

Labels: 0, 1, 2

Features: 4 booleans

first predicted split on label 0

	0	1	2	3
0	1	1	1	1
0	1	1	0	0
0	1	0	1	0
1	0	1	1	1
1	0	1	0	1
1	0	1	1	0
2	0	1	0	0
2	0	0	1	1
2	0	0	0	1
2	0	0	1	0
2	0	0	0	0

00011122222

00011122222

00011122222

00011122222

00011122222

Step 1:

\* Gini on  $f_0$ :

$$r: 1 - (1^2 + 0^2) = 0 \quad l: 1 - (0^2 + \frac{3}{8}^2 + \frac{5}{8}^2) = .46875$$

$$w: \frac{3}{11} \cdot 0 + \frac{8}{11} \cdot .46875 = .3489$$

on  $f_2$ :

$$r: 1 - (\frac{1}{3}^2 + \frac{1}{3}^2 + \frac{1}{3}^2) = \frac{2}{3} \quad l: 1 - (\frac{1}{5}^2 + \frac{1}{5}^2 + \frac{3}{5}^2) = .56$$

$$w: \frac{6}{11} \cdot \frac{2}{3} + \frac{5}{11} \cdot .56 = .618$$

on  $f_1$ :

$$r: 1 - (\frac{1}{3}^2 + \frac{1}{2}^2 + \frac{1}{6}^2) = .61 \quad l: 1 - (\frac{1}{5}^2 + 0 + \frac{4}{5}^2) = .32$$

$$w: \frac{6}{11} \cdot .61 + \frac{5}{11} \cdot .32 = .478$$

on  $f_3$ :

$$r: 1 - (\frac{1}{5}^2 + \frac{2}{5}^2 + \frac{2}{5}^2) = .64 \quad l: 1 - (\frac{1}{3}^2 + \frac{1}{6}^2 + \frac{1}{2}^2) = .61$$

$$w: \frac{5}{11} \cdot .64 + \frac{6}{11} \cdot .61 = .624$$

split on  $f_0$

$r=c_0$

split on  $f_1$

split on  $f_2$

$r=c_2$

$r=c_1$

split on  $f_2$

$r=c_1$

$r=c_2$

Gini imp:  $1 - \sum p_k^2$  where  $p_k$  is prob class picked  
weighted:  $\sum \frac{s_k}{s_r} (g_k)$  for class k

Step 2:

Given on f0:

$$r: 1 - \left(0 + \frac{3^2}{8} + \frac{5^2}{8}\right) = .46875$$

$$w: 0 \cdot 1 + 1 \cdot .46875 = .46875$$

on f1:

$$r: 1 - \left(\frac{3^2}{4} + \frac{1^2}{4}\right) = .375 \quad l: 0$$

$$w: \frac{1}{2} \cdot .375 + 0 = .1875$$

on f2:

$$r: 1 - \left(\frac{1^2}{2} + \frac{1^2}{2}\right) = .5 \quad l: 1 - \left(\frac{1^2}{4} + \frac{3^2}{4}\right) = .375$$

$$w: \frac{1}{2} \cdot .5 + \frac{1}{2} \cdot .375 = .4375$$

on f3

$$r: 1 - \left(\frac{1^2}{2} + \frac{1^2}{2}\right) = .5 \quad l: 1 - \left(\frac{1^2}{4} + \frac{3^2}{4}\right) = .375$$

$$w: .4375$$

Step 3:

Given on f0:

$$r: 1 - \left(1 - \left(\frac{3^2}{4} + \frac{1^2}{4}\right)\right) = .375$$

$$w: .375$$

on f1

$$r: 1 - \left(\frac{3^2}{4} + \frac{1^2}{4}\right) = .375 \quad l: 1$$

$$w: .375$$

on f2

$$r: 1 - (1^2 + 0) = 0 \quad l: 1 - \left(\frac{1^2}{2} + \frac{1^2}{2}\right) = .5$$

$$w: \frac{1}{2} \cdot 0 + \frac{1}{2} \cdot \frac{1}{2} = .25$$

on f3

$$r: 1 - (1^2 + 0) = 0 \quad l: 1 - \left(\frac{1^2}{2} + \frac{1^2}{2}\right) = .5$$

$$w: .25$$

subset set

1	0	1	1	1
1	0	1	0	1
1	0	1	1	0
2	0	1	0	0
2	0	0	1	1
2	0	0	0	1
2	0	0	1	0
2	0	0	0	0

subset set

1	0	1	1	1
1	0	1	0	1
1	0	1	1	0
2	0	1	0	0

Step 4:

set 1 0 1 0 1  
2 0 1 0 0

on f0:

$$r: 1 - \left(1 - \frac{1^2}{2} - \frac{1^2}{2}\right) = \frac{1}{2}$$

$$w: \frac{1}{4}$$

$$\text{on f1: } w: \frac{1}{4}$$

$$\text{on f2: } w: \frac{1}{4}$$

on f3

$$r: 1 - 1^2 - 0^2 = 0 \quad l: 1 - 0^2 - 1^2 = 0$$

$$w: 0$$