$$- = 2 \left[\frac{1 - \tan^2 2}{2 \tan 2} \right] = 2 \times \frac{1}{\tan 2} = 2 \cot 22 = 2 HS$$

ALTHENATIVE

$$\frac{1}{1} = \frac{1}{1} = \frac{1}$$

$$= \frac{\cos 2x}{\sin 2\cos 2x} = \frac{2\cos 2x}{2\sin 2\cos 2x} = \frac{2\cos 2x}{\sin 2x} = 2\omega + 2x = RHS$$

$$2. \quad \left\{ y = \left(2 + e^{3\lambda} \right)^{\frac{3}{2}} \right\}$$

$$\frac{dy}{d\lambda} = \frac{3}{2} \left(2 + e^{3x} \right)^{\frac{1}{2}} \times 3e^{3x} = \frac{9}{2} e^{3x} \left(2 + e^{3x} \right)^{\frac{1}{2}}$$

$$\frac{dy}{dx}\Big|_{x=\frac{1}{3}\ln 2} = \frac{9}{2} \times 2 \times (2+2)^{\frac{1}{2}} = 18$$

3. a)
$$(4a) = e^{-2x} + \frac{\ln 2}{2}$$

$$f(x) = -2e^{-2x} - \frac{\ln 2}{2^2} = -\left[2e + \frac{\ln 2}{2^2}\right] < 0$$

AS THE BRACKET IS ALWAYS POSITIVE

C3, 14GB, PAPER U

b)
$$f(m4) = e^{-2\ln 4} + \frac{\ln 2}{\ln 4} = \frac{1}{16} + \frac{\ln 2}{2\ln 2} = \frac{9}{16}$$

· SINCE foi) IS DECREMENT

4. a)
$$Ey = arcsm2c - 1 \le x \le 13$$

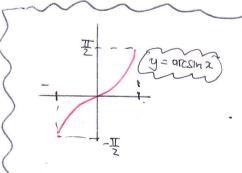
$$\Rightarrow \frac{dx}{dy} = \cos y$$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{6sy}$$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{+\sqrt{1-sin^2y}} \left(see opposite)$$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{\sqrt{1+x^2}}$$

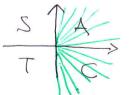
to repulling



144

6 y= 9 25 m2, -1 52 51

$$-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$$



Cosy CANNOT BE NERATIVE

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$$\frac{dy}{dx} = 3 \times \frac{1}{\sqrt{1-x^{2}}} - 6x^{\frac{1}{2}}$$

@ Solut For ZAND

$$\Rightarrow 0 = \frac{3}{(1-x^2)^{\frac{1}{2}}} - 6x^{\frac{1}{2}}$$

$$\Rightarrow 6x^{\frac{1}{2}} = \frac{3}{(1-x^2)^{\frac{1}{2}}}$$

$$\Rightarrow 2x^{\frac{1}{2}} = \frac{1}{(1-x^2)^{\frac{1}{2}}}$$

$$\Rightarrow 4a = \frac{1}{1-\alpha^2}$$

$$\Rightarrow$$
 0= $41^3 + 4x + 1$

$$\Rightarrow 4x^3 + 4x + 1 = 0$$

$$f(0)=1>0$$

 $f(0.5)=-\frac{1}{2}<0$

AS fa) IS CONTINUOUS &

CHANCES IN IN THE INSHUAL,

THRE MUST BE A DOUTION IN

THE INSHUAL

$$x^p = 0.2$$

$$\chi_{1} = 0.375$$

$$f(0.26955) = 0.00014 > 0$$

$$f(0.26965) = -0.00017 < 0$$

CHANGE OF SIW IMPLIFY
0.26955 < Y < 0.26965

$$\therefore \ \ \forall = 0.2696$$
(3 s.f)

5. a)
$$f(-x) = \frac{(-x)^2 - 4}{(-x)^2 + 2} = \frac{x^2 - 4}{(-x)^2 + 2} = f(x)$$

b)
$$f(x) = -\frac{1}{2}$$
 $\Rightarrow \frac{x^2 - 4}{|x| + 2} = -\frac{1}{2}$
 $\Rightarrow 2x^2 - 8 = -|x| - 2$
 $\Rightarrow |x| = 6 - 2x^2$
 $\Rightarrow (x = 6 - 2x^2)$
 $\Rightarrow (x = 6 - 2x^2)$

