ECE 311 Lab 3

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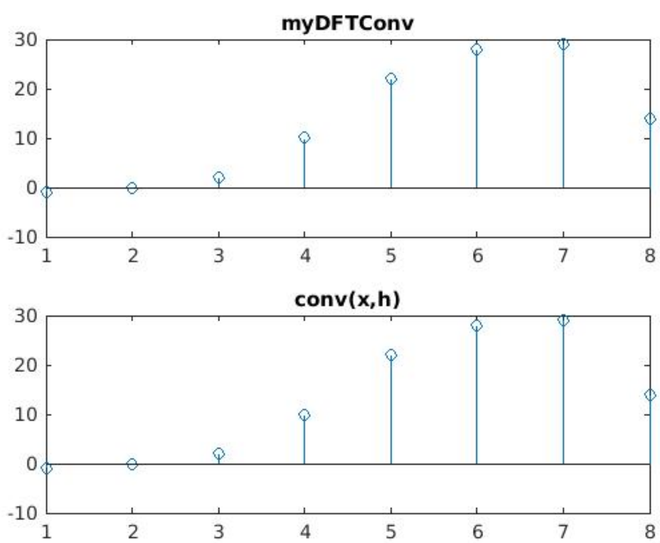
Report Item 1

```
function [ y ] = myDFTConv( x, h )

%transfer over to frequency domain
l = size(x,2) + size(h,2) - 1;
x_w = fft(x,l);
h_w = fft(h,l);

%element multiplication to get y_w
y_w = x_w.*h_w;

%return to discrete domain
y = ifft(y_w);

%plot my result
figure;
subplot(211);
stem(y);
title('myDFTConv');

%plot key
subplot(212);
stem(conv(x,h));
title('conv(x,h)');


end
```

myDFTConv.m

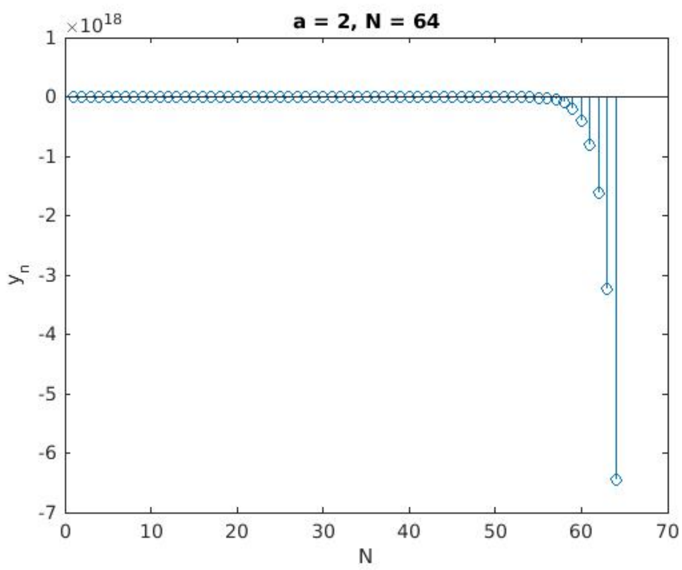


Because of the use of fft and ifft, the time coplexity is also $O(Nlog(N))$.

Report Item 2

```
function [ y_n ] = sys1( a,N )

%get delta function
x_n = zeros(1,N);
x_n(1) = 1;

%get shifted delta function
x_n_1 = zeros(1,N);
x_n_1(2) = 1;

y_n = zeros(1,N+1);

for i = 1:N,
    y_n(i+1) = a.*y_n(i) + 0.3.*x_n(i) -2.*x_n_1(i);
end
y_n = y_n(2:length(y_n)); % remove first element to get to N
figure;
stem(y_n);
title('a = 2, N = 64');
ylabel('y_n');
xlabel('N');
end
```

