

ECE 311 Lab 3

Jacob Hutter

March 6, 2017

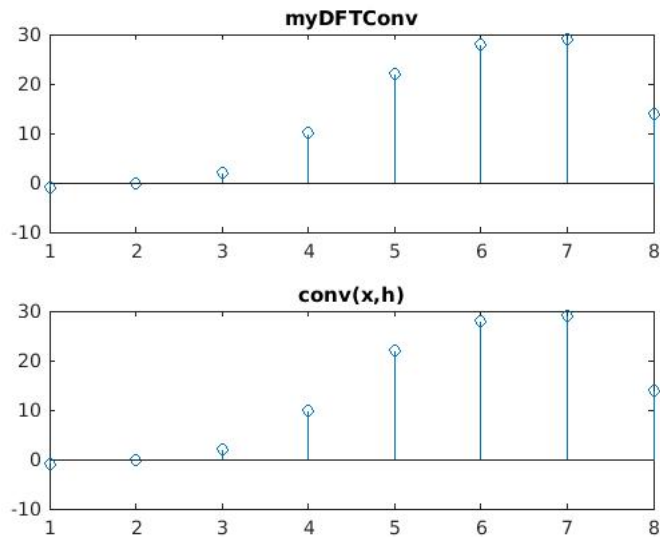
Report Item 1

```

1 function [ y ] = myDFTConv( x, h )
3 %transfer over to frequency domain
  l = size(x,2) + size(h,2) - 1;
5 x_w = fft(x,l);
  h_w = fft(h,l);
7
9 %element multiplication to get y_w
  y_w = x_w.*h_w;
11
13 %return to discrete domain
  y = ifft(y_w);
15
17 %plot my result
  figure;
  subplot(211);
  stem(y);
  title('myDFTConv');
19
21 %plot key
  subplot(212);
  stem(conv(x,h));
  title('conv(x,h)');
23
25 end

```

myDFTConv.m



Because of the use of fft and ifft, the time complexity is also $O(N \log(N))$.

Report Item 2

```

1 function [ y_n ] = sys1( a,N )
3 %get delta function
  x_n = zeros(1,N);
5 x_n(1) = 1;

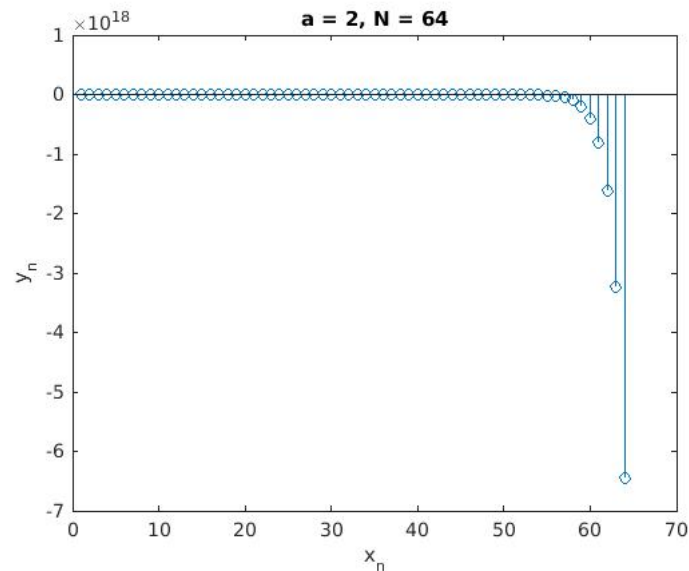
7 %get shifted delta function
  x_n_1 = zeros(1,N);
9 x_n_1(2) = 1;

11 y_n = zeros(1,N+1);

13 for i = 1:N,
    y_n(i+1) = a.*y_n(i) + 0.3.*x_n(i) -2.*x_n_1(i);
15 end
  y_n = y_n(2:length(y_n)); % remove first element to get to N
17 figure;
  stem(y_n);
19 title('a = 2, N = 64');
  ylabel('y_n');
21 xlabel('x_n');
  end

```

sys1.m



Notice that this function is in the order of $-e^x$ therefore, it is not stable $\lim_{x_n \rightarrow \infty} y_n = -\infty$. The system is causal, however, by the finite difference equation, output only depends on past or current inputs.

