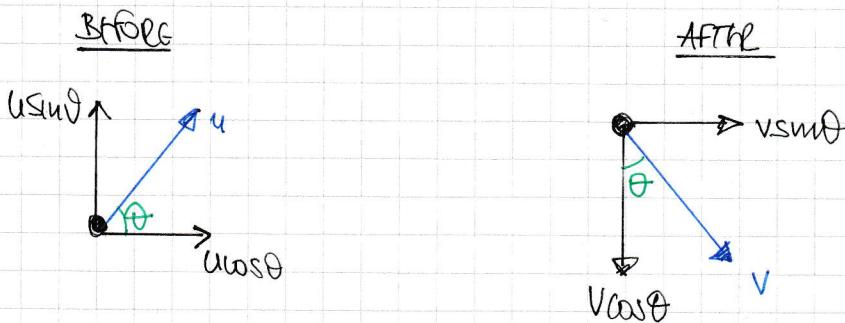


## IYGB - FM | PAPER P - QUESTION 1

a) STARTING WITH A BEFORE & AFTER DIAGRAM - LET THE BOUNCING SPEED BE V



NO MOMENTUM EXCHANGE IN A DIRECTION PARALLEL TO THE WALL

$$\Rightarrow u_{\text{parallel}} = v_{\text{parallel}}$$

$$\Rightarrow \frac{u}{v} = \frac{\sin \theta}{\cos \theta}$$

$$\Rightarrow \tan \theta = \frac{u}{v}$$

BY RESTITUTION, PERPENDICULAR TO THE WALL

$$\Rightarrow e = \frac{\text{SEP}}{\text{APP}}$$

$$\Rightarrow e = \frac{v_{\text{parallel}}}{u_{\text{parallel}}}$$

$$\Rightarrow \frac{1}{e} = \frac{u_{\text{parallel}}}{v_{\text{parallel}}}$$

$$\Rightarrow \frac{1}{e} = \frac{u}{v \tan \theta}$$

COMBINING EQUATIONS FROM ABOVE

$$\frac{1}{e} = \tan^2 \theta$$

$$\tan \theta = \pm \sqrt{\frac{1}{e}} \quad (\theta \text{ acute})$$

$$\tan \theta = \frac{1}{\sqrt{e}}$$

AS REQUIRED

b) FINALLY WE HAVE

$$0 < e < 1$$

$$0 < \sqrt{e} < 1$$

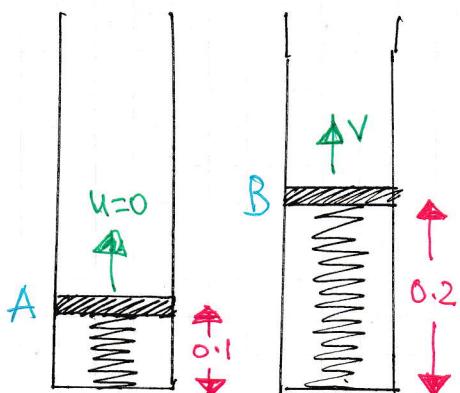
$$1 < \frac{1}{\sqrt{e}} < \infty$$

$$\therefore \tan \theta > 1$$

$$\therefore 45^\circ < \theta < 90^\circ$$

- -

## IYGB - FMI PAPER 0 - QUESTION 2



$$\begin{cases} k = 2000 \text{ N} \\ l = 0.2 \text{ m} \\ m = 1.5 \text{ kg} \end{cases}$$

BY CONSERVING TAKING THE LEVEL OF "A"  
AS THE ZERO GRAVITATIONAL POTENTIAL  
LEVEL

$$\Rightarrow \cancel{KE_A} + \cancel{PE_A} + \cancel{EE_A} + W_{in} - W_{out} = KE_B + PE_B + \cancel{EE_B}$$

$$\Rightarrow \frac{1}{2}kx^2 - F_x d = \frac{1}{2}mv^2 + mgh$$

$$\Rightarrow \frac{2000(0.1)^2}{2(0.2)} - (5.3)(0.1) = \frac{1}{2}(1.5)v^2 + (1.5)(9.8)(0.1)$$

