No books; No calculator; No computer; No email; No internet; No notes; No phone. Do your scratch work elsewhere and enter only your final answer into the spaces provided. Points will be deducted for messy answers. Unreadable answers will be presumed incorrect.

1. Define gcd which uses Euclid's algorithm to find the greatest common divisor for two integers x > 0 and y > 0. The C version is given. Example: gcd(111, 259) = gcd(111, 148) = gcd(111, 37) = gcd(74, 37) = gcd(37, 37) = 37.

```
int gcd (int x, int y) {
   while (x != y) if (x > y) x -= y; else y -= x;
   return x;
}
```

(a) *Scheme*. Use tail recursion. [21] Example call: (define g (gcd 111 259)).

(b) *Ocaml*. Use tail recursion and curried format. [2✓] Example call: let d = gcd 111 259;;.

(c) Smalltalk. Extend class Integer with a keyword method gcd:. Use a loop. [2✓]
 Example call: g := 111 gcd: 259.

(d) *Perl*. Use a loop or tail recursion. Properly prototype the function. [2✓] Example call: \$g = gcd 111, 259;

(e) **Prolog.** [21] Example call: gcd(111, 259, G).

2. λ-calculus. Given the expression in the λ-calculus shown at the top of each box, show the derivation order to the number 25 for each of normal order and applicative order evaluation. [1]

normal order evaluation	applicative order evaluation
$(\lambda x \cdot * x \cdot x) (+23) =$	$(\lambda x \cdot * x \cdot x) (+23) =$

3. Scheme. Using apply, map, max, and cons, define the function depth for any argument. If it is null?, its depth is 1. Otherwise, if it is not a pair?, its depth is 0. The depth of anything else (a list) is one more than the maximum depth of the elements of the list. [2✓]

```
> (depth '(1 2 (3 4 (5 6)) 88))
3
> (depth '(a b c))
1
> (depth '())
1
> (depth 7)
```

4. *Ocaml.* Define drop, which returns its argument list without the first *n* elements. If *n* is larger than the length of the list, it returns a null list. If *n* is not positive, it just returns the list. Use a tail call. Do not compute the length of the list. [2/]

```
# drop;;
-: int -> 'a list -> 'a list = <fun>
# drop 3 [1;2;3;4;5;6;7];;
-: int list = [4; 5; 6; 7]
# drop 10 [1;2;3;4];;
-: int list = []
# drop (-5) [1;2;3;4];;
-: int list = [1; 2; 3; 4]
# drop 5 [];;
-: 'a list = []
```

5. **Smalltalk.** Extend class **Array** with an instance method **find**: whose argument is a value which is searched for in the array. If the value is present in the array, return the index of the first position where it is. If not found, return nil. [21]

```
st> a := #(5 6 7 8 9).
(5 6 7 8 9)
st> a find: 6
2
st> a find: 99
nil
```

6. **Perl.** Write a program which prints out the file size, modification time, and filename for each file mentioned in @ARGV. Hints: The result of the stat function is an array where \$stat[7] is the file size and \$stat[9] is the modification time. Use the strftime format "%b %e %H:%S" to print out the time. Print a suitable error message if @stat has length 0. [31]

```
-bash-60$ ls.perl *.perl

84 Nov 12 13:37 count.perl

240 Nov 16 12:39 euclid.perl

253 Nov 25 19:03 ls.perl

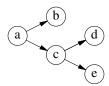
110 Dec 5 17:53 range.perl

91 Mar 14 21:31 wc.perl
```

7. Write the name of a programming language associated with each of the following people. Score 1/4 point for each correct answer, but not more than 2 points total. Choose answers from: AWK, BASIC, C, C++, COBOL, FORTRAN, Java, Lisp, Perl, Python, Scheme, λ-calculus. [2ν]

Alfred Aho	John Backus	Alonzo Church
James Gosling	Grace Hopper	John Kemeny
John McCarthy	Dennis Ritchie	Guy Steele
Bjarne Stroustrup	Larry Wall	Guido van Rossum

