1. a)
$$2 \cos x + \tan y = 2\sqrt{3}$$

Diff w.r.t 2

$$-2 \sin x + \sec^2 y \frac{dy}{dx} = 20$$

$$\sec^2 y \frac{dy}{dx} = 2 \sin x$$

$$\frac{dy}{dx} = 2 \text{cma} \cos^2 y$$

b)
$$\frac{dy}{dz}$$
 = $2\sin \frac{\pi}{6}\cos \frac{\pi}{3}$
= $2x \frac{1}{2} \times \left(\frac{1}{2}\right)^2 = \frac{1}{4}$

$$y - \frac{\pi}{3} = -4(2 - \frac{\pi}{6})$$

$$y - \frac{\pi}{3} = -4x + \frac{2\pi}{3}$$

$$\int 4x \cos 24x \, dx = x \sin 4x - \int \sin 4x \, dx$$

$$\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} = \frac{$$

$$3x - 4y = 3$$

$$2x = 2t^{2} - 1$$

$$3x - 4y = 3$$
Solving
Sillustrations

$$3(2t^{2}-1)-4[3(t+1)]=3$$

 $6t^{2}-3-12t-12=3$
 $6t^{2}-12t-18=0$
 $t^{2}-12t-18=0$
 $(t^{2}-12t-18=0)$
 $(t^{2}-12t-18=0)$
 $(t^{2}-12t-18=0)$

$$\frac{1}{12} = \frac{1}{3} = \frac{1}{12}$$

$$\frac{1}{3} = \frac{1}{12}$$

$$\frac{1}{3} = \frac{1}{12}$$

$$\frac{1}{3} = \frac{1}{12}$$

$$40$$
 9) $\frac{27x+2}{(2-x)(1+3x)} = \frac{P}{2-x} + \frac{9}{1+3x}$

$$(3/x+2 = P(1+3x) + Q(2-x))$$

IF
$$\chi=2$$
 $56=7P \Rightarrow P=8$

IF $\chi=-\frac{1}{3}$ $-7=\frac{7}{3}$ $\Rightarrow P=8$

$$\frac{\pi x + 2}{(2 - x)(1 + 3x)} = \frac{8}{2 - x} - \frac{3}{1 + 3x} = 8(2 - x)^{-1} - 3(1 + 3x)^{-1}$$

$$8(2-x)^{-1} = 8 \times 2^{-1} \left(1 - \frac{1}{2}x\right)^{-1} = 4 \left(1 - \frac{1}{2}x\right)^{-1}$$

$$= 4 \left(1 + \frac{-1}{1} \left(-\frac{1}{2}x\right)^{1} + \frac{-1(-2)}{1 \times 2} \left(-\frac{1}{2}x\right)^{2} + \frac{-1(-2)(-3)}{1 \times 2 \times 3} \left(-\frac{1}{2}x\right)^{3} + o(x^{4})\right)$$

$$= 4 \left(1 + \frac{1}{2}x + \frac{1}{4}x^{2} + \frac{1}{8}x^{2} + o(x^{4})\right)$$

$$= 4 + 2x + 2^{2} + \frac{1}{2}x^{2} + o(x^{4})$$

$$\frac{272+2}{(2-2)(1+32)} = \frac{4+2x+2^2+\frac{1}{2}x^3+O(x^4)}{-3+92-27x^2+81x^3+O(x^4)}$$

$$\frac{-3+92-27x^2+81x^3+O(x^4)}{1+11x-26x^2+\frac{163}{2}x^3+O(x^4)}$$

5. a)
$$\int \frac{\cos z}{1 - \cos z} dz = \int \frac{\cos z \left(1 + \cos z\right)}{\left(1 - \cos z\right) \left(1 + \cos z\right)} dz = \int \frac{\cos z \left(1 + \cos z\right)}{1 - \omega^2 z} dz$$

$$= \int \frac{\cos z \left(1 + \cos z\right)}{\sin^2 z} dz = \int \frac{\cos z + \omega^2 z}{\sin^2 z} dz$$

$$= \int \frac{\cos z}{\sin^2 z} + \frac{\cos^2 z}{\sin^2 z} dz = \int \frac{\cos z}{\sin z} + \cot^2 z dz$$

$$= \int \cot z \cos z + \cot^2 z dz$$

AS REPUIRO

USING STANDARD PROUTS $\frac{d}{dx}(\omega tx) = -\omega sec_{x}$ $\frac{d}{dx}(\omega sec_{x}) = -\omega sec_{x}\omega t_{x}$ $\frac{d}{dx}(\omega sec_{x}) = -\omega sec_{x}\omega t_{x}$ $\frac{d}{dx}(\omega sec_{x}) = -\omega sec_{x}\omega t_{x}$

 $= \int_{\mathbb{T}}^{\frac{\pi}{2}} \omega t x \omega s e \alpha + (\omega s e \alpha - 1) d\lambda = \left[-\omega s e \alpha - \omega t x = x \right]_{\frac{\pi}{2}}^{\frac{\pi}{2}}$

= [x+wtz+wsec] - [\frac{\pi}{2}+wt\frac{\pi}{2}+\osec\frac{\pi}{2}]

