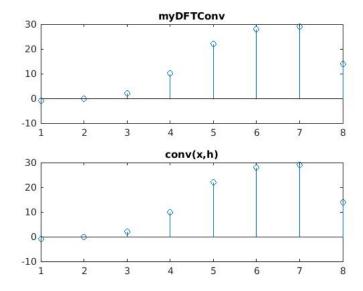
# ECE 311 Lab 3

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```
function [ y ] = myDFTConv(x, h)
3 %transfer over to frequency domain
  l = size(x,2) + size(h,2) - 1;
  x_w = fft(x, 1);
  h_-w = fft(h,l);
  \% element \ multiplication \ to \ get \ y\_w
y_{w} = x_{w} \cdot * h_{w};
11 %return to discrete domain
  y = ifft(y_w);
13
  %plot my result
15 figure;
  subplot (211);
17 stem(y);
   title('myDFTConv');
  %plot key
21
  subplot (212);
  stem(conv(x,h));
23 title ('conv(x,h)');
25
  \quad \text{end} \quad
```

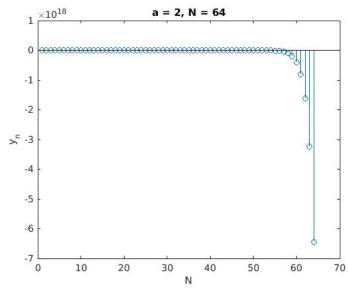
 ${\rm myDFTConv.m}$ 



Because of the use of fft and ifft, the time coplexity is also O(Nlog(N)).

```
function [y_n] = sys1(a,N)
  %get delta function
  x_n = zeros(1,N);
_{5}|_{x_{n}(1)} = 1;
  %get shifted delta function
  x_n_1 = zeros(1,N);
9 | x_n_1(2) = 1;
y_n = zeros(1,N+1);
  for i = 1:N,
      y_n(i+1) = a.*y_n(i) + 0.3.*x_n(i) -2.*x_n_1(i);
  y_n = y_n(2:length(y_n)); % remove first element to get to N
17 figure;
  stem(y_n);
title ('a = 2, N = 64');
ylabel('y_n');
21 xlabel('N');
  end
```

sys1.m



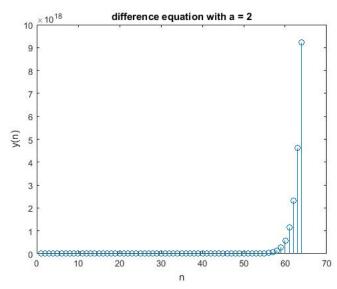
Notice that this function is in the order of a negative exponential, therefore, it is not stable  $\lim_{N\to\infty}y_n=-\infty$ . The system is causal, however, by the finite difference equation, output only depends on past or current inputs.

```
function [ y-n ] = sys2( x-n, a )
N = 64; % length always 64
y_n = zeros(1,N+1);

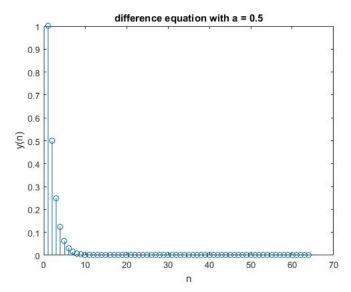
for i = 1:64,
    y_n(i+1) = a*y_n(i) + x_n(i).^2;
end
    y_n = y_n(2:length(y_n)); % remove first element to shorten to
64