$$\Rightarrow 50 - 0.53 = 0.75v^2 + 1.47$$

$$\Rightarrow 48 = 0.75v^2$$

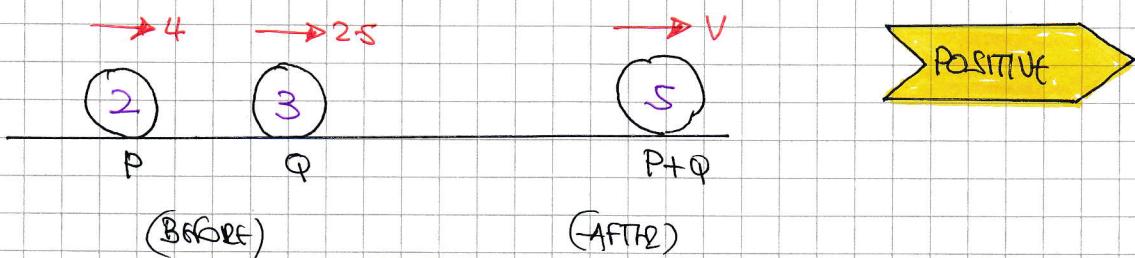
$$\Rightarrow v^2 = 64$$

$$\Rightarrow |v| = 8 \text{ ms}^{-1}$$

-1-

## YG8 - FM1 PAPER 0 - QUESTION 3

a) START WITH A COLLISION DIAGRAM



BY CONSERVATION OF MOMENTUM

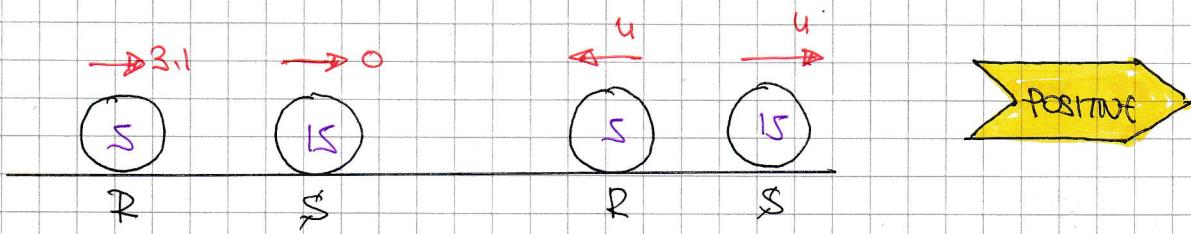
$$(2 \times 4) + (3 \times 2.5) = 5V$$

$$8 + 7.5 = 5V$$

$$5V = 15.5$$

$$V = 3.1 \text{ ms}^{-1}$$

b) GENING A NEW DIAGRAM



B) MOMENTUM CONSERVATION

$$(5 \times 3.1) + 0 = -5u + 15u$$

$$15.5 = 10u$$

$$u = 1.55 \text{ ms}^{-1}$$

FINALLY AS THE PARTICLES MOVE IN OPPOSITE DIRECTION, WITH EQUAL SPEEDS OF  $1.55 \text{ ms}^{-1}$

EVEN SECOND THEY MOVE  $(1.55 + 1.55) \text{ METRES APART}$

$$\therefore d = 3.6 \times 2 \times 1.55$$

$$d = 11.16 \text{ m}$$

# IYG-B - FMI PAPER 0 - QUESTION 4

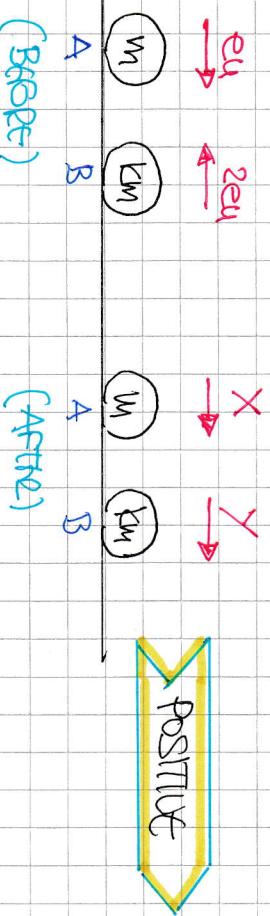
-1-

• STARTING WITH THE COLLISIONS WITH THE WALLS

AFTER REBOUNDING

$$v_A = eu \quad \& \quad v_B = 2eu$$

• NEXT THE COLLISION BETWEEN THEM



POSITIVE

$$\Rightarrow kX - kY = -3keu^2$$

$$\frac{X + kY}{k+1} = eu - 2keu$$

$$(k+1)X = eu - 2keu - 3keu^2$$

$$X = \frac{eu(1 - 2k - 3ke)}{(k+1)}$$

