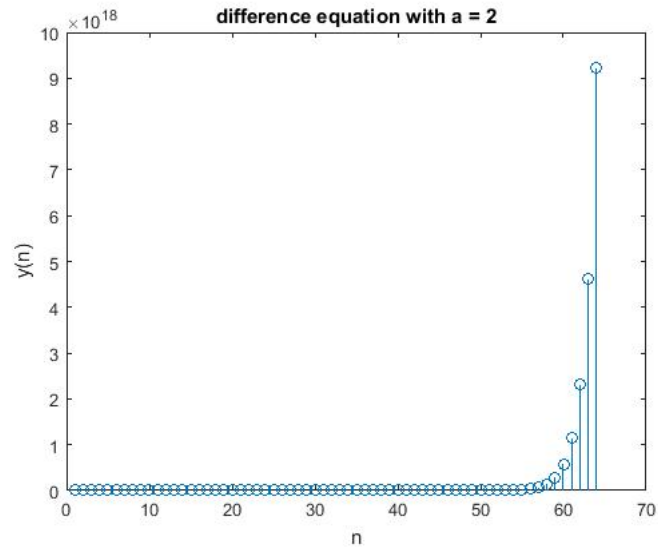
Report Item 3

```matlab
function [ y_n ] = sys2( x_n, a )
N = 64; % length always 64
y_n = zeros(1,N+1);

for i = 1:64,
    y_n(i+1) = a*y_n(i) + x_n(i).^2;
end
    y_n = y_n(2:length(y_n)); % remove first element to shorten to
    64

    figure;
    stem(y_n);
    title('difference equation with a = 2');
    xlabel('n');
    ylabel('y(n)');
end
```
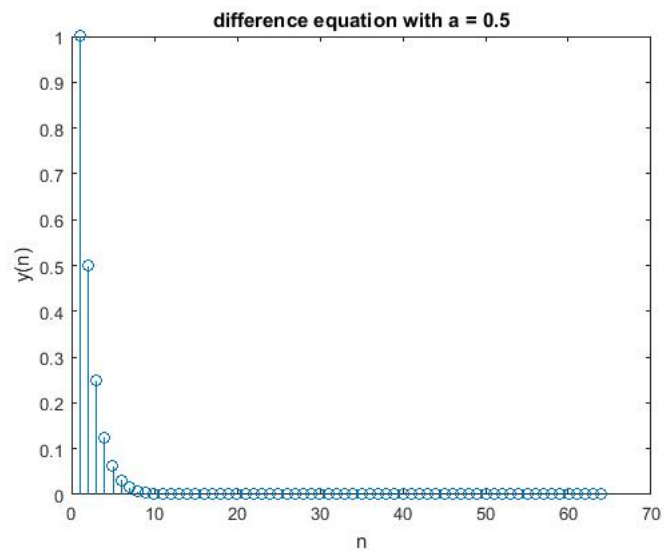
sys2.m

With $a = 2$ and $x(n) = (1, 0, 0, ...)$, or the delta function, we can see that the equation is not linear because of $x(n)^2$. The system is causal because of the fact that the finite difference equation output only depends on past or current inputs. Because the output graph is in the form of an exponential, the equation is unnstable.
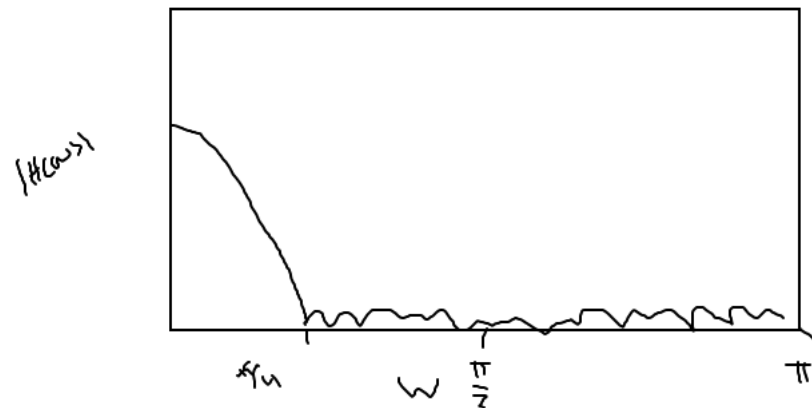
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difference equation with a = 0.5

With $a = 0.5$, the equation is not linear, causal, and is stable because $\lim_{N \to \infty} y_n = 0$.

