# 1YGB - FP2 PAPER O - QUESTION I

$$\frac{d^2y}{dx^2} + 6\frac{dy}{dx} + 13y = 13x^2 - x + 22$$

SOUDING THE AUXILUARY QUATION IN THE L.H.S OF FITE O.D.E.

$$\Rightarrow \lambda^2 + 6\lambda + 13 = 0$$

$$\Rightarrow (2+3)^2 - 9 + 13 = 0$$

$$\implies (7+3)^2 = -4$$

$$\Rightarrow \lambda = -3 \pm 2i$$

COMPLEMENTARY FUNCTION

#### PARTICULAR INTERPAL BY TRIAL

$$\dot{y} = Pa^2 + Qa + R$$

$$\frac{dy}{da} = 2Pa + Q$$

$$\frac{dy}{da^2} = 2P$$

SUBSTITUTE IMO THE O.D.E & LOMPARE

 $2P+6(2Px+Q)+13(Px^2+Qx+R)=13x^2-x+22$  $13Px^2+(12P+BQ)+(2P+6Q+13R)=13x^2-x+22$ 

$$P=1$$
 | •12++130=-1 | •2+6+13R=22  
12+130=-1 2-6+138=22  
130=-13 | 13R=26  
0=-1 R=2

PARTICULAR INHFRAL IS

GENERAL SOUTION IS

$$y = e^{-3\alpha} \left( A \cos 2\alpha + B \sin 2\alpha \right) + \alpha^2 - \alpha + 2$$

# 1YGB-FP2 PAPER O - QUESTION 2

# a) BY INSPECTION (COURS UP METIED OR SIMILAR)

$$\frac{f(r) = \frac{1}{r(r+2)} = \frac{\sqrt{2}}{r} + \frac{1}{r+2} = \frac{\frac{1}{2}}{r} - \frac{\frac{1}{2}}{r+2}$$

$$= \frac{1}{r} - \frac{1}{2(r+2)}$$

### b) SETTING PART (a) AS AN IDENTITY

$$\frac{2}{\Gamma(\Gamma+2)} = \frac{1}{\Gamma}$$

$$r = n - 1$$
  $\frac{2}{(n-1)(n+1)} = \frac{1}{(n-1)} \frac{1}{(n+1)}$ 

$$\bullet \ r = n \qquad \frac{2}{n(n+2)} = \frac{1}{n+2}$$

ADDING

$$\Rightarrow 2 \sum_{r=1}^{n} \frac{1}{r(r+2)} = \frac{3(h^2+3n+2)-2n-4-2n-2}{2(n+1)(n+2)}$$

16 A=3 B=5

# IYGB-FP2 PAPER O - QUESTION 2

$$= ) 2 \frac{n}{r(r+2)} = \frac{3n^2 + 9n + 6 - 4n - 6}{2(n+1)(n+2)}$$

$$= \frac{1}{r(r+2)} = \frac{n(3n+5)}{4(n+1)(n+2)}$$

# 1YGB-FPZ PARGE O - QUESTION 3

MOTATORY DIFFERS , ESTURES , DIFFERS DIFFERSTIATION

$$\Rightarrow f(x) = (1-x)^2 \ln(1-x)$$

$$\Rightarrow \{(x) = (1-2x+x^2) \left[ -x - \frac{1}{2}x^2 - \frac{1}{3}x^3 + o(x^4) \right]$$

$$\Rightarrow f(a) = -x + \frac{3}{2}x^2 - \frac{1}{3}x^3 + O(x^4)$$

### 1YGB - FPZ PAPGE O - QUESTION 4

MANIPULATE THE SURDS AS POLICUS

$$= \left(\sqrt{s}-2\right) \ln \left[ \frac{\left(\sqrt{s}-2\right)\left(\sqrt{s}+2\right)}{\sqrt{s}+2} \right] + \left(\sqrt{s}+2\right) \ln \left(\sqrt{s}+2\right)$$