• ADDING THE EQUATIONS

$$kX - kY = -3keu^2$$

$$\frac{X + kY}{k+1} = eu - 2keu$$

$$(k+1)X = eu - 2keu - 3keu^2$$

$$X = \frac{eu(1 - 2k - 3ke)}{(k+1)}$$

• A DOES NOT CHANGE ITS DIRECTION

$$X > 0$$

$$\Rightarrow \frac{eu(1 - 2k - 3ke)}{k+1} > 0$$

$$\Rightarrow 1 - 2k - 3ke > 0 \quad [eu > 0, k+1 > 0]$$

$$\Rightarrow -3ke > 2k - 1$$

$$\Rightarrow \frac{y-x}{eu+2eu} = e$$

- | -

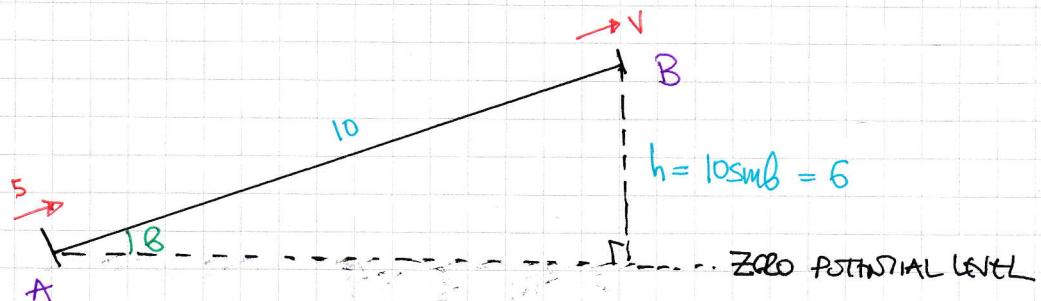
## IYGB - FMI PAPER P - QUESTION 5

AUXILIARIES FIRST

$$\tan \theta = \frac{3}{4} \Rightarrow \begin{array}{c} 3 \\ | \\ 5 \\ | \\ 4 \end{array} \Rightarrow \begin{array}{l} \sin \theta = \frac{3}{5} \\ \cos \theta = \frac{4}{5} \end{array}$$

ONLY THE COMPONENT OF THE TENSION PARALLEL TO THE PLANE PUTS ENERGY INTO THE SYSTEM, i.e.  $1500 \cos \theta = 1500 \times \frac{4}{5} = 1200$

NOW LOOKING AT AN ENERGY DIAGRAM, AND TAKING THE LEVEL OF "A", AS THE ZERO GRAVITATIONAL POTENTIAL LEVEL



$$\Rightarrow K.E_A + P.E_A + W_{in} - W_{out} = K.E_B + P.E_B$$

$$\Rightarrow \frac{1}{2}(20) \times 5^2 + 0 + (1200 \times 10) - (180 \times 10) = \frac{1}{2}(20)v^2 + 120g \times 6 \quad \leftarrow \text{"mgh"}$$