8. **Prolog.** Write facts in Prolog to describe the graph at left. Use the term **arrow** whose first argument is the tail of the arrow and whose second argument is the head of the arrow, i.e., **arrow**(X, Y) means that node X points directly at node Y. Write a rule **arrow2**(X, Y) which finds out if it is possible to get from X to Y by following exactly two **arrows.** [21]



9. Scheme. Draw a picture of the following Scheme expression. For each cons cell, draw a rectangular box divided into to parts, and draw an arrow from each of the car and the cdr fields to the cell or object pointed to.

[21]

```
((a b c) d (e) (f (g) h))
```

10. **Perl.** Write a program that reads files mentioned on the command line, and reads STDIN if none. Do not open files — use the <> operator. At the end of the last file, print each word followed by the number of times it appears. Print the words lexicographically. A word is any sequence of characters that matches m/\w+/. An example is given. [2✓]

example input	example output
This is a test.	This 2
test is a This.	a 3
is this a test?	is 3
testing this.	test 3
	testing 1
	this 2

11. *Ocaml.* Write a function eval which takes an expr as an argument and returns a float result. An expr is either a Number or an Expr with a char operator and two exprs. The only operators recognized are '+' and '*'. [2] Definitions:

Multiple choice. To the *left* of each question, write the letter that indicates your answer. Write Z if you don't want to risk a wrong answer. Wrong answers are worth negative points. [12 \checkmark]

number of		× 1 =	= a
correct answers			
number of		× ½ =	= b
wrong answers			
number of		× 0 =	0
missing answers			
column total	12		= c
$c = \max(a - b, 0)$			

- 1. If a is a valid list, what is equal to a itself?
 - (A) (car (cdr (cons a)))
 - (B) (cons (car (cdr a)))
 - (C) (cons (car a) (cdr a))
 - (D) (cons (cdr a) (car a))
- 2. What is the Perl equivalent to strerror (errno)?
 - (A) "\$!"
 - (B) "\$0"
 - (C) "\$?"
 - (D) "\$_"
- 3. In Perl, how can **\$p** be made to be a reference to an array containing some integers?
 - (A) p = (1, 2, 3, 4);
 - (B) p = 1, 2, 3, 4
 - (C) p = [1, 2, 3, 4];
 - (D) $p = \{1, 2, 3, 4\};$
- What is the Ocaml type signature for the definition: let f x = x;;
 - (A) val f : 'a -> 'a = <fun>
 - (B) val f : $'a \rightarrow 'b \rightarrow 'b * 'a = \langle fun \rangle$
 - (C) val $f : 'a \rightarrow 'b \rightarrow 'b = \langle fun \rangle$
 - (D) val f : int -> int = <fun>
- Passing a parameter by _____ means that it is passed in unevaluated and then evaluated only if needed.
 - (A) name
 - (B) reference
 - (C) value
 - (D) value-result
- 6. An object-oriented language like C++ does dynamic dispatching of method calls using a:
 - (A) friend function
 - (B) heap-allocated closure
 - (C) template declaration
 - (D) virtual function table

- 7. The Perl pattern equivalent to [a-zA-z0-9_] is:
 - (A) \d+
 - (B) \s+
 - (C) \t+
- 8. If we have a function not (bool -> bool) and a function even (int -> bool), how might the function odd be defined?
 - (A) let odd = compose not even
 - (B) let odd = map not even
 - (C) let odd = not even
 - (D) let odd x = not even x
- 9. A closure is:
 - (A) A special field of a structure or class used to point at a base class when implementing shared multiple inheritance.
 - (B) A special type declaration in Ocaml used to distinguish sum types from product types.
 - (C) A structure on the heap, used to hold variables of an outer function when referenced by an inner function.
 - (D) A table used to dynamically dispatch virtual functions in an object-oriented environment.
- 10. In Perl, what command will put the names of files in the current directory in the variable @files?
 - (A) @files = <ls>;
 - (B) @files = 'ls';
 - (C) @files = glob "ls";
 - (D) @files = system 'ls';
- 11. What is the type of car in the following?

```
let car s = match s with | x::xs \rightarrow x
```