Because the equation is not linear, the system is not LSI so you cannot use convolution to find the output to either system.
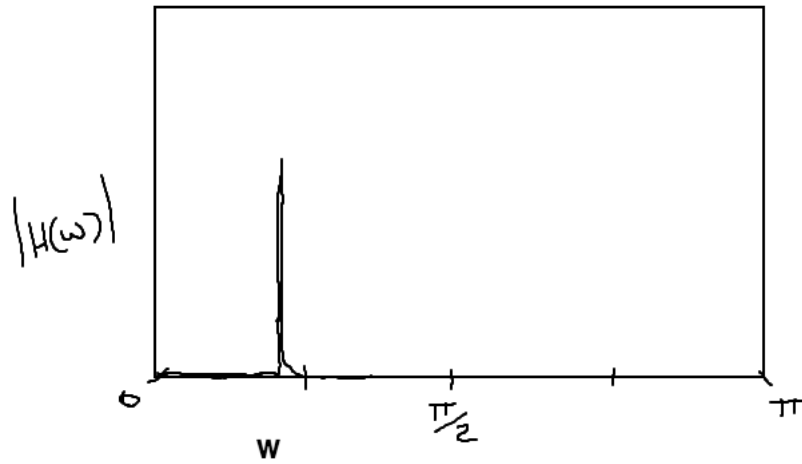
We can see on the interval from $\omega = 0$ to π, that there is only one point where the magnitude is not zero. Therefore, there is a spike at that point.

We can see on the interval from $\omega = 0$ to π that there is a minimum at $\omega = 0$ and a maximum at $\omega = \pi/4$ so the graph is decreasing until that point.
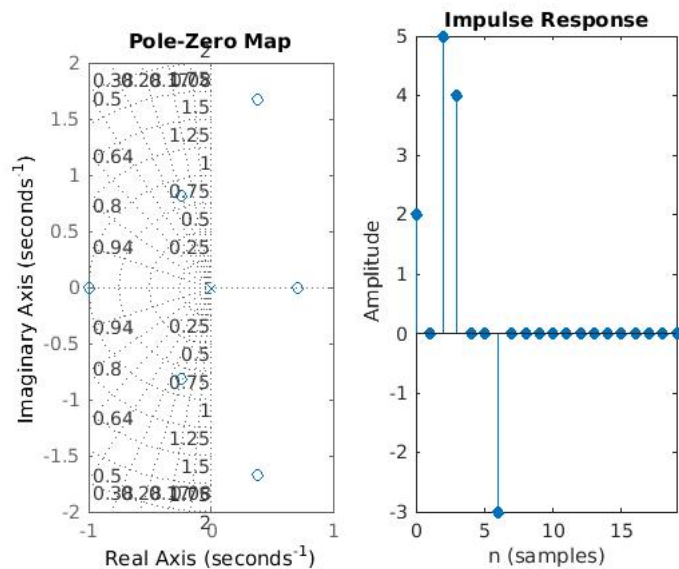
Report Item 5

```matlab
function [ ] = pzplot_impz( a,b )
S = tf(b,a);
N = 20;

figure;
subplot(121);

pzplot(S);
grid on;
subplot(122);
impz(b,a,N);

end
```
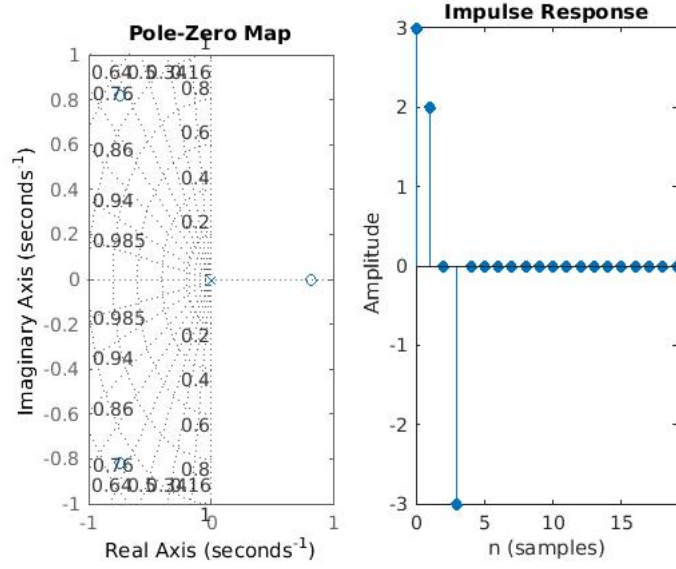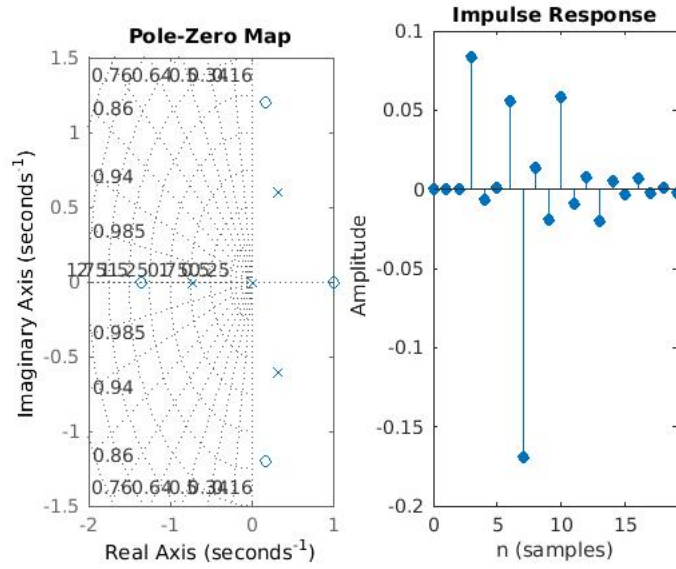
pzplot_impz.m