$$\Rightarrow 100 + 2000 - 1800 = 60v^2 + 7056$$

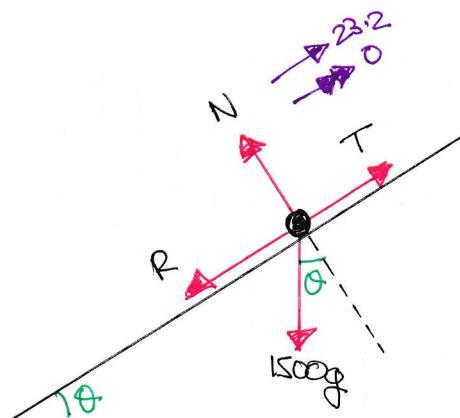
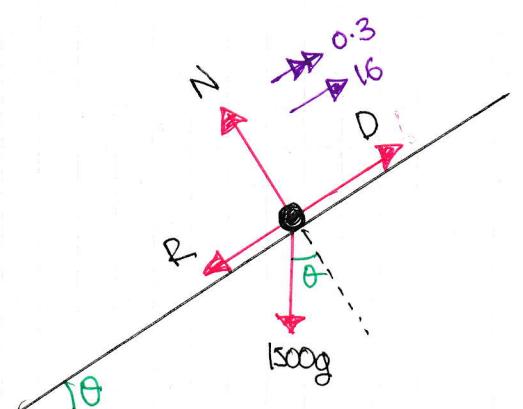
$$\Rightarrow 4644 = 60v^2$$

$$\Rightarrow v^2 = 77.4$$

$$\Rightarrow v \approx 8.80 \text{ ms}^{-1}$$

## IYGB - FMI PAPER 0 - QUESTION 6

- ③ START WITH TWO SEPARATE DIAGRAMS, TRYING TO FORM EQUATIONS



④ "P = D v"

$$\Rightarrow P = D \times 16$$

$$\Rightarrow D = \frac{P}{16}$$

"P = T v"

$$\Rightarrow P = T \times 23.2$$

$$\Rightarrow T = \frac{P}{23.2}$$

⑤ EQUATION OF MOTION

$$\Rightarrow "F = ma"$$

$$\Rightarrow D - R - 1500g \sin \theta = 1500a$$

$$\Rightarrow \frac{P}{16} - R - 1500g \left(\frac{2}{49}\right) = 1500(0.3)$$

$$\Rightarrow \frac{P}{16} - R - 600 = 450$$

$$\Rightarrow \underline{\underline{\frac{P}{16} - R = 1050}}$$

⑥ NO ACCELERATION (EQUILIBRIUM)

$$\Rightarrow T = R + 1500g \sin \theta$$

$$\Rightarrow \frac{P}{23.2} = R + 1500(9.8) \left(\frac{2}{49}\right)$$

$$\Rightarrow \frac{P}{23.2} = R + 600$$

$$\Rightarrow \underline{\underline{\frac{P}{23.2} - R = 600}}$$

⑦ COMBINING EQUATIONS BY SUBTRACTION

$$\frac{P}{16} - \frac{P}{23.2} = 450 \Rightarrow 23.2P - 16P = 167040$$

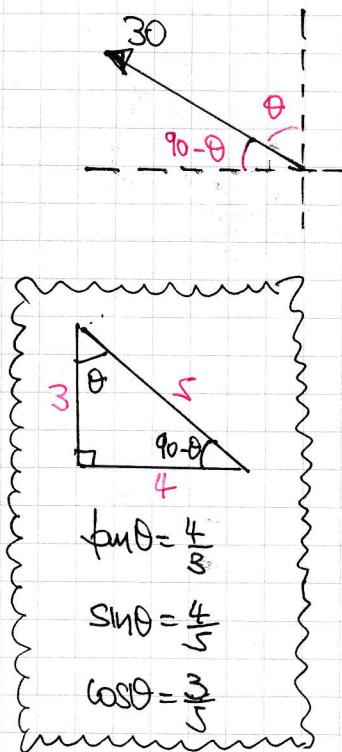
$$\Rightarrow 7.2P = 167040$$

$$P = 23200$$

-1-

## IYGB - FMI PAPER P - QUESTION 7

STARTING WITH A DIAGRAM



IMPULSE = MOMENTUM AFTER - MOMENTUM BEFORE

$$\underline{I} = \underline{m v} - \underline{m u}$$

$$(-30 \sin \theta) \underline{i} + (30 \cos \theta) \underline{j} = 0.5 \underline{v} - 0.5 \times 40 \underline{i}$$

$$-30(0.8) \underline{i} + 30 \times 0.6 \underline{j} = 0.5 \underline{v} - 20 \underline{i}$$