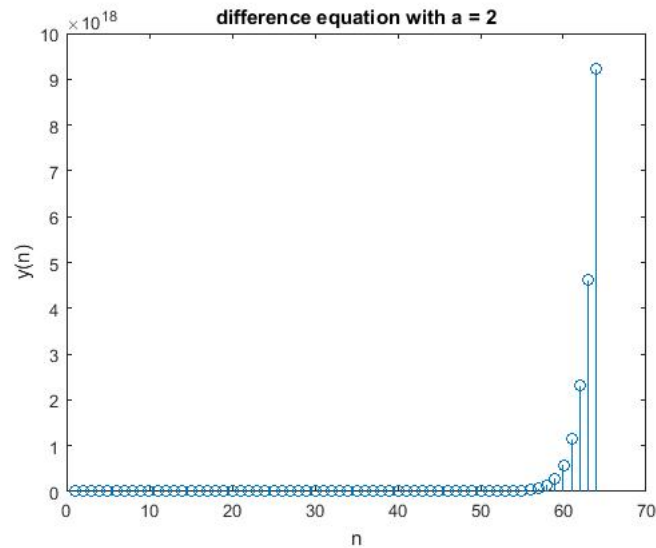
Report Item 3

```

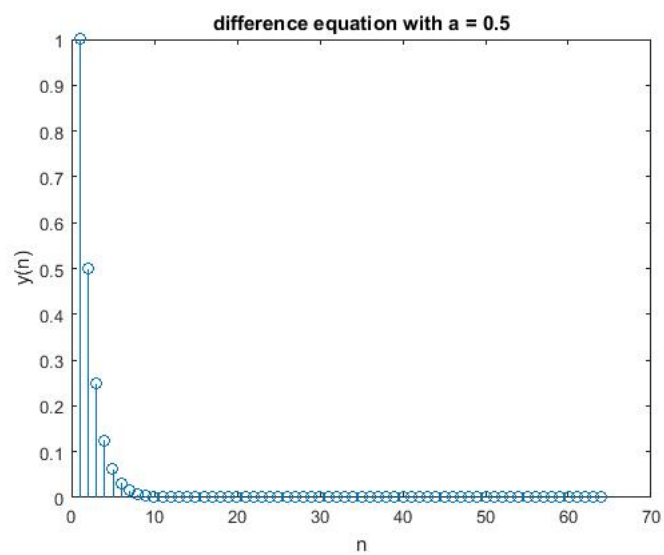
1 function [ y_n ] = sys2( x_n, a )
2 N = 64; % length always 64
3 y_n = zeros(1,N+1);
4
5 for i = 1:64,
6     y_n(i+1) = a*y_n(i) + x_n(i).^2;
7 end
8     y_n = y_n(2:length(y_n)); % remove first element to shorten to
9     64
10
11     figure;
12     stem(y_n);
13     title('difference equation with a = 2');
14     xlabel('n');
15     ylabel('y(n)');
16 end

```

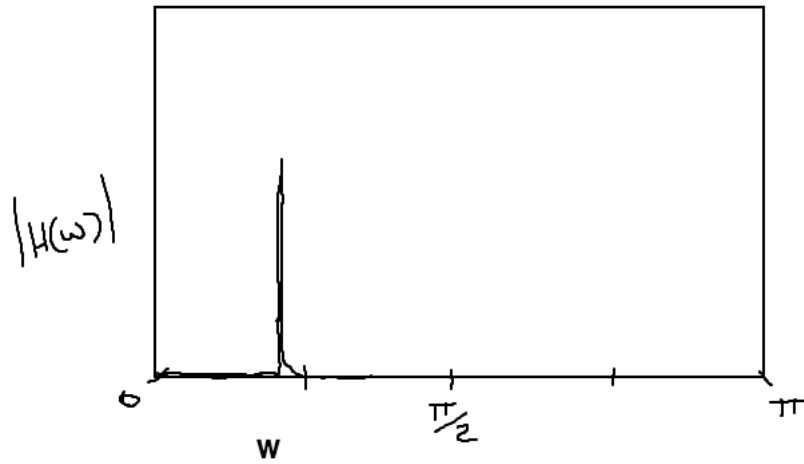
sys2.m



With $a = 2$ and $x(n) = (1, 0, 0, \dots)$, or the delta function, we can see that the equation is not linear because of $x(n)^2$. The system is causal because of the fact that the finite difference equation output only depends on past or current inputs. Because the output graph is in the form of e^x , the equation is unstable.