sys1.m

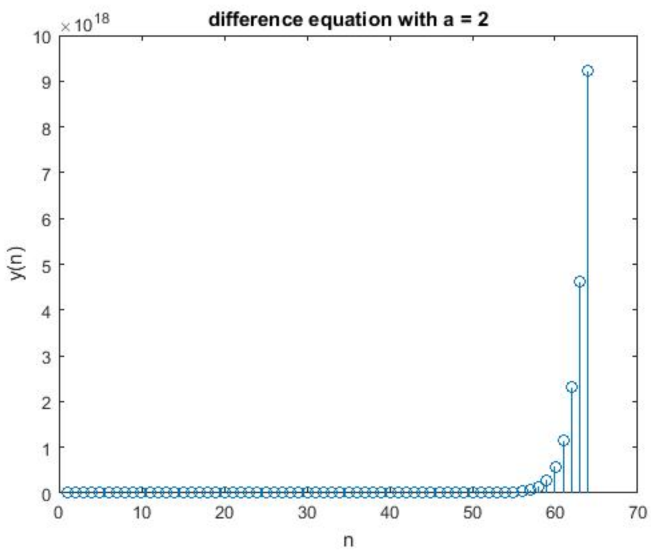


Notice that this function is in the order of a negative exponential, therefore, it is not stable $\lim_{N\to\infty} y_n = -\infty$. The system is causal, however, by the finite difference equation, output only depends on past or current inputs.

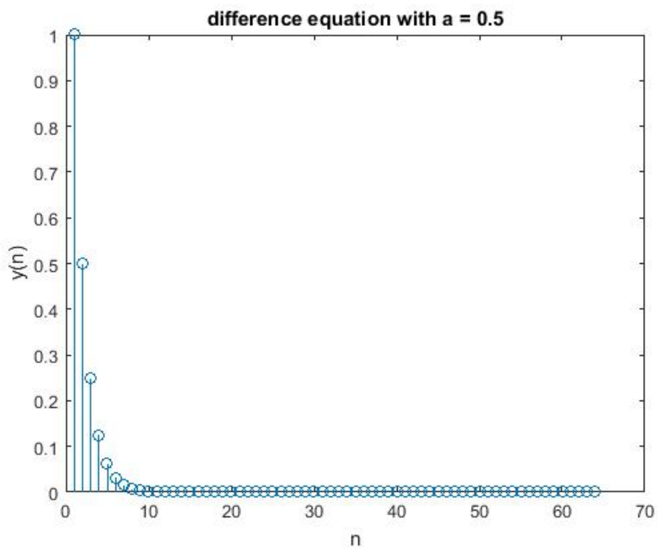
Report Item 3

```
function [ y_n ] = sys2( x_n, a )
N = 64; % length always 64
y_n = zeros(1,N+1);

for i = 1:64,
    y_n(i+1) = a*y_n(i) + x_n(i).^2;
end
    y_n = y_n(2:length(y_n)); % remove first element to shorten to 64

    figure;
    stem(y_n);
    title('difference equation with a = 2');
    xlabel('n');
    ylabel('y(n)');
end
```

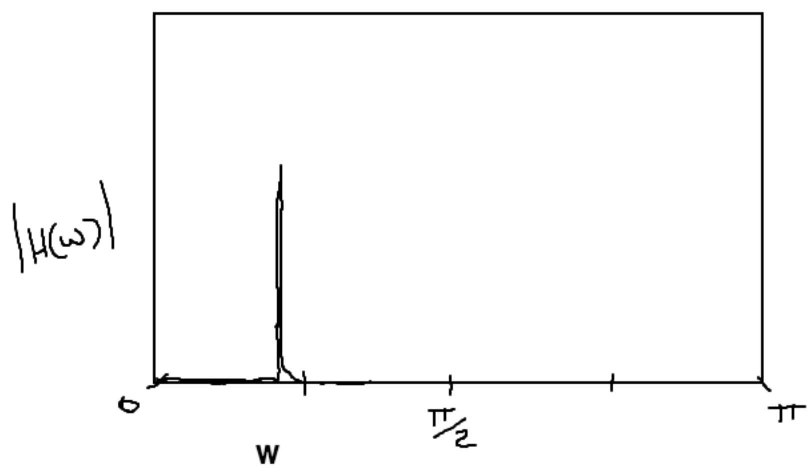
sys2.m



With $a = 2$ and $x(n) = (1, 0, 0, ...)$, or the delta function, we can see that the equation is not linear because of $x(n)^2$. The system is causal because of the fact that the finite difference equation output only depends on past or current inputs. Because the output graph is in the form of an exponential, the equation is unstable.