- (A) val car : 'a -> 'a = <fun>
- (B) val car : $'a \rightarrow 'a$ list = <fun>
- (C) val car : 'a list -> 'a = <fun>
- (D) val car : 'a list -> 'a list = <fun>
- 12. What is the type of tail in the following? let cdr s = match s with | x::xs -> xs
 - (A) val cdr : $'a \rightarrow 'a = \langle fun \rangle$
 - (B) val cdr : $'a \rightarrow 'a$ list = $\{fun\}$
 - (C) val cdr : 'a list -> 'a = <fun>
 - (D) val cdr : 'a list -> 'a list = <fun>

Multiple choice. To the *left* of each question, write the letter that indicates your answer. Write Z if you don't want to risk a wrong answer. Wrong answers are worth negative points. [12 \checkmark]

number of		× 1 =		= a
correct answers				
number of		× ½ =		= <i>b</i>
wrong answers				
number of		× 0 =	0	
missing answers				
column total	12			= <i>c</i>
$c = \max(a - b, 0)$				

- 1. The basic algorithm used in type inference is:
 - (A) code replication
 - (B) interpretation
 - (C) overloading
 - (D) unification
- 2. If guess finds something in a sequence of facts, and verify checks to see if it is a good one, then find can be defined in Prolog as:

```
(A) find(X) :- guess(X), verify(X).
```

- $(B) \ \, \text{find(X)} \ \, :\text{- guess(X)} \, .$
 - find(X) :- verify(X).
- (C) find(X) := guess(X), !, verify(X).
- (D) guess(X), verify(X) := find(X).
- 3. What is 6?
 - (A) (apply + '(1 2 3))
 - (B) (cons + '(1 2 3))
 - (C) (list + '(1 2 3))
 - (D) (map + '(1 2 3))
- 4. Which will unexpectedly start a comment?
 - (A) let f = (*);;
 - (B) let f = (+);;
 - (C) let f = (-);;
 - (D) let f = (/);;
- 5. What Perl statement will open a pipe to a subprocess and allow writing to its standard input?
 - (A) open my \$file, "\$name|"
 - (B) open my \$file, "<\$name"</p>
 - (C) open my \$file, ">\$name"
 - (D) open my \$file, "|\$name"
- 6. Which language uses lazy evaluation by default?
 - (A) Haskell
 - (B) Lisp
 - (C) Ocaml
 - (D) Scheme

- 7. In Ocaml, what is 7?
 - (A) (+) (3, 4);;
 - (B) (+) 3 4;;
 - (C) (+) 3, 4;;
 - (D) 3 (+) 4;;
- 8. What function is called immediately after d() if d() is true?

```
for (a(); b(); c()){
   if (d()) continue;
   e();
   if (f()) break;
   g();
}
```

- h();
- (A) b()
- (B) c()
- (C) e()
- (D) h()
- 9. The following interaction indicates what kind of polymorphism?

```
# List.length;;
- : 'a list -> int = <fun>
```

- (A) conversion
- (B) inclusion
- (C) overloading
- (D) parametric
- 10. If \$key is a key, what is the value associated with it in a hash? \$hash{\$key} %hash{\$key} &hash{\$key} @hash{\$key}
- 11. What kind of function is

```
let f x y z = x + y + z;
```

- (A) curried
- (B) thunked
- (C) tupled
- (D) unified
- 12. Go To Statement Considered Harmful
 - (A) Corrado Böhm & Giuseppe Jacopini
 - (B) Donald E. Knuth
 - (C) Edsger W. Dijkstra
 - (D) Niklaus Wirth