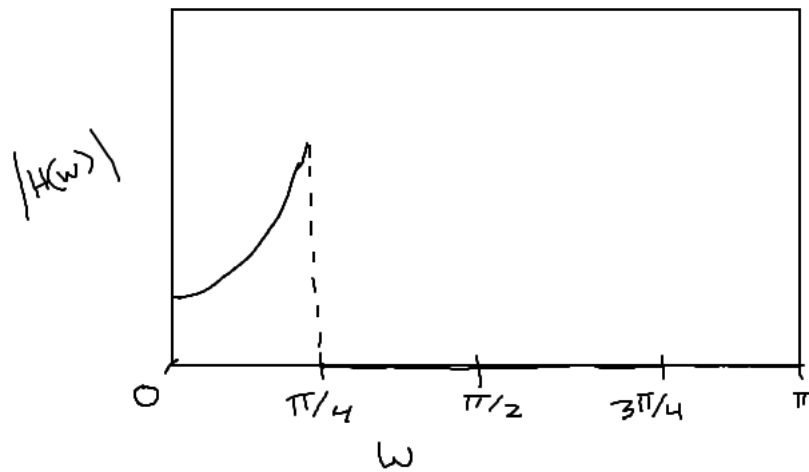


With $a = 0.5$, the equation is not linear, causal, and is stable because $\lim_{n \rightarrow \infty} y_n = 0$.
 (can you find the output to either system by convolving $x(n)$ with $h(n)$?)



Report Item 4

We can see on the interval from $\omega = 0$ to π , that there is only one point where the magnitude is not zero. Therefore, there is a spike at that point.



We can see on the interval from $\omega = 0$ to π that there is a minimum at $\omega = 0$ and a maximum at $\omega = \pi/4$ so the graph is increasing until that point.

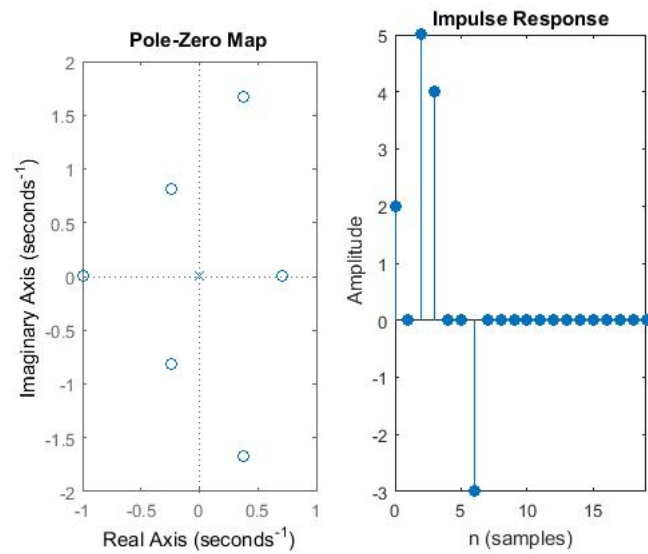
Report Item 5

```

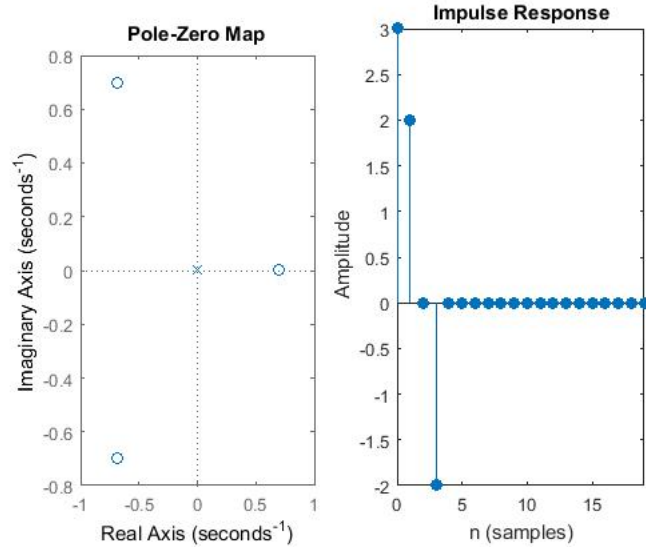
function [ ] = pzplot_impz( a,b )
2 S = tf(b,a);
  N = 20;
4
  figure;
6 subplot(121);
  pzplot(S);
8 subplot(122);
  impz(b,a,N);
10 end