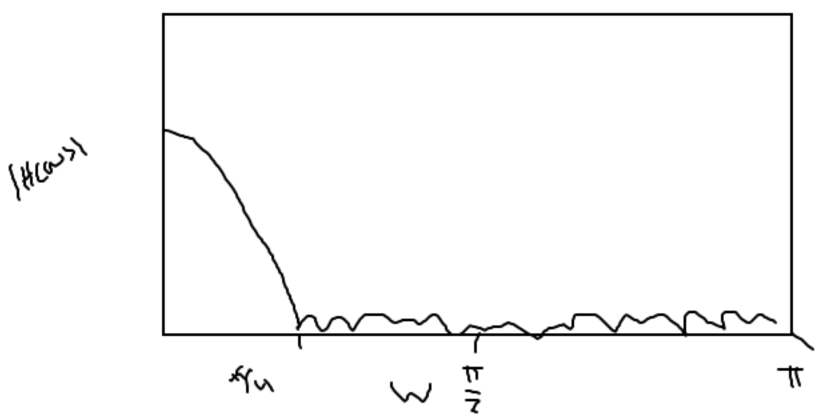


With $a = 0.5$, the equation is not linear, causal, and is stable because $\lim_{N\to\infty} y_n = 0$.
Because the equation is not linear, the system is not LSI so you cannot use convolution to find the output to either system.



Report Item 4

We can see on the interval from $\omega = 0$ to π, that there is only one point where the magnitude is not zero. Therefore, there is a spike at that point.

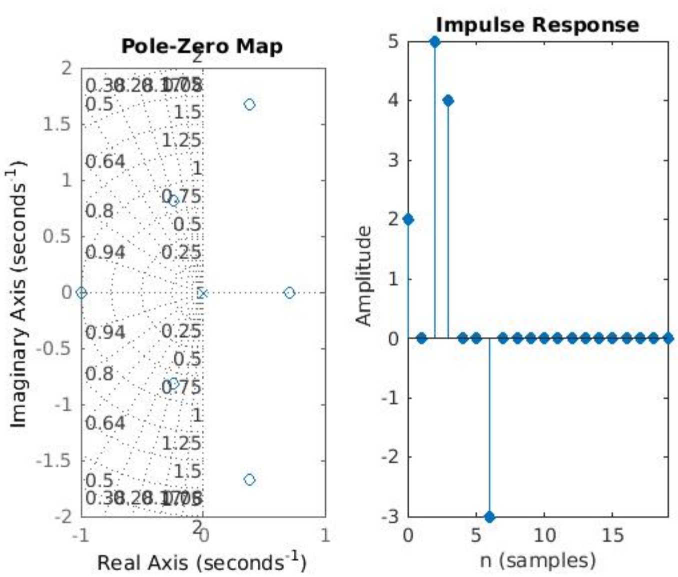


We can see on the interval from $\omega = 0$ to π that there is a minimum at $\omega = 0$ and a maximum at $\omega = \pi/4$ so the graph is increasing until that point.

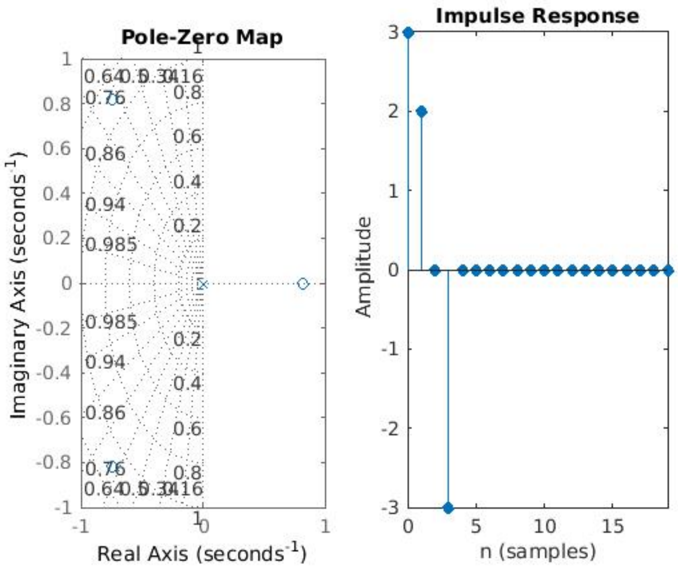
Report Item 5

```
function [   ] = pzplot_impz( a,b )
S = tf(b,a);
N = 20;

figure;
subplot(121);

pzplot(S);
grid on;
subplot(122);
impz(b,a,N);

end
```