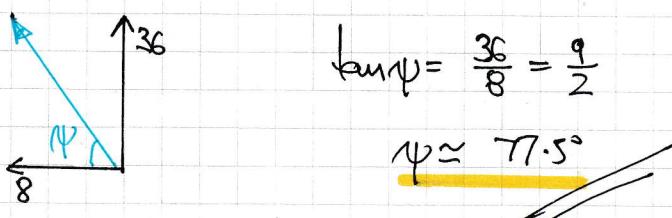
$$-24 \underline{i} + 18 \underline{j} = 0.5 \underline{v} - 20 \underline{i}$$

$$-4 \underline{i} + 18 \underline{j} = 0.5 \underline{v}$$

$$\underline{v} = -8 \underline{i} + 36 \underline{j}$$

$$\therefore |\underline{v}| = \sqrt{(-8)^2 + 36^2} = \sqrt{1360} \approx 36.9 \text{ m s}^{-1}$$

AND THE REQUIRED ANGLE

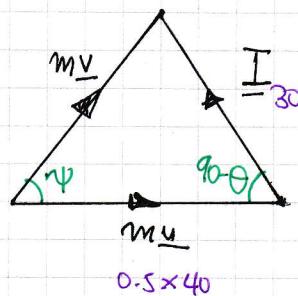


ALTERNATIVE BY GEOMETRY

$$\underline{I} = \underline{m v} - \underline{m u}$$

$$\underline{m u} + \underline{I} = \underline{m v}$$

DRAWING A VECTOR TRIANGLE



- 2 -

## IYGB - FMI PAPER P - QUESTION 7

BY THE COSINE RULE

$$|m_v|^2 = |m_u|^2 + |\underline{I}|^2 - 2|m_u||\underline{I}|\cos(90-\theta)$$

$$|0.5\underline{v}|^2 = 20^2 + 30^2 - 2 \times 20 \times 30 \times \sin \theta$$

$$\left\{ \begin{array}{l} \cos(90-\theta) = \sin \theta \\ \end{array} \right.$$

$$\frac{1}{4}|\underline{v}|^2 = 400 + 900 - 1200 \times \frac{4}{5} \leftarrow (\text{FROM BAGF})$$

$$\frac{1}{4}|\underline{v}|^2 = 340$$

$$|\underline{v}|^2 = 1360$$

$$|\underline{v}| = \sqrt{1360} \approx 36.9 \text{ m/s}$$

As BAGF

AND BY THE SINE RULE

$$\frac{\sin \psi}{|\underline{I}|} = \frac{\sin(90-\theta)}{|m_v|} \Rightarrow \frac{\sin \psi}{30} = \frac{\cos \theta}{\frac{1}{2}\sqrt{1360}}$$

$$\Rightarrow \frac{\sin \psi}{30} = \frac{0.6}{\frac{1}{2}\sqrt{1360}}$$

$$\Rightarrow \sin \psi = 0.976197 \dots$$

$$\Rightarrow \psi \approx 77.5^\circ$$

As BAGF

- -

## IYGB - FMI PAPER P - QUESTION 8

BY Hooke's Law - LET THE NATURAL LENGTH BE  $l$

$$mg = \frac{\gamma}{l} (x-l)$$

$$Mg = \frac{\gamma}{l} (y-l)$$

$$mgl = \gamma(x-l)$$

$$Mgl = \gamma(y-l)$$

$$\frac{mgl}{\gamma} = x-l$$

$$\frac{Mgl}{\gamma} = y-l$$

$$\frac{gl}{\gamma} = \frac{x-l}{m}$$

$$\frac{gl}{\gamma} = \frac{y-l}{M}$$

EQUATING YIELDS

$$\Rightarrow \frac{x-l}{m} = \frac{y-l}{M}$$

$$\Rightarrow Mx - Ml = my - ml$$

$$\Rightarrow Mx - my = Ml - ml$$

$$\Rightarrow Mx - my = l(M-m)$$

$$\Rightarrow l = \frac{Mx - my}{M-m}$$

(b)

As  $l > 0$  &  $M > m$ , so that  $M-m > 0$ , it implies that

$$\Rightarrow Mx - my > 0$$

$$\Rightarrow \underline{\underline{Mx > my}}$$

(b)

AS REQUIRED