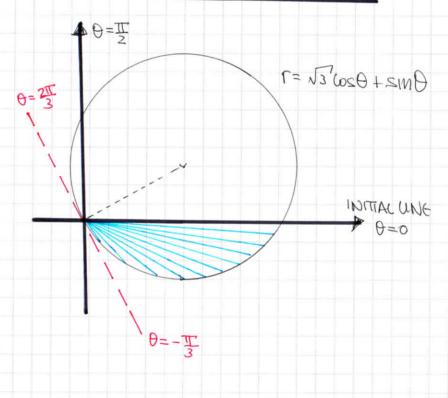
$$= (\sqrt{5}-2) \ln \left[ \frac{1}{\sqrt{5}+2} \right] + (\sqrt{5}+2) \ln (\sqrt{5}+2)$$

= 
$$-(\sqrt{5}-2) \ln [\sqrt{5}+2] + (\sqrt{5}+2) \ln [\sqrt{5}+2]$$

$$= 4 \ln \left[ 2 + \sqrt{2^2 + 1} \right]$$

### 1YGB - FP2 PAPER O - QUESTION 5

## COOKING AT THE DIAFRAM BELOW



$$A_{EEA} = \int_{\theta_{1}}^{\theta_{2}} \frac{1}{2} r^{2} d\theta = \int_{\theta_{1}}^{\theta_{2}} \frac{1}{2} (\sqrt{3} \cos \theta + 9 \sin \theta)^{2} d\theta$$

$$A_{EEA} = \int_{\theta_{1}}^{\theta_{2}} \frac{1}{2} [3 \cos^{2}\theta + 2 \sqrt{3} \cos^{2}\theta \sin^{2}\theta + \sin^{2}\theta] d\theta$$

$$A_{EEA} = \frac{1}{2} \int_{-\frac{\pi}{3}}^{\theta_{1}} \frac{1}{2} (1 + \cos^{2}\theta) + 1 + \sqrt{3} \sin^{2}\theta d\theta$$

$$A_{EAA} = \frac{1}{2} \int_{-\frac{\pi}{3}}^{\theta_{1}} \frac{1}{2} (1 + \cos^{2}\theta) + 1 + \sqrt{3} \sin^{2}\theta d\theta$$

$$A_{EAA} = \frac{1}{2} \int_{-\frac{\pi}{3}}^{\theta_{1}} \frac{1}{2} (\cos^{2}\theta + \sqrt{3} \sin^{2}\theta) d\theta$$

$$A_{EAA} = \frac{1}{2} \left[ 2\theta + \frac{1}{2} \sin^{2}\theta - \frac{\sqrt{3}}{2} \cos^{2}\theta \right] \frac{1}{4}$$

$$A_{EAA} = \frac{1}{2} \left[ (0 + 0 - \frac{\sqrt{3}}{2}) - (-\frac{2\pi}{3} - \frac{\sqrt{3}}{4} + \frac{\sqrt{3}}{4}) \right]$$

$$A_{EAA} = \frac{1}{2} \left[ \frac{2\pi}{3} - \frac{\sqrt{3}}{2} \right]$$

$$A_{EAA} = \frac{1}{2} \left[ 4\pi - 3\sqrt{3} \right] A_{EAA} = \frac{1}{2} \left[ 4\pi - 3\sqrt{3} \right]$$

# 1YGB - FP2 PAPER O - PURSTION 6

#### REMPITE THE INTERCAJO IN TERMS OF EXPONENTIALS

$$\int_0^{\ln 2} \frac{e^x}{\cosh x} dx = \int_0^{\ln 2} \frac{e^x}{\frac{1}{2}(e^x + e^x)} dx = \int_0^{\ln 2} \frac{2e^x}{e^x + e^x} dx$$