figure;
stem(y_n);
title('difference equation with a = 2');
xlabel('n');
ylabel('y(n)');
end
```

sys2.m

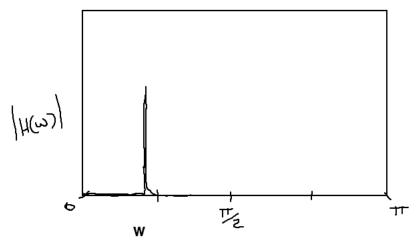


With a=2 and x(n)=(1,0,0,...), or the delta function, we can see that the equation is not linear because of  $x(n)^2$ . The system is causal because of the fact that the finite difference equation output only depends on past or current inputs. Because the output graph is in the form of an exponential, the equation is unnstable.



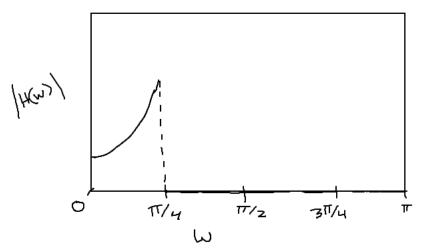
With a=0.5, the equation is not linear, causal, and is stable because  $\lim_{N\to\infty}y_n=0.$ 

Because the equation is not linear, the system is not LSI so you cannot use convolution to find the output to either system.



Report Item 4

We can see on the interval from  $\omega = 0$  to  $\pi$ , that there is only one point where the magnitude is not zero. Therefore, there is a spike at that point.



We can see on the interval from  $\omega=0$  to  $\pi$  that there is a minimum at  $\omega=0$  and a maximum at  $\omega=\pi/4$  so the graph is increasing until that point.

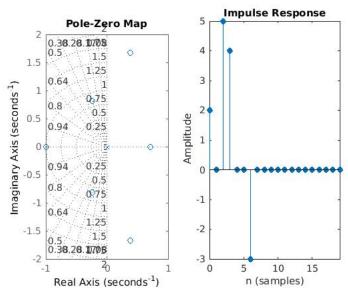
```
function [ ] = pzplot_impz( a,b )
S = tf(b,a);
N = 20;

figure;
subplot(121);

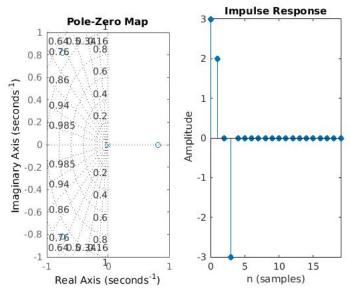
pzplot(S);
grid on;
subplot(122);
impz(b,a,N);

end
```

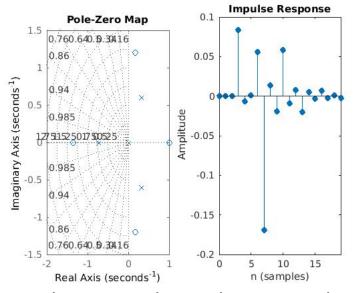
 $pzplot\_impz.m$ 



With a = [1, 0, 0, 0, 0, 0, 0] and b = [2, 0, 5, 4, 0, 0, -3] There are no poles on or outside the unit circle so the system is stable.

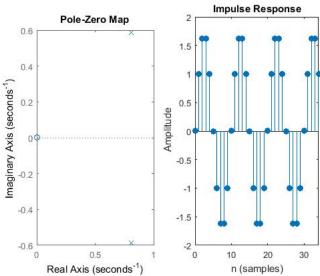


With a = [1,0,0,0] and b = [3,2,0,-3], there are no poles on or outside the unit circle. Therefore, the system is stable.



With a = [12, 1, 0, 4, 0, 0, 0, 0] and b = [0, 0, 0, 1, 0, 0, 1, -2], there are no poles outside or on the unit circle. Therefore, the system is stable.

$$\begin{array}{l} \text{Report Item 6} \\ H(z) = \frac{z}{(z + e^{\frac{-i8\pi}{10}})(z + e^{\frac{i8\pi}{10}})} \\ = \frac{z}{z^2 + ze^{\frac{-i8\pi}{10}} + ze^{\frac{i8\pi}{10}} + 1} \\ = \frac{z}{z^2 + 2zcos(4\pi/5) + 1} \\ = \frac{z^{-1}}{1 + z^{-1}2cos(4\pi/5) + z^{-2}} \end{array}$$



 $a=[1,2cos(4\pi/5),1],b=[0,1,0]$  Real Axis (seconds-1) n (so The system is not BIBO stable, we have two poles on the unit circle. The system is stable when  $|z|>e^{\frac{i8\pi}{10}}$  and unstable when  $|z|=2cos(4\pi/5),\,2sin(4\pi/5),\,e^{\frac{\pm i8\pi}{10}}$  etc.