$$\int x = 6 - 2x^2$$

$$\begin{cases} 2x^2 + x - 6 = 0 \\ 2x^2 - x - 6 = 0 \end{cases}$$

$$\Rightarrow \left(\frac{(2x-3)(x+2)}{(2x+3)(x-2)} = 0 \right)$$

$$\lambda = \frac{3/2}{2}$$

$$6. a) LHS = 4 \cos 2\theta - \sec^2 \theta$$

$$= \frac{4}{\sin^2 2\theta} - \frac{1}{\cos^2 \theta}$$

$$= \frac{4}{(25m0\cos\theta)^2} - \frac{1}{(650)^2}$$

$$=\frac{4}{4\sin^2\theta\cos^2\theta}-\frac{1}{\cos^2\theta}$$

$$= \frac{1}{\text{Sindusio}} - \frac{\text{Sindo}}{\text{cosidsinio}}$$

$$= \frac{1 - \sin^2 \theta}{\sin^2 \theta \cos^2 \theta} = \frac{\cos^2 \theta}{\sin^2 \theta \cos^2 \theta} = \frac{1}{\sin^2 \theta}$$

6)
$$4(\omega \sec^2 2\theta - 2) = \sec^2 \theta - 2\omega \sec \theta$$

 $4(\omega \sec^2 2\theta - 8) = \sec^2 \theta - 2\omega \sec \theta$
 $4(\omega \sec^2 2\theta - \sec^2 \theta) = 8 - 2\omega \sec \theta$
 $\cos^2 \theta = 8 - 2\omega \sec \theta$
 $\cos^2 \theta + 2\omega \sec \theta - 8 = 0$

$$(\omega SCO - 2)(\omega SCO + 4) = 0$$

7. ELET arcsina = arcosy =
$$\theta$$

$$\Rightarrow \begin{cases} arcsy = 0 \\ arccsy = 0 \end{cases}$$

$$\Rightarrow \begin{cases} \sin(arcsmx) = sm\theta \\ \cos(arcsy) = \cos\theta \end{cases}$$

$$\Rightarrow \int_{0}^{\infty} x = \sin \theta$$

$$y = \cos \theta$$

C3, IYGB, PAPER U

8.
$$y = e^{2x}(2\omega s 3x - s \ln 3x)$$

$$\frac{dy}{dx} = 2e^{2x} (2\cos 3x - \sin 3x) + e^{2x} (-6\sin 3x - 3\cos 3x)$$

$$\frac{dy}{dx} = e^{2x} \left[4\omega s_{32} - 2s_{m32} - 6s_{143}x - 3\omega s_{32} \right]$$

$$\frac{dy}{dx} = e^{2x} \left[\cos 3x - 8\sin 3x \right]$$

Diff again

$$\frac{d^2y}{dx^2} = 2e^{2x} \left[\cos 3x - 8\sin 3x \right] + e^{2x} \left[-3\sin 3x - 24\cos 3x \right]$$

$$\frac{d^2y}{dx^2} = e^{2x} \left[26053x - 165143x - 35143x - 246053x \right]$$

$$\frac{d^2y}{dx^2} = e^{2x} \left[-22 \cos 3x - 19 \sin 3x \right]$$

HING

$$= e^{2x} \left[-22\cos 3x - 19\sin 3x \right] - 4 e^{2x} \left[\cos 3x - 8\sin 3x \right] + 13 \times e^{2x} \left[2\cos 3x - \sin 3x \right]$$

$$=e\times0$$

C3, IYGB, PARCE U

9

$$X = De^{-0.2t}$$

$$X = 20e^{-0.2t}$$

$$X = 20e^{-0.2}$$

b)
$$X = 20e^{-0.2t}$$

$$X = 20e^{-0.2 \times 2}$$

$$X = 13.41 > 12$$

is STILL ASLEEP

$$Y_{TOTA} = 20e^{-0.2 \times 3} + 10e^{-0.2 \times 1}$$

WHARE T IS THE TIME SINCE THE START OF THE OPERATION

$$\Rightarrow 12 = 20e^{-0.2T} + 10e^{-0.2(T-2)}$$

$$\Rightarrow$$
 |2 = 20 $e^{-0.2T}$ + 10 $e^{-0.2T}$ $e^{0.4}$

$$\Rightarrow$$
 |2 = $e^{-0.2T}$ [20 + 10e^{0.4}]

$$=\frac{12}{20 + 100^{0.4}}$$

C3, 14GB, PARGE U

$$\Rightarrow e^{0.2\overline{1}} = \frac{20 + 10e^{0.4}}{12}$$

$$\Rightarrow$$
 0.2T = $\ln\left(\frac{10+5e^{0.4}}{6}\right)$

$$\Rightarrow T = 5 \ln \left(\frac{\text{totse}^{0.4}}{6} \right)$$

X 60

80.43 ... MINUTH

As Reported