#### NOW BY SUBSTITUTION WE HAVE

$$u = e^{\alpha}$$

$$\frac{du}{d\alpha} = e^{\alpha}$$

$$\frac{du}{d\alpha} = u$$

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$$\frac{du}{d\alpha} = u$$

#### TRANSPORMING THE INTERAL

$$= \int_{1}^{2} \frac{2u}{u + u^{-1}} \left( \frac{du}{u} \right) = \int_{1}^{2} \frac{2}{u + \frac{1}{u}} du$$

$$= \int_{1}^{2} \frac{2u}{u^{2} + 1} du = \left[ \ln \left( u^{2} + 1 \right) \right]_{1}^{2}$$

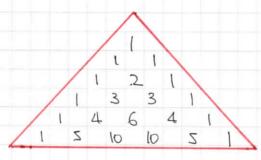
$$= \ln 5 - \ln 2 = \ln \frac{5}{2}$$

# 14GB-FPZ PAPER O- QUESTION 7

a) LET COSO + ismO = C+i\$, AND RAISE BOTH SUES OF THE EXPRESSION TO THE POWER OF 5

$$\Rightarrow (\omega \theta + i \sin \theta)^{2} = (c + i \xi)^{2}$$

FOLLOWING THE PATTINEN



=> cos50+isin50 = C5+5iC45-10c3\$2-10iC2\$3+5c\$4+i\$5

$$\implies SNS0 = 5(1-5^2)^2 5 - 10(1-5^2) 5^3 + 5^5$$

$$\Rightarrow$$
 sm 50 = 5\$ (\$\frac{5}{4} - 2\frac{5}{4} + 1) - 10\frac{5}{4} + 10\frac{5}{4} + \frac{5}{4}

b) START BY SOWING THE EQUATION SINSO = 0

$$50 = MT$$
  $n \in \mathbb{Z}$ 

$$\theta = 0, \frac{\pi}{5}, \frac{2\pi}{5}, \frac{3\pi}{5}, \frac{4\pi}{5}, \frac{\pi}{5}, \frac{\pi}{5}, \dots$$

### 1YGB - FPZ PAPER O - QUESTION 7

ALSO BY LETTING 2 = SMO, THE R.H.S YITUS

$$a(16x^4 - 20x^2 + 5) = 0$$

$$sm0(16sin^40 - 20sin^20 + 5) = 0$$

- (T=0 90) Pm2 CHS190DA7 2HT MORT 21 0 = 0. ●

### C) SOWING THE QUARTIC BY THE PURDRATIC FORMULA

- $16x^4 20x^2 + 5 = 0$  =  $32 = 20 \pm \sqrt{80}$  = 32 = 32 =  $32 = 5 \pm \sqrt{5}$
- $SW^{2}_{5} = S_{5} =$

## 1YGB - FPZ PARGE O - QUESTION 8

# 4) Proces 42 "ADVISED"

$$x = y200$$
 (=

$$\Rightarrow \frac{dx}{dy} = -smy$$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{smy}$$

$$\frac{dy}{dx} = -\frac{1}{\sqrt{1-x^2}}$$

/ AS REPURZIO

SINY + 
$$\omega \zeta y = 1$$
  
SINY =  $\pm \sqrt{1 - \omega \zeta y}$   
 $0 \le y \le \pi$ , so that  
SIN Y CANNOT BE A  
NEGATIVE QUANTITY

#### 6 DIFFERENTIATING THE EPUATION OF THE WELL

$$\Rightarrow \frac{dy}{dx} = -\frac{1}{\sqrt{1-x^2}} - \frac{1}{2} \times \frac{1}{1-x^2} \times (-2x)$$