= (ま+1+12)-(生+1) = まナ(+12)-モー

 $= \sqrt{2} - \frac{1}{4} = \frac{1}{4} \left[4\sqrt{2} - \pi \right]$ $= \sqrt{2} - \frac{1}{4} = \frac{1}{4} \left[4\sqrt{2} - \pi \right]$

$$6.9)$$
 when $y=0 \Rightarrow t-t^2=0$

$$t=$$
 $0 \leftarrow 0819N$

$$V = \pi \int_{x_1}^{x_2} (y(a))^2 dx$$

IN PARAMETER IT BECOMES

$$V = \pi \int_{+}^{+} \left(y(t) \right)^2 dx dt$$

$$V = \pi \int_{0}^{1} \left(t - t^{2} \right)^{2} \left(12t \right) dc$$

$$Q = \pi \int_{0}^{1} 12t(t-t^{2})^{2} dt = \pi \int_{0}^{1} 12t(t^{2}-2t^{3}+t^{4}) dt$$

$$= \pi \int_{0}^{1} |2t^{3} - 24t^{4} + |2t^{5}| dt = \pi \left[3t^{4} - \frac{24}{5}t^{5} + 2t^{6} \right]_{0}^{1}$$

$$= \Pi \left[\left(3 - \frac{24}{5} + 2 \right) - 0 \right] = \frac{1}{5} \Pi$$

CH, IYGB, PARE J

7. a)
$$a = (0_1 8_1 3)$$

 $b = (1_1 13_1 1)$
 $a = b - a = (1_1 13_1 1) - (0_1 8_1 3) = (1_1 5_1 - 2)$

$$\overrightarrow{AB} = b - a = (1,13,1) - (0,18,3) = (1,5,-2)$$

$$(3/1/5) = (3/2) + 3(1/2/-5)$$

b)
$$\Gamma_2 = (70,9) + \mu(2,-3,1)$$

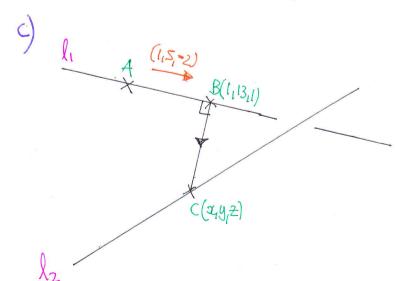
 $(x_1y_1z) = (2\mu+7, -3\mu, \mu+9)$

$$\lambda = 2\left(-\frac{43}{13}\right) + 7 \implies \left(\lambda = \frac{5}{13}\right)$$

CHECK K

$$3-2\lambda = 3-2\times\frac{5}{13} = \frac{29}{13}$$

 $9+9 = -\frac{43}{13}+9 = \frac{14}{13}$



$$b = (x_1 y_1 z)$$

CHIYGB PARELJ

NOW
$$\angle RC = 90$$
 ⇒ $(2-1, y-13, z-1) \cdot (1_15, -2) = 0$
⇒ $2-1+5y-65-2z+2=0$
⇒ $2+5y-2z=6+1$

$$x = 2\mu + 7$$

 $y = -3\mu$
 $z = \mu + 9$

THUS
$$(2y+7) + 5(-3y) - 2(y+9) = 6t$$

 $2y+7 - 15y - 29 - 18 = 6t$
 $-15y = 75$

80 a)
$$\frac{dV}{dt} = +k \times \frac{1}{V}$$

PLATE OF GYPANDS PROPORTIONAL

VOLUME

$$\Rightarrow \frac{dv}{dt} = \frac{k}{v}$$

$$\Rightarrow \frac{dV}{dP} \times \frac{dP}{dt} = \frac{k}{V}$$

$$\Rightarrow \left(-\frac{c}{p^2}\right)\frac{dP}{dt} = \frac{k}{V}$$

$$\Rightarrow \frac{dP}{olt} = \frac{k}{V} \times \left(-\frac{P^2}{c}\right)$$

$$\frac{dP}{dt} = \frac{k}{s} \times \frac{-P^2}{c}$$

$$\Rightarrow \frac{dP}{dt} = \frac{KP}{C} \times \frac{P^2}{C}$$

$$PV = constant$$

$$PV = c$$

$$V = C$$

$$V = CP^{-1}$$

$$dV = -CP^{-2}$$

$$dV = -CP^{-2}$$

$$dV = -CP^{-2}$$

$$\frac{dP}{dt} = -AP^3 \left(t = \frac{k}{c^2}\right)$$

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b) sparate variables

$$-\frac{1}{P^3}dP = Adt$$

$$\Rightarrow \frac{1}{2}P^{-2} = At + C$$

$$\Rightarrow \left| \frac{1}{2P^2} = At + C \right|$$

$$\frac{1}{2P^2} = At + \frac{1}{2}$$

when
$$t=2$$
, $P=\frac{1}{3}$ $\Rightarrow \frac{1}{\frac{2}{9}}=2A+\frac{1}{2}$
 $\frac{9}{2}=2A+\frac{1}{2}$
 $4=2A$

$$\frac{1}{2P^2} = 2t + \frac{1}{2}$$

$$\frac{1}{P^2} = 4t + 1$$

$$P^2 = \frac{1}{4t + 1}$$
As REQUIRED