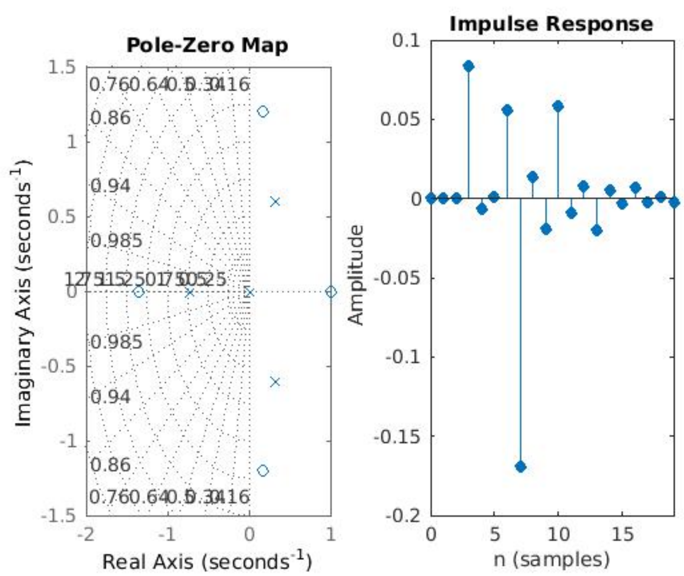
pzplot_impz.m



With $a = [1, 0, 0, 0, 0, 0, 0]$ and $b = [2, 0, 5, 4, 0, 0, -3]$ There are no poles on or outside the unit circle so the system is stable.



With $a = [1, 0, 0, 0]$ and $b = [3, 2, 0, -3]$, there are no poles on or outside the unit circle. Therefore, the system is stable.



With $a = [12, 1, 0, 4, 0, 0, 0, 0]$ and $b = [0, 0, 0, 1, 0, 0, 1, -2]$, there are no poles outside or on the unit circle. Therefore, the system is stable.

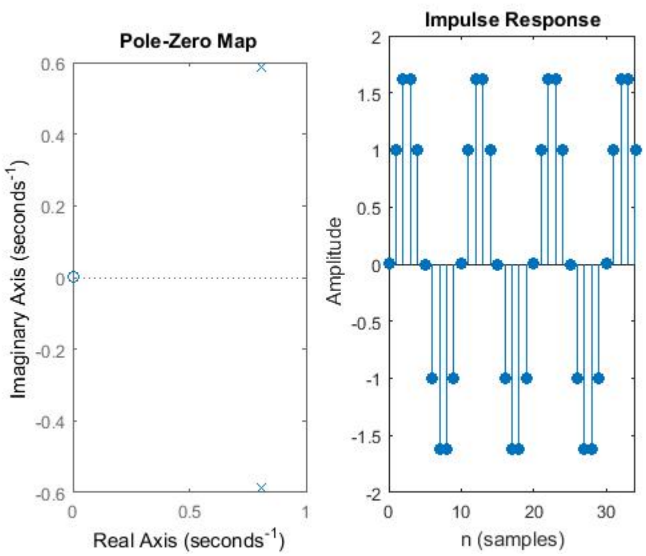
Report Item 6

$H(z) = \frac{z}{(z+e^{\frac{-i8\pi}{10}})(z+e^{\frac{i8\pi}{10}})}$

$= \frac{z}{z^2+ze^{\frac{-i8\pi}{10}}+ze^{\frac{i8\pi}{10}}+1}$

$= \frac{z}{z^2+2zcos(4\pi/5)+1}$

$= \frac{z^{-1}}{1+z^{-1}2cos(4\pi/5)+z^{-2}}$



$a = [1, 2cos(4\pi/5), 1], b = [0, 1, 0]$

The system is not BIBO stable, we have two poles on the unit circle. The system is stable when $|z| < e^{\frac{\pm i8\pi}{10}}$ and unstable when $|z| = -e^{\frac{\pm i8\pi}{10}}$.