$$\Rightarrow \frac{dy}{dx} = \frac{x}{1-x^2} - \frac{1}{\sqrt{1-x^2}}$$

$$\implies \frac{dy}{d\lambda} = \frac{x - \sqrt{1 - \chi^2}}{1 - \chi^2}$$

### SOWING FOR ZEND YIEVES

$$\Rightarrow 2 - \sqrt{1 - 2^2} = 0$$

$$\Rightarrow x = \sqrt{1-\chi^2}$$

$$\Rightarrow x^2 = 1 - x^2$$

# 1YGB - FPZ PAPGE O - QUESTION 8

$$\implies 2x^2 = 1$$

$$\Rightarrow$$
  $3^2 = \frac{1}{2}$ 

$$\Rightarrow x = \pm \frac{1}{\sqrt{2}}$$

### FINDING THE Y CO-DEDINATE

$$\Rightarrow y = \alpha R (052 - \frac{1}{2} \ln (1 - x^2))$$

$$\Rightarrow g = \arccos\left(\frac{1}{\sqrt{2}}\right) - \frac{1}{2}\ln\left(1 - \frac{1}{2}\right)$$

$$\Rightarrow y = \frac{1}{4} \left[ \pi + 2 \ln 2 \right]$$

$$\Rightarrow y = \frac{1}{4} \left( \pi + \ln 4 \right)$$

AS REPUIRED

# 1YGB - FPZ PAPER O - QUESTION 9

$$(1-x^2)\frac{dy}{dx}+y=(1-x^2)(1-x)^{\frac{1}{2}}$$

#### REWRITE THE O.D.E IN "STANDARD" FIRM AND WOOK FOR

AN INTERPATING PACTOR

$$\Rightarrow \frac{dy}{dx} + \frac{1}{1-x^2} \frac{dy}{dx} = (1-x)^{\frac{1}{2}}$$

$$= e^{\int \frac{1}{1+x} + \frac{1}{1-x} dx} = e^{\int \frac{1}{1-x} \left| \frac{1+x}{1-x} \right|} = e^{\int \frac{1}{1-x} \left| \frac{1+x}{1-x} \right|} = e^{\int \frac{1}{1-x} \left| \frac{1+x}{1-x} \right|}$$

$$\Rightarrow \frac{d}{dx} \left[ y \left( \frac{\sqrt{1+x'}}{\sqrt{1-x'}} \right) \right] = (1-x)^{\frac{1}{2}} \left( \frac{\sqrt{1+x'}}{\sqrt{1-x'}} \right)$$

$$\frac{y(1+x)^{\frac{1}{2}}}{(1-x)^{\frac{1}{2}}} = \int (1+x)^{\frac{1}{2}} dx$$

$$\frac{3(1+x)^{\frac{1}{2}}}{(1-x)^{\frac{1}{2}}} = \frac{2}{3}(1+x)^{\frac{3}{2}} + A$$

$$\frac{y(1+x)^{\frac{1}{2}}}{(1-x)^{\frac{1}{2}}} = \frac{2}{3}(1+x)^{\frac{3}{2}} + A$$

$$\Rightarrow y = \frac{2}{3}(1+x)(1-x)^{\frac{1}{2}} + A \frac{(1-x)^{\frac{1}{2}}}{(1+x)^{\frac{1}{2}}}$$

$$\Rightarrow \frac{\sqrt{2}}{2} = \frac{2}{3} \times \frac{3}{2} \times \frac{\sqrt{2}}{2} + \frac{1}{\sqrt{2}}$$

$$\Rightarrow \frac{\sqrt{2}}{2} = \frac{\sqrt{2}}{2} + A \frac{\sqrt{2}}{3}$$

$$\Rightarrow A = 0$$

# 1YGB-FP2 PARGE O- QUESTION 9

$$y = \frac{2}{3}(1+x)(1-x)^{\frac{1}{2}}$$

$$\Rightarrow y = \frac{2}{3}(1+x)^{\frac{1}{2}}(1+x)^{\frac{1}{2}}(1-x)^{\frac{1}{2}}$$

$$\Rightarrow y = \frac{2}{3}(1+x)^{\frac{1}{2}}\sqrt{1-x^2}$$

$$y = \frac{2}{3}\sqrt{(1+x)(1-x^2)^{\frac{1}{2}}}$$
At REPURED