```

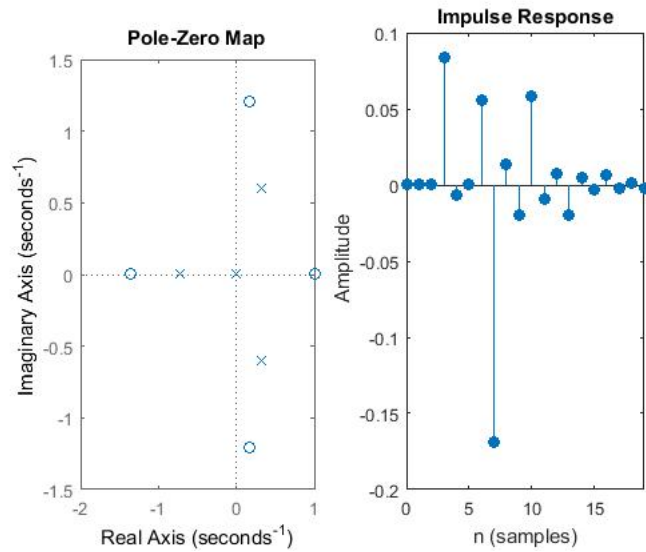
pzplot_impz.m



With $a = [1, 0, 0, 0, 0, 0, 0]$ and $b = [2, 0, 5, 4, 0, 0, -3]$ There are no poles on the unit circle so the system is stable.



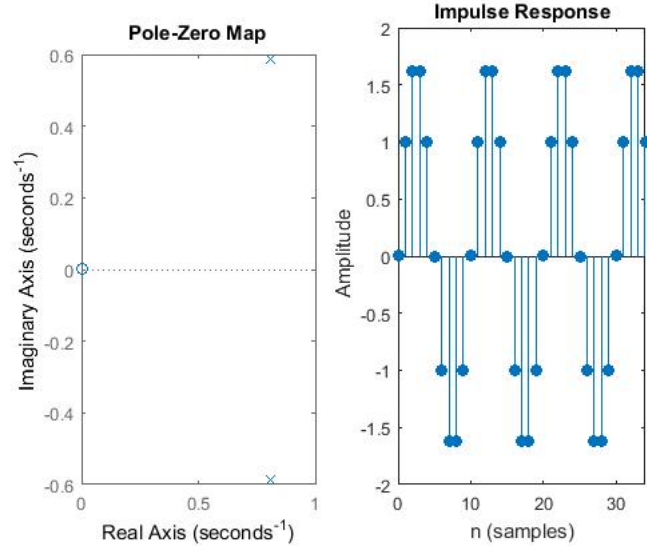
With $a = [1, 0, 0, 0]$ and $b = [3, 2, 0, -3]$, there are no poles outside the unit circle. Therefore, the system is stable.



With $a = [12, 1, 0, 4, 0, 0, 0, 0]$ and $b = [0, 0, 0, 1, 0, 0, 1, -2]$, there are no poles outside the unit circle. Therefore, the system is stable.

Report Item 6

$$\begin{aligned}
 H(z) &= \frac{z}{(z+e^{-\frac{i8\pi}{10}})(z+e^{\frac{i8\pi}{10}})} \\
 &= \frac{z}{z^2+ze^{-\frac{i8\pi}{10}}+ze^{\frac{i8\pi}{10}}+1} \\
 &= \frac{z}{z^2+2z\cos(4\pi/5)+1} \\
 &= \frac{z^{-1}}{1+z^{-1}2\cos(4\pi/5)+z^{-2}}
 \end{aligned}$$



$$a = [1, 2\cos(4\pi/5), 1], b = [0, 1, 0]$$

The system is not BIBO stable, if we have a bounded input $z = -e^{\frac{+i8\pi}{10}}$ then the output approaches infinity so the system is not BIBO stable. The system is stable when $|z| > e^{\frac{i8\pi}{10}}$ and unstable when $|z| \leq e^{\frac{i8\pi}{10}}$.