With $a = [1, 0, 0, 0, 0, 0, 0]$ and $b = [2, 0, 5, 4, 0, 0, -3]$ There are no poles on or outside the unit circle so the system is stable.

With $a = [1, 0, 0, 0]$ and $b = [3, 2, 0, -3]$, there are no poles on or outside the unit circle. Therefore, the system is stable.

With $a = [12, 1, 0, 4, 0, 0, 0, 0]$ and $b = [0, 0, 0, 1, 0, 0, 1, -2]$, there are no poles outside or on the unit circle. Therefore, the system is stable.
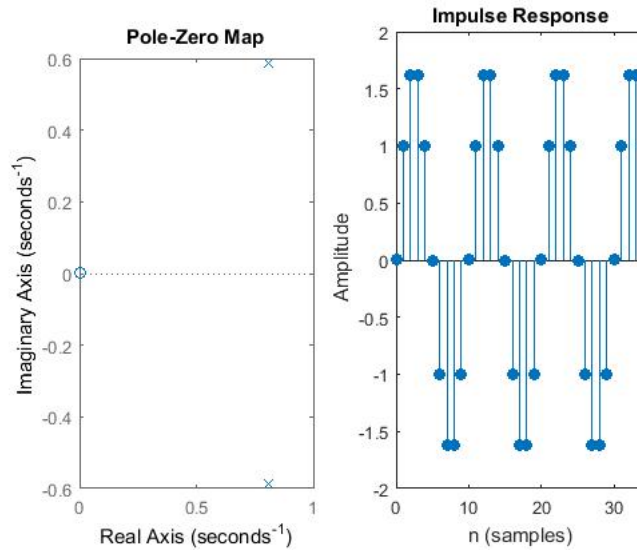
Report Item 6

$$H(z) = \frac{z}{(z+e^{\frac{-i8\pi}{10}})(z+e^{\frac{i8\pi}{10}})}$$

$$= \frac{z}{z^2 + ze^{\frac{-i8\pi}{10}} + ze^{\frac{i8\pi}{10}} + 1}$$

$$= \frac{z}{z^2 + 2z\cos(4\pi/5) + 1}$$

$$= \frac{z^{-1}}{1 + z^{-1}2\cos(4\pi/5) + z^{-2}}$$

$$a = [1, 2\cos(4\pi/5), 1] \quad b = [0, 1, 0] \quad N = 35$$

```
function [ ] = pzplot_impz2( a,b )
S = tf(b,a);
N = 35;

figure;
subplot(121);
pzplot(S);
subplot(122);
impz(b,a,N);

end
```

pzplot_impz2.m

The system is not BIBO stable, we have two poles on the unit circle. The system is stable when $x[n]$ does not have poles that overlap with our poles from $h[n]$. The sysem is unstable when $|z| = -e^{\frac{\pm i8\pi}{10}}$ or whenever $x[n]$ has poles that overlap with the poles from $h[n]$.

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